Time-varying treatment effect dgp

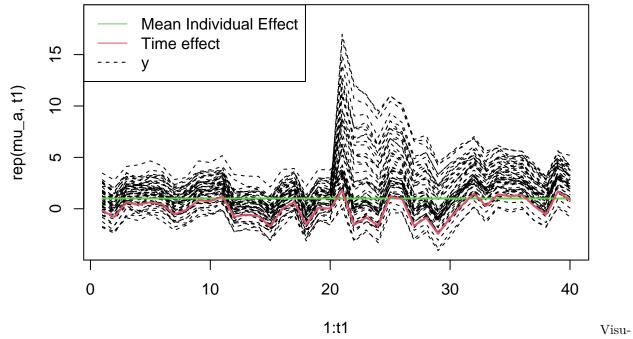
DGP

```
Data Size
n = 100
t1 = 40
t0 = 21
p = 1
Individual effect
\# alpha_i \sim N(mu_a, sig_a)
mu_a = 1
sig_a = 1
alpha = rnorm(n, mu_a, sig_a)
Time fixed effect
\# gamma_t \sim N(mu_g, sig_g)
mu_g = 0
sig_g = 1
gamma = rnorm(t1, mu_g, sig_g)
Time-varying (lagged) Treatment effect
x = as.matrix(rnorm(n))
tau \leftarrow function(x)\{a = (x + 1.5)^2; 5*sqrt(a) + sin(5*a)\}
tau_mat <- matrix(0, n, t1-t0+1)</pre>
tau_mat[,1] <- tau(x)</pre>
for (i in 2:(t1-t0+1)){
  tau_mat[,i] <- 0.9*tau_mat[,i-1]</pre>
}
Treatment
z = rbinom(n, 1, 0.5)
{\bf Error\ term}
eps = matrix(rnorm(n*t1, 0, 0.2), nrow = n, ncol = t1)
Generate observations
y0 = y1 = y = matrix(0, nrow = n, ncol = t1)
for (i in 1:n){
  y0[i,] = y0[i,] + alpha[i]
for (j in 1:t1){
  y0[,j] = y0[,j] + gamma[j]
y0 = y0 + eps
y1 = y0
```

```
y1[, t0:t1] = y0[, t0:t1] + tau_mat
z_mat = matrix(rep(z, t1), n, t1)
y = y0 * (1-z_mat) + y1 * z_mat

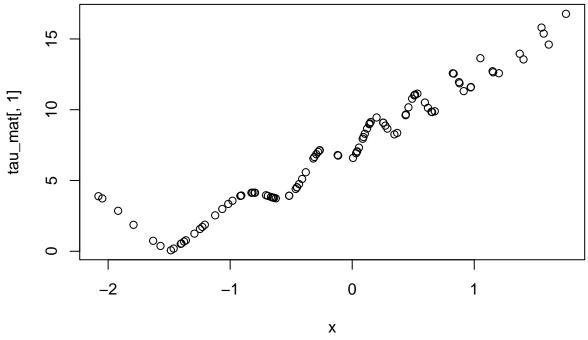
Visualize time series
plot(1:t1, rep(mu_a, t1), type = "l", col = 3, ylim = range(y), lwd = 2) # mean indiviudal
for (i in 1:50){
```

```
plot(1:t1, rep(mu_a, t1), type = "1", col = 3, ylim = range(y), lwd = 2) # mean indiviudal effect
for (i in 1:50){
    lines(1:t1, y[i,], col = 1, lty = 2)
}
lines(1:t1, rep(mu_a, t1), col = 3, lwd = 2)
lines(1:t1, gamma, col = 2, lwd = 2) # time effect
legend("topleft", legend = c("Mean Individual Effect", "Time effect", "y"), col = c(3, 2, 1), lty = c(1)
```

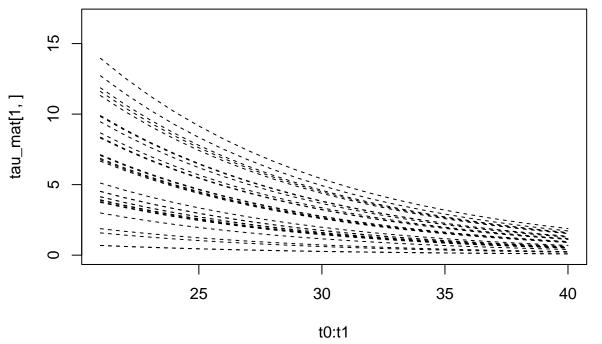


alize treatment effect

```
# treatment effect over x
plot(x, tau_mat[,1])
```



```
# treatment effect over time
plot(t0:t1, tau_mat[1,], type = "l", lty = 2, ylim = range(tau_mat))
for (i in seq(1, n, length.out = 30)){
   lines(t0:t1, tau_mat[i,], lty=2)
}
```



Demo model Model

```
source('longBet_xbcf.R')
library(XBCF)
mc = 50
burnin = 10
```

##

```
fit <- longBet_xbcf(y, x, z, t0, mc, burnin)

plot(t0:t1, rowMeans(fit$tauhat[1,t0:t1,]), type = "l", col = 1, ylim = range(fit$tauhat),lty = 2, ylab

for (i in seq(1, n, length.out = 20)){
    lines(t0:t1, rowMeans(fit$tauhat[i,t0:t1,]), col = 1, lty = 2)}
} lines(t0:t1, rep(0, t1-t0+1), col = 3, lty = 1, lwd = 2)
legend("topleft", legend = c("tauhat"), col = c(1), lty = c(2))

---- tauhat

---- tauhat
```

```
plot(t0:t1, rowMeans(fit$tauhat[1,t0:t1,]) - tau_mat[1,], type = "l", col = 1, ylim = range(fit$tauhat
for (i in seq(1, n, length.out = 20)){
    lines(t0:t1, rowMeans(fit$tauhat[i,t0:t1,]) - tau_mat[i,], col = 1, lty = 2)
}
lines(t0:t1, rep(0, t1-t0+1), col = 3, lty = 1, lwd = 2)
```

35

40

30

t0:t1

25

legend("topleft", legend = c("tauhat - tau"), col = c(1), lty = c(2))

