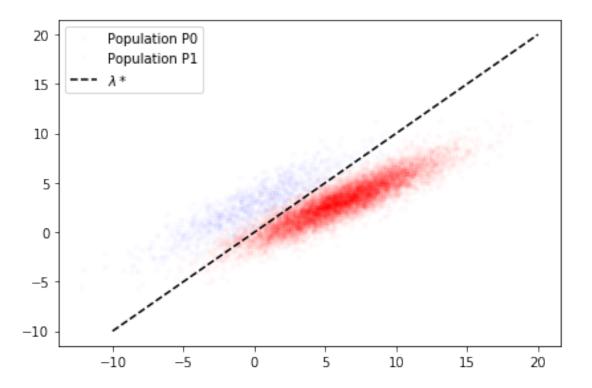
Aufgabe12h

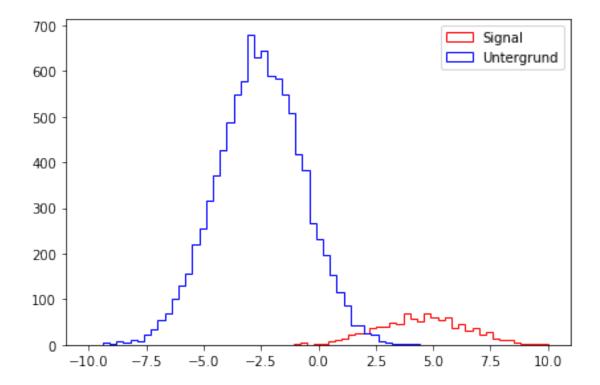
November 15, 2018

Aufgabe 12h

```
In [1]: import pandas as pd
        import matplotlib.pyplot as plt
        import numpy as np
        from numpy.linalg import inv
In [2]: P0 = pd.read_hdf('zwei_populationen.h5', key='P_0_1000')
        P1 = pd.read_hdf('zwei_populationen.h5', key='P_1')
In [3]: PO_x = PO['x']
        PO_y = PO['y']
        P1_x = P1['x']
        P1_y = P1['y']
In [4]: mu_P0_x = np.mean(P0_x)
        mu_P0_y = np.mean(P0_y)
        mu_P1_x = np.mean(P1_x)
        mu_P1_y = np.mean(P1_y)
        print("mu_P0")
        print(mu_PO_x, mu_PO_y)
        print("mu_P1")
        print(mu_P1_x, mu_P1_y)
mu_P0
-0.09576791285523094 2.878846798570514
mu P1
5.986448205069931 3.085282896934817
In [5]: V_P0 = np.cov(P0_x - mu_P0_x, P0_y - mu_P0_y)
        V_P1 = np.cov(P1_x - mu_P1_x, P1_y - mu_P1_y)
        V_P0_P1 = V_P0 + V_P1
        mat_mu = np.mat(((mu_P0_x - mu_P1_x), (mu_P0_y - mu_P1_y))).T
        V_B = mat_mu*mat_mu.T
        print('V_PO', V_PO)
        print('V_P1', V_P1)
        print('V_P0_P1', V_P0_P1)
        print('V_B', V_B)
```

```
V_P0 [[ 12.23612255
                      8.16049883]
 [ 8.16049883
                6.75819008]]
V_P1 [[ 12.35218537
                      7.41075614]
 [ 7.41075614
                5.47731503]]
V_P0_P1 [[ 24.58830792 15.57125497]
 [ 15.57125497 12.2355051 ]]
V_B [[ 36.99335291
                     1.25558896]
 [ 1.25558896  0.04261586]]
In [6]: lambda1 = inv(V_P0_P1)*mat_mu
        print(lambda1)
        \# ay = bx \iff y = b/a x
        a = np.round(-float(lambda1[0]/lambda1[1]))
        print('Geradengleichung: y =', np.round(float(-lambda1[0]/lambda1[1]), 4), 'x')
        \#S\_V\_S\_B = inv(V\_PO\_P1)*V\_B
        #print(S_W_S_B)
        \#Det = (S_W_S_B[0,0])
        #print(Det)
[[-1.21953973]
 [ 1.53514938]]
Geradengleichung: y = 0.7944 x
In [7]: \#mat_mu = np.mat(((-5.4), (-4))).T
        \#V\_B = mat\_mu*mat\_mu.T
        \#V_P0_P1 = np.mat(((13.2, -2.2), (-2.2, 26.4)))
        \#lambda1 = inv(V_P0_P1)*mat_mu
        #print(lambda1)
        \#a = [1, 2, 3]
        #b = [5, 0, 4]
        #print(min(min(a),min(b)))
In [8]: def lin(x,a):
            return x*a
In [9]: x = np.linspace(-10,20)
        plt.plot(P0_x,P0_y,'b.',alpha=0.01,label='Population P0')
        plt.plot(P1_x,P1_y,'r.',alpha=0.01,label='Population P1')
        plt.plot(x, lin(x,a), 'k--',label=r'$\lambda *$')
        plt.legend(loc='best')
        plt.tight_layout()
        plt.show()
```





Wie schon bei den vorherigen Teil habe ich es nicht hinbekommen λ_{cut} als Fkt. von λ bzw. die jeweiligen Fkt. in Abhängigkeit von λ_{cut} darzustellen. Ich habe den Rest so geschrieben, dass wenn man diesen Fehler korrigiert direkt weiter machen kann.

```
In [12]: # Reinheit
         reinh =[]
         #Effizenz
         effiz =[]
         value = []
         # Signal zu Hintergrund
         S_B = []
         # Signifikanz
         sqrt_S_B =[]
         tp = 0
         eff = 0
         fp = 0
         sq_s_b = 0
         fn = 0
         i = 0
         # Hier muss ein Fehler sein
         for x_value in range(-10,10):
              while i < 1000:
                  if x_value < datahist_P0.T[i]:</pre>
                      tp += 1
                  if x_value < datahist_P1.T[i]:</pre>
```

```
fp += 1
                                                          else:
                                                                         fn += 1
                                                           i += 1
                                             rein = tp / (tp + fp)
                                             eff = tp / (tp + fn)
                                             s_b = tp / fp
                                             sq_s_b = tp / (np.sqrt(tp + fp))
                                            reinh.append(rein)
                                             effiz.append(eff)
                                            S_B.append(s_b)
                                             sqrt_S_B.append(sq_s_b)
                                             value.append(x_value)
[-10, -9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
In [13]: \#x\_value = np.linspace(4, 6)
                               \#x\_value = np.linspace(min(min(datahist\_P0), min(datahist\_P1)), max(max(datahist\_P0), max(max(datahist\_P0)), max
                               plt.plot(value, reinh, 'b-', label='Reinheit')
                              plt.plot(value, effiz, 'g-', label='Effizenz')
                               plt.plot(value, S_B,'r-',label='Signal zu Hintergrund')
                              plt.plot(value, sqrt_S_B, 'g-', label='Signifikanz')
                               #plt.legend(loc='best')
                               #plt.tight_layout()
                               plt.show()
                               0.52
                               0.51
                               0.50
                               0.49
                               0.48
                                                  -10.0
                                                                           -7.5
                                                                                                    -5.0
                                                                                                                             -2.5
                                                                                                                                                         0.0
                                                                                                                                                                                  2.5
                                                                                                                                                                                                           5.0
                                                                                                                                                                                                                                   7.5
```

Trotz der 10 fach kleineren Zahl an "Signal"-Werten sind die Ergebnisse wie die Mittelwerte, Kovarianzmatrizen der beiden Verteilungen (P_0_10000 und P_0_1000) nahe zu gleich. Zum Rest kann ich leider nicht sagen :(