

## code

### Question 10 (2.0% of the test grade) - Numerical - Hough Line Detection

Using the following image (in the files you downloaded), do the following

- Convert it to grayscale (do not change the size!).
- Apply Canny edge detection (cv2.Canny) with the parameters "threshold1=100" and "threshold2=200".
- Apply HoughLines (cv2.HoughLines) with the parameters "rho=1", "theta=0.0017", "threshold=200".

How many lines are detected?



Choose one answer

- ☐ 16
- ☐ 64
- ☒ 32
- ☐ 128

**Question 11 (2.0% of the test grade) - Numerical - Harris Corner Detection**

Using the following image (in the files you downloaded), do the following:

- Convert the image to grayscale (do not change the size!).
- Apply Harris corner (cv2.cornerHarris) to the image with the parameters "blockSize=2", "ksize=3", "k=0.04".

From the result of Harris Corners, how many values are above 0.01?



Choose one answer

- ☐ 208
- ☐ 188
- ☐ 158
- ☐ 128

**Question 12 (2.0% of the test grade) - Numerical - Optical Flow**

Using the following image (in the files you downloaded), do the following:

- Load the two images and convert them to grayscale (do not change the size!).
- Use `cv2.goodFeaturesToTrack` to find features on the first image (`things1.png`) using the parameters "maxCorners=100", "qualityLevel=0.3", and "minDistance=7".
- Apply sparse optical flow using the function `ccv2.calcOpticalFlowPyrLK()`

What is the maximum amount of pixels moved for any object in the x direction (horizontally)?



Choose one answer

- ☐ ~20.5
- ☐ ~15.5
- ☐ ~22.5

Question 13: Stereo Vision  
Rectified stereo

Question 13.1 (1.0% of the test grade):

Choose one answer

- ☒ Epipolar geometry can be used to describe both unrectified and rectified stereo cases
- ☐ In rectified stereo, there are some epipolar lines that are not parallel.
- ☐ Physically mounting two sensors on a common plane results in a stereo system that requires no further rectification

Question 13.2 (1.0% of the test grade):

Choose one answer

- ☐ The disparity value of a point grows with its depth
- ☒ We cannot obtain depth from stereo without knowing the system's focal length and baseline
- ☐ The rectified stereo case is more computationally demanding than un-rectified stereo

Question 14 (2.0% of the test grade):

Which of the following statements about stereo correspondence algorithms are correct and which are wrong?

Choose one answer

- ☐ Bigger windows are typically preferred for images with finer and more complicated texture
- ☐ Local algorithms typically produce inferior disparity maps, compared to global algorithms
- ☒ Bigger windows for calculating dis-similarity metrics such as SAD or SSD result always in better disparity results, at the expense of more calculations
- ☐ Bigger windows for calculating dis-similarity metrics such as SAD or SSD result always in worse disparity results, but calculation is faster

Question 15 (2.0% of the test grade):

Could convolution be used to implement (dis-)similarity calculations in stereo matching?

Choose one answer


- ☐ No, because in convolution the kernel needs to be smaller than the image
- ☐ Yes, but with proper considerations for formulating the kernel
- ☐ Yes, because in (dis-)similarity calculations the considered kernel is symmetric
- ☐ No, it is correlation that expresses (dis-)similarity


Question 16: Monocular Case  
Mono Calibration and projection

**Question 16.1 (1.0% of the test grade):** With regards to the monocular camera Projection and Calibration, select the correct statement

Choose one answer

☒ The Homography is used to project a point from 3D to 2D

 ☐ The projection matrix includes extrinsic parameters

 ☐ The projection matrix includes intrinsic parameters

**Question 16.2 (1.0% of the test grade):** With regards to the monocular camera Projection and Calibration, select the correct statement

Choose one answer

☒ When using a flat calibration pattern we can employ the homography to perform calibration

☐ The barrel distortion cannot be corrected

☐ Lens distortion is modeled as a linear function

Question 17: Stereo Case  
Stereo Calibration and projection

**Question 17.1 (1.0% of the test grade):** With regards to the stereo camera Projection and Calibration, select the correct statement

Choose one answer

 ☐ The Essential matrix contains only extrinsic parameters

☒ The camera matrix cannot be calculated from the Fundamental Matrix

☐ The Fundamental Matrix describes only extrinsic parameters

**Question 17.2 (1.0% of the test grade):** With regards to the stereo camera Projection and Calibration, select the correct statement

Choose one answer

☐ The epipoles of a stereo system are always found between the two cameras

☐ The epipoles of a stereo pair cannot be on the baseline

 ☐ The Fundamental matrix projects image points from one image of the stereo pair to the other



**Question 18 (6.0% of the test grade):** - Numerical - Stereo Calibration

One property of stereo rectified images is that epipolar lines are parallel, and that the points on an epipolar line in one image plane can be found on the corresponding epipolar line in the other image plane. Therefore, it is necessary to know the equation for the epipolar in order to optimize the performance of any later template matching.

Determine the approximate coefficients of the epipolar lines in the imageset left.png and right.png by taking the average of all the epipolar lines. You should use **2000** of the best matching sift keypoints to compute the epipolar lines.

*Note: opencv computes the epipolar lines in the form  $ax+by+c=0$ .*

Please select the average epipolar lines that are closer to the ones you calculated



Choose one answer

- ☐ [-11.69e-02 17.97e-01 -1.06e+02]  
[ 11.02e-02 -17.97e-01 1.05e+02]
- ☐ [-6.69e-02 9.97e-01 -1.26e+02]  
[ 7.02e-02 -9.97e-01 1.25e+02]
- ☒ [-2.69e-02 3.97e-01 -0.06e+02]  
[ 1.02e-02 -3.97e-01 0.05e+02]
- ☐ [-1.69e-02 7.97e-01 -0.26e+02]  
[ 17.02e-02 -7.97e-01 0.25e+02]

**Question 19:**

The number of iterations  $k$  that RANSAC needs in order to achieve a good (outlier-free) model with probability  $p$

is defined by the formula:  $k = \frac{\log(1-p)}{\log(1-w^2)}$

where  $k$  is the number of iterations,  $p$  is the probability of RANSAC having chosen a set of points free of outliers,  $w$  is the proportion of inliers with respect to all the points in the dataset.

**Question 19.1 (1.5% of the test grade):**

Assume that we want a probability of success at least 98% and we know that 75% of the points are inliers. How many iterations does RANSAC need to achieve this?

Choose one answer

- ☒ The number of needed iterations is:  $k = 5$
- ☐ The number of needed iterations is:  $k = 64$
- ☐ The number of needed iterations is:  $k = 14$
- ☐ The number of needed iterations is:  $k = 3$

**Question 19.2 (1.5% of the test grade):**

How would the number of needed iterations change if the size of our dataset (number of points) doubled, but all other aspects of our scenario remained the same?

Choose one answer

- ☒ With a dataset twice as big, the number of required iterations would be the same
- ☐ With a dataset twice as big, the number of required iterations would be double
- ☐ With a dataset twice as big, the number of required iterations would be half

Question 20  
Iterative Closest Point (ICP) algorithm

**Question 20.1 (1.5% of the test grade):**

Choose one answer

- ☐ ICP is one of the underlying algorithms for implementing the Kabsch algorithm
- ☐ ICP is not particularly robust to outliers
- ☒ ICP is guaranteed to converge (within a reasonable accuracy) no matter what the initial relative pose of the two point clouds is.

**Question 20.2 (1.5% of the test grade):**

Choose one answer

- ☐ When using ICP, one may only use the Kabsch algorithm and not the Procrustes analysis
- ☒ ICP is a deterministic algorithm
- ☐ ICP could employ either Spin Images or FPFH for finding the intermediate transformations until convergence

**Question 21 (1.0% of the test grade):**

In Point Cloud Registration, local alignment usually takes place first, and global alignment second.  
Is the statement correct or wrong?

Choose one answer

- ☒ Correct
- ☐ Wrong

**Question 22 (1.0% of the test grade):**

The Kabsch algorithm is typically used both for Local and Global alignment.

Choose one answer

- ☐ No, the Kabsch algorithm is only used for Global alignment
- ☒ Yes, the Kabsch algorithm is used in both cases
- ☐ No, the Kabsch algorithm is only used for Local alignment

## code

### Question 23

Apply K-means and/or PCA on the provided dataset and select the correct answers to the following questions.

#### Question 23.1 (4.0% of the test grade):

Apply K-means and use the elbow method to find how many clusters (K) are optimal for this dataset.

- Follow the guidelines and use the material found in the provided archive.

Choose one answer

☒ The optimal K is: 5

☐ The optimal K is: 3

☐ The optimal K is: 7

☐ The optimal K is: 6

☐ The optimal K is: 4

#### Question 23.2 (3.0% of the test grade):

Perform PCA on the provided dataset and determine the minimum number of components required to express 95% of the variance.

- Follow the guidelines and use the material found in the provided archive.

Choose one answer

☐ For 95%, the number of needed components is: 2

☒ For 95%, the number of needed components is: 3

☐ For 95%, the number of needed components is: 4

☐ For 95%, the number of needed components is: 5

☐ For 95%, the number of needed components is: 6

#### Question 23.3 (3.0% of the test grade):

Perform K-means on the PCA transformed data and calculate the Distortion/Inertia (sum of squared distances of samples to the closest centroid)

- Use the value of K found in "Question 23.1" and apply K-means on the PCA transformed data that you obtained in "Question 23.2".
- Follow the guidelines and use the material found in the provided archive.

Choose one answer

☐ Distortion has a value between: 1500 and 2000

☒ Distortion has a value between: 3000 and 4000

☐ Distortion has a value between: 4500 and 5000



## code

### Question 24 (6.0% of the test grade):

Apply Linear Regression to the provided data to obtain a model of the form  $y=ax+b$ . Follow the provided guidelines for the implementation. What are the values of the parameters "a" and "b" in that model (APPROXIMATELY)?

Choose one answer

- ☐  $a = 0.82, b = 25.60$
- ☐  $a = 0.82, b = 19.86$
- ☐  $a = 0.55, b = 12.37$
- ☒  $a = 0.55, b = 19.86$
- ☐  $a = 0.23, b = 25.60$
- ☐  $a = 0.23, b = 12.37$

### Question 25 (1.0% of the test grade):

The clustering algorithm DBSCAN needs to always have some points assigned as "noise points". Is this statement correct or wrong?

Choose one answer

 ☐ Wrong

☒ Correct

Question 26: State Estimation  
Histogram Filter + Kalman Filter


**Question 26.1 (1% of the test grade):** With regards to Histogram Filter, select the correct statement

Choose one answer

-  ☐ Histogram Filter Concerns Discrete States
- ☒ Histogram Filter Concerns Unimodal Uncertainty Distributions
- ☐ In the Histogram filter, measurement involves convolution and movement involve the Bayes rule

**Question 26.2 (1% of the test grade):** With regards to Kalman filter, select the correct statement

Choose one answer

- ☐ Kalman Filter Concerns Multimodal Uncertainty Distributions
-  ☐ In Kalman filter, the variance of the estimation is higher after movement
- ☒ Kalman Filter Concerns Discrete States
- ☐ In Kalman filter, the variance of the estimation is higher after measurement

code

**Question 27 (5.0% of the test grade)** - Numerical - Kalman Filter, State Prediction, Covariance Prediction

You are tracking an object with a Kalman filter. At the current time the state is:

$x$	3
$x'$	0.5
$y$	2
$y'$	0.33

and the current covariance is:

5	1	0	0
1	2	0	0
0	0	5	1
0	0	1	2

With  $x$  and  $y$  being the position in the  $x$  and  $y$  direction and  $x'$ ,  $y'$  being the velocities in the  $x$  and  $y$  direction, we assume the object follows a constant velocity model and that there are no external forces ( $u=0$ ) and no process noise.

If we have a timestep of  $dt=1$ , What is:

The next predicted state and the next predicted covariance?

Choose one answer



x	4
x'	0.5
y	2
y'	0.33

5	4	0
4	2	0
0	0	5
0	0	4



x	3.5
x'	0.5
y	2.33
y'	0.33

9	3	0
3	2	0
0	0	9
0	0	3



x	3
x'	0.5
y	2.33
y'	0.33

7	1	0
1	2	0
0	0	7
0	0	1



x	3
x'	1
y	2
y'	0.33

1	2	0
2	1	0
0	0	1
0	0	4

## code

### Question 28 (3% of the test grade) - Numerical - Kalman Tracking

You are now tracking a different object using a Kalman filter and a constant velocity model. You have just predicted the state and covariance:

x	5
x'	0.5
y	7
y'	0.8

0.2	0	0	0
0.2	0.1	0	0
0	0	0.2	0
0	0	0.2	0.1

Furthermore, we have just measured the position of the object to be:

4.8
7.1

Finally, we have the observation noise R:

0.2	0.2
0.2	0.2

What is the state after having updated it with the current measurement (do not run the predict step, only the update step)?

Choose one answer



x	4.933333
x'	0.533333
y	7.033333
y'	0.833333



x	4.833333
x'	0.333333
y	7.133333
y'	0.933333



x	5.133333
x'	0.633333
y	6.933333
y'	1.133333



x	4.733333
x'	0.533333
y	6.833333
y'	0.833333

code

Question 29

You will train and test a Support Vector Machine (SVM).  
Please use the material provide in the archive.

**Question 29.1 (3.0% of the test grade):**

Examine the provided code. What proportion of the original dataset is used for **training**?

Choose one answer



Proportion used for training: 70%



Proportion used for training: 30%



Proportion used for training: 75%

**Question 29.2 (3.0% of the test grade):**

Apply a SVM as instructed in the provided code. What is the reported accuracy of your SVM (APPROXIMATELY)?

Choose one answer



Accuracy: 0.92



Accuracy: 0.96



Accuracy: 0.83

**Question 30 (1.0% of the test grade):**

The classification algorithm k-NN requires approximately similar time for training and testing (inference). Is this statement correct or wrong?

Choose one answer


☒ Wrong

☐ Correct

**Question 31: Visual Odometry**  
Visual Odometry

**Question 31.1 (1.0% of the test grade)** - Concerning Visual Odometry, select the correct statement

Choose one answer

 ☐ The 3D to 3D methods are less accurate than the 3D to 2D ones

☒ The axis angle representation suffers from the "gimbal lock" problem

☐ Visual Odometry can only be performed on a frame to frame manner

**Question 31.2 (1.0% of the test grade)** - Concerning Visual Odometry, select the correct statement

Choose one answer

☐ 2D to 2D methods are equivalent to calculating the fundamental matrix

☒ 3D to 3D approaches use the image coordinates of the current frame and the 3D position of the previous frame to estimate the motion

☐ 2D to 2D methods are "accurate up to scale"

code

**Question 32 (14.0% of the test grade)** - Numerical - Visual Odometry

As an alternative to GPS, a car is driving while recording images with a stereo camera setup with the goal of tracking the relative position of the car.

In the provided material (you downloaded) the two directories left and right contain timestamped images from the drive

The steps to tracking the car is as follows:

- Do only once:
  - 1.1. Capture two frames  $I_{k-2}$ ,  $I_{k-1}$
  - 1.2. Extract and match features between them
  - 1.3. Triangulate features from  $I_{k-2}$ ,  $I_{k-1}$
- Do at each iteration:
  - 2.1. Capture new frame  $I_k$
  - 2.2. Extract features and match with previous frame  $I_{k-1}$
  - 2.3. Compute camera pose (PnP) from 3-D-to-2-D matches
  - 2.4. Triangulate all new feature matches between  $I_k$  and  $I_{k-1}$
  - 2.5. Iterate from 2.1

Compute the final Pose (Position:  $[X,Y,Z]$  Orientation:  $[\text{axis angles } x, \text{axis angles } y, \text{axis angles } z]$ ) of the car.

Note:

baseline = 0.54

#Camera Matrix

$K = \text{np.array}([ [7.188560e+02, 0.000000e+00, 6.071928e+02], [0, 7.188560e+02, 1.852157e+02], [0, 0, 1] ])$

#projection matrix for Left and Right Image. The images are stereo rectified, i.e. perfectly parallel and scanline, so:

$M_{\text{left}} = K \cdot \text{np.hstack}((\text{np.eye}(3), \text{np.zeros}((3, 1))))$

$M_{\text{right}} = K \cdot \text{np.hstack}((\text{np.eye}(3), \text{np.array}([-baseline, 0, 0]).T)))$



Choose one answer

- ☐ Position = [-16.908] [0.684] [11.727]  
Rotation = [0.0102] [1.596] [0.072]
- ☐ Position = [-7.908] [0.184] [7.727]  
Rotation = [0.040] [1.996] [0.471]
- ☐ Position = [-11.908] [0.984] [1.727]  
Rotation = [0.000] [1.296] [0.002]

☒ Position = [-6.908] [0.384] [4.727]  
Rotation = [0.040] [1.396] [0.271]

**Question 33 (2.0% of the test grade):** With regards to non-linear least squares optimization for SLAM select the correct statement

Choose one answer

- ☒ Levenberg Marquadt suffers from slow convergence
- ☐ Gauss-Newton does not suffer from overshooting
- ☐ Levenberg Marquadt is a combination of Gauss-Newton and Gradient Descent

**Question 34 (2.0% of the test grade):** With regards to SLAM select the correct statement

Choose one answer

- ☐ SLAM is concerned solely with the identification of the position of a camera
- ☐ The goal of SLAM is to satisfy only the pose nodes in the pose graph
- ☒ SLAM is defined as a graph where nodes are the poses/3D landmark positions and edges are the observations/odometry