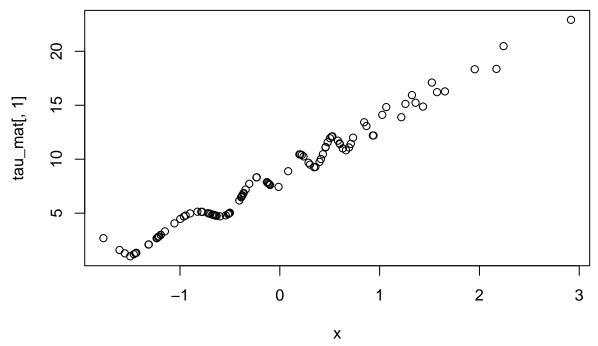
Time-varying treatment effect dgp

DGP

```
Data Size
n = 100
t1 = 40
t0 = 21
p = 1
Individual effect
\# alpha_i \sim N(mu_a, sig_a)
mu_a = 0
sig_a = 1
alpha = rnorm(n, mu_a, sig_a)
Time fixed effect
\# gamma_t \sim N(mu_g, sig_g)
mu_g = 1
sig_g = 1
gamma = rnorm(t1, mu_g, sig_g)
Time-varying (lagged) Treatment effect
x = as.matrix(rnorm(n))
tau \leftarrow function(x)\{a = (x + 1.5)^2; 5*sqrt(a) + sin(5*a)+1\}
tau_mat <- matrix(0, n, t1-t0+1)</pre>
tau_mat[,1] <- tau(x)</pre>
for (i in 2:(t1-t0+1)){
  tau_mat[,i] <- 0.9*tau_mat[,i-1]</pre>
}
Treatment
z = rbinom(n, 1, 0.5)
{\bf Error\ term}
eps = matrix(rnorm(n*t1, 0, 0.2), nrow = n, ncol = t1)
Generate observations
y0 = y1 = y = matrix(0, nrow = n, ncol = t1)
# for (i in 1:n){
# y0[i,] = y0[i,] + alpha[i]
# for (j in 1:t1){
y0[,j] = y0[,j] + gamma[j]
y0 = y0 + eps
y1 = y0
```

```
y1[, t0:t1] = y0[, t0:t1] + tau_mat
z_mat = matrix(rep(z, t1), n, t1)
y = y0 * (1-z_mat) + y1 * z_mat
Visualize time series
plot(1:t1, rep(mu_a, t1), type = "1", col = 3, ylim = range(y), lwd = 2) # mean indiviudal effect
for (i in 1:50){
  lines(1:t1, y[i,], col = 1, lty = 2)
lines(1:t1, rep(mu_a, t1), col = 3, lwd = 2)
lines(1:t1, gamma, col = 2, lwd = 2) # time effect
legend("topleft", legend = c("Mean Individual Effect", "Time effect", "y"), col = c(3, 2, 1), lty = c(1
                    Mean Individual Effect
      20
                    Time effect
                    У
      15
rep(mu_a, t1)
      10
      2
      0
            0
                             10
                                               20
                                                                 30
                                                                                   40
                                               1:t1
                                                                                         Visu-
alize treatment effect
```

```
\# treatment effect over x
plot(x, tau_mat[,1])
```



```
# # treatment effect over time
# plot(t0:t1, tau_mat[1,], type = "l", lty = 2, ylim = range(tau_mat))
# for (i in seq(1, n, length.out = 30)){
# lines(t0:t1, tau_mat[i,], lty=2)
# }
```

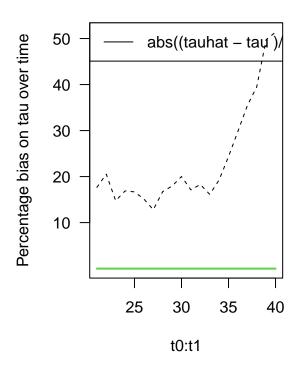
Demo model

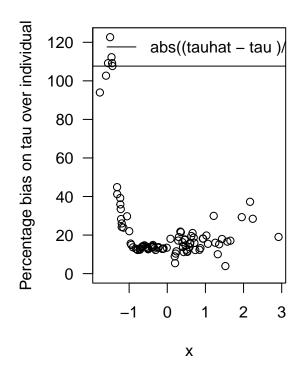
Model

```
source('longBet_xbcf.R')
library(XBCF)
mc = 50
burnin = 10
fit <- longBet_xbcf(y[,t0:t1], x, z, 1, mc, burnin)

pct_bias <- abs((colMeans(fit$tauhat) - tau_mat) / tau_mat)
par(mfrow=c(1,2))
plot(t0:t1, colMeans(pct_bias), type = "l", col = 1, ylim = range(0, colMeans(pct_bias)),lty = 2, ylab = lines(t0:t1, rep(0, t1-t0+1), col = 3, lty = 1, lwd = 2)
axis(2, at=pretty(colMeans(pct_bias)), lab=pretty(colMeans(pct_bias)) * 100, las=TRUE)
legend("topleft", legend = c("abs((tauhat - tau )/tau)"), col = c(1), lty = c(1,2))

plot(x, rowMeans(pct_bias), col = 1, ylim = range(0, rowMeans(pct_bias)), ylab = 'Percentage bias on taraxis(2, at=pretty(rowMeans(pct_bias)), lab=pretty(rowMeans(pct_bias)) * 100, las=TRUE)
legend("topleft", legend = c("abs((tauhat - tau )/tau)"), col = c(1), lty = c(1,2))</pre>
```





Plot yhat

```
yhat <- matrix(0, n, t1)
# yhat[, t0:t1] <- yhat[,t0:t1] + colMeans(fit$muhat)
yhat[,t0:t1] <- yhat[,t0:t1] + colMeans(fit$tauhat) * matrix(rep(z, t1-t0+1), n, t1-t0+1)

plot(1:t1, rep(mu_a, t1), type = "l", col = 3, ylim = range(yhat), lwd = 2) # mean individual effect
for (i in 1:50){
    lines(1:t1, yhat[i,], col = 1 + 3*z[i], lty = 2)
}
gamma <- rep(0, t1)
lines(1:t1, rep(mu_a, t1), col = 3, lwd = 2)
lines(1:t1, gamma, col = 2, lwd = 2) # time effect
legend("topleft", legend = c("Mean Individual Effect", "Time effect", "yhat untreated", "yhat treated")
    col = c(3, 2, 1, 4), lty = c(1, 1, 2))</pre>
```

