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Introduction:

Tree is a collection of nodes and among those nodes, one node is

taken as root node. Rest of the nodes are taken as disjoint subsets.

Each subset is a tree again or a subtree again.

Root -> The first node of the tree.

Parent -> A node is a parent to its very next descendants.

children -> descendants which are connected by a single edge with a node.

Siblings -> Children of same parents.

Descendants -> they are the sets of nodes which can be reached from a particular node downwards.

Ancestors -> Between the path of two particular nodes, all other nodes along the path are called ancestors.

Degree of a node -> Number of direct children of a particular node.

Leaf Nodes -> Nodes with degree 0 are leaf nodes./External nodes./Terminal nodes

Non-Leaf Nodes -> Nodes with degrees > 0 are non-leaf nodes/internal nodes/non-terminal nodes.

Levels -> starts from 1 and horizontally measured .

Height -> Root is of height 0, So height of a tree starts from 0 onwards till the last reachable node.

Forest -> A collection of tree is a forest.

Binary tree -> Every node can have max true children min 0 children.

Shapes of binary tree -> For n nodes, $2n C_n / n+1$ binary trees can be formed.

Binary trees of max height -> For n nodes, 2^{n-1} binary trees of max height are possible.

Binary trees of max height(labeled nodes) -> For n label nodes, $(2n C_n / n+1) * n!$ binary trees of max height are possible.

Minimum Nodes of a binary tree -> $n=h+1$ (h =height)

Maximum Nodes of a binary tree -> $n= 2^{h+1} - 1$; (h =height)

Minimum Height of a binary tree -> $\log_2 (n+1)-1$;

Maximum Height of a binary tree -> $h=n-1$; (n =node)

In Binary tree ,the number of $\deg(2) = \text{the number of } \deg(0) + 1$

Strict Binary Tree -> The binary tree which can have either 0 child or 2 children.

For Strict Binary Tree ->

Minimum Nodes -> $(2^h)+1$ (h=height)

Maximum Nodes -> $2^{h+1} - 1$

Minimum Height -> $\log_2(n+1)-1$ (n=nodes)

Maximum Height -> $(n-1)/2$ (n=nodes)

External Nodes(Leaf Nodes)=Internal Nodes(Non-leaf nodes)+1

M-ary Trees -> the degree of the tree is M,so in M-ary trees,every nodes of the tree can have from 0 to at most M children.Not more than that.

Strict M-ary Trees -> Every nodes of the tree can have either 0 children or M children.

For M-ary Trees->

Minimum Nodes -> $Mh + 1$ (M=degree,h=height)

Maximum Nodes -> $(M^{(h+1)}-1)/(M-1)$ (M=degree,h=height)

Minimum Height -> $h = (n-1)/M$

(M=degree,h=height,n=nodes)

Maximum Height -> $\log_M[n(M-1)+1]-1$

(M=degree,h=height,n=nodes)

External Nodes(Leaf Nodes)

$= (M-1) * (\text{Internal Nodes(Non-leaf nodes)}) + 1$