## **WORKSHEET STATISTICS WORKSHEET-1**

Q1 to Q9 have only one correct answer. Choose the correct option to answer your question.

- 1. Bernoulli random variables take (only) the values 1 and 0.
- a) True b) False

Answer :True

- 2. Which of the following theorem states that the distribution of averages of iid variables, properly normalized, becomes that of a standard normal as the sample size increases?
- a) Central Limit Theorem
- b) Central Mean Theorem
- c) Centroid Limit Theorem
- d) All of the mentioned

Answer: Central Limit theorem

- 3. Which of the following is incorrect with respect to use of Poisson distribution?
- a) Modeling event/time data
- b) Modeling bounded count data
- c) Modeling contingency tables
- d) All of the mentioned

Answer: Modeling Bounded count data.

- 4. Point out the correct statement.
- a) The exponent of a normally distributed random variables follows what is called the lognormal distribution
- b) Sums of normally distributed random variables are again normally distributed even if the variables are dependent
- c) The square of a standard normal random variable follows what is called chi-squared distribution
- d) All of the mentioned

Answer: d) All of the mentioned

- 5. random variables are used to model rates.
- a) Empirical
- b) Binomial
- c) Poisson
- d) All of the mentioned

Answer: Poisson

- Usually replacing the standard error by its estimated value does change the CLT.
- a) True b) False

Answer: False

- 7. Which of the following testing is concerned with making decisions using data?
- a) Probability
- b) Hypothesis
- c) Causal
- d) None of the mentioned

Answer: Hypothesis

- 8. Normalized data are centered at\_\_\_\_\_and have units equal to standard deviations of the original data.
- a) 0
- b) 5
- c) 1
- d) 10

Answer: 0

- 9. Which of the following statement is incorrect with respect to outliers?
- a) Outliers can have varying degrees of influence
- b) Outliers can be the result of spurious or real processes
- c) Outliers cannot conform to the regression relationship
- d) None of the mentioned

Answer: Outliers cannot conform to the regression relationship

Q10and Q15 are subjective answer type questions, Answer them in your own words briefly.

10. What do you understand by the term Normal Distribution?

Answer: The normal distribution is a continuous probability distribution that is symmetrical around its mean, most of the observations cluster around the central peak, and the probabilities for values further away from the mean taper off equally in both directions. Extreme values in both tails of the distribution are similarly unlikely. While the normal distribution is symmetrical, not all symmetrical distributions are normal. For example, the Student's t, Cauchy, and logistic distributions are symmetric.

The normal distribution, also known as the Gaussian distribution, is the most important probability distribution in statistics for independent, random variables.

## 11. How do you handle missing data? What imputation techniques do you recommend?

Answer: Missing data appear when no value is available in one or more variables of an individual. Due to Missing data, the statistical power of the analysis can reduce, which can impact the validity of the results. After classified the patterns in missing values, it needs to treat them.

Deletion:

The Deletion technique deletes the missing values from a dataset. followings are the types of missing data.

Listwise deletion:Listwise deletion is preferred when there is a Missing Completely at Random case. In Listwise deletion entire rows(which hold the missing values) are deleted. It is also known as complete-case analysis as it removes all data that have one or more missing values. Listwise deletion is not preferred if the size of the dataset is small as it removes entire rows if we eliminate rows with missing data then the dataset becomes very short and the machine learning model will not give good outcomes on a small dataset.

#### Pairwise Deletion:

Pairwise Deletion is used if missingness is missing completely at random i.e MCAR.Pairwise deletion is preferred to reduce the loss that happens in Listwise deletion. It is also called an available-case analysis as it removes only null observation, not the entire row.

# Imputation techniques:

The imputation technique replaces missing values with substituted values. The missing values can be imputed in many ways depending upon the nature of the data and its problem. Imputation techniques can be broadly they can be classified as follows:

## Mean imputation

Calculate the mean of the observed values for that variable for all non-missing people. It has the advantage of maintaining the same mean and sample size, but it also has a slew of drawbacks. Almost all of the methods described below are superior to mean imputation.

#### Substitution

Assume the value from a new person who was not included in the sample. To put it another way, pick a new subject and employ their worth instead.

## Hot deck imputation

A value picked at random from a sample member who has comparable values on other variables. To put it another way, select all the sample participants who are comparable on other factors, then choose one of their missing variable values at random.

One benefit is that you are limited to just feasible values. In other words, if age is only allowed to be between 5 and 10 in your research, you will always obtain a value between 5 and 10.Another factor is the random element, which introduces some variation. For exact standard errors, this is crucial.

## Cold deck imputation

A value picked deliberately from an individual with similar values on other variables. In most aspects, this is comparable to Hot Deck, but without the random variance. As an example, under the same experimental condition and block, you can always select the third individual.

#### Regression imputation

The result of regressing the missing variable on other factors to get a predicted value. As a result, instead of utilizing the mean, you're relying on the anticipated value, which is influenced by other factors. This keeps the associations between the variables in the imputation model, but not the variability around the anticipated values.

## Stochastic regression imputation

The predicted value of a regression plus a random residual value. This has all of the benefits of regression imputation plus the random component's benefits. The majority of multiple imputation is based on stochastic regression imputation.

# Interpolation and extrapolation

An estimate based on other observations made by the same person. It generally only works with data that is collected over time. Proceed with caution, though. For a variable like height in children—one that cannot be reduced through time—interpolation would make more sense. Extrapolation entails estimating beyond the data's true range, which necessitates making more assumptions than is necessary.

# 12. What is A/B testing?

Answer: A/B testing is a basic randomized control experiment. It is a way to compare the two versions of a variable to find out which performs better in a controlled environment.

For instance, let's say you own a company and want to increase the sales of your product. Here, either you can use random experiments, or you can apply scientific and statistical methods. A/B testing is one of the most prominent and widely used statistical tools.

# 13. Is mean imputation of missing data acceptable practice?

#### 14. What is linear regression in statistics?

Answer: Linear regression is a basic and commonly used type of predictive analysis. The overall idea of regression is to examine two things: (1) does a set of predictor variables do a good job in predicting an outcome (dependent) variable? (2) Which variables in particular are significant predictors of the outcome variable, and in what way do they-indicated by the magnitude and sign of the beta estimates-impact the outcome variable? These regression estimates are used to explain the relationship between one dependent variable and one or more independent variables. The simplest form of the regression equation with one dependent and one independent variable is defined by the formula y = c + b\*x, where y = estimated dependent variable score, c = constant, b = regression coefficient, and x = score on the independent variable.

Naming the Variables. There are many names for a regression's dependent variable. It may be called an outcome variable, criterion variable, endogenous variable, or regressand. The independent variables can be called exogenous variables, predictor variables, or regressors.

Three major uses for regression analysis are (1) determining the strength of predictors, (2) forecasting an effect, and (3) trend forecasting.

#### 15. What are the various branches of statistics?

Answer: Statistics is a method of interpreting, analysing and summarising the data. Hence, the types of statistics are categorised based on these features: Descriptive and inferential statistics. Based on the representation of data such as using pie charts, bar graphs, or tables, we analyse and interpret it.

Statistics is the application of Mathematics, which was basically considered as the science of the different types of stats. For example, the collection and interpretation of data about a nation like its economy and population, military, literacy, etc.

# **Descriptive Statistics**

In this type of statistics, the data is summarised through the given observations. The summarisation is one from a sample of population using parameters such as the mean or standard deviation.

Descriptive statistics is a way to organise, represent and describe a collection of data using tables, graphs, and summary measures. For example, the collection of people in a city using the internet or using Television.

Descriptive statistics are also categorised into four different categories:

- Measure of frequency
- Measure of dispersion
- Measure of central tendency
- Measure of position

The frequency measurement displays the number of times a particular data occurs. Range, Variance, Standard Deviation are measures of dispersion. It identifies the spread of data. Central tendencies are the mean, median and mode of data. And the measure of position describes the percentile and quartile ranks.

## Inferential Statistics

This type of statistics is used to interpret the meaning of Descriptive statistics. That means once the data has been collected, analysed and summarised then we use these stats to describe the meaning of the collected data. Or we can say, it is used to draw conclusions from the data that depends on random variations such as observational errors, sampling variation, etc.

Inferential Statistics is a method that allows us to use information collected from a sample to make decisions, predictions or inferences from a population. It grants us permission to give statements that goes beyond the available data or information. For example, deriving estimates from hypothetical research.