



Assignment

Course Code: CSE 133 .

Course Title: Data Structure.

Submitted To

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-Ans. to the Q. no. 1(a)

Given,

$$\text{Infix} = P - (Q * R * S + (G / H ^ I ^ J) * K)$$

$$\text{Reverse} =) K *) J ^ I ^ H / G (+ S * R * Q (- P .$$

Input	Stack	Prefix Expression.
))	
K)	K
*) *	K
)) *	K
J) *	KJ
^) *) ^	KJ
I) *) ^	KJ I
^) *) ^	KJ I ^
H) *) ^	KJ I ^ H
/) *) /	KJ I ^ H ^ /
G) *) /	KJ I ^ H ^ G
() *	KJ I ^ H ^ G /
+) +	KJ I ^ H ^ G / +
S) +	KJ I ^ H ^ G / * S
*) + *	KJ I ^ H ^ G / * S
R) + *	KJ I ^ H ^ G / * S R
*) + * *	KJ I ^ H ^ G / * S R
Q) + * *	KJ I ^ H ^ G / * S R Q
(KJ I ^ H ^ G / * S R Q * * +
-	-	KJ I ^ H ^ G / * S R Q * * +
P	-	KJ I ^ H ^ G / * S R Q * * + P
		KJ I ^ H ^ G / * S R Q * * + P -

Final Infix to Prefix Expression:-

$$P + * * Q R S * / G ^ H ^ I J K$$

Ans. to the Q. No. 1(b)

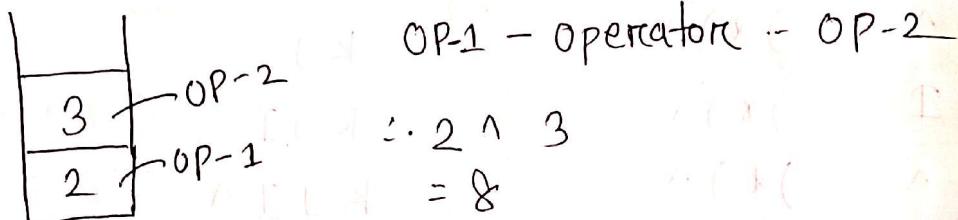
Given,

Postfix Expression: AB^C A A ^ * + D E / -

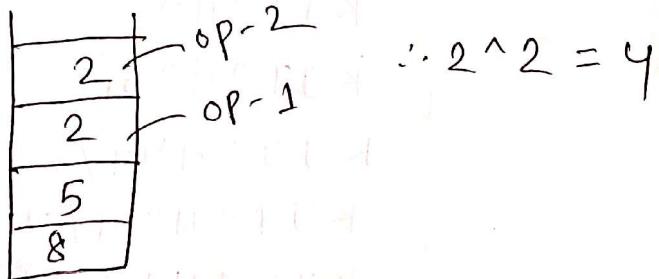
where, A=2, B=3, C=5, D=12, E=6

Postfix Expression: 2 3 ^ 5 2 2 ^ * + 12 6 / -

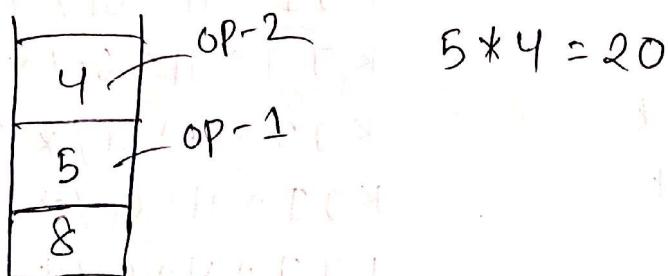
Step 1:-

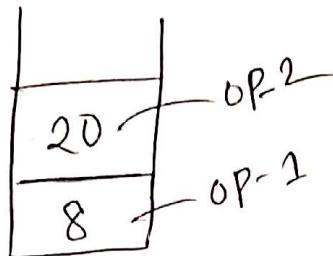


Step 2:-

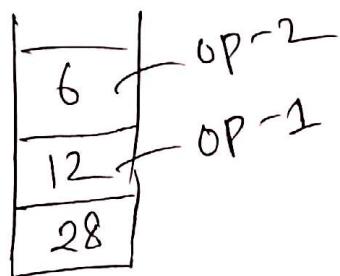


Step 3:-

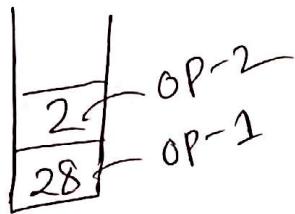


Step 4:-

$$\therefore 8 + 20 = 28$$

Step 5:-

$$\therefore 12 / 6 = 2$$

Step 6:-

$$28 - 2 = 26$$

$$\therefore \text{Ans} = 26$$

Ans. to the Q. No. 1 @

Given,

$$\text{Front} = 1$$

$$\text{Rear} = 4$$

Queue:

	B	C	D	E
0	1	2	3	4

f R

2. Enqueue(J)

J	B	C	D	E
0	1	2	3	4

R

$$\text{Front} = 1$$

$$\begin{aligned}\text{Rear} &= (4+1) \% 5 \\ &= 0\end{aligned}$$

2. Enqueue(K)

Queue is overflow.

3. Dequeue()

J		C	D	E
0	1	2	3	4

R

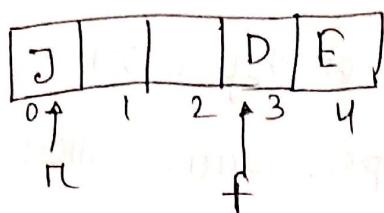
f

B removed from the queue.

$$\text{Front} = 2$$

$$\text{Rear} = 0.$$

4. Dequeue()

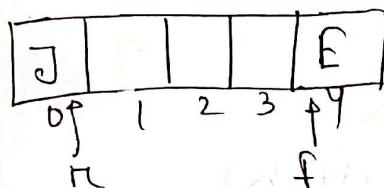


C removed from the Queue.

$$\text{Front} = 3$$

$$\text{Rear} = 0$$

5. Dequeue()

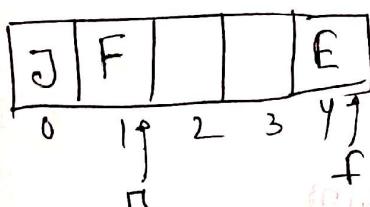


D removed from the Queue.

$$\text{Front} = 4$$

$$\text{Rear} = 0$$

6. Enqueue(F)



F insert into the Queue.

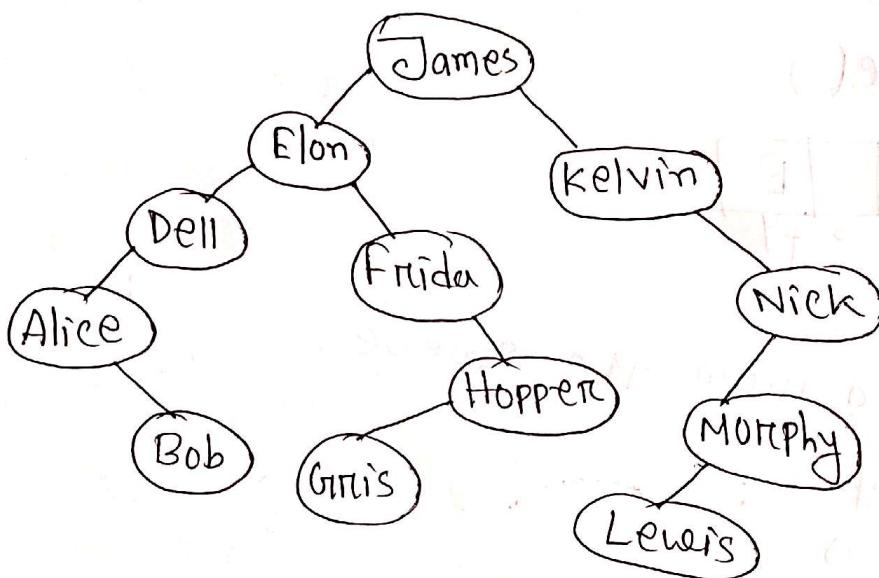
$$\text{Front} = 4$$

$$\text{Rear} = 1$$

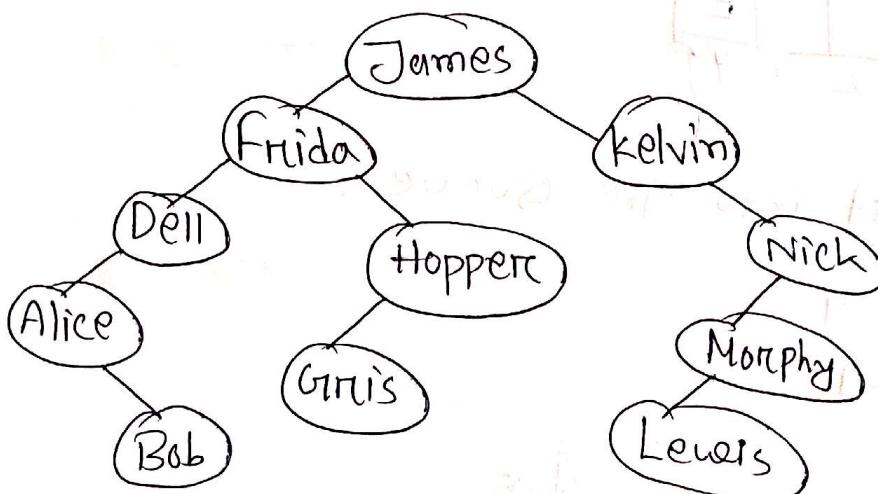
Ans

-Ans. to the Q. No. 2(a)

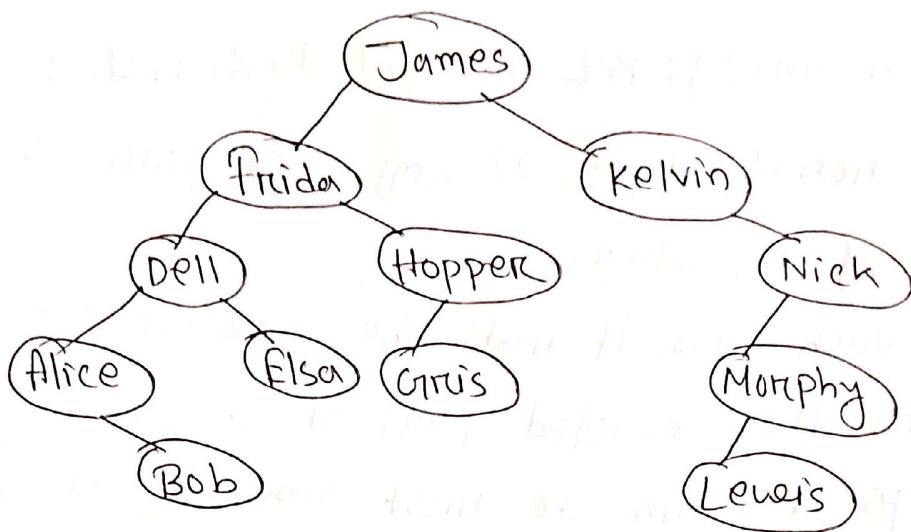
Given: {James, Kelvin, Nick, Morphy, Elon, Frida, Lewis, Dell, Hopper, Gruis, Alice, Bob}.

B.S.T :--Ans. to the Q. No 2(b)

After delete "Elon".

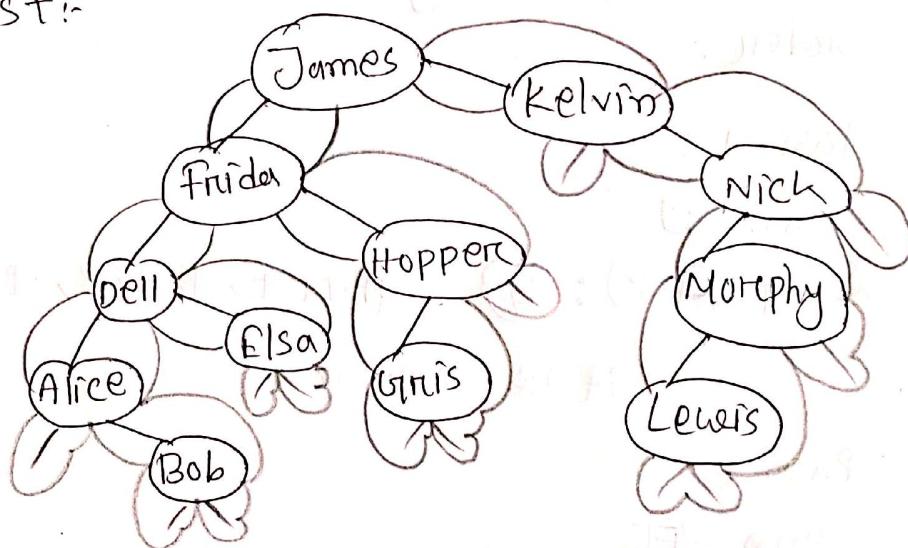


After Insert "Elsa".



Ans. to the Q. No. 2(c)

from 2(b), BST:-



Pre-order: James, Frida, Dell, Alice, Bob, Elsa, Hopper, Gris, Kelvin, Nick, Morphy, Lewis.

Post-order: Bob, Alice, Elsa, Dell, Gris, Hopper, Frida, Lewis, Morphy, Nick, Kelvin, James.

Ans. to the Q. No. 3(a)

Given Array: P, L, A, N, E, T, A, R, I, U, M.

Selection Sort is a simple comparison-based sorting algorithm.

In each pass, it finds the smallest element from the unsorted part of the array and swaps it with the first element of that unsorted part. This process repeats until the entire array is sorted in ascending order.

Pass 1:

$$\min = A$$

Swap (A, P): (A), L, P, N, E, T, A, R, I, U, M.

A is sorted.

Pass 2:

$$\min = A$$

Swap (A, L): (A), (A), P, N, E, T, L, R, I, U, M

A and A are sorted.

Pass 3:

$$\min = E$$

Swap (E, P): (A), (A), (E), N, P, T, L, R, I, U, M

Pass 4:-

 $\min = I$

Swap (I, N) :- (A), (A), (E), (I), P, T, L, R, N, U, M.

Pass 5:-

 $\min = L$

Swap (L, P) :- (A), (A), (E), (I), (L), T, P, R, N, U, M.

Pass 6:-

 $\min = M$

Swap (M, T) :- (A), (A), (E), (I), (L), (M), P, R, N, U, T.

Pass 7:-

 $\min = N$

Swap (N, P) :- (A), (A), (E), (I), (L), (M), (N), R, P, U, T.

Pass 8:-

 $\min = P$

Swap (P, R) :- (A), (A), (E), (I), (L), (M), (N), (P), R, U, T.

Pass 9:-

 $\min = R$ $\Rightarrow (A), (A), (E), (I), (L), (M), (N), (P), (R), U, T.$

Pass 10:-

 $\min = T$

swap (T, U) :- (A), (A), (E), (I), (L), (M), (N), (P), (R), (T), U.

Pass 11:-

 $\min = U$

Sorted Array : (A), (A), (E), (I), (L), (M), (N), (P), (R), (T), (U).

(Ans)

Ans. to the Q. no. 3(b)

From 3@, Sorted Array:

A	A	E	I	L	M	N	P	R	T	U
0	1	2	3	4	5	6	7	8	9	10

$$\text{key} = T; n = 11$$

$$\text{Initially } l=0, r=n-1$$

Step 1: Check the array is sorted in ascending/descending order.

Step 2: Find the middle element of the array.

Step 3: If arr[mid] = key, the search stop and value is found.

Step 4: If arr[mid] < key, left element is updated.

$$l = mid + 1$$

Step 5: If arr[mid] > key, right element is update.

$$r = mid - 1$$

Now,

case 1:

A	A	E	I	L	M	N	P	R	T	U
0	1	2	3	4	5	mid	6	7	8	10

$$mid = \frac{l+r}{2} = \frac{0+10}{2} = 5$$

$$arr[mid] < T$$

$$l = \text{mid} + 1$$

$$= 5 + 1$$

$$= 6; r = 10$$

case 2:

N	P	R	T	V
6	7	8	9	10

$$\text{mid} = \frac{6+10}{2} = \frac{16}{2} = 8$$

$$\text{arr[mid]} < T$$

$$l = \text{mid} + 1$$

$$= 8 + 1$$

$$= 9; r = 10$$

case 3: if arr[mid] == T then

T	V
9	10

$$\text{mid} = \frac{9+10}{2} = \frac{19}{2} = 9.5 \approx 9$$

$$\text{arr[mid]} = T \text{ in complete}$$

$\therefore T$ found at index 9.

from 9th element to 10th element to confirm T
from 9th element to 10th element to confirm T
from 9th element to 10th element to confirm T
from 9th element to 10th element to confirm T

Ans. to the Q. No. 3(c)

The three most common Asymptotic notations are Big O, Big Omega(Ω), and Big Theta(Θ).

i) Big O notation: Big O notation describes the upper bound or the worst case scenario for an algorithm's running time. It focuses on the maximum time an algorithm can take to complete.

Example: In a linear search algorithm, the worst case is when the target element is at the very end of the list or not present at all. The algorithm has to check every element. Thus, its time complexity is $O(n)$, where n is the no. of elements.

ii) Big Omega(Ω) notation: Big Omega notation describes the lower bound or the best-case scenario for an algorithm's running time. It is the opposite of Big O notation.

Example:- For a linear search algorithm, the best case is when the target element is the first element in the list. In this case, the

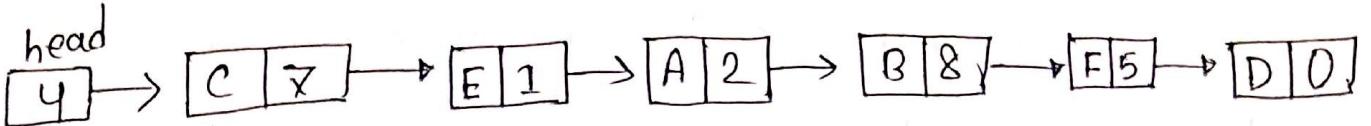
algorithm takes a constant amount of time, regardless of the list's size. Its time complexity is $\Theta(1)$.

(iii) Big theta(Θ) notation: Big theta notation describes the average-case performance, or a tight bound for an algorithm's running time. It is used when the best-case and worst-case complexities are the same.

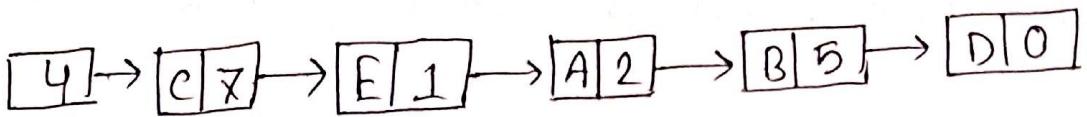
Example: The Merge Sort Algorithm performs consistently in all cases (best, worst and average) due to its divide-and-conquer approach. Its time complexity is $\Theta(n \log n)$, meaning its running time is always in the order of $n \log n$.

Q@

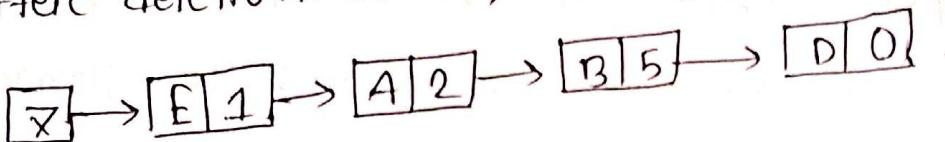
START = 4



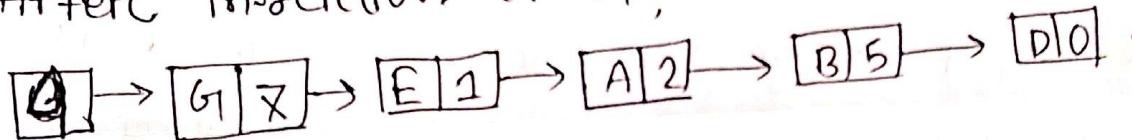
Q(B) After deletion of F,



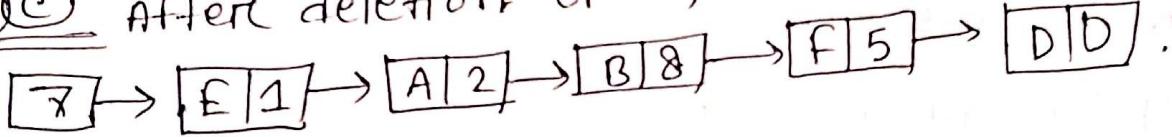
After deletion of C,



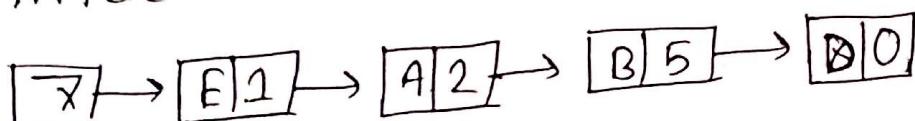
After insertion of G1,



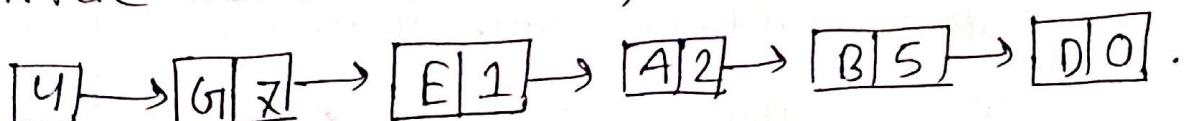
Q(C) After deletion of C,



After deletion of F,

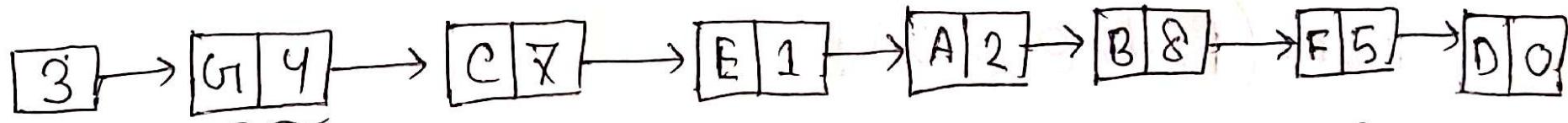


After insertion of G1,



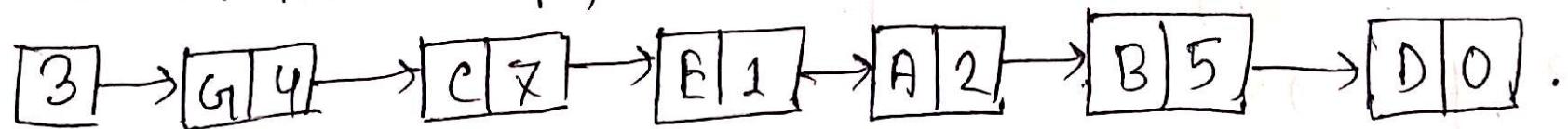
Qd

After insertion of G,

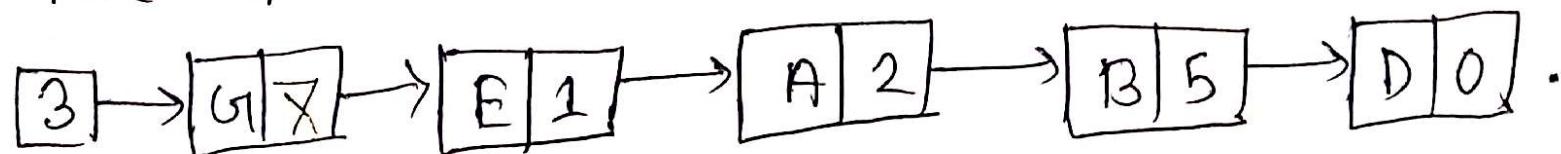


replaced 6 with 4 as the correct link for G.

After deletion of F,



After deletion of C.



Ans. to the Q. no. 5(a)

Starting from vertex F.

from (F),

$$F-d = 6 \checkmark$$

$$f-e = 8$$

$$f-g = 11$$

from (F, d):

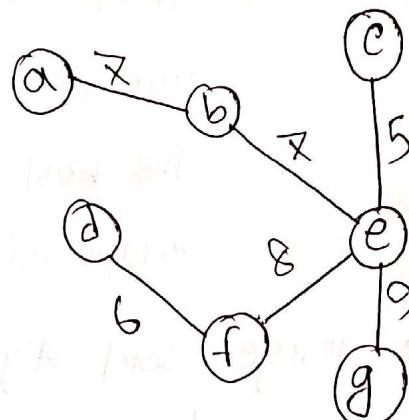
$$d-a = 9$$

$$d-b = 9$$

$$d-e = 15$$

$$f-e = 8 \checkmark$$

$$f-g = 11$$



from (f, d, e):

$$\text{Total minimum cost} = 6 + 8 + 5 + 7 + 9 = 42$$

$$e-g = 9$$

$$e-c = 5 \checkmark$$

$$e-b = 8$$

vertex = 8

from (f, d, e, c):

$$\text{Edge} = 8 - 1$$

$$c-b = 8$$

$$e-b = 8 \checkmark$$

from (f, d, e, c, b):

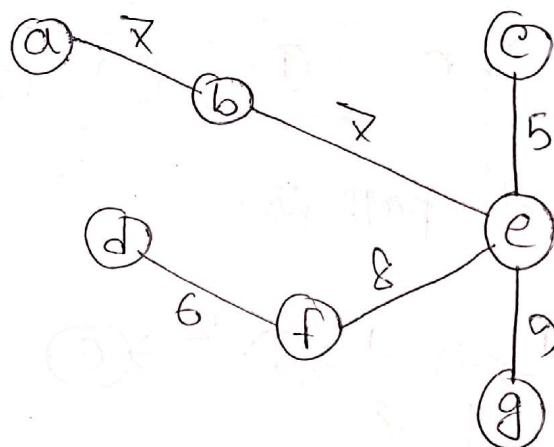
$$b-a = 8 \checkmark$$

from remaining vertex g:-

$$e-g = 9 \checkmark$$

Ans. to the Q. No. 5(b)

no.	source	destination	weight
1	c	e	5
2	d	f	6
3	a	b	7
4	b	e	7
5	e	f	8
x6	a	d	9
x7	b	d	9
8	e	g	9
x9	f	g	9
x10	d	e	11
			15

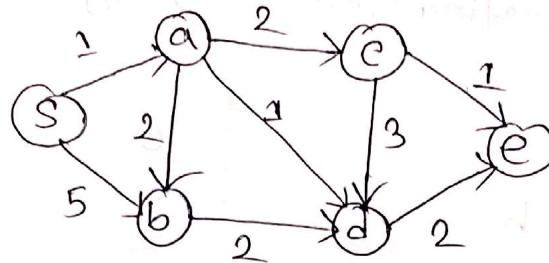


$$\text{vertex} = 7$$

$$\begin{aligned}\text{Edge} &= 7 - 1 \\ &= 6\end{aligned}$$

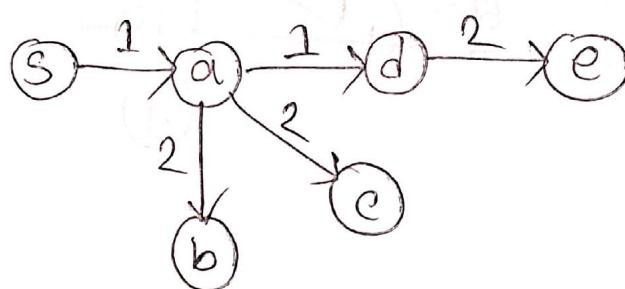
$$\begin{aligned}\text{Total cost} &= 5 + 6 + 7 + 7 + 8 + 9 \\ &= 42\end{aligned}$$

Ans. to the Q. no. 6 - @



Visited vertex	a	b	c	d	e
S	∞	∞	∞	∞	∞
S, a	①	5	∞	∞	∞
S, a, d	①	3	3	②	∞
S, a, d, b	①	③	3	②	4
S, a, d, b, c	①	③	③	②	4
S, a, d, b, c, e	①	③	③	②	④

The shortest path is:-



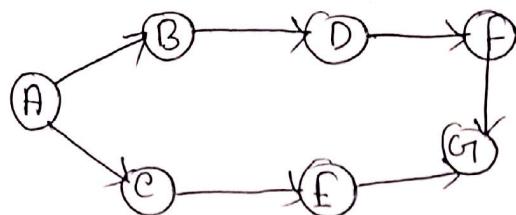
Path followed :- S-a-d-e

Ans. to the Q. No. 6b

Given nodes = {A, B, C, D, E, F, G}

edges = {(A, B), (A, C), (B, D), (C, E), (D, F), (E, G), (F, G)}.

The graph is:-



Unvisited Array:

F	F	F	F	F	F	F
0	1	2	3	4	5	6

Visited Array:

A	B	C	D	E	F	G
T	T	T	T	T	T	T

Queue :-

A	B	C	A	D	A'	B	B	F	E	G	D	G	E	F
---	---	---	---	---	----	---	---	---	---	---	---	---	---	---

B.F.S :-

A	B	C	D	E	F	G
---	---	---	---	---	---	---

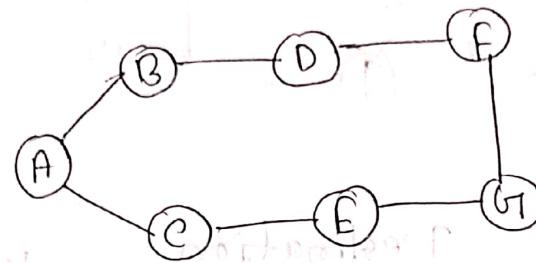
Ans

DFS

Given nodes = {A, B, C, D, E, F, G}

edges = {(A, B), (A, C), (B, D), (C, E), (D, F), (E, G), (F, G)}

The graph is,



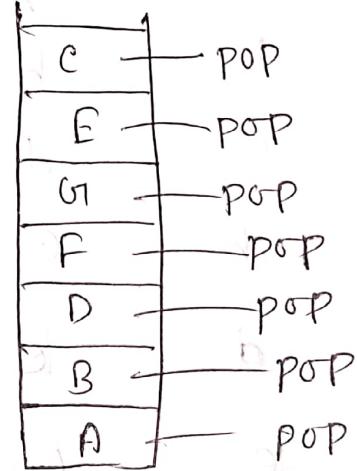
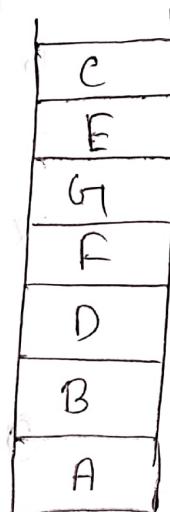
Unvisited Array:

F	F	F	F	f	f	f
0	1	2	3	4	5	6

Visited Array:

+	+	+	+	+	+	+
0	1	2	3	4	5	6

Stack:

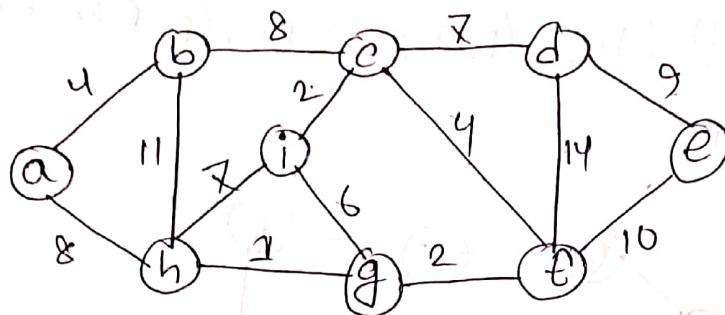


D.F.S :-

A	B	D	F	G	E	C
0	1	2	3	4	5	6

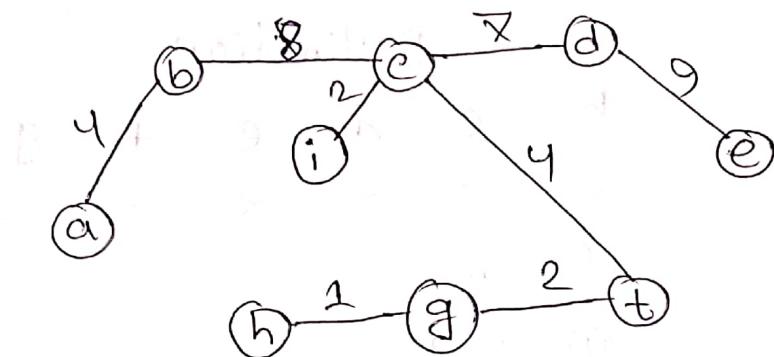
(Ans)

Ans. to the Q. No. 7@



no.	Source	Destination	weight
1	i	h	1
2	g	t	2
3	c	i	2
4	a	b	4
5	c	f	4
6	i	g	6
7	i	h	7
8	c	d	7
9	b	c	8
10	a	h	8
11	d	e	9
12	e	f	10
13	b	h	11
14	d	f	14

MST:-



$$\text{vertex} = 9$$

$$\begin{aligned}\text{Edge} &= 9 - 1 \\ &= 8\end{aligned}$$

$$\begin{aligned}\text{Total weight} &= 4 + 8 + 7 + 9 + 2 + 4 + 2 + 1 \\ &= 37\end{aligned}$$

Ans. to the Q.-No. 2(b)

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Source	Destination							
a	b	c	d	e	f	g	h	i
	∞	∞	∞	∞	∞	∞	∞	∞
a	(4)	∞	∞	∞	∞	∞	8	∞
a, b	(4)	12	∞	∞	∞	∞	(8)	∞
a, b, h	(4)	12	∞	∞	∞	(9)	(8)	15
a, b, h, g	(4)	12	∞	∞	(11)	(9)	(8)	15
a, b, h, g, f	(4)	(12)	25	21	(11)	(9)	(8)	15
a, b, h, g, f, e	(4)	(12)	19	21	(11)	(9)	(8)	15
a, b, h, g, f, e, i	(4)	(12)	(10)	21	(11)	(9)	(8)	(14)
a, b, h, g, f, e, i, d	(4)	(12)	(10)	(21)	(11)	(9)	(8)	(14)
a, b, h, g, f, e, i, d, e	(4)	(12)	(10)	(21)	(11)	(9)	(8)	(14)

The shortest path:-

