

**TARGET : JEE (M + A) : 2026**

**CLASS : IIT-NURTURE (ELITE) PHASE - I & II**

**TEST TYPE: OFFLINE**

**DATE : 13.07.2026**

**PATTERN : JEE ADVANCED**

**Time : 3 Hours**

**INTERNAL TEST - 04**

**Maximum Marks : 198**

**Student's Form No. : .....**

**Batch : .....**

**Student's Name : .....**

## INSTRUCTIONS

**READ THE INSTRUCTIONS CAREFULLY**

### QUESTION PAPER FORMAT AND MARKING SCHEME

- The question paper has **three parts** : **PHYSICS, CHEMISTRY and MATHEMATICS**. Each part has **THREE SECTIONS**.
- Carefully read the instructions given at the beginning of each section.
- Section I(i):** This section contains **SIX (06)** questions. Each question has Four options (A), (B), (C) and (D). **ONLY ONE** of these four options is correct. **SINGLE CHOICE QUESTIONS**  
**Marking scheme** : +3 for correct answer, 0 if not attempted and -1 in all other cases.
- Section I(ii):** This section contains **SIX (06)** questions. The Answer to each question is a **ONE OR MORE THAN ONE CORRECT OPTIONS (MCQ)**  
**Marking scheme** : +4 for correct answer, 0 if not attempted and -2 in all other cases.  
*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen.  
*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct options.  
*Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option.
- Section II:** This section contains **SIX (06)** questions. **The answer to each question is a NUMERICAL VALUE.**  
**Marking scheme** : +4 If **ONLY** the correct numerical value is entered. 0 In all other cases.

## ALLEN South India Campuses

### Bengaluru Campuses

#### Jayanagar Campus (HO)

No. 36, 15th Cross, 3rd Block, Near Southend Circle,  
Opp. City Central Library, Jayanagar, Bengaluru-560011  
Tel : 080-46704000

Jayanagar I Koramangala I Marathahalli I  
Banashwadi I Hebbal I Hsr Layout I Bannerghatta  
Basaveshwara Nagar I Sarjapura I Jalahalli  
Indiranagar I Whitefield

### Mysuru Campus

#### Saraswathipuram Campus

B.M. Arcade, No-2923, 1st Main, 5th Cross,  
Saraswathipuram, Opp. SVC Bank, Mysuru-570009  
Tel : 0821-4526818, 9945588588

### Mangaluru Campus

#### B1 Vikaas Pre-University College

Vikas Group of institutions, Airport Road,  
Mary Hill Mangaluru, Karnataka-575008  
Tel : 9900090058

### Chennai Campuses

#### Ashok Nagar Campus (HO)

No. 346 & 347, Next to Kasi Theater,  
Jafferkhanpettai, Ashok Nagar, Chennai-600083  
Tel : 9116687301/302

#### Madipakkam Campus

Pathima Markaz Building, Plot Nos. 14 & 19 and 15 & 18,  
Madipakkam velachery Main Road, Near Nakshatra Restaurant,  
Ram Nagar, Madipakkam, Chennai - 600091, Tel : 9116687303/304

#### Anna Nagar West Campus

Newry Square, No. 99, 13th Main Road, 6th Avenue,  
1st Block, Anna Nagar West, Chennai-600040  
Tel : 6366366903/904

#### Adyar Campus

No. 7, City Tower, 2nd Floor, 3rd Cross Street,  
Kasthuribai Nagar, Adyar, Chennai-600020  
Tel : 9116687307/308

### Paavai Campus

#### Sholinganallur Campus

S.M.J. Tower, Door No.16, IT Expressway,  
Beside Novotel, Old Mahabalipuram Road,  
Sholinganallur, Chennai-600119  
Tel : 6366366901/902

#### Anna Nagar East Campus

New No. 80, Old No. 419, Kilpauk  
Garden Road, Anna Nagar East,  
Chennai-600010  
Tel : 9116687305/306

Paavai Vidya Nagar Puduchatram, Service  
Road Paavai Tamil Nadu-637018  
Tel.: 9611994455, 9566404272

### Kochi Campuses

#### Palarivattom Campus (HO)

RK Commercial, PJ Antony Cross  
Road, Palarivattom, Kochi-682025  
Tel : 9116687309/310

#### M.G. Road Campus

Primer Plaza, AK Sheshadiri Road, Near  
Maharajas College Ground, Kochi - 682011  
Tel : 9116687309/310

### Puducherry Campuses

#### Vedam Campus (HO)

No. 372 & 374, Bharathi Street,  
Puducherry-605001  
Tel : 9900804950, 9741303080

#### Gurugram Campus

VIP Nagar, Villianur Main Road,  
Arumparthapuram, Puducherry-605110  
Tel : 9900804950, 9741018090

### Tirupati Campuses

#### AIR Road Campus

#170, First Floor, Above MGB Bajaj, New Balaji  
Colony AIR bypass road, Tirupati - 517501  
Tel.: 9900070050

#### Residential Campus

D.No. 162, Vedanthapura Agraharam,  
NR Layout, R.C. Road, Tirupati -517507  
Tel.: 9900070050

### Coimbatore Campus

35, 7th street Tatabad, Gandhipuram  
Coimbatore - 641012,  
Tel : 9606071654, 9900963850

SOME USEFUL CONSTANTS		
<b>Atomic No.</b>	H = 1, B = 5, C = 6, N = 7, O = 8, F = 9, Al = 13, P = 15, S = 16, Cl = 17, Br = 35, Xe = 54, Ce = 58,	
<b>Atomic masses :</b>	H = 1, Li = 7, B = 11, C = 12, N = 14, O = 16, F = 19, Na = 23, Mg = 24, Al = 27, P = 31, S = 32, Cl = 35.5, Ca = 40, Fe = 56, Br = 80, I = 127, Xe = 131, Ba = 137, Ce = 140,	
•	<b>Boltzmann constant</b>	$k = 1.38 \times 10^{-23} \text{ JK}^{-1}$
•	<b>Coulomb's law constant</b>	$\frac{1}{4\pi\epsilon_0} = 9 \times 10^9$
•	<b>Universal gravitational constant</b>	$G = 6.67259 \times 10^{-11} \text{ N-m}^2 \text{ kg}^{-2}$
•	<b>Speed of light in vacuum</b>	$c = 3 \times 10^8 \text{ ms}^{-1}$
•	<b>Stefan-Boltzmann constant</b>	$\sigma = 5.67 \times 10^{-8} \text{ Wm}^{-2}\text{-K}^{-4}$
•	<b>Wien's displacement law constant</b>	$b = 2.89 \times 10^{-3} \text{ m-K}$
•	<b>Permeability of vacuum</b>	$\mu_0 = 4\pi \times 10^{-7} \text{ NA}^{-2}$
•	<b>Permittivity of vacuum</b>	$\epsilon_0 = \frac{1}{\mu_0 c^2}$
•	<b>Planck constant</b>	$h = 6.63 \times 10^{-34} \text{ J-s}$

## INTERNAL TEST - 04 IIT-NURTURE (ELITE)

### PHASE 1 & 2

<b>PATTERN : JEE ADVANCED</b>		<b>DATE: 13.07.2026</b>
<b>SYLLABUS</b>		
<b>PHYSICS</b>	:	Mathematical Tools & Vectors, Rectilinear Motion, Projectile Motion, Relative Motion.
<b>CHEMISTRY</b>	:	Atomic Structure And Some Basic Concept Of Chemistry.
<b>MATHS</b>	:	Basic Mathematics Including Logarithm (Except trig. Formula & limits).

PHYSICS

SECTION-I(i) : (Maximum Marks: 18)

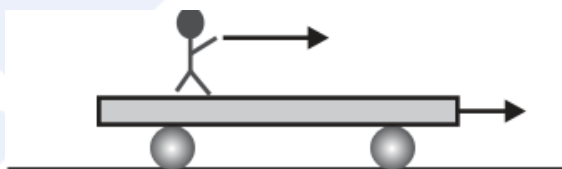
- This section contains **SIX (06)** questions.
- Each question has Four options (A), (B), (C) and (D). **ONLY ONE** of these four options is correct.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme :

Full Marks : +3 If ONLY the correct option is chosen.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered)

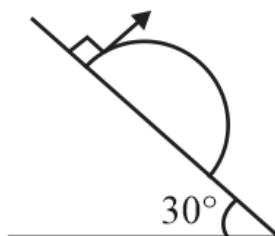
Negative Marks : -1 In all other cases

1. A man walks 30 m towards north, then 20 m towards east and in the last  $30\sqrt{2}$  m towards south-west. The displacement from origin is :  
 (A) 10m towards east (B) 10 m towards west  
 (C)  $60\sqrt{2}$  m towards north west (D)  $60\sqrt{2}$  m towards east north
2. A trolley is moving horizontally with a constant velocity of  $v$  m/s w.r.t. earth. A man starts running from one end of the trolley with a velocity  $1.5v$  m/s w.r.t. to trolley. After reaching the opposite end, the man turn back and continues running with a velocity of  $1.5 v$  m/s w.r.t. the trolley in the backward direction. If the length of the trolley is  $L$  then the displacement of the man with respect to earth during the time he reaches to starting point?



- (A) 1.5 L (B) 2.5 L  
(C)  $\frac{4L}{3}$  (D)  $\frac{5L}{3}$
3. A girl is walking on a road with velocity of 8 kph. Suddenly rain starts falling at 10 kph in vertically downward direction. The velocity of rain w.r.t to girl is :  
 (A)  $\sqrt{7}$  kph (B)  $\sqrt{13}$  kph  
 (C)  $\sqrt{164}$  kph (D)  $\sqrt{6}$  kph
4. With what speed should a body be thrown upwards so that the distances travelled in 5<sup>th</sup> second and 6<sup>th</sup> second are equal?  
 (A) 58.4 m/s (B) 49 m/s  
 (C) 98 m/s (D)  $\sqrt{98}$  m/s

5. A ball thrown up in vacuum returns after 12 sec. Its position after five seconds will be same as after
- (A) 7 sec (B) 3 sec
- (C) 3.5 sec (D) 4 sec
6. A ball is projected from point A with a velocity 10 m/s perpendicular to the inclined plane as shown in figure. Range of the ball on the inclined plane is :



- (A)  $\frac{20}{13}$  m (B)  $\frac{13}{40}$  m
- (C)  $\frac{40}{3}$  m (D)  $\frac{13}{20}$  m

SECTION-I(ii) : (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all ) the correct answer(s)
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 If only (all) the correct option(s) is (are) chosen.

*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen.

*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen and both of which are correct.

*Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option.

*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered).

*Negative Marks* : -2 In all other cases.

- **For Example :** If first, third and fourth are the **ONLY** three correct options for a question with second option being an incorrect option; selecting only all the three correct options will result in +4 marks. Selecting only two of the three correct options (e.g. the first and fourth options), without selecting any incorrect option (second option in this case), will result in +2 marks. Selecting only one of the three correct options (either first or third or fourth option), without selecting any incorrect option (second option in this case), will result in +1 marks. Selecting any incorrect option(s) (second option in this case), with or without selection of any correct option(s) will result in -2 marks.

7. If  $\vec{A} = 2\hat{i} + \hat{j} + \hat{k}$  &  $\vec{B} = \hat{i} + \hat{j} + \hat{k}$  are two vectors, then the unit vector

(A) Perpendicular to  $\vec{A}$  is  $\frac{-\hat{j} + \hat{k}}{\sqrt{2}}$ .

(B) Parallel to  $\vec{A}$  is  $\frac{2\hat{i} + \hat{j} + \hat{k}}{\sqrt{6}}$ .

(C) Perpendicular to  $\vec{B}$  is  $\left( \frac{-\hat{j} + \hat{k}}{\sqrt{2}} \right)$ .

(D) Parallel to  $\vec{A}$  is  $\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$ .

8. A force of  $\sqrt{3}$ N makes equal angles with X-axis, Y-axis and Z-axis. The possible value of force are

(A)  $(\hat{i} + \hat{j} + \hat{k})$ N

(B)  $(-\hat{i} + \hat{j} - \hat{k})$ N

(C)  $(-\hat{i} - \hat{j} - \hat{k})$ N

(D)  $(-\hat{i} + \hat{j} + \hat{k})$ N

9. Check up the only correct statements in the following

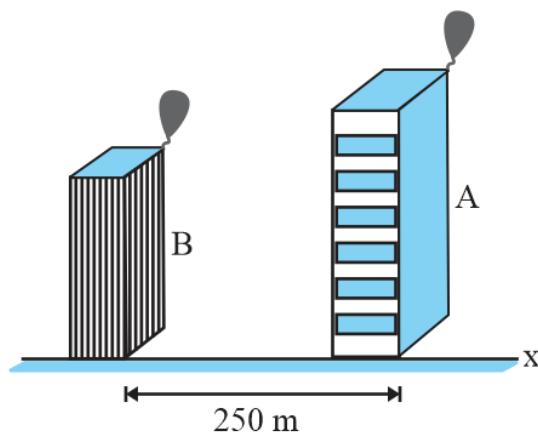
(A) A body having a constant velocity still can have varying speed.

(B) A body having a constant speed can have varying velocity.

(C) A body having constant speed can have an acceleration.

(D) If velocity and acceleration are in the same direction, then distance is equal to displacements.

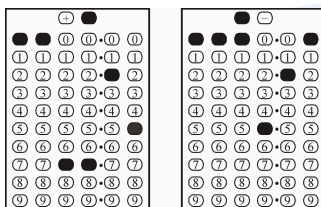
10. A particle moves along a straight line and its velocity depends on time as  $v = 4t - t^2$ . Then for first 5 seconds.
- (A) Average velocity is  $\frac{25}{3}$  m/s. (B) Average speed is 10 m/s.
- (C) Average velocity is  $\frac{5}{3}$  m/s. (D) Acceleration velocity is  $4\text{ m/s}^2$  at  $t = 0$ .
11. Mark the correct statement(s) :
- (A) A particle can have zero displacement and non-zero average velocity.
- (B) A particle can have zero displacement and non-zero velocity.
- (C) A particle can have zero acceleration and non-zero velocity.
- (D) A particle can have zero velocity and non-zero acceleration
12. Two balloons are simultaneously released from two buildings A and B. Balloon from A rises with constant velocity 10 m/s, While the other one rises with constant velocity of 20 m/s. Due to wind the balloons gather horizontal velocity  $V_x = 0.5 y$ , where  $y$  is the height from the point of release. The buildings are at a distance of 250 m and after some time  $t$  the balloons collide. Choose the correct option(s) :



- (A)  $t = 5$  seconds
- (B) difference in height of buildings is 100 m.
- (C) difference in height of buildings is 500 m.
- (D)  $t = 10$  seconds

SECTION-II : (Maximum Marks: 24)

- This section contains **SIX (06)** questions. The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer in the place designated to enter the answer. If the numerical value has more than two decimal places, **truncate/round-off** the value to **Two** decimal places; e.g. 6.25, 7.00, -0.33, -0.30, 30.27, -127.30, if answer is 11.36777..... then both 11.36 and 11.37 will be correct)

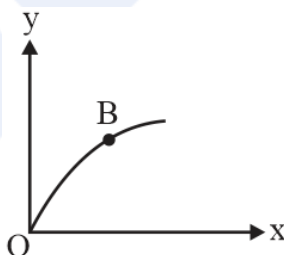


- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 If ONLY the correct numerical value is entered.

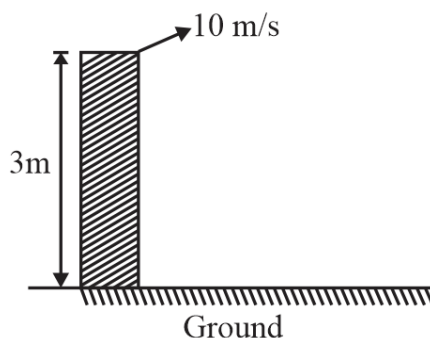
*Zero Marks* : 0 In all other cases.

1. A particle is projected vertically up with initially velocity 45 m/s. Distance travelled in 5<sup>th</sup> second ( $g = 10 \text{ m/s}^2$ ) =  $n/2$ . Then the value of  $n$  is \_\_\_\_.
2. A particle is moving in XY-plane. It starts to move from origin O at an angle  $\alpha$  with X-axis.

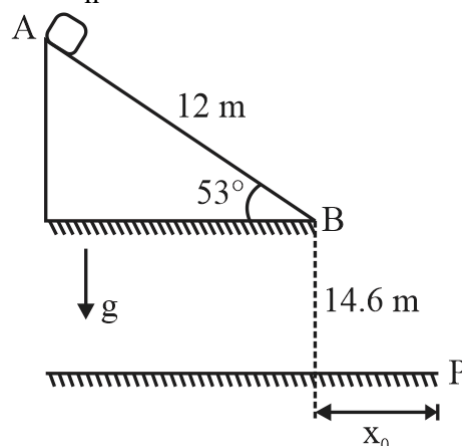


It has a constant acceleration in negative Y-direction. After some time it passes through a point B in a direction making angle  $\beta$  with the X-axis. If OB makes  $\theta = 45^\circ$  angle with the X-axis, find the value of  $\tan \alpha + \tan \beta$ .

3. A stone is projected from top of a vertical pole of height 3 m with initial velocity 10 m/s. The maximum range on the ground is  $x\sqrt{10}$  m. Find the value of  $x$  is \_\_\_\_\_. ( $g = 10 \text{ m/s}^2$ )



4. A particle starts from point A and moves under the action of some forces that lead it to have an acceleration of  $6 \text{ m/s}^2$  until it reaches B after which it is in free fall. It finally strikes point P after travelling some distance in air. If  $x_0 = \frac{36}{n} \text{ m}$ . Find the value of n is \_\_\_\_\_. ( $g = 10 \text{ m/s}^2$ )



5. In a square cut, the speed of the cricket ball changes from  $30 \text{ m/s}$  to  $40 \text{ m/s}$  during the time of its contact  $\Delta t = 0.01 \text{ s}$  with the bat. If the ball is deflected by the bat through an angle of  $\theta = 90^\circ$ . The magnitude of the average acceleration of the ball is  $n \times 10^3 \text{ m/s}^2$ . Then the value of n is \_\_\_\_\_.
6. A particle is projected up an inclined plane of inclination  $\beta$  at an elevation  $\alpha$  to the horizontal. Find the ratio between  $\tan \alpha$  and  $\tan \beta$ , if the particle strikes the plane horizontally.



## CHEMISTRY

## SECTION-I(i) : (Maximum Marks: 18)

- This section contains **SIX (06)** questions.
- Each question has Four options (A), (B), (C) and (D). **ONLY ONE** of these four options is correct.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme :

Full Marks : +3 If ONLY the correct option is chosen.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered)

Negative Marks : -1 In all other cases

1. The dissociation energy of  $H_2$  is 430.53 kJ/mol. If  $H_2$  is dissociated by illumination with radiation of wavelength 253.7 nm. The fraction of the radiant energy which will be converted into K.E is given by :  
(A) 8.86 % (B) 2.33 %  
(C) 1.3 % (D) 90%
2. 1.61 gm of  $Na_2SO_4 \cdot 10H_2O$  contains same number of oxygen atoms as present in  
(A) 0.98 gm  $H_2SO_4$  (B) 0.08 gm  $SO_3$   
(C) 1.78 gm  $H_2S_2O_7$  (D) 0.05 gm  $CaCO_3$
3. The wavelength of the first Lyman lines of hydrogen,  $He^+$  and  $Li^{2+}$  ions are  $\lambda_1, \lambda_2, \lambda_3$ . The ratio of these wavelengths is :  
(A) 1 : 4 : 9 (B) 9 : 4 : 1  
(C) 36 : 9 : 4 (D) 6 : 3 : 2
4. Diborane tetrachloride was treated with NaOH and the following reaction occurred  
$$B_2Cl_4 + NaOH \rightarrow NaBO_2 + H_2O + H_2 + NaCl.$$
  
If 1362 ml of hydrogen gas is formed at STP, how much amount of  $B_2Cl_4$  was consumed?  
(A) 9.97 g (B) 9.84 g  
(C) 0.0968 g (D) 23.57 g
5. For which orbit in  $He^+$  ion, the circumference is  $26.5\overset{\circ}{A}$ ?  
(A) 2 (B) 4  
(C) 3 (D) 16
6. The mass composition of universe may be given as 90%  $H_2$  and 10% He. The average molecular mass of universe should be :  
(A) 2.20 (B) 2.10  
(C) 3.80 (D) 3.64

## SECTION-I(ii) : (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all ) the correct answer(s)
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*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen.

*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen and both of which are correct.

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- **For Example :** If first, third and fourth are the **ONLY** three correct options for a question with second option being an incorrect option; selecting only all the three correct options will result in +4 marks. Selecting only two of the three correct options (e.g. the first and fourth options), without selecting any incorrect option (second option in this case), will result in +2 marks. Selecting only one of the three correct options (either first or third or fourth option), without selecting any incorrect option (second option in this case), will result in +1 marks. Selecting any incorrect option(s) (second option in this case), with or without selection of any correct option(s) will result in -2 marks.

7. The density of a liquid 1.2 gm/mL. There are 25 drops in 2 mL. The number of molecules in one drop is: [Given molecular mass of liquid = 50 amu]

(A)  $\frac{6}{5} \times \frac{1}{(25)^2} N_A$

(B)  $\left(\frac{1}{25}\right)^2 N_A$

(C)  $\frac{1.2}{(25)^2} N_A$

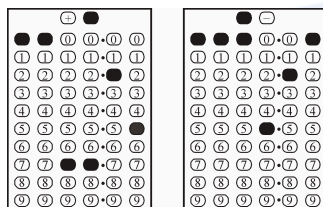
(D)  $1.2 \times 25 N_A$

8. Which of the following statements is/are correct regarding an oxide of iron, in which the mass per cent of iron and oxygen are 69.9 and 30.1, respectively ? (Fe = 56 g/mol)
- (A) The minimum molecular mass of the compound is 160.
- (B) The minimum molecular mass of the compound is 272
- (C) If all  $O^{16}$  atoms are replaced by  $O^{18}$ , the new mass per cent of O is 32.5%
- (D) If all  $O^{16}$  atoms are replaced by  $O^{18}$ , the new mass per cent of O is 28.9%

9. In a H-like sample electrons make transition from 4<sup>th</sup> excited state to 2<sup>nd</sup> state then :
- (A) 10 different spectral lines are observed  
(B) 6 different spectral lines are observed.  
(C) Number of lines belonging to the balmer series is 3.  
(D) Number of lines belonging to paschen series is 2.
10. Calculate mass % and mole % of H<sub>2</sub> in a mixture of H<sub>2</sub> and O<sub>2</sub> if average molecular mass of the mixture is 14?
- (A) 50% by mole  
(B) 60% by mole  
(C) 8.57% by mass  
(D) 10% by mass
11. Which of the following is/are correct statement(s)?
- (A) 3s orbital is spherically symmetrical with two nodes.  
(B)  $d_{x^2-y^2}$  orbitals has lobes of electron density in XY-plane along X and Y-axis.  
(C) The radial probability curve RPDF vs. r of 1s, 3p and 5d have one, two and three maxima.  
(D)  $3d_{z^2}$  has zero electron density in XY-plane.
12. As an electron jumps from the fourth orbit to the second orbit in Be<sup>3+</sup> ion, its :
- (A) K.E increases  
(B) Speed increases  
(C) Frequency of revolution increases  
(D) |PE| decreases

SECTION-II : (Maximum Marks: 24)

- This section contains **SIX (06)** questions. The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer in the place designated to enter the answer. If the numerical value has more than two decimal places, **truncate/round-off** the value to **Two** decimal places; e.g. 6.25, 7.00, -0.33, -0.30, 30.27, -127.30, if answer is 11.36777..... then both 11.36 and 11.37 will be correct)



- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 If ONLY the correct numerical value is entered.

*Zero Marks* : 0 In all other cases.

1. For a 3s-orbital

$$\psi(3s) = \frac{1}{9\sqrt{3}} \left( \frac{1}{a_0} \right)^{3/2} (6 - 6\sigma + \sigma^2) e^{-\sigma/2}$$

where ;  $\sigma = \frac{2rz}{3a_0}$

the maximum distance of radial node from nucleus is  $\frac{A}{B} \frac{(C + \sqrt{3})}{z} a_0$

Calculate  $\frac{(A+B)^2 - C^2}{4}$

2. Calculate minimum uncertainty involved in the location of a particle whose de Broglie wavelength is  $\sqrt{150\pi} \text{ Å}$  with an uncertainty of  $0.01 \pi \text{ Å}$ . Express answer in nm.
3. Specific charges of two particles A and B are in ratio 2 : 3. If their mass ratio  $m_A : m_B$  is 2 : 3, then the value of  $\frac{18}{8} \times \left( \frac{q_A}{q_B} \right)$  is \_\_\_\_.
4. What is the quantity of water (in g) that should be added to 16 g methanol to make the mole fraction of methanol as 0.25?
5. Not considering the electronic spin the degeneracy of the second excited state of H-atom is 9, while the degeneracy of the second excited state of  $\text{Li}^+$  is \_\_\_\_.
6. Calculate the mass of urea ( $\text{NH}_2\text{CONH}_2$ ) containing 1 gram-atom H.

MATHEMATICS

SECTION-I(i) : (Maximum Marks: 18)

- This section contains **SIX (06)** questions.
- Each question has Four options (A), (B), (C) and (D). **ONLY ONE** of these four options is correct.
- For each question, choose the option corresponding to the correct answer.
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Full Marks : +3 If ONLY the correct option is chosen.

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered)

Negative Marks : -1 In all other cases

- Number of solution(s) of the equation  $\log_2(x^2 + 3) = \frac{1}{2}\log_{1/3}\left(x + \frac{1}{x}\right)$ ,  $x > 0$  is :  
 (A) 0 (B) 1 (C) 2 (D) Infinite
- Check whether following statements are True or False and mark the correct order :  
 $S_1 : 3\sqrt{\log_3 7} = 7\sqrt{\log_7 3}$   
 $S_2 : \text{Number of solution to the equation } x^{\log_{10} 2x} = 5 \text{ is } 2.$   
 $S_3 : \text{Solution set of } \frac{(x-2)}{(x-4)} \leq 0 \text{ is } x \in [2, 4].$   
 $S_4 : \text{Solution set of the inequality } \left(\frac{1}{3}\right)^{\log_{1/9}\left(x^2 - \frac{10}{3}x + 1\right)} \leq 1 \text{ is } x \leq \frac{10}{3}.$   
 (A) T F F T (B) T T F F (C) T T T F (D) F T T F
- $N = \frac{81^{\frac{1}{\log_5 9}} + 3^{\frac{3}{\log_{\sqrt{6}} 3}}}{409} \left( (\sqrt{7})^{\frac{2}{\log_{25} 7}} - (125)^{\log_{25} 6} \right)$ , then  $\log_2 N$  has the value  
 (A) 0 (B) 1 (C) -1 (D) None of these
- Solution set of the inequality  $\log_{10}^2 x - 3(\log_{10} x)(\log_{10}(x-2)) + 2\log_{10}^2(x-2) < 0$ , is :  
 (A) (0, 4) (B)  $(-\infty, 1)$  (C) (4,  $\infty$ ) (D) (2, 4)
- Product of all values of  $x$  satisfying the equation  $\sqrt{2^x \sqrt[3]{4^x (0.125)^{1/x}}} = 4(\sqrt[3]{2})$  is :  
 (A)  $\frac{14}{5}$  (B) 3  
 (C)  $-\frac{1}{5}$  (D)  $-\frac{3}{5}$
- The product of all values of  $x$  satisfying the equation  $|x-1|^{\log_3 x^2 - 2\log_x 9} = (x-1)^7$ , is :  
 (A) 162 (B) 81  
 (C)  $\frac{162}{\sqrt{3}}$  (D)  $\frac{81}{\sqrt{3}}$

## SECTION-I(ii) : (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all ) the correct answer(s)
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 If only (all) the correct option(s) is (are) chosen.

*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen.

*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen and both of which are correct.

*Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option.

*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered).

*Negative Marks* : -2 In all other cases.

- **For Example :** If first, third and fourth are the **ONLY** three correct options for a question with second option being an incorrect option; selecting only all the three correct options will result in +4 marks. Selecting only two of the three correct options (e.g. the first and fourth options), without selecting any incorrect option (second option in this case), will result in +2 marks. Selecting only one of the three correct options (either first or third or fourth option), without selecting any incorrect option (second option in this case), will result in +1 marks. Selecting any incorrect option(s) (second option in this case), with or without selection of any correct option(s) will result in -2 marks.

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7. The equation  $x^{\frac{3}{4}(\log_2 x)^2 + \log_2 x - \frac{5}{4}} = \sqrt{2}$ , has

- (A) at least one real solution
- (B) exactly three solutions
- (C) exactly one irrational solution
- (D) complex roots

8. Consider the quadratic equation,  $(\log_{10} 8)x^2 - (\log_{10} 5)x = 2(\log_2 10)^{-1} - x$ . Which of the following quantities are rational?

- (A) Sum of roots
- (B) Product of roots
- (C) (Sum of roots)  $\times$  (Product of roots)
- (D) None of these

9. If positive  $p, q, r$  satisfy  $pqr = 1$ , then for equation  $\frac{2px}{pq + p + 1} + \frac{2qx}{qr + q + 1} + \frac{2rx}{rp + r + 1} = 1$ ,  $x$  equals :
- (A)  $p + q + r$   
 (B) 1  
 (C) Independent of  $p, q$  and  $r$   
 (D)  $1/2$
10. Interval containing all the solutions of the equality  $7^{x+2} - \frac{1}{7} \cdot 7^{x+1} - 14 \cdot 7^{x-1} + 2 \cdot 7^x = 48$ , is
- (A)  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$  (B)  $(\pi, \pi^2)$   
 (C)  $(-\pi, \pi)$  (D)  $(-e, e)$
11. If  $\log_4 5 = x$  and  $\log_5 6 = y$ , then
- (A)  $\log_4 6 = xy$   
 (B)  $\log_6 4 = xy$   
 (C)  $\log_3 2 = \frac{1}{2xy - 1}$   
 (D)  $\log_2 3 = \frac{1}{2xy - 1}$
12. For the equation  $\log_{3\sqrt{x}} x + \log_{3x} \sqrt{x} = 0$ , which of the following do not hold good?
- (A) no real solution  
 (B) one prime solution  
 (C) one integral solution  
 (D) no irrational solution

SECTION-II : (Maximum Marks: 24)

- This section contains **SIX (06)** questions. The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer in the place designated to enter the answer. If the numerical value has more than two decimal places, **truncate/round-off** the value to **Two** decimal places; e.g. 6.25, 7.00, -0.33, -0.30, 30.27, -127.30, if answer is 11.36777..... then both 11.36 and 11.37 will be correct)

⊖	⊕								
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9
0	1	2	3	4	5	6	7	8	9

- Answer to each question will be evaluated according to the following marking scheme:

**Full Marks** : +4 If ONLY the correct numerical value is entered.

**Zero Marks** : 0 In all other cases.

1. The number of negative integral values of  $x$  satisfying the inequality

$$\log_{\left(x+\frac{5}{2}\right)} \left( \frac{x-5}{2x-3} \right)^2 < 0 \text{ is:}$$

2. Find  $x$ , if

$$\begin{cases} 4^{\frac{x+y}{y}} = 32 \\ \log_3(x-y) + \log_3(x+y) = 1 \end{cases}$$

3. If set of all real values of  $x$  satisfying

$$|x^2 - 3x - 1| < |3x^2 + 2x + 1| + |2x^2 + 5x + 2|, x^2 - 3x - 1 \neq 0 \text{ is}$$

$$(-\infty, -a) \cup (-b, \infty), \text{ then find the value of } a + \log ab.$$

4. If  $x = \sqrt{\log_{11} 7}$ ,  $y = \sqrt{\log_7 11}$ , then the value of  $e^{y \log_e 7 - x \log_e 11}$ .

5. If  $\log_x \log_{18} (\sqrt{2} + \sqrt{8}) = \frac{1}{3}$ , then the value of  $32x =$

6. Find the number of real values of  $x$  satisfying the equation

$$\log_2 (4^{x+1} + 4) \cdot \log_2 (4^x + 1) = \log_{\frac{1}{\sqrt{2}}} \sqrt{\frac{1}{8}}$$