

CARLETON UNIVERSITY

MODELLING OF INTEGRATED DEVICES
ELEC 4700

Assignment 3

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1 Monte Carlo Simulation

1.1 Constant applied voltage

Applying a 0.1V applied voltage across the x dimension of the semiconductor region, in the Monte Carlo simulation tool results in Figure 4 below. Plotting the trajectories of the electrons shows the effects of the constant applied voltage, where the path of the electron curves. This figure also shows that without the presence of any objects in the regions, the drift current will eventually stabilize at a value.

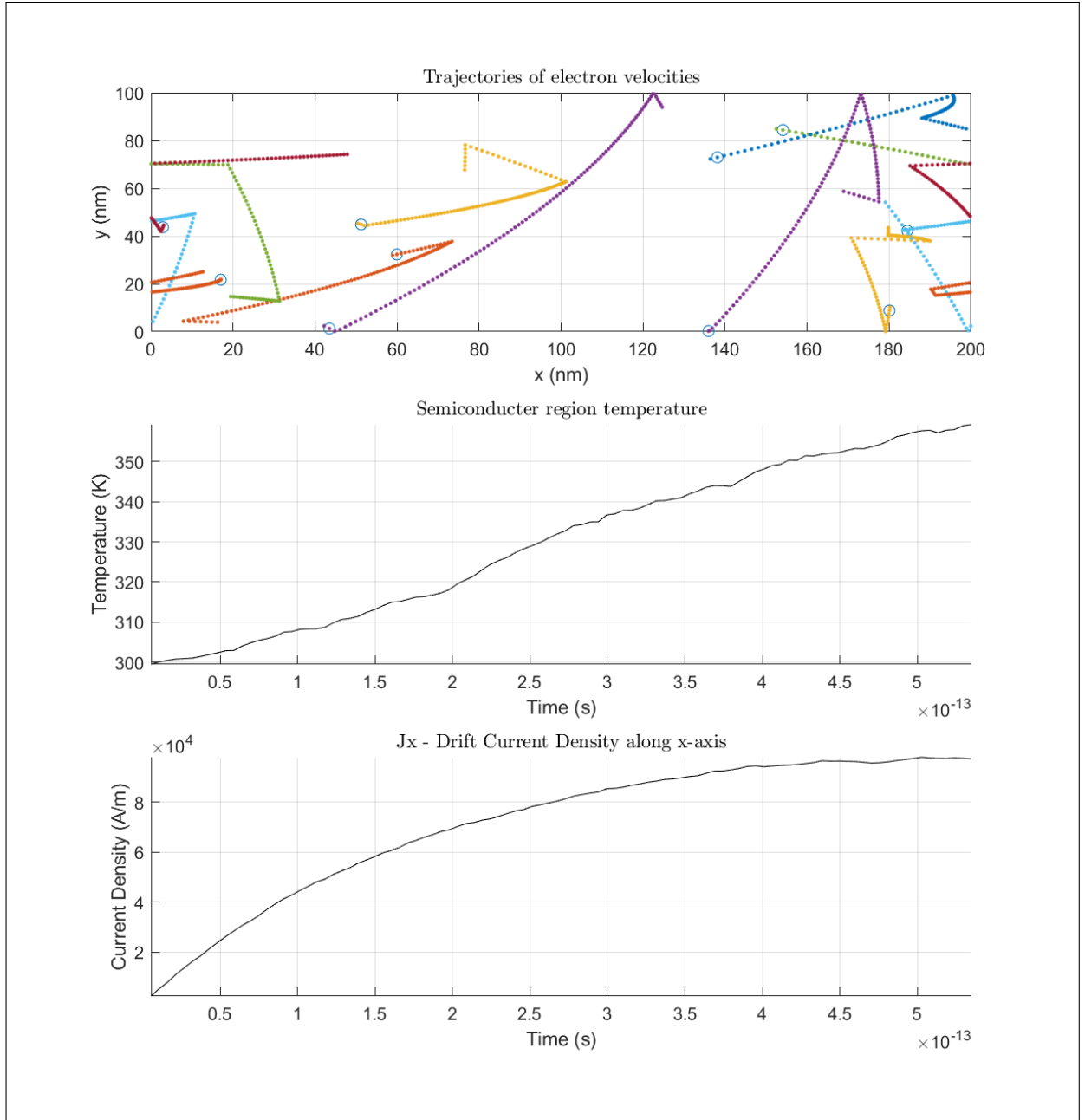


Figure 1: Monte Carlo Simulation

Force on electron The simulation was ran with a constant electric field applied only in the x -axis, therefore the force on an individual electron can be calculated as,

$$F_{ex} = Q_e * E_x = \boxed{-8.0109e^{-14}} \quad (1)$$

1.2 Electron Density

Figure 2 below shows the surface plot of the electron density, which shows the expected distribution of the densities. Without the presence of a bottleneck the electrons are approximately even distribution across the semiconductor region.

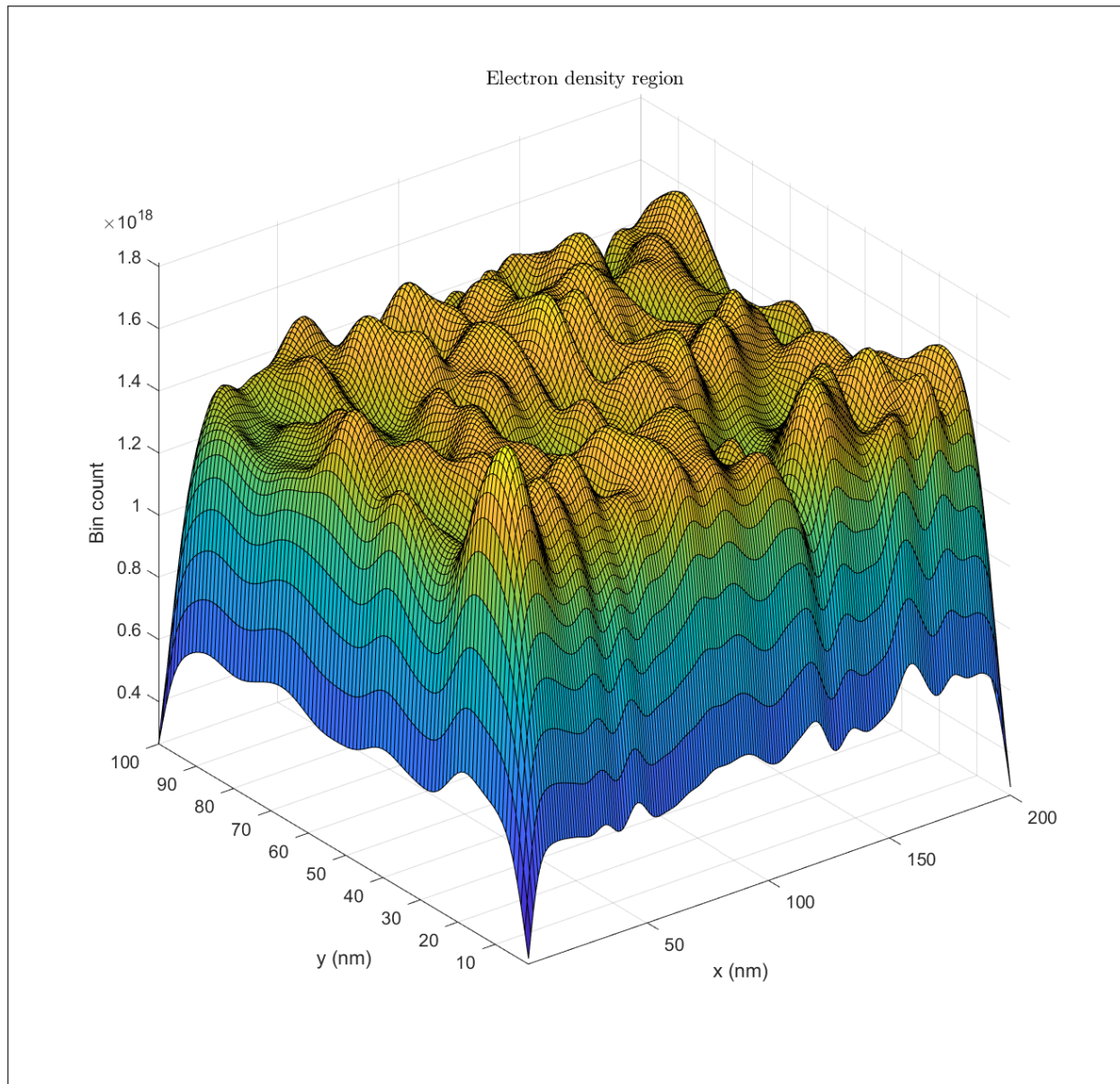


Figure 2: Electron Density at constant applied voltage

1.3 Electron Temperature

Figure 3 below shows the surface plot of the temperature in the region, which once again shows the expected result.

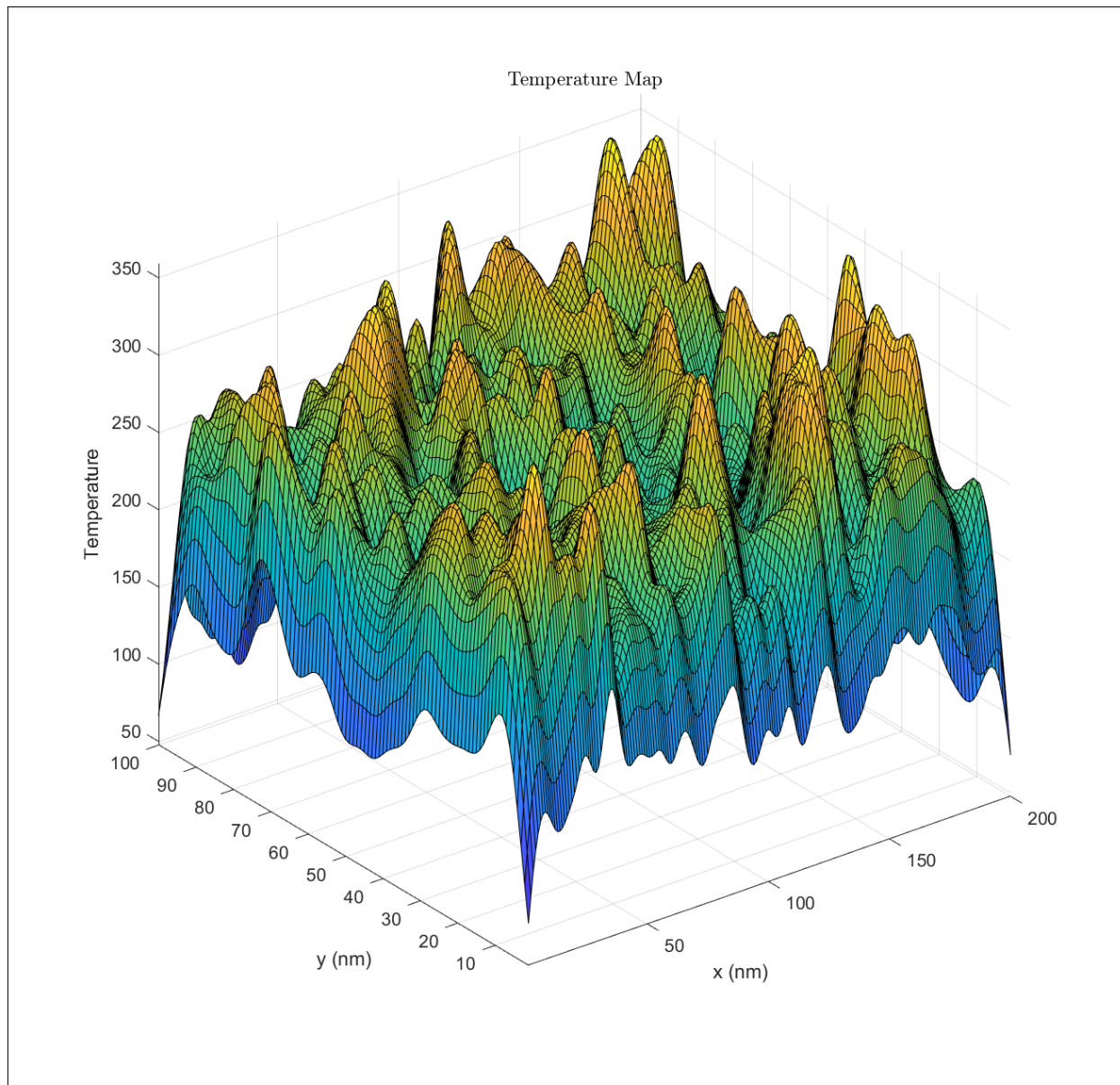


Figure 3: Electron temperature map at constant applied voltage

2 Finite Difference Method

2.1 Bottleneck

Introducing a bottleneck in the simulation, as shown below in Figure 2, the region is now simulated using the Finite Difference Method. This figure shows a blue region that is insulate (much lower sigma) then the rest of the region (yellow). This will create a bottleneck as the electrons cannot move into the bottleneck region.

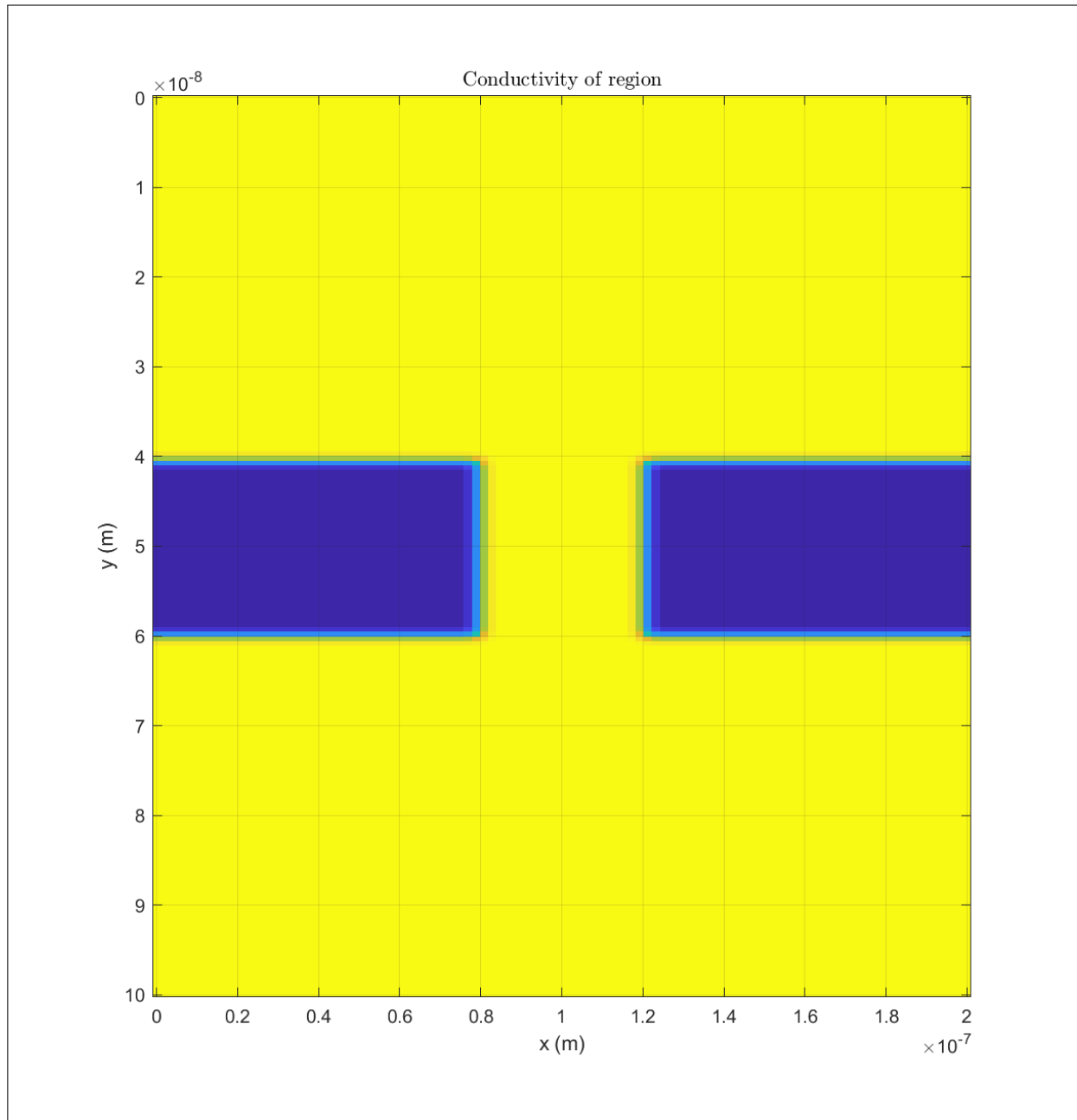


Figure 4: Conductivity map of region

2.2 Voltage Map

Figure 2 below shows the voltage map across the region including a bottleneck. This shows a result as expected, where due to the bottleneck there is a non-linear element at the position of the bottleneck.

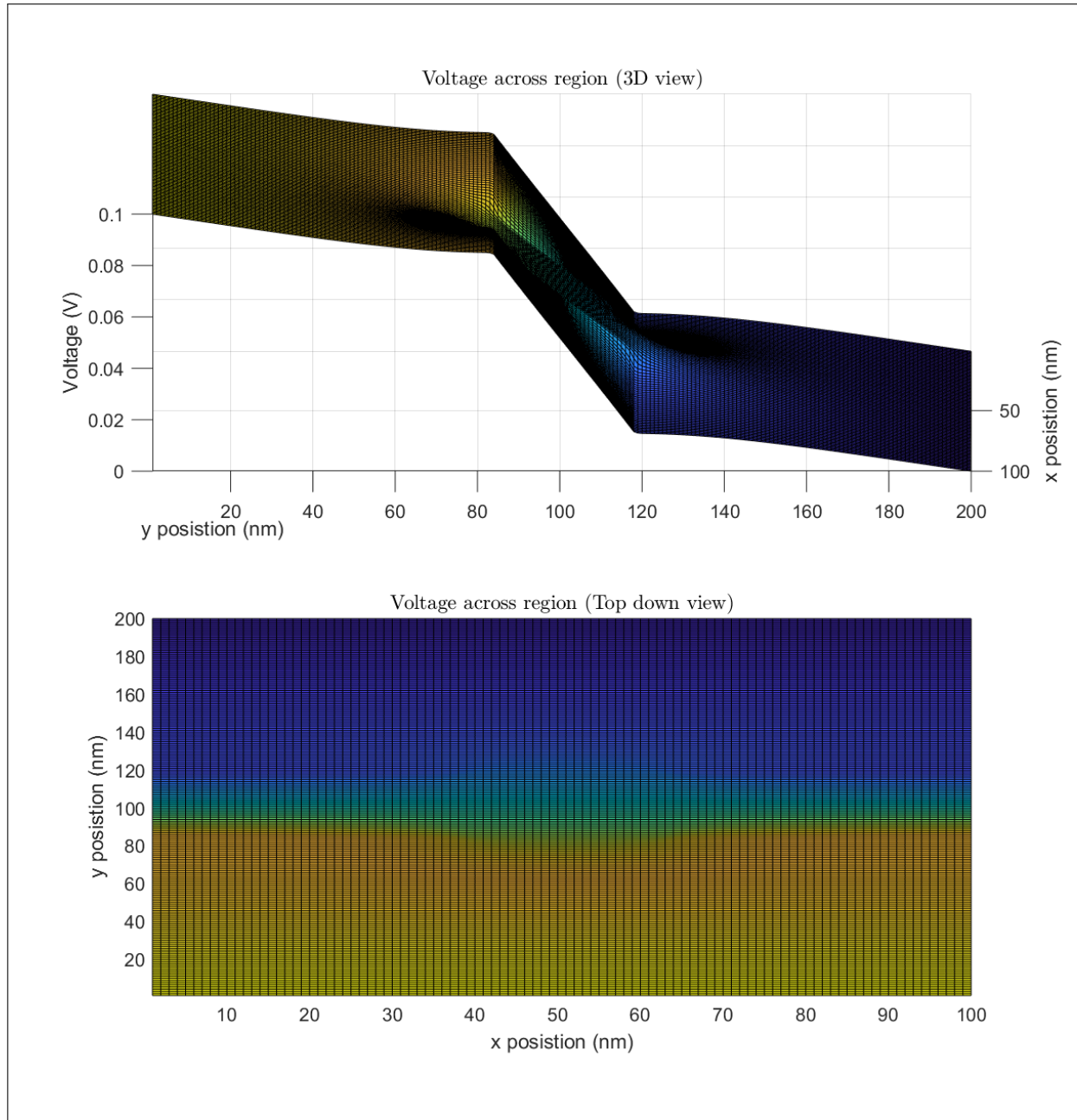


Figure 5: Voltage map using Finite Difference Method

2.3 Quiver plot

Figure 6 below shows the quiver plot across the semiconductor region including a bottleneck. This shows expected results, where the region inside of the bottle neck causes a disturbance in the linearity of the region.

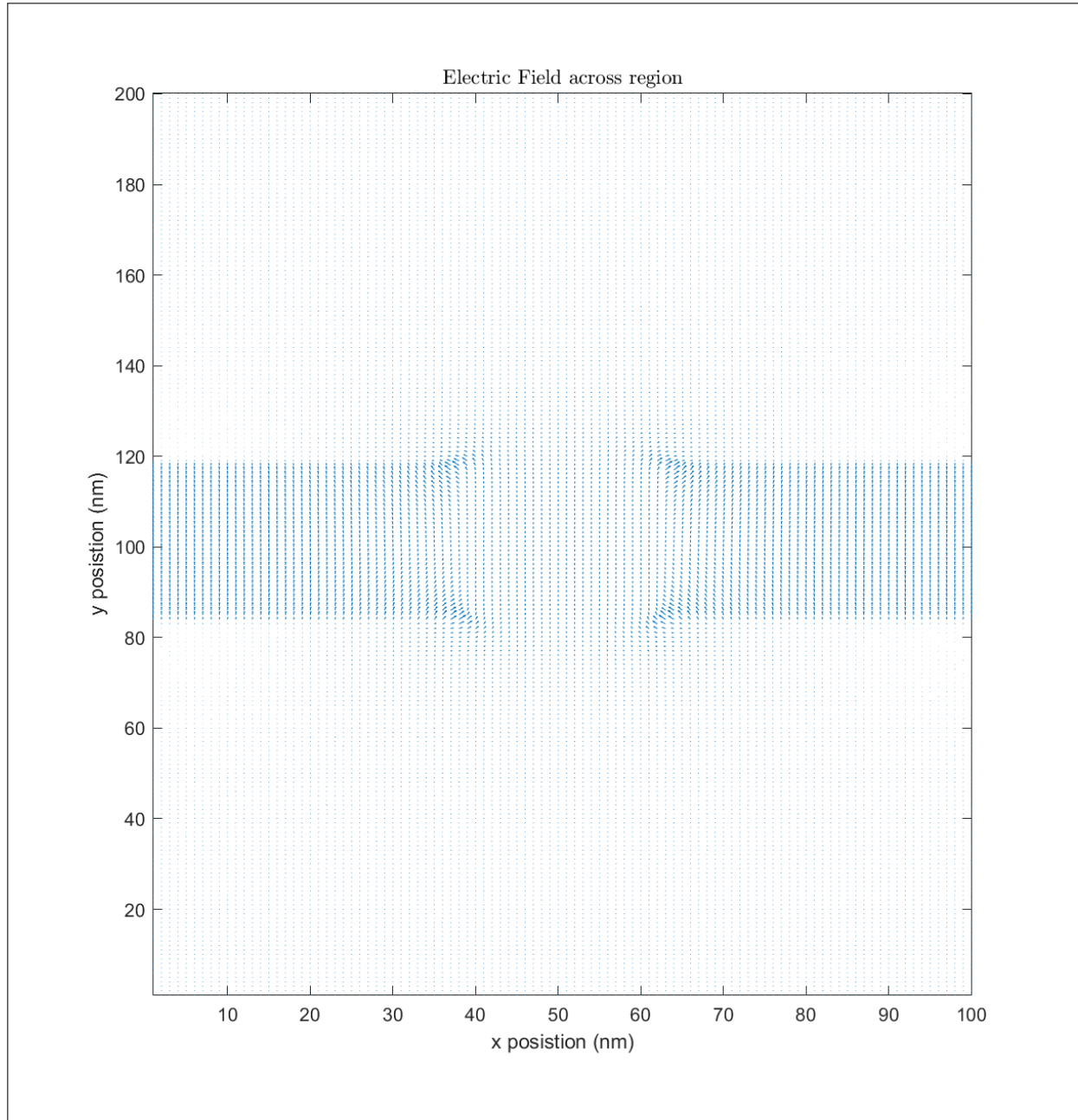


Figure 6: Quiver plot using Finite Difference Method

3 Coupled Simulations

Figure 7 below shows the results of the coupled simulation, where a constant voltage field is applied across the semiconductor region with the inclusion of a bottleneck. These results confirm the proper functionality of the simulator, where the "bending" of the electron path can be observed, as well as the "blocking" of the bottleneck.

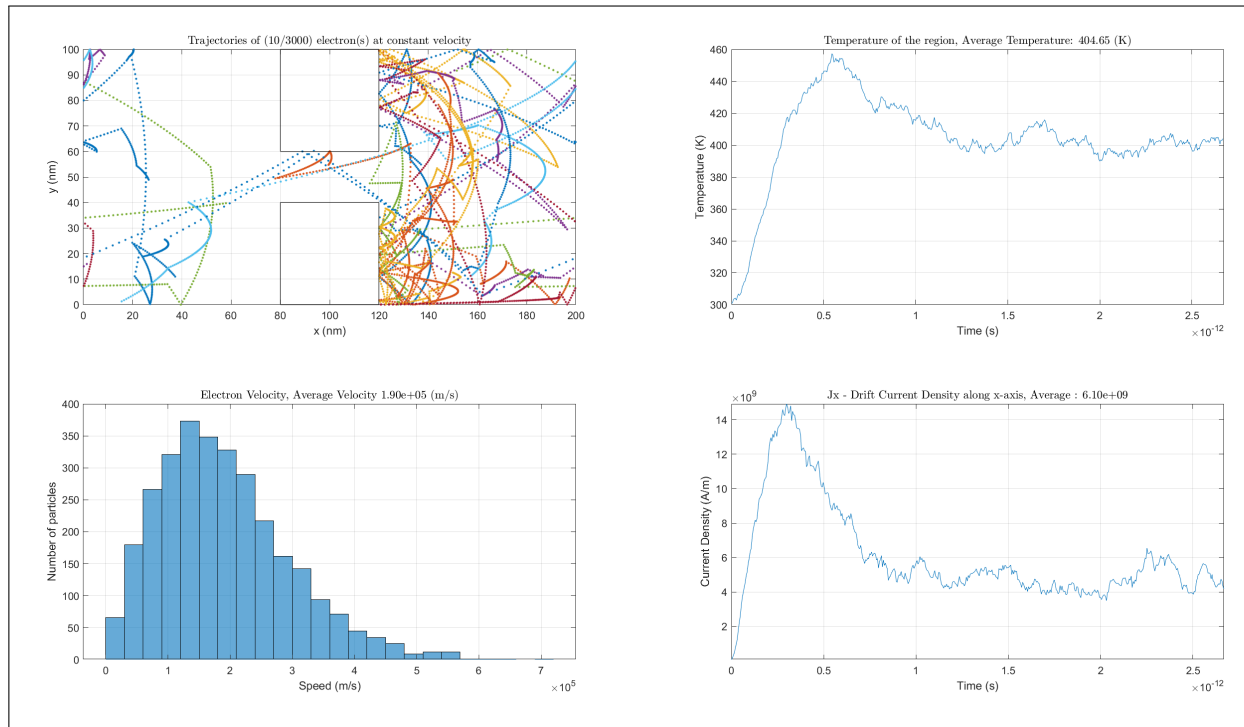


Figure 7: Coupled Simulation results

3.1 Electron Density

Figure 8 below shows the surface plot of the electron density in the semiconductor region with the bottleneck. This clearly shows the effect of the bottleneck and applied voltage, where a large concentration of electrons are stuck on one side of the bottleneck.

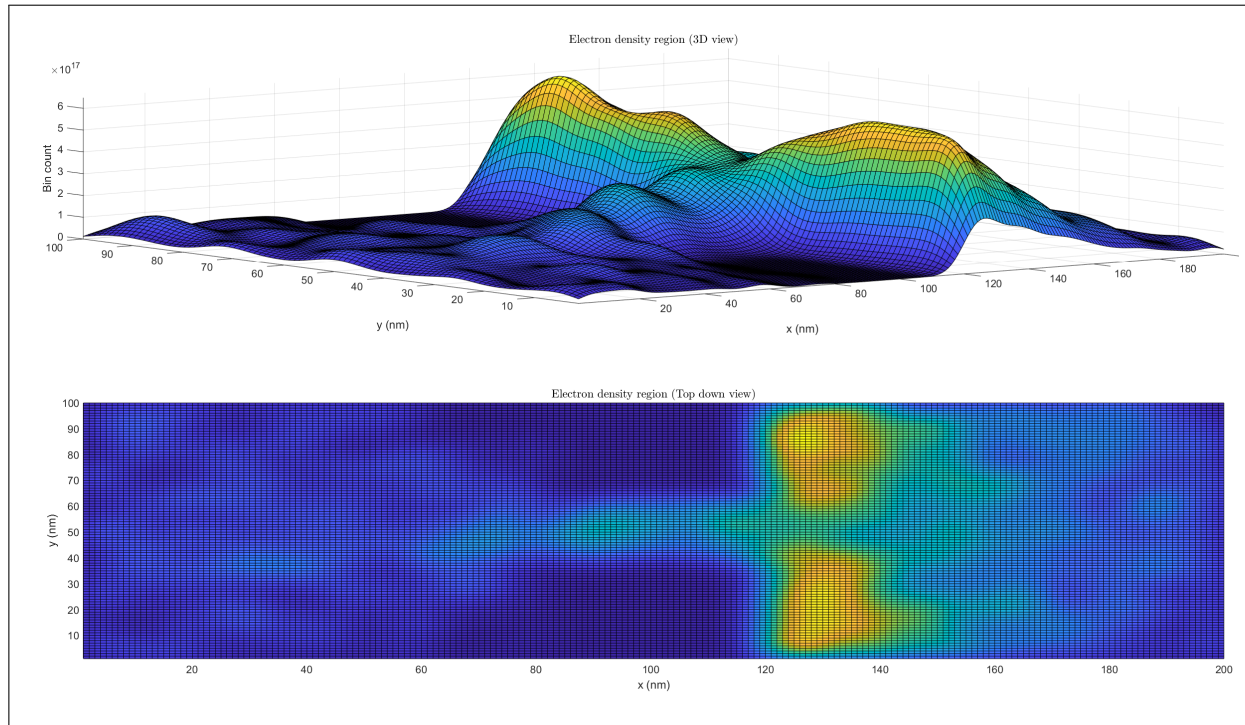


Figure 8: Electron Density using Coupled Simulations

3.2 Effect of bottleneck on drift current

Figure 9 below shows the plotted data from changing the bottleneck width, and its affects on the current density. This results makes sense, as the increased gap size allows for the easier flow of electrons, and the same visa-versa (smaller gap \Rightarrow small J_x).

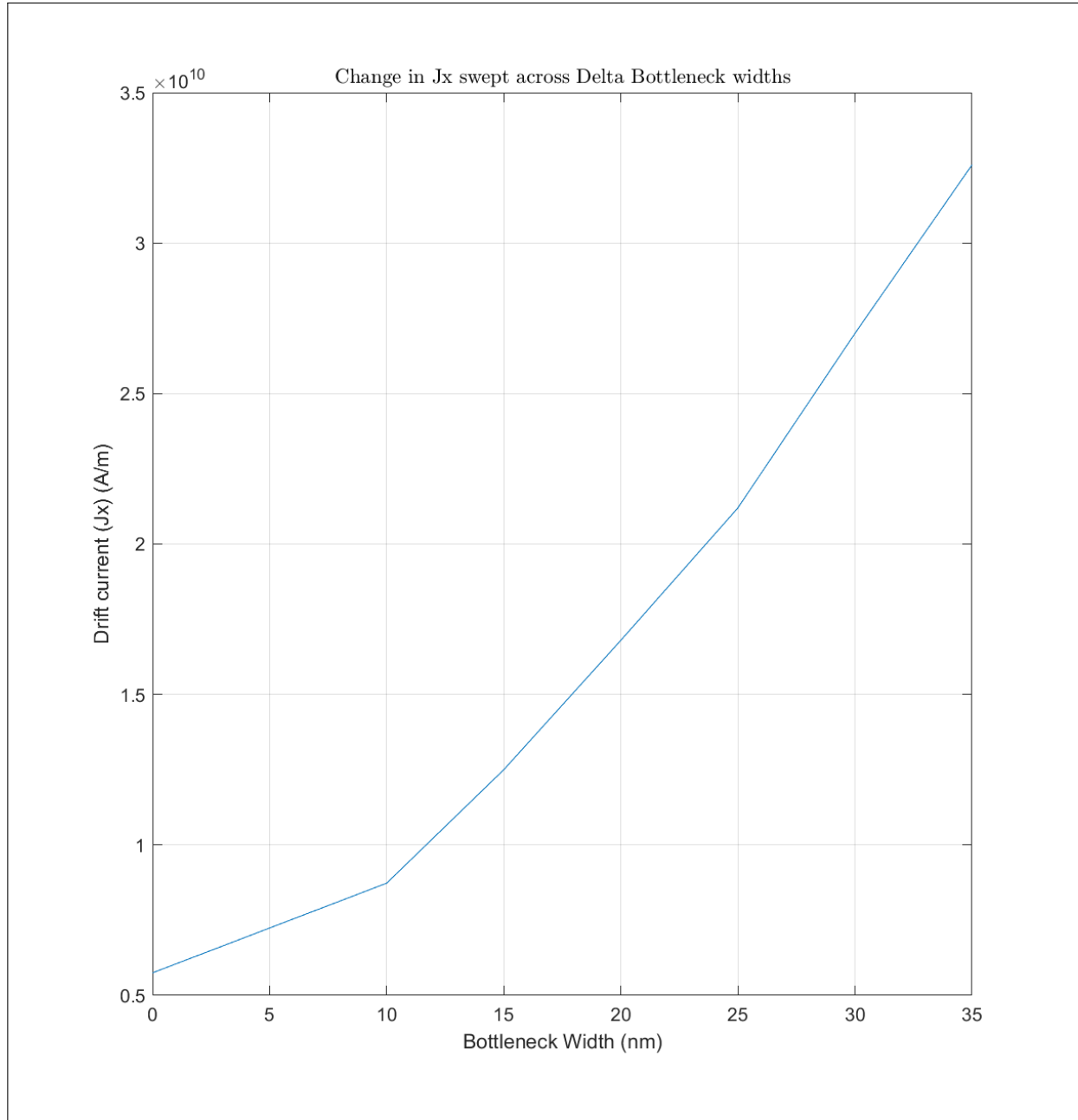


Figure 9: ΔJ_x with varying bottleneck width

3.3 Improvements/Next Step

Improvements to the accuracy of the simulator can be made by adding a third dimension (x,y, and z), increasing the number of iterations, mesh accuracy (smaller mesh size), number of electrons simulated.

4 Appendix

4.1 Part 1 Code

```

1  %{
2  % Author: Maharshi Gurjar
3  % ELEC 4700 - Modeling of Integrated Devices
4  % Assignment 3
5  % Part 1
6  %}
7  %%
8  clc; close all; clear;
9  set(0, 'DefaultFigureWindowStyle', 'docked')
10 %Define simulation environment and constants
11 MO = 9.10938356e-31; %Rest mass of electron
12 Mass_n = 0.26*MO; %Effective mass of electron
13 Qe = -1.60217662e-19; %Electron Charge
14 Vx = 0.1; % Voltage along the x-axis
15 Vy = 0; %Voltage along the y-axis
16 EConcentration = 1e15 * 100^2; %Electron concentration (1/m^2)
17 T = 300; % Simulation environment temperature (K)
18 k = 1.38064852e-23; % Boltzmans constant
19 V_thermal = sqrt(2*k*T/Mass_n); %Thermal Veleocity
20 Height = 100e-9; % The height of the simulation environment
21 Length = 200e-9; % The lengthof the simulation environment
22 nElectrons = 30e3; % Total number of electrons to simulate
23 nPlotted_Electrons = 10; %Total number of electrons displayed
24 Time_Step = Height/V_thermal/100; % Time step of simulation
25 Iterations = 1000; % Number of iterations to simulate
26 Show_Movie = 1; %Display steps control
27 % The mean free path is determined by multiplying the thermal velocity
28 ... by the mean time between collisions:
29 MFP = V_thermal * 0.2e-12 %Mean free path
30 %The state of the electron (postion and velocity) is stored in a array
31 ... where each index refers to [x-position y-position v-in-x v-in-y]
32 Electron_State = zeros(nElectrons,4);
33 %Setting the top/bottom of the boxes specularity
34 Top_Specular = 1;
35 Bottom_Specular = 1;
36 %Temperature will be recorded in the array below
37 Temperature = zeros(Iterations,1);
38 %Create a scattering probability
39 P_Scatterieng = 1 - exp(-Time_Step/0.2e-12);
40 %Create a distribution using the matlab makedist function
41 Velocity_PDF = makedist('Normal', 'mu', 0, 'sigma', sqrt(k*T/Mass_n));
42 %Generate a random inital population postion and velocity
43 %%
44 % The electric field compoennts (assuming uniform fields) given by:
45 Ex = Vx/Length;
46 Ey = Vy/Height;
47 %%
48 % Force on individual force given by:
49 Fx = Qe*Ex
50 Fy = Qe*Ey
51 %%
52 Temperature = zeros(Iterations,1);
53 J = zeros(Iterations,2);
54 %%
55 for i = 1:nElectrons
56     Electron_State(i,:) = [Length*rand() Height*rand() random(Velocity_PDF) random(Velocity_PDF)];
57 end
58 %%
59 figure(1);

```

```

60 subplot(3,1,1)
61 plot([],[]);
62 axis ([0 Length/1e-9 0 Height/1e-9]);
63 title("Trajectories of electron velocities",'interpreter','latex');
64 xlabel('x (nm)');
65 ylabel('y (nm)');
66 grid on;
67 subplot(3,1,2)
68 Temp_Plot = animatedline;
69 title("Semiconductor region temperature",'interpreter','latex');
70 xlabel('Time (s)');
71 ylabel('Temperature (K)');
72 grid on;
73 axis tight;
74 subplot(3,1,3)
75 Current_Plot = animatedline;
76 title("Jx - Drift Current Density along x-axis",'interpreter','latex');
77 xlabel('Time (s)');
78 ylabel('Current Density (A/m)');
79 grid on;
80 axis tight;
81 %We will now move (iterate) over time, updating the positions and direction
82 ...while plotting the state
83 %%
84 for i = 1:Iterations
85     %%
86     %The line below updates Vx and Vy by calculating the change in
87     %velocity under the influence of the electric field
88     Electron_State(:,3) = Electron_State(:,3) + Fx*Time_Step/Mass_n;
89     Electron_State(:,4) = Electron_State(:,4) + Fy*Time_Step/Mass_n;
90
91     %The line below updates the x,y position by moving it to a new position
92     ... using its current position + the velocity*(time step)
93     Electron_State(:,1:2) = Electron_State(:,1:2) + Time_Step.*Electron_State(:,3:4);
94
95     %Checking boundary conditions using Matlab matrix equations
96
97     %Check if and move all electrons at X=200nm Bound:
98     Electron_State((Electron_State(:,1)>Length),1) = Electron_State((Electron_State(:,1)>Length),1)
99     ↪ - Length;
100
101     %Check if and move all electrons at X=0nm Bound:
102     Electron_State((Electron_State(:,1)<0),1) =Electron_State((Electron_State(:,1)<0),1) + Length;
103
104     %Check (if) and move all electrons at Y Bounds and if specular or diffusive:
105     if (Top_Specular == 1)
106         Electron_State((Electron_State(:,2)>Height),4) =
107         ↪ -1*Electron_State((Electron_State(:,2)>Height),4) ;
108         Electron_State((Electron_State(:,2)>Height),2) = 2*Height -
109         ↪ Electron_State((Electron_State(:,2)>Height),2);
110     else
111         %Electron_State((Electron_State(:,2)>Height),2) = Height;
112         Electron_State((Electron_State(:,2)>Height),4) = -random(Velocity_PDF);
113         Electron_State((Electron_State(:,2)>Height),3) = random(Velocity_PDF);
114     end
115     if (Bottom_Specular == 1)
116         Electron_State((Electron_State(:,2)<0),4) = -1*Electron_State((Electron_State(:,2)<0),4) ;
117         Electron_State((Electron_State(:,2)<0),2) = -Electron_State((Electron_State(:,2)<0),2);
118     else
119         %Electron_State((Electron_State(:,2)<0),2) = 0;
120         Electron_State((Electron_State(:,2)<0),4) = random(Velocity_PDF);
121         Electron_State((Electron_State(:,2)<0),3) = random(Velocity_PDF);
122     end
123     %%

```

```

121     %Add scattering
122     j = rand(nElectrons,1) < P_Scatterieng;
123     Electron_State(j,3:4) = random(Velocity_PDF,[sum(j),2]);
124
125     % Stores the Electron [x y] posistions in the Trajectories vector
126     ... for each different electron in a new coloum
127     for j = 1: nPlotted_Electrons
128         Trajectories_x(i,j) = Electron_State(j,1);
129         Trajectories_y(i,j) = Electron_State(j,2);
130     end
131     %To calcuatle the themal energy, Maxwell's principle of equipartion
132     ... is used, where the final equation then becomes;
133     Temperature(i) = ( sum (Electron_State(:,3).^2) + sum(Electron_State(:,4).^2)) * Mass_n / k / 2
134     ↪ / nElectrons;
135
136     %To calculate the current density
137     J(i,1) = Qe.*EConcentration.*mean(Electron_State(:,3));
138     J(i,2) = Qe.*EConcentration.*mean(Electron_State(:,4));
139     % Add the temperature and current data to the respective plots using
140     % addpoints command
141     addpoints(Temp_Plot,Time_Step.*i, Temperature(i));
142     addpoints(Current_Plot,Time_Step.*i,J(i,1));
143
144     %Shows the pathing of the electron, as well as the updating trajectory
145     if Show_Movie && mod(i,50)
146         figure(1)
147         subplot(3,1,1);
148         hold off;
149         plot(Electron_State(1:nPlotted_Electrons,1)./1e-9,Electron_State(1:nPlotted_Electrons,2)./1e-9
150             ↪ -9,'o');
151         grid on;
152         axis([0 Length/1e-9 0 Height/1e-9]);
153         xlabel('x (nm)');
154         ylabel('y (nm)');
155         title("Trajectories of electron velocities",'interpreter','latex');
156         hold on;
157     end
158
159     %%
160     figure(1)
161     subplot(3,1,1)
162     hold on;
163     plot(Trajectories_x(:,1:nPlotted_Electrons)./1e-9, Trajectories_y(:,1:nPlotted_Electrons)./1e-9, '.'
164         ↪ );
165     hold off;
166     axis([0 Length/1e-9 0 Height/1e-9]);
167     xlabel('x (nm)');
168     ylabel('y (nm)');
169     grid on;
170     title("Trajectories of electron velocities",'interpreter','latex');
171
172     %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
173     ↪ Results','[Part1]TrajResults.png'),'png')
174
175     %%
176     Density = hist3(Electron_State(:,1:2),[200 100]);
177     N = 20;
178     sigma = 3;
179     %Creating a Gaussian filtering matrix
180     [x,y]=meshgrid(round(-N/2):round(N/2), round(-N/2):round(N/2));
181     G=exp(-x.^2/(2*sigma^2)-y.^2/(2*sigma^2));
182     G=G./sum(G(:));
183
184     figure("name","Electron Density (with Gaussian filtering)")
185     Density = conv2(Density,G,'same') / (Height./size(Density,1)*Length./size(Density,2));

```

```

181 surf(conv2(Density,G,'same'));
182 xlabel('x (nm)')
183 ylabel('y (nm)')
184 zlabel('Bin count')
185 axis tight
186 title("Electron density region",'interpreter','latex');
187 %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
↪ Results','[Part1]ElectronDensity.png'),'png')
188 %For the temperature density plot the electrons positions were binned
189 %Used the same process I did in the first assignment
190 Temperature_Sum_X = zeros(200,100);
191 Temperature_Sum_Y = zeros(200,100);
192 Temperature_Bin_Count = zeros(200,100);
193 for i=1:nElectrons
194     x = floor(Electron_State(i,1)/1e-9);
195     y = floor(Electron_State(i,2)/1e-9);
196     if(x==0)
197         x = 1;
198     end
199     if(y==0)
200         y = 1;
201     end
202     Temperature_Sum_X(x,y) = Temperature_Sum_X(x,y) + Electron_State(i,3)^2;
203     Temperature_Sum_Y(x,y) = Temperature_Sum_Y(x,y) + Electron_State(i,4)^2;
204     Temperature_Bin_Count(x,y) = Temperature_Bin_Count(x,y) + 1;
205 end
206 % Now, with the velocities added up, calculate the temperatures:
207 TemperatureDensity = (Temperature_Sum_X + Temperature_Sum_Y).*Mass_n./k./2./Temperature_Bin_Count;
208 %If somewhere in the calculation the density beame nan then make it 0
209 TemperatureDensity(isnan(TemperatureDensity)) = 0;
210 %Transpose the matrix
211 TemperatureDensity = TemperatureDensity';
212 [x,y] = meshgrid(round(-N/2):round(N/2), round(-N/2):round(N/2));
213 G=exp(-x.^2/(2*sigma^2)-y.^2/(2*sigma^2));
214 G=G./sum(G(:));
215 figure("Name","Electron heat denstiy (with Guassian filtering)")
216 surf(conv2(TemperatureDensity,G,'same'))
217 set(gca,'YDir','normal');
218 title('Temperature Map','interpreter','latex');
219 xlabel('x (nm)');
220 ylabel('y (nm)');
221 zlabel('Temperature');
222 axis tight
223 %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
↪ Results','[Part1]ElectronHeatDensity.png'),'png')

```

Source Code 1: Part 1 - Monte Carlo Simulator

4.2 Part 2 Code

```

224  %{
225  Author : Maharshi Gurjar
226  Elec 4700 Assignment 3 - Finite Difference Method
227  Part 2
228  %}
229  %%
230  clc; close all; clear;
231  set(0, 'DefaultFigureWindowStyle', 'docked')
232  %Define simulation parameters
233  W = 100e-9; %Width of region
234  L = 200e-9; %Length of region
235  L_Box = 40e-9; %Length of Box
236  W_Box = 40e-9; %Width of Box
237  MeshSize = 1e-9; % Preset mesh size
238  nx = ceil(L/MeshSize); %X bins
239  ny = ceil(W/MeshSize); %Y bins
240
241  Conductivity_1 = 1; %Conductivity of region
242  Conductivity_2 = 1e-2; %Conductivity in box
243
244  Conductivity_Map = zeros(nx,ny);
245
246  for i = 1:nx
247      for j = 1:ny
248          if ((i-1)>0.5*(L-L_Box)/MeshSize && (i-1)<0.5*(L+L_Box)/MeshSize && ((j-1)<W_Box/MeshSize
↪      || (j-1)>(W-W_Box)/MeshSize))
249              Conductivity_Map(i,j) = Conductivity_2;
250          else
251              Conductivity_Map(i,j) = Conductivity_1;
252          end
253      end
254  end
255  % Numerical issues can happen if the derivatives are too large, thus using
256  % the imgaussfilt function the matrix is filtered
257  Conductivity_Map = imgaussfilt(Conductivity_Map,1);
258
259
260  figure(1);
261  imagesc(linspace(0,L,nx),linspace(0,W,ny),Conductivity_Map);
262  title('Conductivity of region','interpreter','latex')
263  xlabel('x (m)')
264  ylabel('y (m)')
265  view(2)
266  axis tight
267  grid on;
268  %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
↪  Results','[Part2]ConductivityMap.png'),'png')
269  G = sparse(ny*nx);
270  F = zeros(1,ny*nx);
271
272
273  for i = 1:(nx)
274      for j = 1:(ny)
275          %Create variable for node mapping
276          n = j + (i-1)*ny;
277          %Calculate changes in x and y
278          if i == 1 % V = 1, x = 0
279              G(n,n) = 1;
280              F(n) = 0.1;
281          elseif i == nx %V=0, x = L
282              G(n,n) = 1;

```

```

283     elseif j == 1
284         xM = j + (i-2)*ny;
285         xP = j + i*ny;
286         yP = j+1 + (i-1)*ny;
287         %Resistance Values
288         rxM = (Conductivity_Map(i,j) + Conductivity_Map(i-1,j))/2;
289         rxP = (Conductivity_Map(i,j) + Conductivity_Map(i+1,j))/2;
290         ryP = (Conductivity_Map(i,j) + Conductivity_Map(i,j+1))/2;
291         %node equations
292         G(n,n) = -(rxM + rxP + ryP);
293         G(n,xM) = rxM;
294         G(n,xP) = rxP;
295         G(n,yP) = ryP;
296     elseif j == ny %BC @ y=W
297         xM = j + (i-2)*ny;
298         xP = j + i*ny;
299         nym = j-1 + (i-1)*ny;
300         %Resistance Values
301         rxM = (Conductivity_Map(i,j) + Conductivity_Map(i-1,j))/2;
302         rxP = (Conductivity_Map(i,j) + Conductivity_Map(i+1,j))/2;
303         rym = (Conductivity_Map(i,j) + Conductivity_Map(i,j-1))/2;
304         %node equations
305         G(n,n) = -(rxM + rxP + rym);
306         G(n,xM) = rxM;
307         G(n,xP) = rxP;
308         G(n,nym) = rym;
309         %internal nodes
310     else
311         xM = j + (i-2)*ny;
312         xP = j + i*ny;
313         nym = j-1 + (i-1)*ny;
314         yP = j+1 + (i-1)*ny;
315         %Resistor Values
316         rxM = (Conductivity_Map(i,j) + Conductivity_Map(i-1,j))/2;
317         rxP = (Conductivity_Map(i,j) + Conductivity_Map(i+1,j))/2;
318         ryp = (Conductivity_Map(i,j) + Conductivity_Map(i,j+1))/2;
319         rym = (Conductivity_Map(i,j) + Conductivity_Map(i,j-1))/2;
320         %node equations
321         G(n,n) = -(rxM + rxP + rym + ryp);
322         G(n,xM) = rxM;
323         G(n,xP) = rxP;
324         G(n,nym) = rym;
325         G(n,yP) = ryp;
326     end
327 end
328 end
329
330 V = G\F';
331 Voltage_Map = zeros(nx,ny);
332 for i = 1:nx
333     for j = 1:ny
334         Voltage_Map(i,j) = V(j + (i-1)*ny);
335     end
336 end
337
338 % [X, Y] = meshgrid(0:MeshSize:L, 0:MeshSize:W);
339 figure(2)
340 subplot(2,1,1)
341 surf(Voltage_Map) %X',Y',
342 axis tight
343 xlabel('x posistion (nm)')
344 ylabel('y posistion (nm)')
345 zlabel('Voltage (V)')
346 title('Voltage across region (3D view)', 'interpreter', 'Latex')

```

```
347 view(90,25)
348 subplot(2,1,2)
349 surf(Voltage_Map) %X',Y',
350 axis tight
351 xlabel('x posistion (nm)')
352 ylabel('y posistion (nm)')
353 zlabel('Voltage (V)')
354 title('Voltage across region (Top down view)','interpreter','Latex')
355 view(2)
356 %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
↵ Results','[Part2]VoltageMap.png'),'png')
357
358 [Ex, Ey] = gradient(Voltage_Map,MeshSize);
359 Ex=-Ex;
360 Ey=-Ey;
361 figure(3)
362 quiver(Ex,Ey);
363 axis tight
364 xlabel('x posistion (nm)')
365 ylabel('y posistion (nm)')
366 title('Electric Field across region','interpreter','Latex')
367 %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
↵ Results','[Part2]QuiverPlot.png'),'png')
```

Source Code 2: Part 2 - Finite Difference Method Simulator

4.3 Part 3 Code

```

368  %{
369  Author : Maharshi Gurjar
370  Elec 4700 Assignment 3 - Finite Difference Method
371  Part 3
372  %}
373  %%
374  clc; close all; clear;
375  set(0, 'DefaultFigureWindowStyle', 'docked')
376  %%
377  %Define simulation environment and constants
378  MO = 9.10938356e-31; %Rest mass of electron
379  Mass_n = 0.26*MO; %Effective mass of electron
380  Qe = -1.60217662e-19; %Electron Charge
381  Vx = -0.4; % Voltage along the x-axis
382  Vy = 0; %Voltage along the y-axis
383  EConcentration = 1e15 * 100^2; %Electron concentration (1/m^2)
384  T = 300; % Simulation environment temperature (K)
385  k = 1.38064852e-23; % Boltzmanns constant
386  V_thermal = sqrt(2*k*T/Mass_n); %Thermal Veleocity
387  Height = 100e-9; % The height of the simulation environment
388  Length = 200e-9; % The length of the simulation environment
389  nElectrons = 30e3; % Total number of electrons to simulate
390  nPlotted_Electrons = 20; %Total number of electrons displayed
391  Time_Step = Height/V_thermal/100; % Time step of simulation
392  Iterations = 500; % Number of iterations to simulate
393  Show_Movie = 0; %Display steps control
394  %%
395  % The mean free path is determined by multipling the thermal velocity
396  ... by the mean time between collisions:
397  MFP = V_thermal * 0.2e-12; %Mean free path
398  %%
399  %The state of the electron (postion and velocity) is stored in a array
400  ... where each index refers to [x-position y-position v-in-x v-in-y]
401  Electron_State = zeros(nElectrons,4);
402  %%
403  %Temperature will be recorded in the array below
404  Temperature = zeros(Iterations,1);
405  %%
406  %Create a scattering probability
407  P_Scattering = 1 - exp(-Time_Step/0.2e-12);
408  %%
409  %Create a distribution using the matlab makedist function
410  Velocity_PDF = makedist('Normal', 'mu', 0, 'sigma', sqrt(k*T/Mass_n));
411  %%
412  %Setting the top/bottom of the boudnary specularity
413  Top_Specular = 1;
414  Bottom_Specular = 1;
415  %Set the box characteristics (0 = diffusive)
416  Top_Box_Specular = 1;
417  Bottom_Box_Specular = 1;
418  %Create Box-positions [x1, x2, y1,y2]
419  %Box_pos = 1e-9.*[80 120 0 32.5; 80 120 67.5 100]; % [Gap size 35nm]
420  %Box_pos = 1e-9.*[80 120 0 35; 80 120 65 100]; % [Gap size 30nm]
421  %Box_pos = 1e-9.*[80 120 0 37.5; 80 120 62.5 100]; % [Gap size 25nm]
422  %Box_pos = 1e-9.*[80 120 0 40; 80 120 60 100]; % [Gap size 20nm] [Control ]
423  %Box_pos = 1e-9.*[80 120 0 42.5; 80 120 57.5 100]; % [Gap size 15nm]
424  %Box_pos = 1e-9.*[80 120 0 45; 80 120 55 100]; % [Gap size 10nm]
425  %Box_pos = 1e-9.*[80 120 0 47.5; 80 120 52.5 100]; % [Gap size 5nm]
426  %%
427  % The electric field compoennts (assuming uniform fields) given by:
428  Ex = Vx/Length;

```

```

429 Ey = Vy/Height;
430 %%
431 % Force on individual force given by:
432 Fx = Qe*Ex;
433 Fy = Qe*Ey;
434 %%
435 % Current Density vector
436 J = zeros(Iterations,2);
437 %% Current plot and Temperature plot stuff
438 Temp_Plot = zeros(Iterations,1);
439 Current_Plot = zeros(Iterations,1);
440 %%
441 %Create the state of the box (specular or diffusive)
442 %Generate a random initial population position and velocity
443 for i = 1:nElectrons
444     Electron_State(i,:) = [Length*rand() Height*rand() random(Velocity_PDF) random(Velocity_PDF)];
445     Electron_State( (Electron_State(:,1)>Box_pos(1,1) & Electron_State(:,1)<Box_pos(1,2) & ...
446         (Electron_State(:,2)<Box_pos(1,4))) ,1) = Length*rand();
447     Electron_State( (Electron_State(:,1)>Box_pos(2,1) & Electron_State(:,1)<Box_pos(2,2) & ...
448         (Electron_State(:,2)>Box_pos(2,3))) ,1) = Length*rand();
449 end
450 %%
451 %Figure below used to test initial position of electrons, and if movie is off
452 %shows the the same.
453 figure("Name","Electron positions")
454 plot(Electron_State(1:nPlotted_Electrons,1)./1e-9,Electron_State(1:nPlotted_Electrons,2)./1e-9,'o');
455 grid on;
456 axis([0 Length/1e-9 0 Height/1e-9]);
457 xlabel('x (nm)');
458 ylabel('y (nm)');
459 title(sprintf("Plotting (%d/%d) electron ",nPlotted_Electrons,nElectrons));
460 %saveas(gcf,'Part_Three_Boxes.png')
461 hold on;
462 for j=1:size(Box_pos,1)
463     plot([Box_pos(j, 1) Box_pos(j, 1) Box_pos(j, 2) Box_pos(j, 2) Box_pos(j, 1)]./1e-9,...
464         [Box_pos(j, 3) Box_pos(j, 4) Box_pos(j, 4) Box_pos(j, 3) Box_pos(j, 3)]./1e-9, 'k-');
465 end
466 hold off;
467 %%
468 %We will now move (iterate) over time, updating the positions and direction
469 ...while plotting the state
470 for i = 1:Iterations
471     %The line below updates the x,y position by moving it to a new position
472     ... using its current position + the velocity*(time step)
473     Electron_Prev_State = Electron_State(:,1:2);
474     Electron_State(:,3) = Electron_State(:,3) + Fx*Time_Step/Mass_n;
475     Electron_State(:,4) = Electron_State(:,4) + Fy*Time_Step/Mass_n;
476     Electron_State(:,1:2) = Electron_State(:,1:2) + Time_Step*Electron_State(:,3:4);
477     %Checking boundary conditions using Matlab matrix equations/indexing
478     %Check (if) and move all electrons at X=200nm Bound:
479     Electron_State((Electron_State(:,1)>Length),1) = Electron_State((Electron_State(:,1)>Length),1)
480     ↪ - Length;
481
482     %Check (if) and move all electrons at X=0nm Bound:
483     Electron_State((Electron_State(:,1)<0),1) =Electron_State((Electron_State(:,1)<0),1) + Length;
484
485     %Check (if) and move all electrons at Y Bounds and if specular or diffusive:
486     Electron_State((Electron_State(:,2)>Height & Top_Specular==1),4) =
487     ↪ -1*Electron_State((Electron_State(:,2)>Height & Top_Specular),4);
488     Electron_State((Electron_State(:,2)>Height & Top_Specular==1),2) = 2*Height -
489     ↪ Electron_State((Electron_State(:,2)>Height & Top_Specular),2);
490     Electron_State((Electron_State(:,2)>Height & Top_Specular==0),4) = -random(Velocity_PDF);
491     Electron_State((Electron_State(:,2)>Height & Top_Specular==0),3) = random(Velocity_PDF);
492     Electron_State((Electron_State(:,2)<0 & Bottom_Specular==1),4) =
493     ↪ -Electron_State((Electron_State(:,2)<0 & Bottom_Specular==1),4);

```

```

490 Electron_State((Electron_State(:,2)<0 & Bottom_Specular==1),2) =
    ↪ -Electron_State((Electron_State(:,2)<0 & Bottom_Specular==1),2);
491 Electron_State((Electron_State(:,2)<0 & Bottom_Specular==0),4) = random(Velocity_PDF);
492 Electron_State((Electron_State(:,2)<0 & Bottom_Specular==0),3) = random(Velocity_PDF);
493 %%
494 %BOX SPECULAR CASE :
495 %Check if bottom Box is specular and if so then bounce
496 Electron_State( (Bottom_Box_Specular==1 & Electron_State(:,1)>Box_pos(1,1) &
    ↪ Electron_State(:,1)<Box_pos(1,2) & ((Electron_State(:,2)<Box_pos(1,4) &
    ↪ Electron_Prev_State(:,2)<Box_pos(1,4))))),3) ...
497 =-Electron_State( (Bottom_Box_Specular==1 & Electron_State(:,1)>Box_pos(1,1) &
    ↪ Electron_State(:,1)<Box_pos(1,2) & ((Electron_State(:,2)<Box_pos(1,4) &
    ↪ Electron_Prev_State(:,2)<Box_pos(1,4))))),3);
498
499 %Check if top Box is specular and if so then bounce
500 Electron_State( (Top_Box_Specular==1 & Electron_State(:,1)>Box_pos(2,1) &
    ↪ Electron_State(:,1)<Box_pos(2,2) & ((Electron_State(:,2)>Box_pos(2,3) &
    ↪ Electron_Prev_State(:,2)>Box_pos(2,3))))),3) ...
501 =-Electron_State( (Top_Box_Specular==1 & Electron_State(:,1)>Box_pos(2,1) &
    ↪ Electron_State(:,1)<Box_pos(2,2) & ((Electron_State(:,2)>Box_pos(2,3) &
    ↪ Electron_Prev_State(:,2)>Box_pos(2,3))))),3);
502
503 %Top Horizontal
504 Electron_State( (Top_Box_Specular==1 & Electron_State(:,1)<Box_pos(2,2) &
    ↪ Electron_State(:,1)>Box_pos(2,1)) & (Electron_State(:,2)>Box_pos(2,3)) & ...
505 (Electron_Prev_State(:,1)>Box_pos(2,1) & Electron_Prev_State(:,1)<Box_pos(2,2)),4) =
    ↪ -Electron_State( (Top_Box_Specular==1 & Electron_State(:,1)<Box_pos(2,2) &
    ↪ Electron_State(:,1)>Box_pos(2,1)) & (Electron_State(:,2)>Box_pos(2,3)) & ...
506 (Electron_Prev_State(:,1)>Box_pos(2,1) & Electron_Prev_State(:,1)<Box_pos(2,2)),4);
507 %Bottom Horizontal
508 Electron_State( (Bottom_Box_Specular==1 & Electron_State(:,1)<Box_pos(1,2) &
    ↪ Electron_State(:,1)>Box_pos(1,1)) & (Electron_State(:,2)<Box_pos(1,4)) & ...
509 (Electron_Prev_State(:,1)>Box_pos(1,1) & Electron_Prev_State(:,1)<Box_pos(1,2)),4) =
    ↪ -Electron_State( (Bottom_Box_Specular==1 & Electron_State(:,1)<Box_pos(1,2) &
    ↪ Electron_State(:,1)>Box_pos(1,1)) & (Electron_State(:,2)<Box_pos(1,4)) & ...
510 (Electron_Prev_State(:,1)>Box_pos(1,1) & Electron_Prev_State(:,1)<Box_pos(1,2)),4);
511 %BOX SPECULAR CASE END :
512 %%
513 %BOX DIFFUSIVE CASE:
514 %Check if bottom Box is specular and if so then bounce
515 Electron_State( (Bottom_Box_Specular==0 & Electron_State(:,1)>Box_pos(1,1) &
    ↪ Electron_State(:,1)<Box_pos(1,2) & ((Electron_State(:,2)<Box_pos(1,4) &
    ↪ Electron_Prev_State(:,2)<Box_pos(1,4))))),3) ...
516 =random(Velocity_PDF);
517 Electron_State( (Bottom_Box_Specular==0 & Electron_State(:,1)>Box_pos(1,1) &
    ↪ Electron_State(:,1)<Box_pos(1,4) & ((Electron_State(:,2)<Box_pos(1,4) &
    ↪ Electron_Prev_State(:,2)<Box_pos(1,4))))),4) ...
518 =random(Velocity_PDF);
519
520 %Check if Top Box is specular and if so then bounce
521 Electron_State( (Top_Box_Specular==0 & Electron_State(:,1)>Box_pos(2,1) &
    ↪ Electron_State(:,1)<Box_pos(2,2) & ((Electron_State(:,2)>Box_pos(2,3) &
    ↪ Electron_Prev_State(:,2)>Box_pos(2,3))))),3) ...
522 =random(Velocity_PDF);
523 Electron_State( (Top_Box_Specular==0 & Electron_State(:,1)>Box_pos(2,1) &
    ↪ Electron_State(:,1)<Box_pos(2,2) & ((Electron_State(:,2)>Box_pos(2,3) &
    ↪ Electron_Prev_State(:,2)>Box_pos(2,3))))),4) ...
524 =random(Velocity_PDF);
525
526 %Bottom Horizontal
527 Electron_State( (Bottom_Box_Specular==0 & Electron_State(:,1)<Box_pos(1,2) &
    ↪ Electron_State(:,1)>Box_pos(1,1)) & (Electron_State(:,2)<Box_pos(1,4)) & ...
528 (Electron_Prev_State(:,1)>Box_pos(1,1) & Electron_Prev_State(:,1)<Box_pos(1,2)),3) =
    ↪ random(Velocity_PDF);

```

```

529 Electron_State( (Bottom_Box_Specular==0 & Electron_State(:,1)<Box_pos(1,2) &
    ↳ Electron_State(:,4)<0 & Electron_State(:,1)>Box_pos(1,1)) &
    ↳ (Electron_State(:,2)<Box_pos(1,4)) &...
530     (Electron_Prev_State(:,1)>Box_pos(1,1) & Electron_Prev_State(:,1)<Box_pos(1,2)),4) =
    ↳ random(Velocity_PDF);
531 %Top Horizontal
532 Electron_State( (Top_Box_Specular==0 & Electron_State(:,1)<Box_pos(2,2) &
    ↳ Electron_State(:,1)>Box_pos(2,1)) & (Electron_State(:,2)>Box_pos(2,3)) &...
533     (Electron_Prev_State(:,1)>Box_pos(2,1) & Electron_Prev_State(:,1)<Box_pos(2,2)),3) =
    ↳ random(Velocity_PDF);
534 Electron_State( (Top_Box_Specular==0 & Electron_State(:,4)>0 & Electron_State(:,1)<Box_pos(2,2)
    ↳ & Electron_State(:,1)>Box_pos(2,1)) & (Electron_State(:,2)>Box_pos(2,3)) &...
535     (Electron_Prev_State(:,1)>Box_pos(2,1) & Electron_Prev_State(:,1)<Box_pos(2,2)),4) =
    ↳ -random(Velocity_PDF);
536 %%
537 %Add scattering
538 j = rand(nElectrons,1) < P_Scattering;
539 Electron_State(j,3:4) = random(Velocity_PDF,[sum(j),2]);
540 %%
541 %Electron shifting
542 %Region 1 (Bottom left)
543 Electron_State((Electron_State(:,1)>Box_pos(1,1) & Electron_State(:,1)<Box_pos(1,2) &
    ↳ ((Electron_State(:,2)<Box_pos(1,4) & Electron_Prev_State(:,2)<Box_pos(1,4))) &...
544     Electron_Prev_State(:,1)<Box_pos(1,1)),1) = 2*Box_pos(1,1) - Electron_State(
    ↳ (Electron_State(:,1)>Box_pos(1,1) & Electron_State(:,1)<Box_pos(1,2) &
    ↳ ((Electron_State(:,2)<Box_pos(1,4) & Electron_Prev_State(:,2)<Box_pos(1,4))) &...
545     Electron_Prev_State(:,1)<Box_pos(1,1)),1);
546 %Region 3 (Top left)
547 Electron_State((Electron_State(:,1)>Box_pos(2,1) & Electron_State(:,1)<Box_pos(2,2) &
    ↳ ((Electron_State(:,2)>Box_pos(2,3) & Electron_Prev_State(:,2)>Box_pos(2,3))) &...
548     Electron_Prev_State(:,1)<Box_pos(2,1)),1) = 2*Box_pos(2,1) - Electron_State(
    ↳ (Electron_State(:,1)>Box_pos(2,1) & Electron_State(:,1)<Box_pos(2,2) &
    ↳ ((Electron_State(:,2)>Box_pos(2,3) & Electron_Prev_State(:,2)>Box_pos(2,3))) &...
549     Electron_Prev_State(:,1)<Box_pos(2,1)),1);
550 %Region 2 (Bottom right)
551 Electron_State((Electron_State(:,1)>Box_pos(1,1) & Electron_State(:,1)<Box_pos(1,2) &
    ↳ ((Electron_State(:,2)<Box_pos(1,4) & Electron_Prev_State(:,2)<Box_pos(1,4))) &...
552     Electron_Prev_State(:,1)>Box_pos(1,2)),1) = 2*Box_pos(1,2) - Electron_State(
    ↳ (Electron_State(:,1)>Box_pos(1,1) & Electron_State(:,1)<Box_pos(1,2) &
    ↳ ((Electron_State(:,2)<Box_pos(1,4) & Electron_Prev_State(:,2)<Box_pos(1,4))) &...
553     Electron_Prev_State(:,1)>Box_pos(1,2)),1);
554 %Region 4 (Top Right)
555 Electron_State((Electron_State(:,1)>Box_pos(2,1) & Electron_State(:,1)<Box_pos(2,2) &
    ↳ ((Electron_State(:,2)>Box_pos(2,3) & Electron_Prev_State(:,2)>Box_pos(2,3))) &...
556     Electron_Prev_State(:,1)>Box_pos(2,2)),1) = 2*Box_pos(2,2) - Electron_State(
    ↳ (Electron_State(:,1)>Box_pos(2,1) & Electron_State(:,1)<Box_pos(2,2) &
    ↳ ((Electron_State(:,2)>Box_pos(2,3) & Electron_Prev_State(:,2)>Box_pos(2,3))) &...
557     Electron_Prev_State(:,1)>Box_pos(2,2)),1);
558
559 %Bottom Horizontal (going top down)
560 Electron_State( (Electron_State(:,1)<Box_pos(1,2) & Electron_State(:,1)>Box_pos(1,1) &
    ↳ (Electron_State(:,2)<Box_pos(1,4) & Electron_Prev_State(:,2)>Box_pos(1,4)) &...
561     (Electron_State(:,4)<0)),2) = 2*Box_pos(1,4) + Electron_State(
    ↳ (Electron_State(:,1)<Box_pos(1,2) & Electron_State(:,1)>Box_pos(1,1) &
    ↳ (Electron_State(:,2)<Box_pos(1,4) & Electron_Prev_State(:,2)>Box_pos(1,4)) &...
562     (Electron_State(:,4)<0)),2);
563 %Top Horizontal (going bottom up)
564 Electron_State( (Electron_State(:,1)<Box_pos(2,2) & Electron_State(:,1)>Box_pos(2,1) &
    ↳ (Electron_State(:,2)>Box_pos(2,3) & Electron_Prev_State(:,2)<Box_pos(2,3)) &...
565     (Electron_State(:,4)>0)),2) = 2*Box_pos(2,3) - Electron_State(
    ↳ (Electron_State(:,1)<Box_pos(2,2) & Electron_State(:,1)>Box_pos(2,1) &
    ↳ (Electron_State(:,2)>Box_pos(2,3) & Electron_Prev_State(:,2)<Box_pos(2,3)) &...
566     (Electron_State(:,4)>0)),2);
567 %Electron shifting end

```



```

568 %%
569 % Stores the Electron [x y] positions in the Trajectories vector
570 ... for each different electron in a new column
571 for j = 1:nPlotted_Electrons
572     Trajectories_x(i,j) = Electron_State(j,1);
573     Trajectories_y(i,j) = Electron_State(j,2);
574 end
575 %To calculate the thermal energy, Maxwell's principle of equipartition
576 ... is used, where the final equation then becomes;
577     Temperature(i) = ( sum (Electron_State(:,3).^2) + sum(Electron_State(:,4).^2)) * Mass_n
        ↪ / k / 2 / nElectrons;
578 %To calculate the current density
579 J(i,1) = Qe.*EConcentration.*mean(Electron_State(:,3));
580 J(i,2) = Qe.*EConcentration.*mean(Electron_State(:,4));
581 % Add the temperature and current data to the respective plots
582 Temp_Plot(i,1) = Temperature(i);
583 Current_Plot(i,1) = J(i,1)^2 + J(i,2)^2;
584 %Shows the pathing of the electron, as well as the updating trajectory
585 if Show_Movie && mod(i,2)
586     figure(1)
587     plot(Electron_State(1:nPlotted_Electrons,1)./1e-9,Electron_State(1:nPlotted_Electrons,2)
        ↪ ./1e-9,'o');
588     grid on;
589     axis([0 Length/1e-9 0 Height/1e-9]);
590     xlabel('x (nm)');
591     ylabel('y (nm)');
592     title(sprintf("Plotting (%d/%d) electron at constant
        ↪ velocity",nPlotted_Electrons,nElectrons));
593     hold on;
594     for j=1:size(Box_pos,1)
595         plot([Box_pos(j, 1) Box_pos(j, 1) Box_pos(j, 2) Box_pos(j, 2) Box_pos(j,
            ↪ 1)]./1e-9,...
596             [Box_pos(j, 3) Box_pos(j, 4) Box_pos(j, 4) Box_pos(j, 3) Box_pos(j, 3)]./1e-9,
            ↪ 'k-');
597     end
598     hold off;
599     pause(0.01)
600 end
601 end
602 %%
603 figure("name","Trajectory, temperature and speed results results")
604 subplot(2,2,1)
605 plot(Trajectories_x(:,1:nPlotted_Electrons)./1e-9, Trajectories_y(:,1:nPlotted_Electrons)./1e-9, '.'
    ↪ );
606 hold on;
607 for j=1:size(Box_pos,1)
608     plot([Box_pos(j, 1) Box_pos(j, 1) Box_pos(j, 2) Box_pos(j, 2) Box_pos(j, 1)]./1e-9,...
609         [Box_pos(j, 3) Box_pos(j, 4) Box_pos(j, 4) Box_pos(j, 3) Box_pos(j, 3)]./1e-9, 'k-');
610 end
611 hold off
612 axis([0 Length/1e-9 0 Height/1e-9]);
613 xlabel('x (nm)');
614 ylabel('y (nm)');
615 grid on;
616 title(sprintf("Trajectories of (%.2d/%.2d) electron(s) at constant
    ↪ velocity",nPlotted_Electrons,nElectrons),'interpreter','latex');
617 subplot(2,2,2)
618 plot(Time_Step*(0:Iterations-1), Temperature);
619 grid on;
620 xlim([0 Time_Step*Iterations])
621 title(sprintf("Temperature of the region, Average Temperature: %.2f
    ↪ (K)",mean(Temperature)),'interpreter','latex')
622 xlabel('Time (s)');
623 ylabel('Temperature (K)');

```

```

624 subplot(2,2,3)
625 Velocity = sqrt(Electron_State(:,3).^2 + Electron_State(:,4).^2);
626 histogram(Velocity);
627 title(sprintf("Electron Velocity, Average Velocity %.2d
↪ (m/s)",mean(Velocity)), 'interpreter','latex');
628 xlabel("Speed (m/s)");
629 ylabel("Number of particles");
630 grid on;
631 subplot(2,2,4)
632 plot(Time_Step*(0:Iterations-1),Current_Plot)
633 title(sprintf("Jx - Drift Current Density along x-axis, Average : %.2d
↪ (A/m)",mean(Current_Plot)), 'interpreter','latex');
634 xlabel('Time (s)');
635 ylabel('Current Density (A/m)');
636 grid on;
637 axis tight;
638 %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
↪ Results','[Part3]Trajectory_Temperature_DriftCurr.png'),'png')
639 %%
640 Density = hist3(Electron_State(:,1:2),[200 100]);
641 N = 20;
642 sigma = 3;
643 %Creating a Gaussian filtering matrix
644 [x,y]=meshgrid(round(-N/2):round(N/2), round(-N/2):round(N/2));
645 G=exp(-x.^2/(2*sigma^2)-y.^2/(2*sigma^2));
646 G=G./sum(G(:));
647 Density = conv2(Density,G,'same') / (Height./size(Density,1)*Length./size(Density,2));
648 %%
649 %Plot drift current
650 figure('Name','Drift current (x-axis) and Electron Density')
651 subplot(2,1,1)
652 surf(conv2(Density,G,'same'));
653 xlabel('x (nm)')
654 ylabel('y (nm)')
655 zlabel('Bin count')
656 axis tight
657 title("Electron density region (3D view)", 'interpreter','latex');
658 %%
659 % Plot the electron density
660 subplot(2,1,2)
661 surf(conv2(Density,G,'same'));
662 xlabel('x (nm)')
663 ylabel('y (nm)')
664 zlabel('Bin count')
665 axis tight
666 title("Electron density region (Top down view)", 'interpreter','latex');
667 view(2)
668 %saveas(gcf,fullfile('D:\School Work\ELEC 4700\My 4700 Code\Assignment 3\Simulation
↪ Results','[Part3]ElectronDensity.png'),'png')

```

Source Code 3: Part 3 - Coupled Simulator