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Partial Differential Equations

Proceedings of a Symposium held in
Tianjin, June 23 – July 5, 1986



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FOREWORD

This volume contains a selection of papers presented at the 7th symposium on differential geometry and differential equations(=DD7), which took place at Nankai Institute of Mathematics, Tianjin, China, June 23 — July 5, 1986. The subject was partial differential equations. It was a culmination of a year-long activity in 1985-1986 at the institute. A list of the other papers presented at the symposium can be found at the end of this volume, some of which will be published elsewhere.

For the record I would like to give a list of the preceding DD-Symposia as follows:

	<u>Subject</u>	<u>Date</u>	<u>Place</u>	<u>Publication</u>
DD1	Differential geometry and differential equations	Aug. 18- Sept. 21, 1980	Beijing, China	Proceedings of the 1980 Beijing Symposium on Differential Geometry and Differential Equations, Science Press, Beijing, China, 1982
DD2	Differential geometry	Aug. 20- Sept. 13, 1981	Shanghai-Hefei, China	Proceedings of the 1981 Symposium on Differential Geometry and Differential Equations, Shanghai-Hefei, Science Press, Beijing, China, 1984
DD3	Partial differential equations	Aug. 23- Sept. 16, 1982	Changchun, China	Proceedings of the 1982 Changchun Symposium on Differential Geometry and Differential Equations, Science Press, Beijing, China, 1986
DD4	Ordinary differential equations	Aug. 29- Sept. 10, 1983	Beijing, China	Proceedings of the 1983 Beijing Symposium on Differential Geometry and Differential Equations, Science Press, Beijing, China, 1986
DD5	Computation on partial differential equations	Aug. 13- aug. 17, 1984	Beijing, China	Proceedings of the 1984 Beijing Symposium on Differential Geometry and Differential Equations, Science Press, Beijing, China, 1985
DD6	Differential geometry	Jun. 21- Jul. 6, 1985	Shanghai, China	Differential Geometry and Differential Equations, Proceedings, Shanghai 1985, Lecture Notes in Mathematics 1255, Springer-Verlag 1987

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June 1987

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A TABLE OF CONTENTS OF DD7 SYMPOSIUM ON PARTIAL
DIFFERENTIAL EQUATIONS — A SELECTION OF PAPERS

1.	F.Almgren, W.Browder & E.H.Lieb : Co-area, Liquid Crystals and Minimal Surfaces	1
2.	Richard Beals : Non-elliptic Problems and Complex Analysis	23
3.	Chen Shuxing : Smoothness of Shock Front Solutions for System of Conservation Laws.	38
4.	Chen Yazhe : On Degenerate Monge-Ampere Equations.	61
5.	Fu Hong-Yuan : Initial and Boundary Problems for the Degenerate or Singular Systems of Filtration Type.	69
6.	Huang Yumin : On Interior Regularity of Solutions of a Class of Hypoelliptic Differential Equations.	84
7.	Jin Zhiren : A Counterexample to the Yamabe Problem for Complete Noncompact Manifolds.	93
8.	Li Huilai : Free Boundary Problem for Degenerate Parabolic Equations.	102
9.	Li Ta-tsien & Zhao Yanchun : Global Perturbation of the Riemann Problem for the System of One-dimensional Isentropic Flow.	131
10.	Qiu Qing-jiu & Qian Si-xin : Analysis of C^∞ Singularities for a Class of Operators with Varying Multiple Characteristics.	141
11.	Tan Yongji : An Inverse Problem for Nonlocal Elliptic BVP and Resistivity Identificating.	149

12. Jean E.Taylor :	160
Local Ellipticity of F and Regularity of F Minimizing Currents.	
13. Friedrich Tomi & A.J.Tromba :	174
A Geometric Proof of the Mumford Compactness Theorem.	
14. Wang Guanglie :	182
Harnack Inequalities for Functions in de Giorgi Parabolic Class.	
15. Wang Zhiqiang :	202
Equivariant Morse Theory for Isolated Critical Orbits and Its Applications to Nonlinear Problems.	
16. Wu Fantong :	224
A Class Diffractive Boundary Value Problem with Multiple Characteristic.	
17. Wu Lancheng :	240
Existence, Uniqueness and Regularity of the Minimizer of a Certain Functional.	
18. Yan Ziqian :	255
Everywhere Regularity for Solutions to Quasilinear Elliptic Systems.	
19. Zhang Kewei :	262
On the Dirichlet Problem of a Class of Elliptic Systems.	
20. Zhou Yulin & Guo Boling :	278
Initial Value Problems for a Nonlinear Singular Integral-Differential Equation of Deep Water.	