

Advanced course of Measurement and Signal Processing

Assignment II Report

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All the code can be found in the attachment of this report and aslo the Github repo:
<https://github.com/Magicboomliu/Japan-Tide-analysis-forcast>

Task one

“Perform wavelet analysis using Gabor wavelet on air temperature (気温) observation data of 1 year for every hour, and describe what is revealed by the analysis briefly.”

Data source :

Location	Naha(那覇)
Year/Month/Day	2020/01/01-2021/01/01
Amount of data	8760 hours

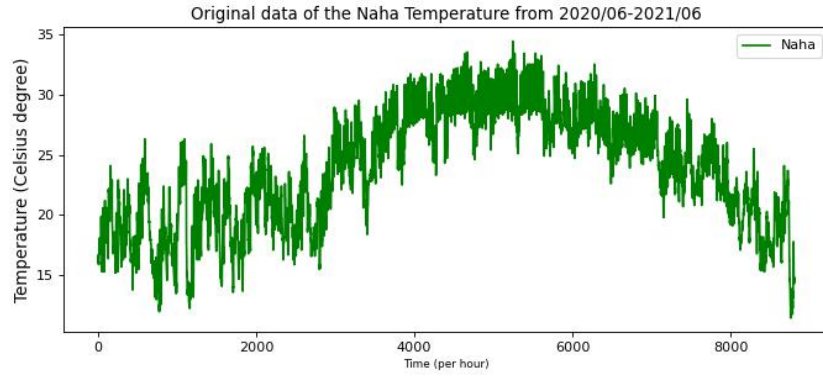
1.1 Introduction

For this task , I mainly use Python to do data processing and Gabor and Morlet transform. The city I choose is Naha(那覇), which is the capital city of the Okinawa Prefecture, the southernmost prefecture of Japan. The following third libraries were used:

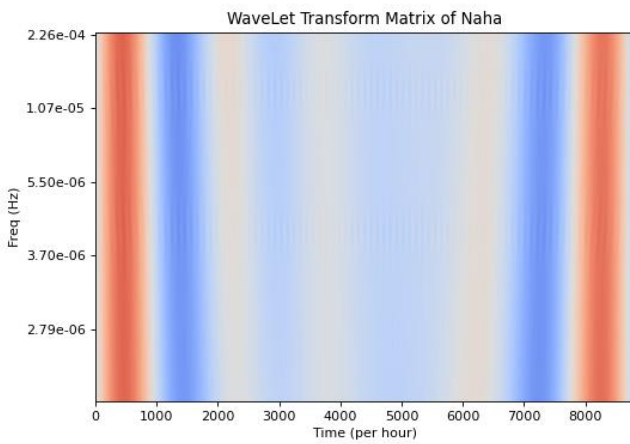
- *Numpy, pandas* : To read data from csv and using bilinear interpolation which using the mean value of nearest 6 values to replace the NaN value.
- *PyWavelets(pywt)*: Do wavelet transform, use *pywt.cwt* function to do the CWT, and set wavelet type as'morl', scales as integers within [1, 3000]. then use the *pywt.scale2frequency* to transfer the scales into the frequencies, and use the sampling period of this data (1 hour or 3600s) to scale the frequency values to Hz.
- *Matlib.pyplot*: For visualization

I draw the related results which in section 1.2 , the y-axis is of the original data is Celesius degree and the y-axis of the Gabor transform is the frequency(Hz). The X-axis of the all the data is the aggregated hours from 2020/01/01 1:00 ~ 2020/01/01 0:00.

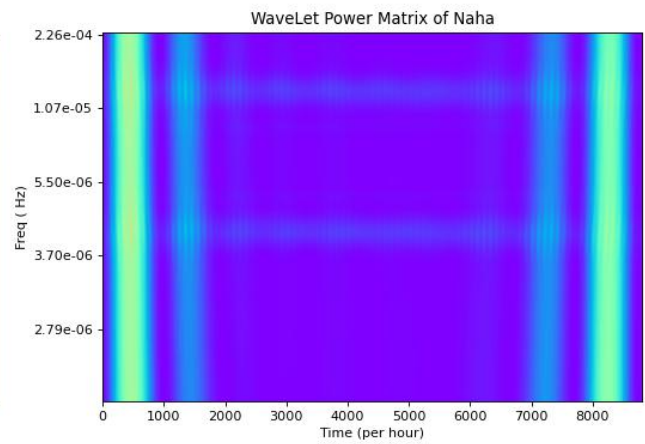
1.2 Gabor (Morlet) Transform Result of NAHA 2020-2021



(a)



(b)



(c)

Fig1 (a) The original temperature observation data from 2020/01/01-2021/01/01, which interval is one hour. (b) The Gabor WaveLet correlation Matrix(using coolwarm cmp, the yellow means bigger correlation and blue means small correlation) (c) The WaveLet Power Matrix(The blue area means smaller, yet the green area means bigger).

1.3 Result Analysis

As we can see from the Correlation Matrix and the Power Spectrum, there are two bright lines in the graph, where indicate that the absolute value of correlation or the power spectrum is quite high. (The 0-1000 hours and the 6800-8700 hours).

And we can also see from graph (b) and graph (c), the Gabor wavelets with the frequency of $1.39e-5$ and $4.23e-5$ have a very high correlation with the temperature wave. The frequency of $1.30e-5$ is corresponding to **23** hours and the frequency of $4.23e-5$ is corresponding to **68** hours. So from the result data, we can say that the temperature changes of 1 day (which is close to 23 hours) and the temperature changes of 3 days (which is close to 68 hours) have a positive and negative correlation to the Gabor walet.

In addition, just like what I have said, there are two bright lines in the graph, where indicate that the absolute value of correlation or the power spectrum is quite high. (The 0-1000 hours and the 6800-8700 hours). This period is from Late November to the Mid-February, the winter season of Naha, shows higher similarity to Gabor wavelet at the frequency ($1.39e-5$ and $4.23e-5$), which the rest of the year do not show the relationship like this. This is possible that because Naha is located in the Okinawa region, the winter temperature changes are affected by the ocean, and there is a strong regularity.

Task Two

“Perform fractal analysis to the wind speed(风速) observational data. Try box count method and power spectrum method. Plot log-log chart and find fractal dimension.”

2.1 Introduction

Location	Kyoto(京都)
Year/Month/Day	2020/01/01-2021/01/01
Amount of data	8760 hours

2.2.1 The power spectrum method

For this task, I mainly use Python to do data processing. And use the Kansei city Kyoto as the data source. Because there is no directly library for fractal analysis, I use the following Api from <https://github.com/inuritdino/HiguchiFractalDimension> to get the *hdf Api* which compile from a C file to use. If you want to run my code, first compile the C file to generate the .so library using following instructions:

```
gcc -shared hfd.c -o libhfd.so -lm -fPIC
```

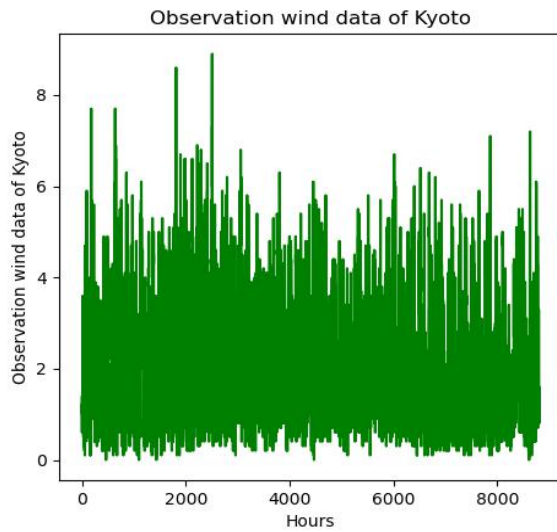
I draw the related results which in section 1.3. I mainly use the numpy library to do the Fourier Transform get the power spectrum. Using the equation $P(f) = k/f^\beta$, here the $P(f)$ is the power spectrum. Then we use log function of $P(f)$ and log function on the right side of the equation:

$$\log(P(f)) = \log(k) - \beta \log(f)$$

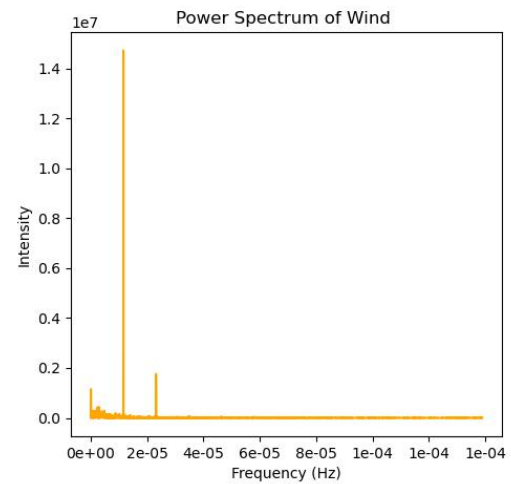
The $-\beta$ here is the slope of the curve $\log(F)$ - $\log(\text{power spectrum})$. The use a Least squares Function to do linear regression to fit the data, as we can see in figure3.

Finally use the the space dimension and the $-\beta$ to calculate the fractal dimension.

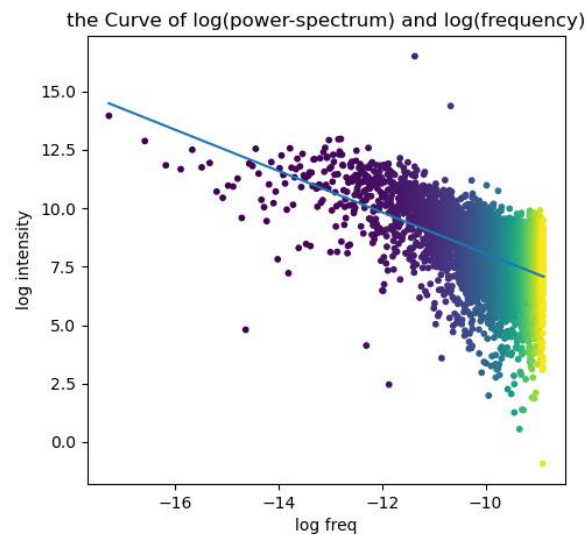
2.2.1.1 Visualization Result



(a)



(b)

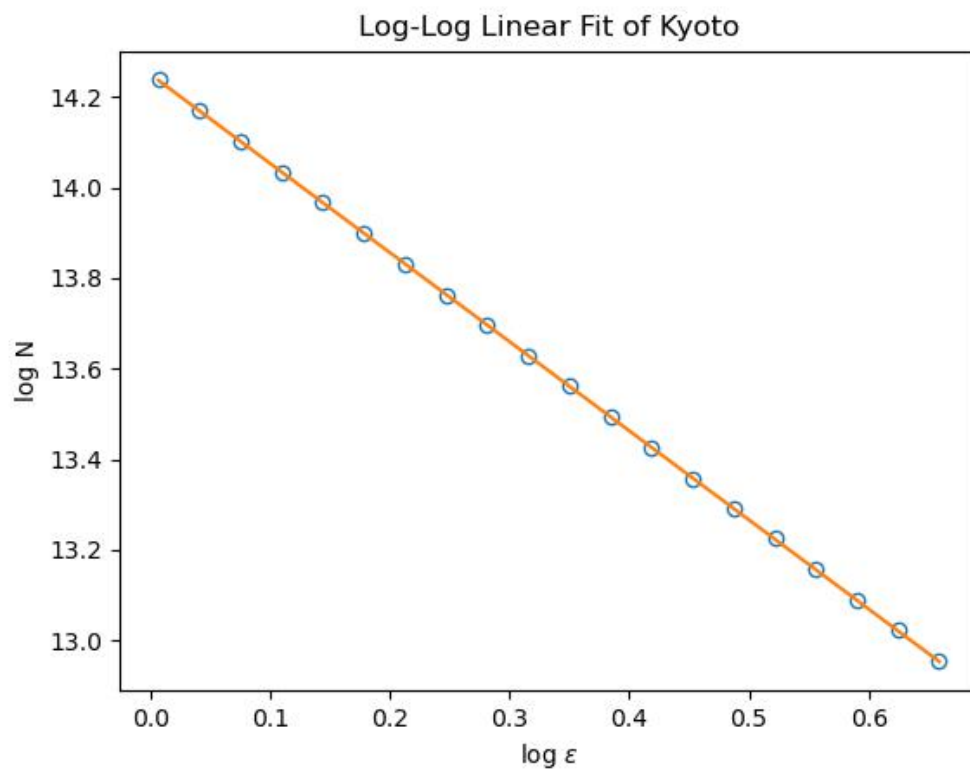


(c)

According to the calculation , the fractal dimension is 1.970823920446978.

2.2.1 The Box count method

For this section, I mainly use python numpy to fo the box counting.The x-axis is the $\log(N)$, (here N is the scale) and the y-axis is the $\log(\epsilon)$. I apply the linear regression on the log-log curve, use the the Hausdorff dimension as thd box count result.



According to the calculation , the fractal dimension is 1.9701293382118037

2.3 Conclusion

Method	Fractal Dimension
Box counting	1.9701293382118037
Power Spectrum	1.970823920446978.