

Session for lecture 11: Understanding Program Efficiency: 2

LAST TIME

- *The important performance measures for programs*
- *Methods for evaluating program performance*
- *“Big-oh” notation*
- *Estimating the running time of programs using the big-oh notation*

TODAY

- *Classes of complexity*
- *Examples characteristic of each class*

1. $O(1)$ denotes constant running time
2. $O(\log n)$ denotes logarithmic running time
3. $O(n)$ denotes linear running time
4. $O(n \log n)$ denotes log-linear running time
5. $O(n^c)$ denotes polynomial running time (c is a constant)
6. $O(c^n)$ denotes exponential running time (c is a constant being raised to a power based on size of input)

Hints: you may make use of the following functions.

```
import time
import random
def plot(sizes, times):
    import matplotlib.pyplot as plt
    plt.figure()
    plt.plot(sizes, times)
    plt.xlabel("Sizes")
    plt.ylabel("Times(s)")
    plt.grid(True, which="both")
    plt.show()

def generate_list(length):
    L = []
    for i in range(length):
        L.append(random.randint(1,1000))
    return L
```

Q.1 [1 mk] → run the following program and notice its complexity order.

```
def someFunction(x,y):
    return x**y

t = []
s = []
for i in range(5, 25):
    time_start = time.clock()
    someFunction(i, i)
    time_end = time.clock() - time_start
    t.append(time_end)
    s.append(i)
plot(s,t)
```

Q.2 [1 mk] → run the following program and notice its complexity order.

```
def bisect_search(L, e):
    def bisect_search_helper(L, e, low, high):
        #print('low: ' + str(low) + '; high: ' + str(high)) #added to visualize
        if high == low:
            return L[low] == e
        mid = (low + high)//2
        if L[mid] == e:
            return True
        elif L[mid] > e:
            if low == mid: #nothing left to search
                return False
            else:
                return bisect_search_helper(L, e, low, mid - 1)
        else:
            return bisect_search_helper(L, e, mid + 1, high)
    if len(L) == 0:
        return False
    else:
        return bisect_search_helper(L, e, 0, len(L) - 1)
```

```
# testList = []
# for i in range(100):
#     testList.append(i)
# test the code
# print(bisect_search(testList, 76))
```

```
for i in range(1, 5):
    L = generate_list(10**i)
    time_start = time.clock()
    bisect_search(L, len(L))
    time_end = time.clock() - time_start
    t.append(time_end)
    s.append(i)
plot(s,t)
```

Q.3 [1 mk] → run the following program and notice its complexity order.

```
def linear_search(L, e):
    found = False
    for i in range(len(L)):
        if e == L[i]:
            found = True
    return found

for i in range(1, 5):
    L = generate_list(10**i)
    time_start = time.clock()
    linear_search(L, len(L))
    time_end = time.clock() - time_start
    t.append(time_end)
    s.append(i)
plot(s,t)
```

Q.4 [1 mk] → run the following program and notice its complexity order.

```
def bubbleSort(L):
    for i in range(len(L)):
        for j in range(len(L)-i-1): # Last i elements are already in place
            if L[j] > L[j+1]:
                tmp = L[j]
                L[j] = L[j+1]
                L[j+1] = tmp

for i in range(1, 5):
    L = generate_list(10**i)
    time_start = time.clock()
    bubbleSort(L)
    time_end = time.clock() - time_start
    t.append(time_end)
    s.append(i)
plot(s,t)
```

Q.5 [1 mk] → run the following program and notice its complexity order.

```
def fibonacci(n):  
    if n <= 2:  
        return 1  
    else:  
        return fibonacci(n-1) + fibonacci(n-2)  
t = []  
s = []  
for i in range(5, 25):  
    time_start = time.clock()  
    fibonacci(i)  
    time_end = time.clock() - time_start  
    t.append(time_end)  
    s.append(i)  
plot(s,t)
```

“Take pride in how far you’ve come. Have faith in how far you can go. But don’t forget to enjoy the journey.”