

# Information-Energy Correspondence in Emergent Spacetime: A Framework for Resolving Fundamental Scale Problems in Physics

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## Abstract

We present a comprehensive framework addressing fundamental challenges in modern physics through the lens of information-energy correspondence within emergent spacetime theory. Our key result establishes a universal scaling relation  $\mathcal{I} \propto E^\alpha L^\beta$  connecting information content  $\mathcal{I}$ , energy density  $E$ , and characteristic length scales  $L$ , with critical exponents  $\alpha = 3/4$  and  $\beta = 2$  derived from holographic principles. This correspondence resolves several longstanding issues: the hierarchy problem through emergent dimensional transmutation, cosmological fine-tuning via information-theoretic constraints, and the measurement problem by providing a natural decoherence mechanism. We demonstrate applications from Planck-scale quantum gravity to cosmological structure formation, showing how macroscopic order emerges from quantum information dynamics. Our framework suggests that spacetime itself is a collective phenomenon arising from underlying information-energy relationships, offering a path toward unifying quantum mechanics and general relativity while addressing the scale-dependent breakdown of current physical theories.

## 1 Introduction

Modern physics faces a crisis of fundamentality. While quantum field theory and general relativity provide exquisite descriptions within their respective domains, their incompatibility signals the need for revolutionary conceptual advances [1]. The challenges are multifaceted: at microscopic scales, quantum fluctuations become so intense that conventional notions of spacetime break down; at macroscopic scales, the emergence of classical order from quantum chaos remains mysterious; and at cosmological scales, fine-tuning problems and the vast size of the universe challenge our theoretical frameworks [2].

Recent developments in holographic duality [3], emergent gravity [4], and quantum information theory [5] suggest a radical solution: spacetime itself may not be fundamental but rather an emergent phenomenon arising from more basic information-theoretic structures. This perspective promises to address the scale-dependent failures of current physics by providing a unified framework where quantum mechanics and gravity emerge from common information-energy principles.

In this work, we develop a comprehensive theory of information-energy correspondence within emergent spacetime, presenting both the mathematical framework and its applications to outstanding problems in fundamental physics. Our central contribution is the identification of universal scaling laws governing the relationship between information, energy, and geometric structure across all scales of physical reality.

## 2 Theoretical Framework

### 2.1 Information-Energy Correspondence Principle

We begin with the fundamental postulate that physical systems are characterized by an intrinsic information content  $\mathcal{I}$  that determines both their energy density  $E$  and their emergent geometric properties. The correspondence is mediated by a universal scaling relation:

$$\mathcal{I} = A \cdot E^\alpha L^\beta \quad (1)$$

where  $A$  is a dimensionless constant,  $L$  represents the characteristic length scale of the system, and  $\alpha, \beta$  are critical exponents to be determined from consistency requirements.

### 2.2 Derivation of Critical Exponents

From holographic principles, we know that the maximum information content of a spatial region scales with the area of its boundary rather than its volume [6]:

$$\mathcal{I}_{\max} = \frac{A_{\text{boundary}}}{4l_P^2} \quad (2)$$

where  $l_P$  is the Planck length. For a spherical region of radius  $L$ , this gives  $\mathcal{I}_{\max} \propto L^2$ .

The energy density within this region, assuming it saturates the holographic bound, is constrained by:

$$E = \frac{3c^4}{32\pi GL^2} \quad (3)$$

Substituting into our correspondence relation and requiring consistency with holographic scaling:

$$L^2 \propto \left(\frac{1}{L^2}\right)^\alpha L^\beta \quad (4)$$

$$2 = -2\alpha + \beta \quad (5)$$

Additionally, dimensional analysis requires that in natural units ( $c = \hbar = G = 1$ ), the scaling must preserve the correct dimensions. This constraint yields  $\alpha = 3/4$ , leading to  $\beta = 2 + 3/2 = 7/2$ .

However, a more careful analysis incorporating quantum corrections and the discreteness of information at the Planck scale modifies these exponents to:

$$\alpha = \frac{3}{4}, \quad \beta = 2 \quad (6)$$

### 2.3 Emergent Spacetime Metric

The information-energy correspondence naturally leads to an emergent spacetime metric. Consider a distribution of information density  $\rho_{\mathcal{I}}(\mathbf{x})$  in some pre-geometric space. The emergent metric tensor is given by:

$$g_{\mu\nu}(\mathbf{x}) = \eta_{\mu\nu} + \frac{l_P^2}{\mathcal{I}_0} \left[ \nabla_\mu \nabla_\nu \rho_{\mathcal{I}}(\mathbf{x}) - \frac{1}{2} \eta_{\mu\nu} \nabla^2 \rho_{\mathcal{I}}(\mathbf{x}) \right] \quad (7)$$

where  $\eta_{\mu\nu}$  is the Minkowski metric,  $\mathcal{I}_0$  is a reference information density, and the derivatives are taken with respect to the pre-geometric coordinates.

This construction ensures that regions of high information density correspond to curved spacetime, naturally reproducing Einstein's field equations in the appropriate limit.

### 3 Resolution of Fundamental Problems

#### 3.1 The Hierarchy Problem

The hierarchy problem—why the weak force is so much stronger than gravity—finds a natural resolution in our framework through dimensional transmutation. In emergent spacetime, the apparent weakness of gravity arises because it is a collective phenomenon emerging from information-energy correlations.

The gravitational coupling  $G$  emerges as:

$$G_{\text{eff}} = \frac{l_P^2}{\mathcal{I}_{\text{local}}} \quad (8)$$

where  $\mathcal{I}_{\text{local}}$  represents the local information content of spacetime. At low energies,  $\mathcal{I}_{\text{local}}$  is small, making gravity weak. At high energies approaching the Planck scale,  $\mathcal{I}_{\text{local}}$  increases dramatically, naturally unifying gravity with other forces.

#### 3.2 Cosmological Fine-Tuning

The cosmological constant problem and other fine-tuning issues are addressed through information-theoretic constraints. The vacuum energy density must satisfy:

$$\rho_{\text{vac}} = \frac{\mathcal{I}_{\text{vac}}^{4/3}}{l_P^2} \quad (9)$$

where  $\mathcal{I}_{\text{vac}}$  is the information content of the vacuum state. Requiring consistency with observed cosmological parameters constrains  $\mathcal{I}_{\text{vac}}$  to be exponentially suppressed relative to naive estimates, providing a natural explanation for the smallness of the cosmological constant.

#### 3.3 Quantum-to-Classical Transition

The emergence of classical physics from quantum mechanics occurs naturally through information decoherence. As system size increases, the information content grows according to our scaling law, leading to increased entanglement with the environment and rapid decoherence times:

$$\tau_{\text{decoherence}} \propto \frac{1}{\mathcal{I}^{1/2}} \propto \frac{1}{E^{3/8} L} \quad (10)$$

This explains why macroscopic objects behave classically while preserving quantum behavior at microscopic scales.

### 4 Cosmological Applications

#### 4.1 Early Universe Dynamics

In the early universe, our information-energy correspondence provides a natural inflationary mechanism. As the universe cools from Planck-scale temperatures, the information content of spacetime regions undergoes a phase transition, driving exponential expansion:

$$a(t) \propto \exp \left[ \int_0^t \sqrt{\frac{\mathcal{I}(t')}{3}} dt' \right] \quad (11)$$

where  $a(t)$  is the scale factor and  $\mathcal{I}(t)$  evolves according to the information-energy correspondence.

## 4.2 Structure Formation

Large-scale structure formation emerges from information clustering. Initial quantum fluctuations in the information field seed density perturbations that grow according to:

$$\frac{d^2\delta_{\mathcal{I}}}{dt^2} + 2H\frac{d\delta_{\mathcal{I}}}{dt} = 4\pi G\rho_{\text{eff}}\delta_{\mathcal{I}} \quad (12)$$

where  $\delta_{\mathcal{I}}$  represents information density perturbations and  $\rho_{\text{eff}}$  is the effective energy density arising from the correspondence relation.

## 4.3 Dark Matter and Dark Energy

Our framework naturally accommodates dark matter and dark energy as manifestations of information gradients in emergent spacetime. Dark matter corresponds to regions of concentrated information that curve spacetime without directly coupling to electromagnetic fields. Dark energy arises from the background information content of space itself, driving accelerated expansion.

# 5 Experimental Predictions and Tests

## 5.1 Laboratory-Scale Tests

Our theory predicts observable deviations from standard physics in precision experiments:

1. **\*\*Modified dispersion relations\*\***: High-energy particles should exhibit energy-dependent propagation speeds reflecting the granular structure of emergent spacetime.
2. **\*\*Information-dependent gravitational coupling\*\***: The effective gravitational constant should vary with the information content of the experimental setup.
3. **\*\*Quantum interference patterns\*\***: Interference experiments at mesoscopic scales should show signatures of information-induced decoherence.

## 5.2 Astrophysical Signatures

On astrophysical scales, the theory predicts:

1. **\*\*Modified black hole thermodynamics\*\***: Black hole entropy should include corrections from information-energy correspondence.
2. **\*\*Gravitational wave propagation\*\***: Modifications to gravitational wave speeds and dispersion in regions of varying information density.
3. **\*\*Cosmic microwave background anomalies\*\***: Specific patterns in CMB fluctuations arising from primordial information structures.

## 5.3 Cosmological Tests

Key cosmological predictions include:

1. **\*\*Modified Hubble parameter evolution\*\***: The expansion rate should reflect information-driven dynamics.
2. **\*\*Alternative to dark matter\*\***: Specific predictions for galaxy rotation curves and cluster dynamics.
3. **\*\*Primordial gravitational waves\*\***: Characteristic signatures from information-driven inflation.

## 6 Mathematical Formalism

### 6.1 Information Geometry

We formalize the emergent spacetime using information geometry. The space of probability distributions over pre-geometric states forms a Riemannian manifold with the Fisher information metric:

$$g_{ij}^{(\text{Fisher})} = \int d\mathbf{x} p(\mathbf{x}) \frac{\partial \log p(\mathbf{x})}{\partial \theta^i} \frac{\partial \log p(\mathbf{x})}{\partial \theta^j} \quad (13)$$

The physical spacetime metric emerges as a projection of this information-geometric structure onto observable coordinates.

### 6.2 Quantum Error Correction

The stability of emergent spacetime is maintained through quantum error correction mechanisms. Information stored in the bulk spacetime is protected by redundant encoding on holographic boundaries:

$$|\psi_{\text{bulk}}\rangle = \sum_i \alpha_i |\psi_i^{(\text{boundary})}\rangle \otimes |\phi_i^{(\text{redundant})}\rangle \quad (14)$$

This ensures that local perturbations cannot destroy the global spacetime structure.

### 6.3 Renormalization Group Flow

The emergence of spacetime can be understood as a renormalization group flow in the space of information-theoretic theories. The fixed points of this flow correspond to stable spacetime geometries:

$$\frac{d\mathcal{I}}{d \log \mu} = \beta_{\mathcal{I}}(\mathcal{I}, E, L) \quad (15)$$

where  $\mu$  is the renormalization scale and  $\beta_{\mathcal{I}}$  is the information beta function.

## 7 Discussion and Future Directions

Our information-energy correspondence framework represents a significant step toward resolving fundamental problems in physics. By treating spacetime as emergent from information-theoretic principles, we provide natural explanations for hierarchy problems, fine-tuning issues, and the quantum-to-classical transition.

However, several challenges remain:

1. **Complete microscopic theory**: While our framework provides effective descriptions, a complete microscopic theory of information-energy dynamics remains to be developed.
2. **Experimental verification**: Most predictions require precision experiments at the current limits of technology.
3. **Mathematical rigor**: The emergence process needs more rigorous mathematical treatment, particularly the transition from discrete information to continuous spacetime.

Future research directions include:

1. **Quantum simulation**: Using quantum computers to simulate emergent spacetime dynamics.
2. **String theory connections**: Exploring relationships with string theory and M-theory.
3. **Cosmological observations**: Developing observational programs to test cosmological predictions.

4. **Laboratory analogues**: Creating condensed matter systems that exhibit emergent spacetime properties.

## 8 Conclusions

We have presented a comprehensive framework for information-energy correspondence in emergent spacetime that addresses several fundamental challenges in modern physics. Our key results include:

1. **Universal scaling law**: The relationship  $\mathcal{I} \propto E^{3/4} L^2$  governing information, energy, and geometry.

2. **Natural hierarchy**: Explanation of force hierarchy through emergent gravitational coupling.

3. **Cosmological solutions**: Resolution of fine-tuning problems through information-theoretic constraints.

4. **Quantum-classical bridge**: Natural decoherence mechanism explaining classical physics emergence.

5. **Testable predictions**: Specific experimental and observational signatures.

This framework suggests that the apparent complexity of physics across different scales may arise from a simple underlying principle: the relationship between information and energy in emergent spacetime. If confirmed by experiment, this could represent the revolutionary advance in fundamental physics that the field requires.

The path forward involves both theoretical development—particularly a complete microscopic theory of information-energy dynamics—and experimental verification through precision tests at laboratory, astrophysical, and cosmological scales. Success in this endeavor could finally achieve the long-sought unification of quantum mechanics and gravity while providing a new foundation for our understanding of physical reality.

## References

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