Theoretical Mechanics Homework 4

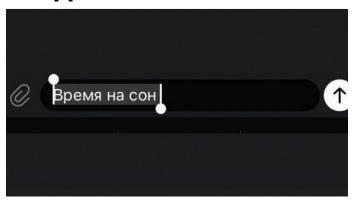
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1 MEME

Me, while doing all the homeworks (i'm slow) and preparing for theoretical mechanics midterms:

КОГДА НАКОНЕЦ-ТО СМОГ ВЫДЕЛИТЬ ВРЕМЯ НА СОН:

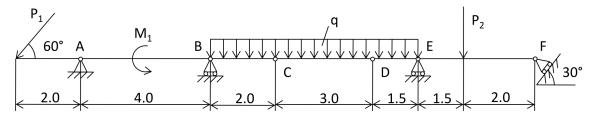


2 LINKS

Link back to GitHub

3 Task 1

3.1 Task description

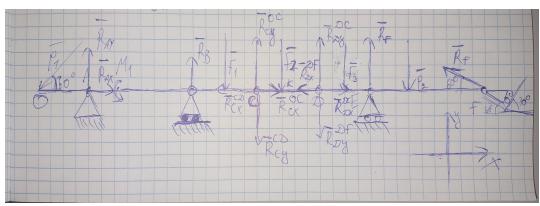


Given:

1.
$$P_1 = 6, P_2 = 10, M_1 = 30, q = 1.5$$

Find all reaction forces on A, B, C, D, E, F

Solution 3.2



Research object: 3 rigid bodies: rods OC, CD, DF

Force analysis:

Points C and D are in equilibrium, it means that reaction forces that are applied on them are compensated, hence, we get: $\vec{R}_{CX}^{CD} = -\vec{R}_{CX}^{OC}; \vec{R}_{CY}^{CD} = -\vec{R}_{CY}^{OC} \\ \vec{R}_{DX}^{DC} = -\vec{R}_{DX}^{DF}; \vec{R}_{DY}^{DC} = -\vec{R}_{DY}^{DF} \\ \text{Let's clarify that:} \\ R_{CX}^{OC} = R_{CX} \text{ and } R_{CY}^{OC} = R_{CY} \\ R_{DY}^{DC} = R_{DY} \text{ and } R_{DX}^{DC} = R_{DX}$

$$\vec{R}_{CY}^{CD} = -\vec{R}_{CY}^{OC}; \vec{R}_{CY}^{CD} = -\vec{R}_{CY}^{OC}$$

$$\vec{R}_{DC}^{DC} = -\vec{R}_{DE}^{DE} \cdot \vec{R}_{DC}^{DC} = -\vec{R}_{DE}^{DE}$$

$$R_{GY}^{OC} = R_{GY}$$
 and $R_{GY}^{OC} = R_{GY}$

$$R_{DV}^{DC} = R_{DV}$$
 and $R_{DV}^{DC} = R_{DV}$

$$O_x : -P_1 \cdot \cos 90^{\circ} + R_{CX}^{OC} + R_{AX} = 0$$

$$O_u: -P_1 \cdot \sin 60^\circ + R_{CV}^{OC} + R_B - F_1 = 0$$

$$\begin{array}{l} 3 \text{ equations for rod } OC : \\ O_x : -P_1 \cdot \cos 90^\circ + R_{CX}^{OC} + R_{AX} = 0 \\ O_y : -P_1 \cdot \sin 60^\circ + R_{CY}^{OC} + R_B - F_1 = 0 \\ M(a) : 2 \cdot P_1 \sin 60^\circ + M_1 + 4 \cdot R_B - 5 \cdot F_1 + 6 \cdot R_{CY}^{OC} = 0 \end{array}$$

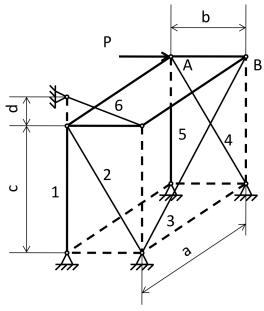
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\begin{array}{l} 3 \text{ equations for rod } CD: \\ O_x: -R_{CX}^{CD} + R_{DX}^{DC} = 0 \\ O_y: -R_{CY}^{CD} + R_{DY}^{DC} = 0 \\ O_y: -R_{CY}^{CD} + R_{DY}^{DC} = 0 \\ M(C): -1.5 \cdot F_2 + 3 \cdot R_{DY}^{DC} = 0 \\ 3 \text{ equations for rod } DF: \\ O_x: -R_{DX}^{DF} - R_F \cdot \cos 60^\circ = 0 \\ O_y: -R_{DY}^{DF} - F_3 + R_E - P_2 + R_F \cdot \sin 60^\circ = 0 \\ M(D): -0.75 \cdot F_3 + 1.5 \cdot R_E - 3 \cdot P_2 + 5 \cdot R_F \cdot \sin 60^\circ = 0 \\ \text{After feeding everything to sympy, it gave me:} \\ R_{AX} = 4.639 \\ R_{AY} = 13.419 \\ R_B = -2.973 \\ R_{CX} = -1.639 \\ R_{CY} = -2.25 \\ R_{DX} = -1.639 \\ R_{DY} = 2.25 \\ R_E = 11.660 \\ R_F = 3.278 \end{array}
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3.3 Answer

$$\begin{split} R_{AX} &= 4.639 \\ R_{AY} &= 13.419 \\ R_B &= -2.973 \\ R_{CX} &= -1.639 \\ R_{CY} &= -2.25 \\ R_{DX} &= -1.639 \\ R_{DY} &= 2.25 \\ R_E &= 11.660 \\ R_F &= 3.278 \end{split}$$

4 Task 2

4.1 Task description

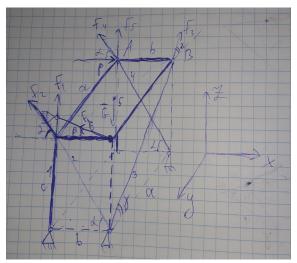


Given:

- 1. G = 10, P = 20;
- $2. \ a=8.5, \ b=2.5, \ c=3.5, \ d=2$

Find reaction forces in rods 1-6

Solution 4.2



Object of study: 1 rigid body.

Force analysis:

Firstly, I need to find angles α , β , γ .

 $\alpha = \arctan \frac{c}{b};$

 $\beta = \arctan \frac{d}{b};$ $\gamma = \arctan \frac{c}{a}.$

Then I can write down projection of forces on O_x , O_y , O_z :

 $O_x : -F_2 \cdot \cos \alpha - F_r \cdot \cos \alpha - F_6 \cdot \cos \beta + P = 0$

 $O_y: -F_3 \cdot \cos \gamma = 0$

 $O_z: F_1 + F_2 \cdot \sin \alpha + F_3 \cdot \sin \gamma + F_4 \cdot \sin \alpha + F_5 + F_6 \sin \beta - G = 0$

And I can write equations of momentums that rotate the plate around x, y, and z axes in point A:

 $\begin{aligned} M_A^x : -F_2 \cdot a \cdot \sin \alpha - F_1 \cdot a - F_6 \cdot a \cdot \sin \beta + G \cdot \frac{a}{2} &= 0 \\ M_A^y : b \cdot F_3 \cdot \sin \gamma + b \cdot F_6 \cdot \sin \beta - G_2^b &= 0 \\ M_A^z : b \cdot F_3 \cdot \cos \gamma - a \cdot F_2 \cdot \cos \alpha - a \cdot F_6 \cdot \cos \beta &= 0. \end{aligned}$

After feeding those 6 equations to sympy, I got this answer:

 $F_1 = 8.750;$

 $F_2 = -10.752;$

 $F_3 = 0.000;$

 $F_4 = 34.409;$

 $F_5 = -23.000;$

 $F_6 = 8.003$

4.3 Answer

$$\begin{split} F_1 &= 8.750; \\ F_2 &= -10.752; \\ F_3 &= 0.000; \\ F_4 &= 34.409; \\ F_5 &= -23.000; \\ F_6 &= 8.003 \end{split}$$