

Time-varying treatment effect dgp

DGP

Data Size

```
n = 100
t1 = 40
t0 = 21
p = 1
```

Individual effect

```
#  $\alpha_i \sim N(\mu_a, \sigma_a)$ 
mu_a = 1
sig_a = 1
alpha = rnorm(n, mu_a, sig_a)
```

Time fixed effect

```
#  $\gamma_t \sim N(\mu_g, \sigma_g)$ 
mu_g = 0
sig_g = 1
gamma = rnorm(t1, mu_g, sig_g)
```

Error term

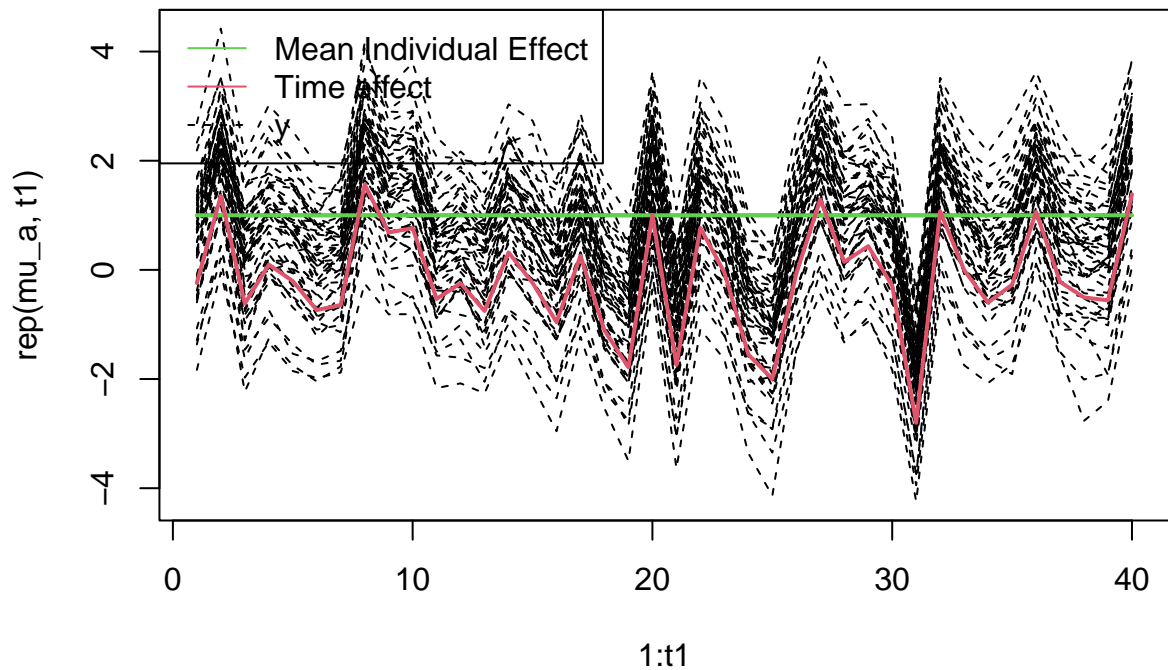
```
eps = matrix(rnorm(n*t1, 0, 0.2), nrow = n, ncol = t1)
```

Generate observations

```
y0 = y1 = y = matrix(0, nrow = n, ncol = t1)
for (i in 1:n){
  y0[i,] = y0[i,] + alpha[i]
}
for (j in 1:t1){
  y0[,j] = y0[,j] + gamma[j]
}
y0 = y0 + eps
y = y0
```

Visualize time series

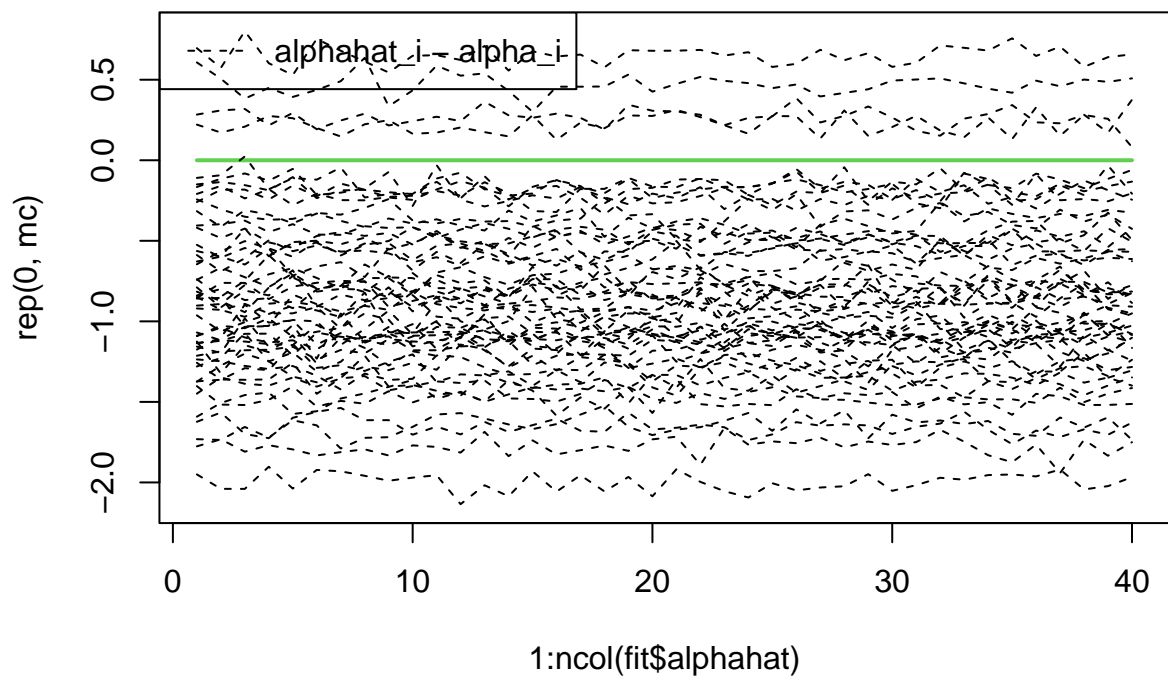
```
plot(1:t1, rep(mu_a, t1), type = "l", col = 3, ylim = range(y), lwd = 2) # mean individual effect
for (i in 1:50){
  lines(1:t1, y[i,], col = 1, lty = 2)
}
lines(1:t1, rep(mu_a, t1), col = 3, lwd = 2)
lines(1:t1, gamma, col = 2, lwd = 2) # time effect
legend("topleft", legend = c("Mean Individual Effect", "Time effect", "y"), col = c(3, 2, 1), lty = c(1, 2, 1))
```



Demo model Model

```
source('two_way.R')
fit <- longBet_tw(y, x, 50, 10)
```

```
mc = ncol(fit$alphahat)
plot(1:ncol(fit$alphahat), rep(0, mc), type = "l", col = 3, ylim = range(fit$alphahat - alpha), lwd = 2)
for (i in 1:50){
  lines(1:ncol(fit$alphahat), fit$alphahat[i,]-alpha[i], col = 1, lty = 2)
}
legend("topleft", legend = c("alphahat_i - alpha_i"), col = c(1), lty = c(2))
```



```

mc = ncol(fit$gammahat)
plot(1:t1, gamma, type = "l", col = 3, ylim = range(fit$gammahat, gamma), lwd = 2)
for (i in 1:mc){
  lines(1:t1, fit$gammahat[,i], col = 1, lty = 2)
}
lines(1:t1, gamma, col = 3, lwd = 2)
legend("topleft", legend = c("gamma", "gammahat"), col = c(3,1), lty = c(1,2))

```

