

Leakage-Resilience Meets Incompressibility

Maresh Sreekumar Rajasree

Post-Doctoral Fellow

Department of Computer Science & Engineering
IIT Delhi

(Joint work with Kaartik Bhushan (IITB), Rishab Goyal (UW-Madison), Venkata Koppula (IITD), Varun Narayanan (UCLA) and Manoj Prabhakaran (IITB))

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Contents

Contents

- Introduction

Contents

- Introduction
- Standard Security

Contents

- Introduction
- Standard Security
- Leakage-Resilience Security

Contents

- Introduction
- Standard Security
- Leakage-Resilience Security
- Incompressible Security

Contents

- Introduction
- Standard Security
- Leakage-Resilience Security
- Incompressible Security
- Leakage-Resilient Incompressible Security

Contents

- Introduction
- Standard Security
- Leakage-Resilience Security
- Incompressible Security
- Leakage-Resilient Incompressible Security
- Incompressible Functional Encryption

Contents

- Introduction
- Standard Security
- Leakage-Resilience Security
- Incompressible Security
- Leakage-Resilient Incompressible Security
- Incompressible Functional Encryption
- Conclusion

Introduction

Encryption Scheme

Encryption Scheme



ALICE

Encryption Scheme



ALICE



BOB

Encryption Scheme



ALICE



BOB

Encryption Scheme

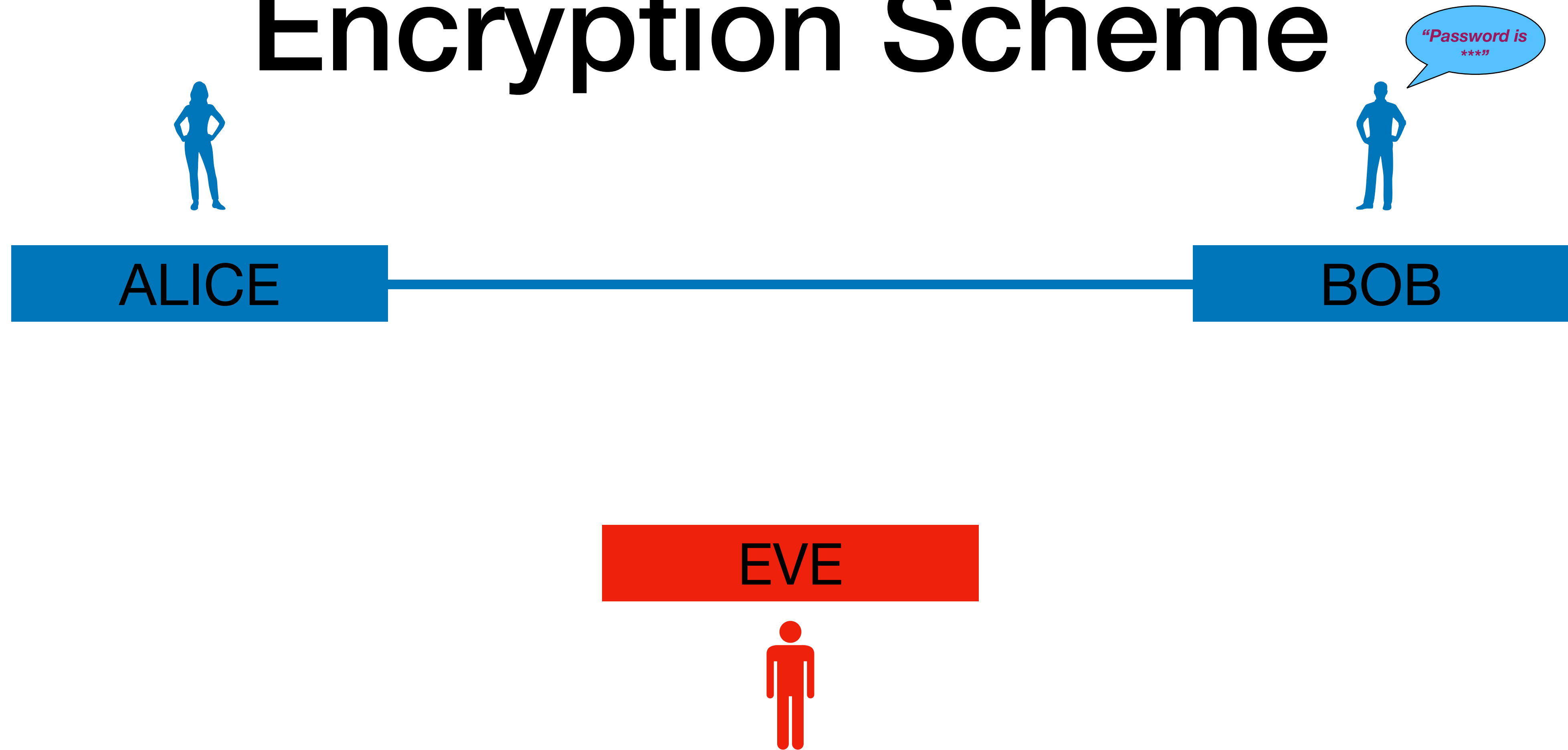


ALICE

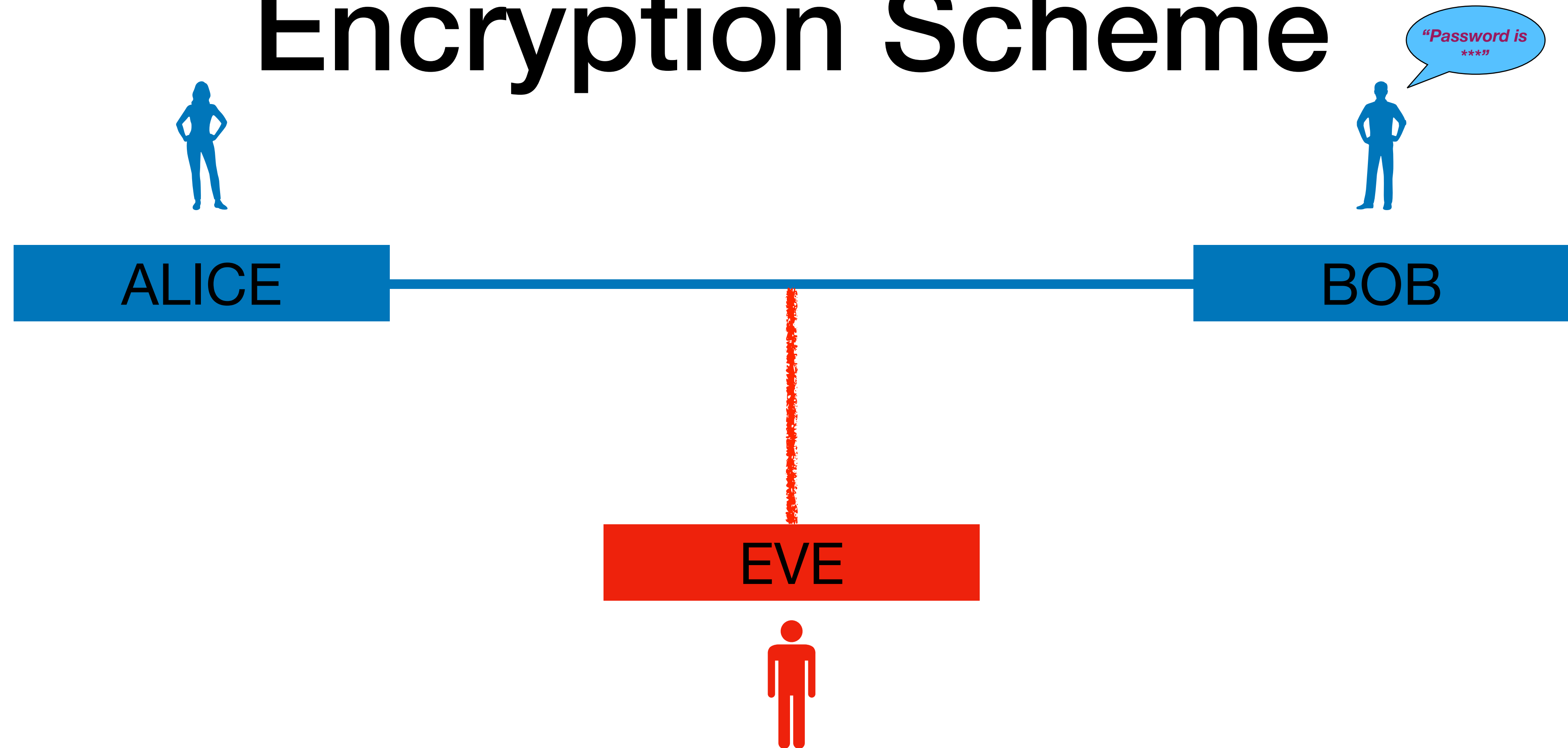


BOB

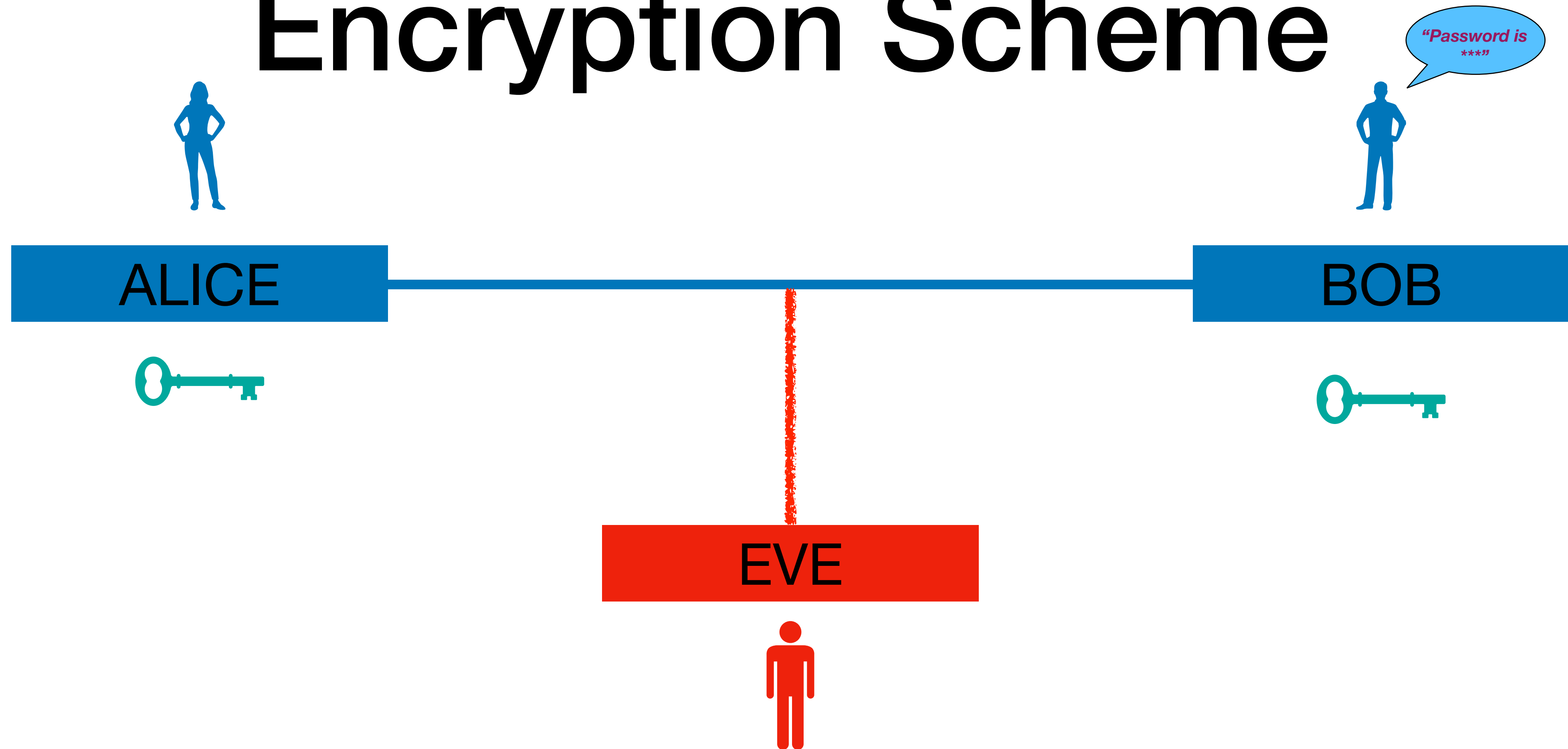
Encryption Scheme



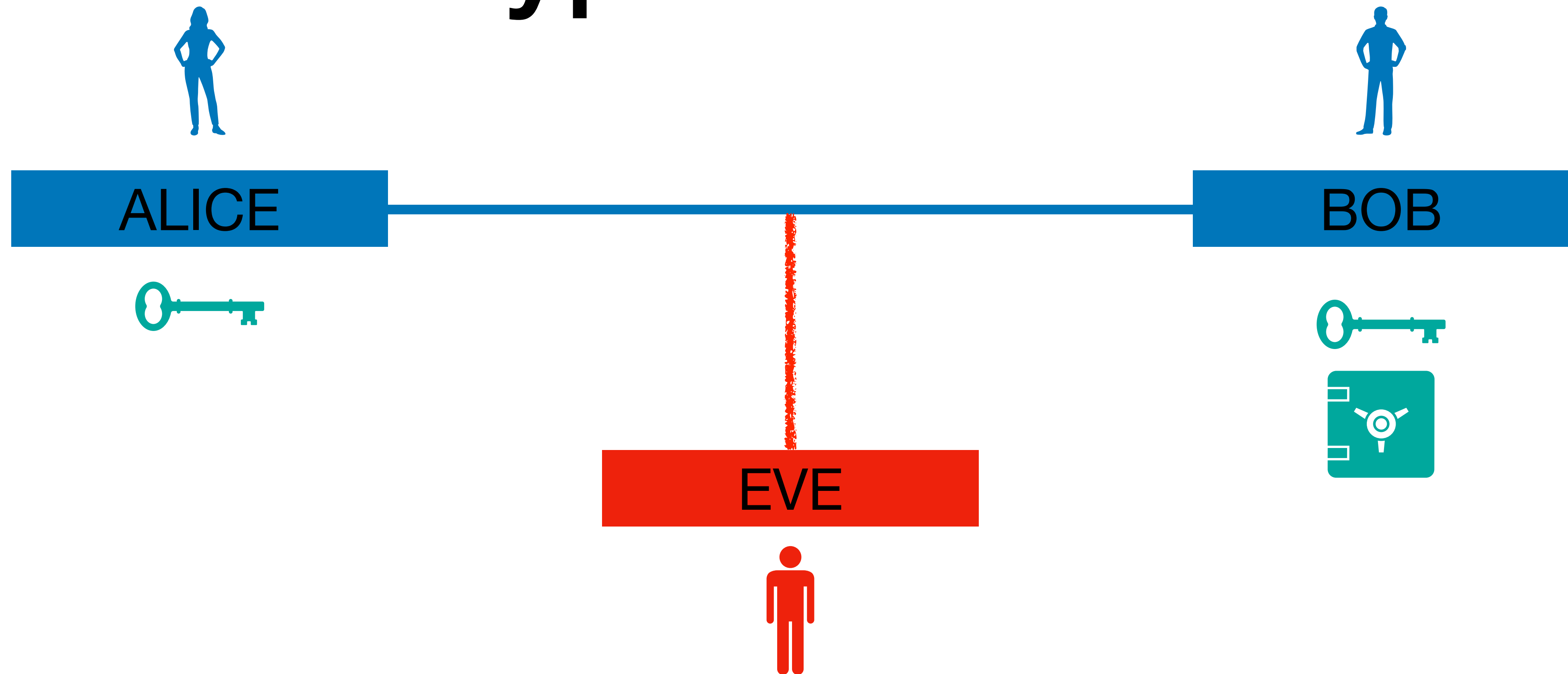
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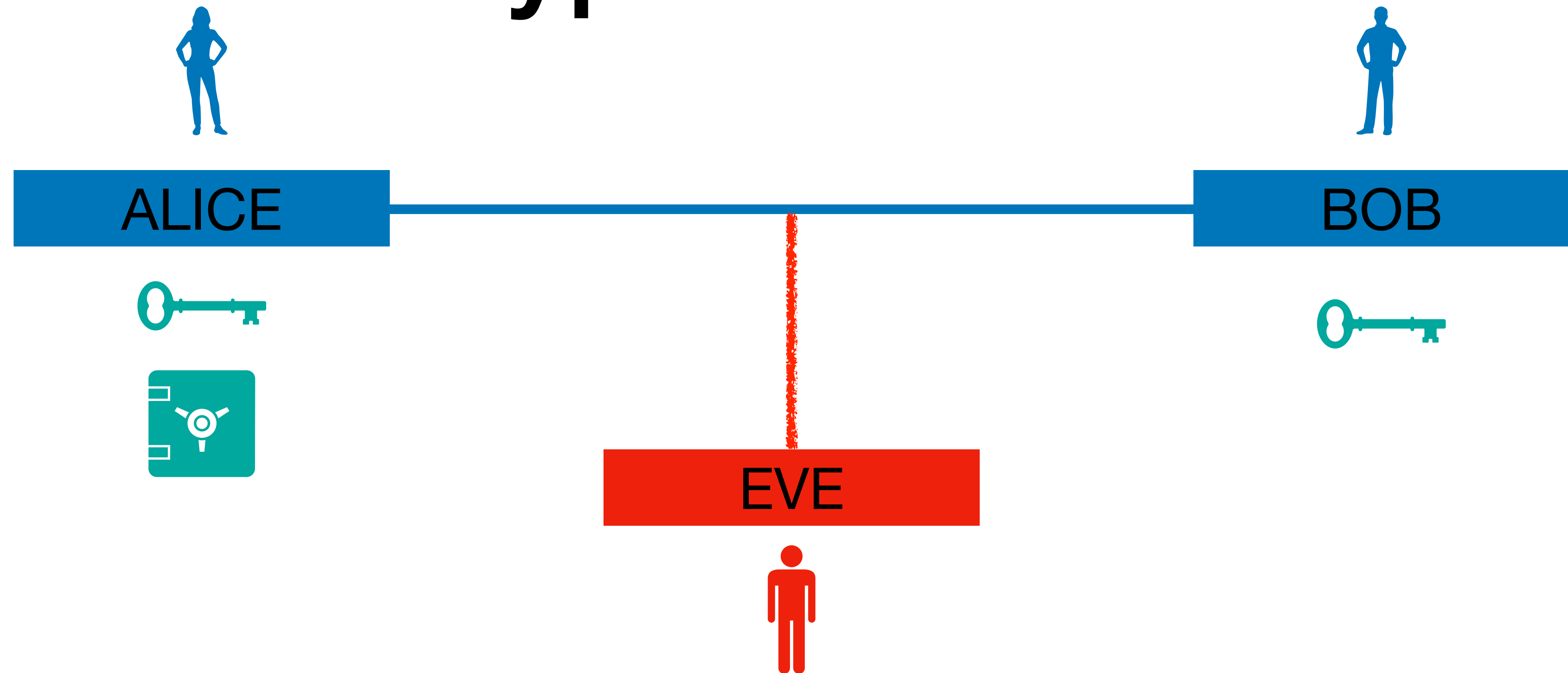
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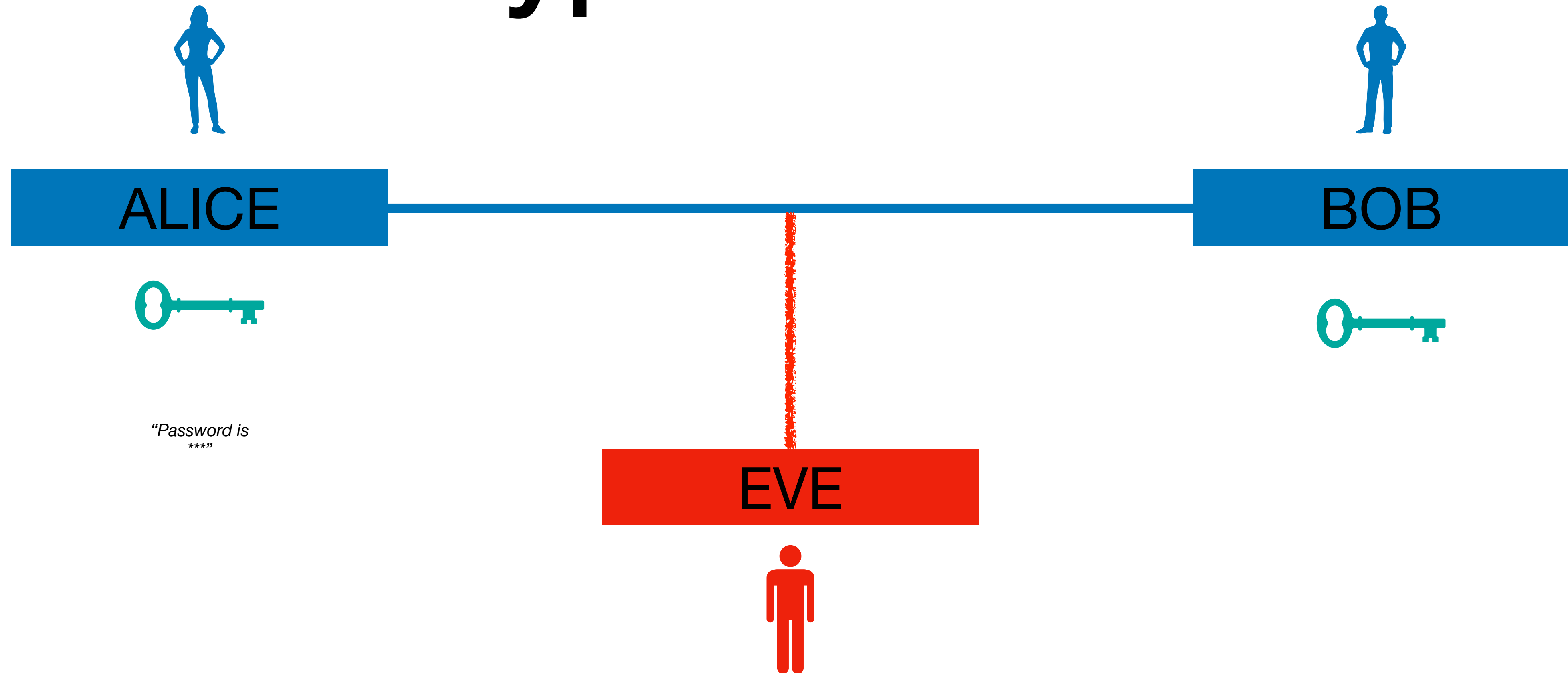
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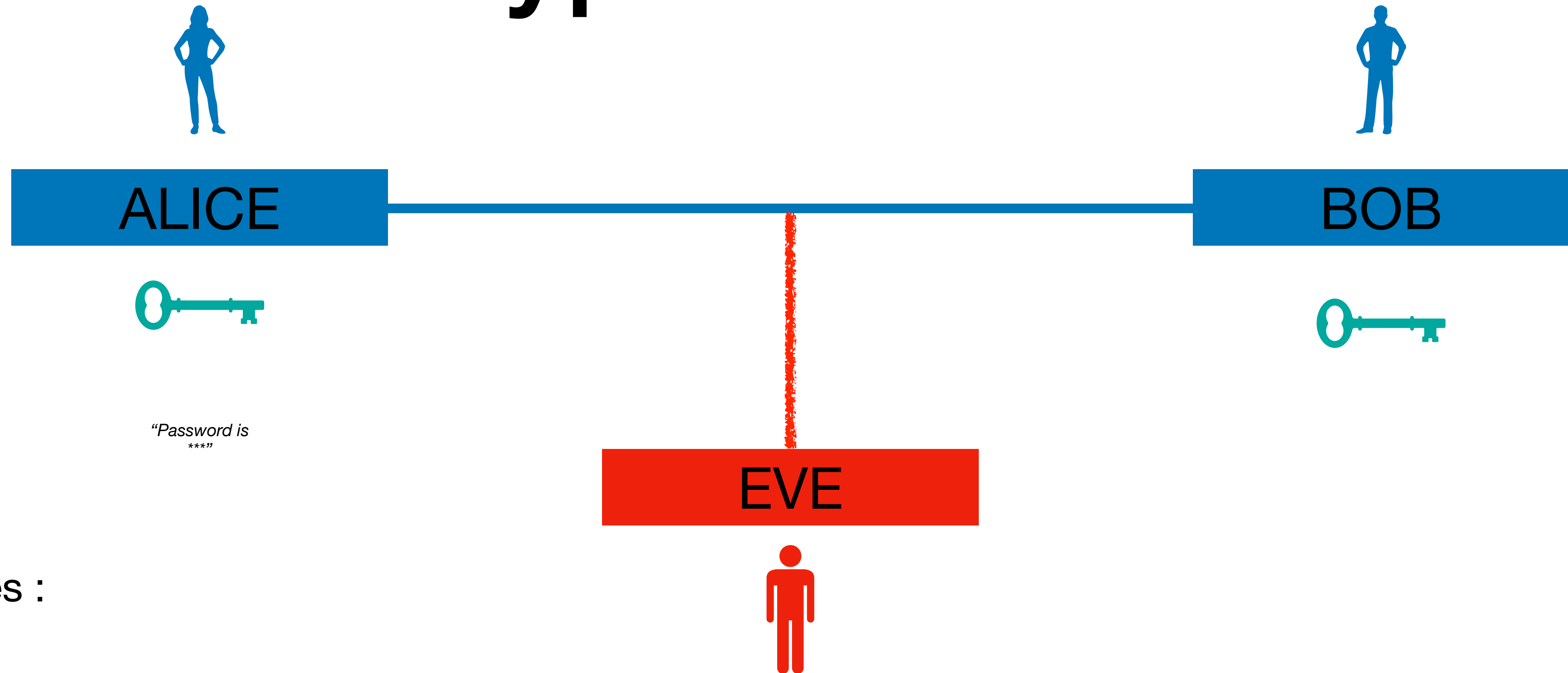
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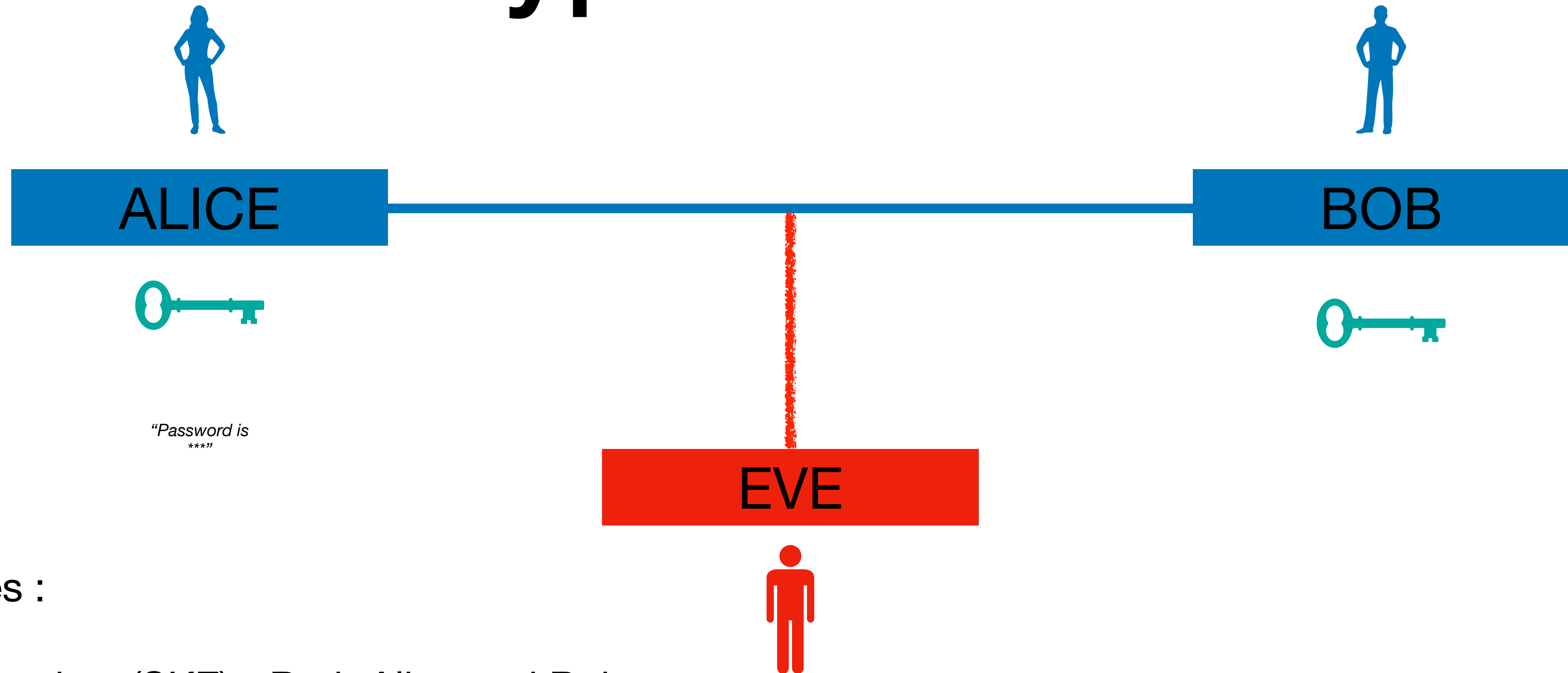


Encryption Scheme



2 types :

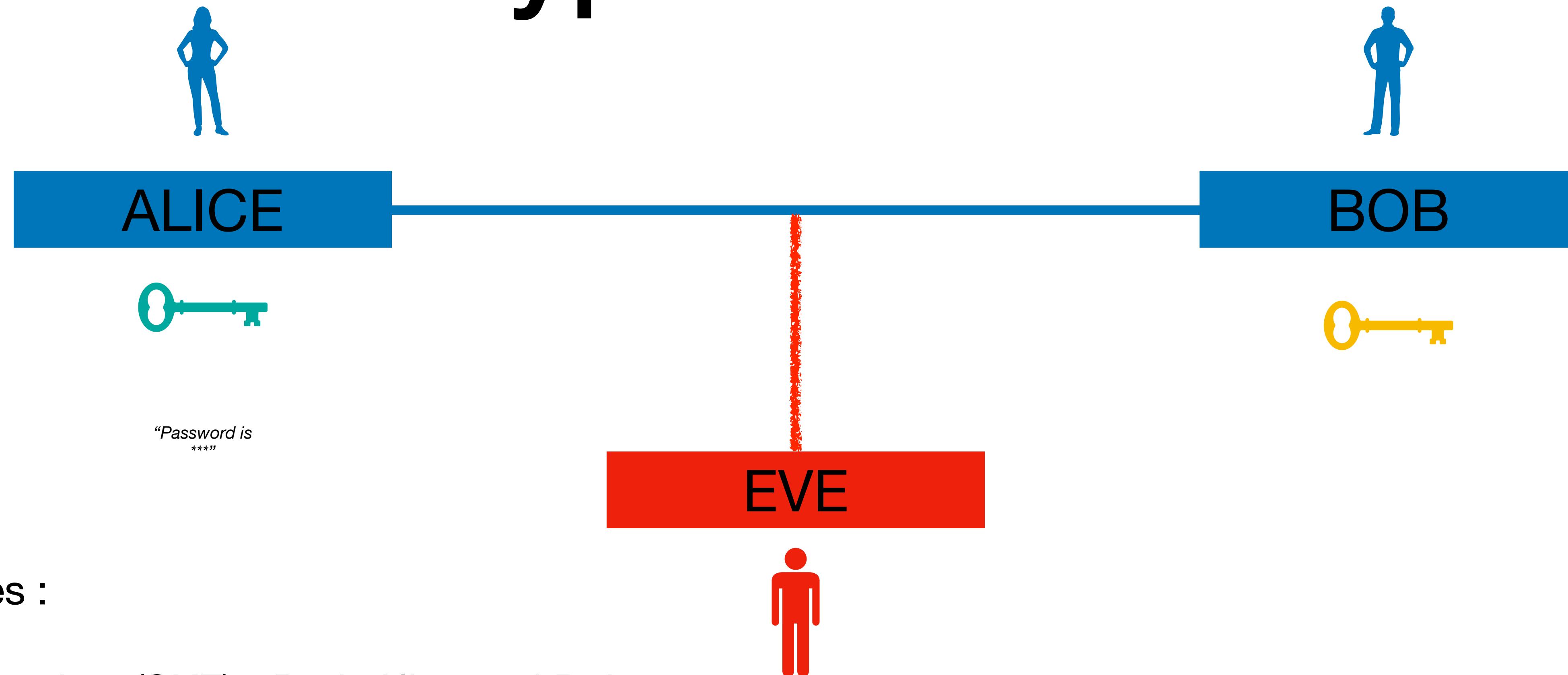
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2 types :

- secret key (SKE) - Both Alice and Bob have the same key.

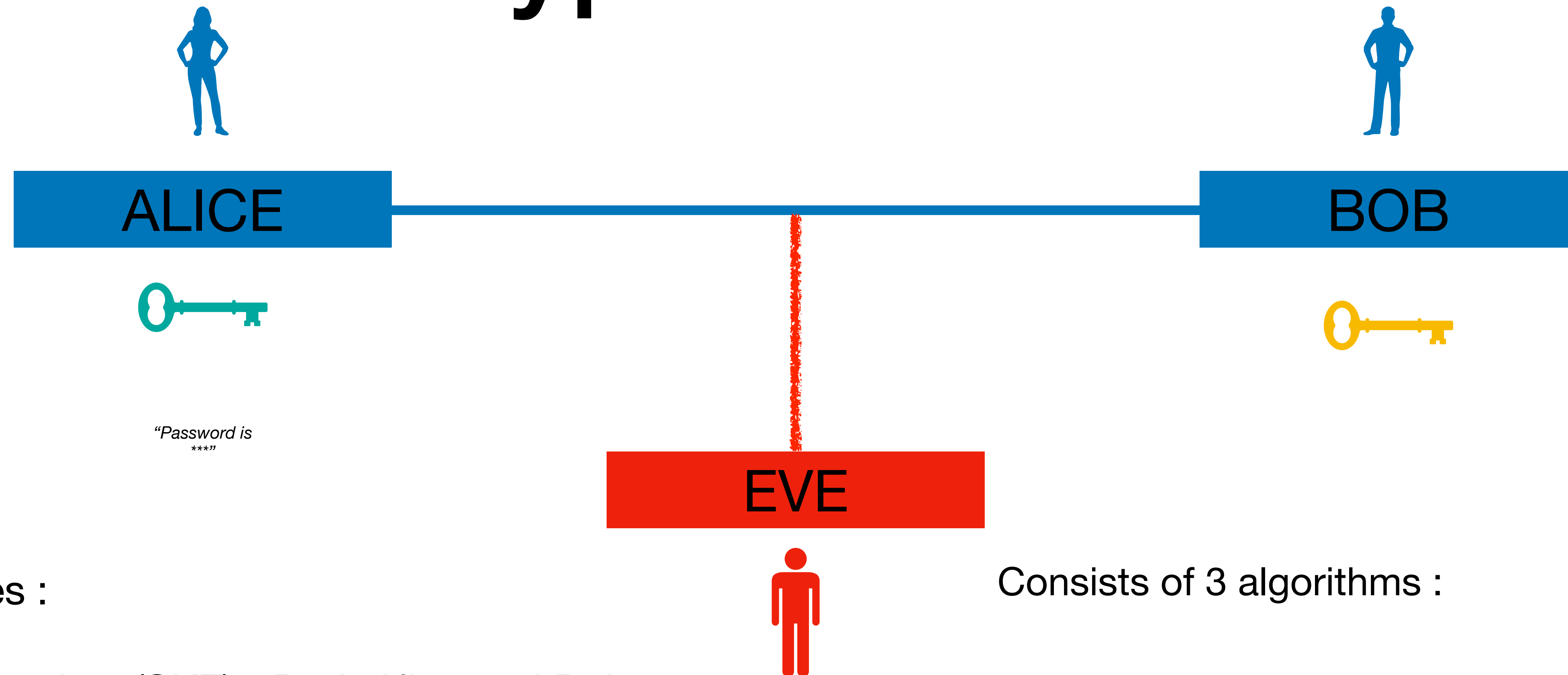
Encryption Scheme



2 types :

- secret key (SKE) - Both Alice and Bob have the same key.
- public key (PKE) - Encryptor has public key and decryption has secret key.

Encryption Scheme

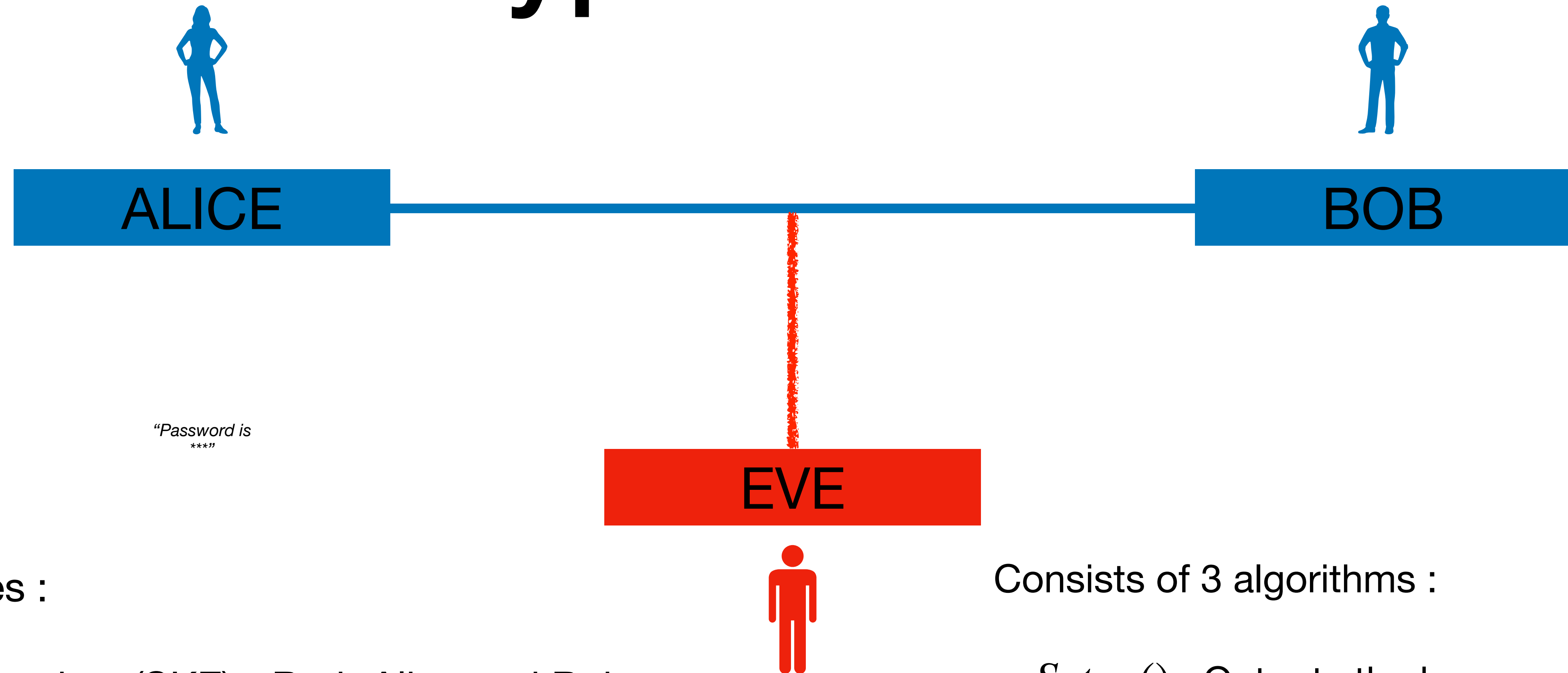


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Consists of 3 algorithms :

Encryption Scheme



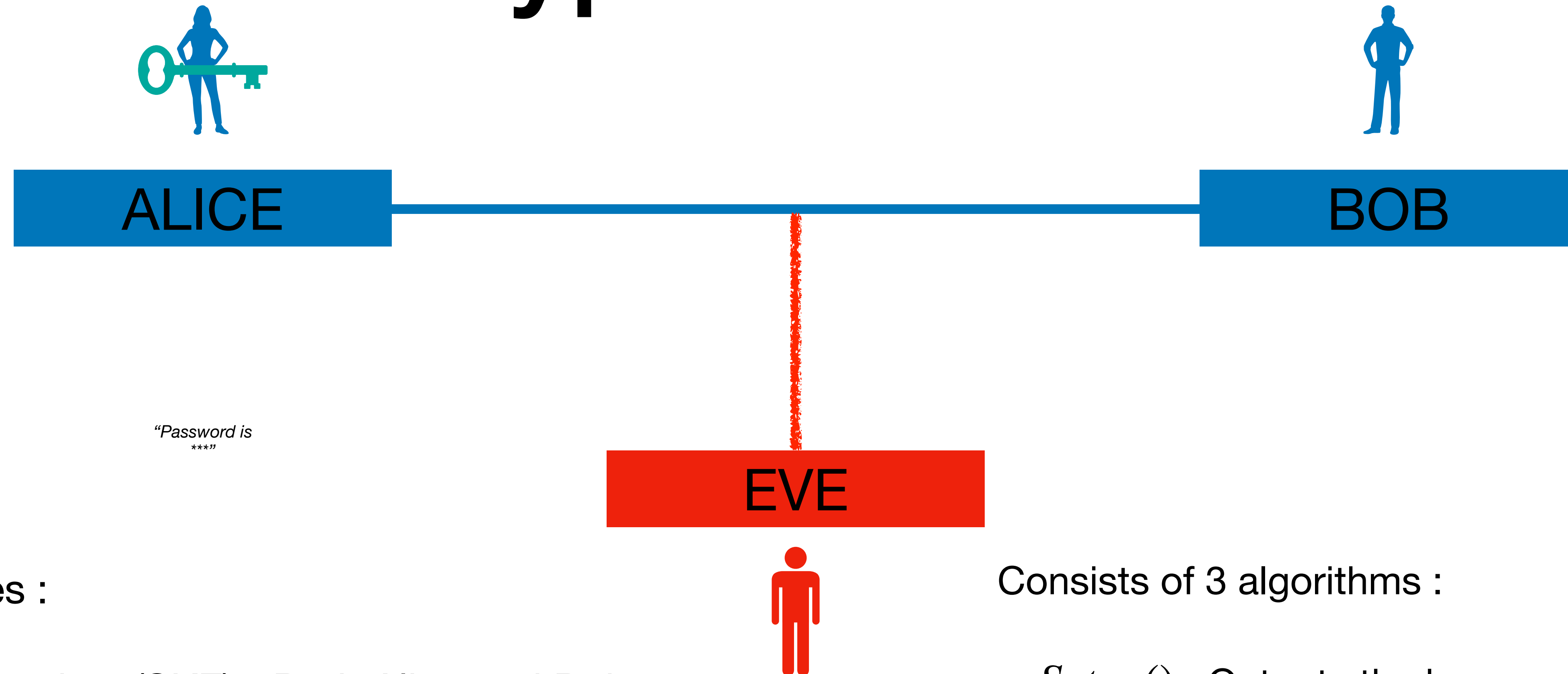
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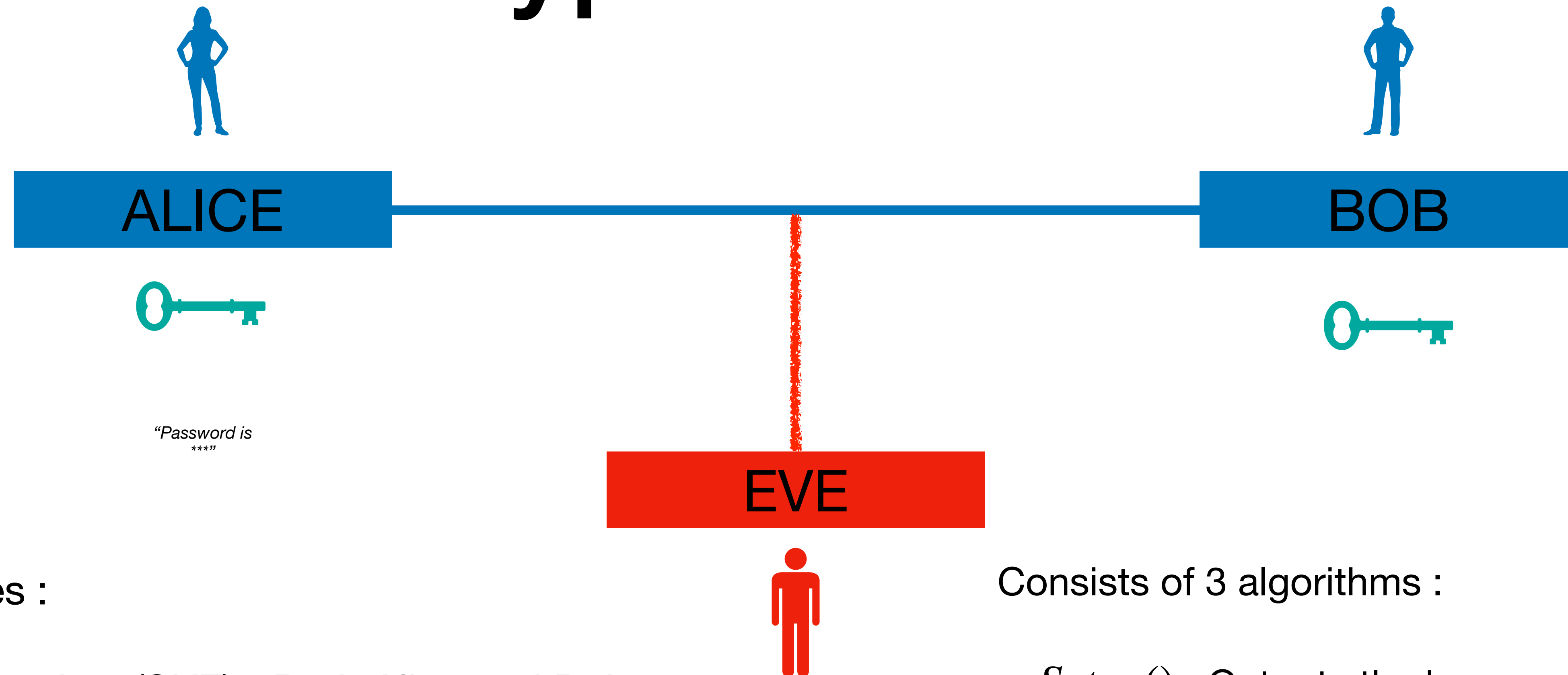
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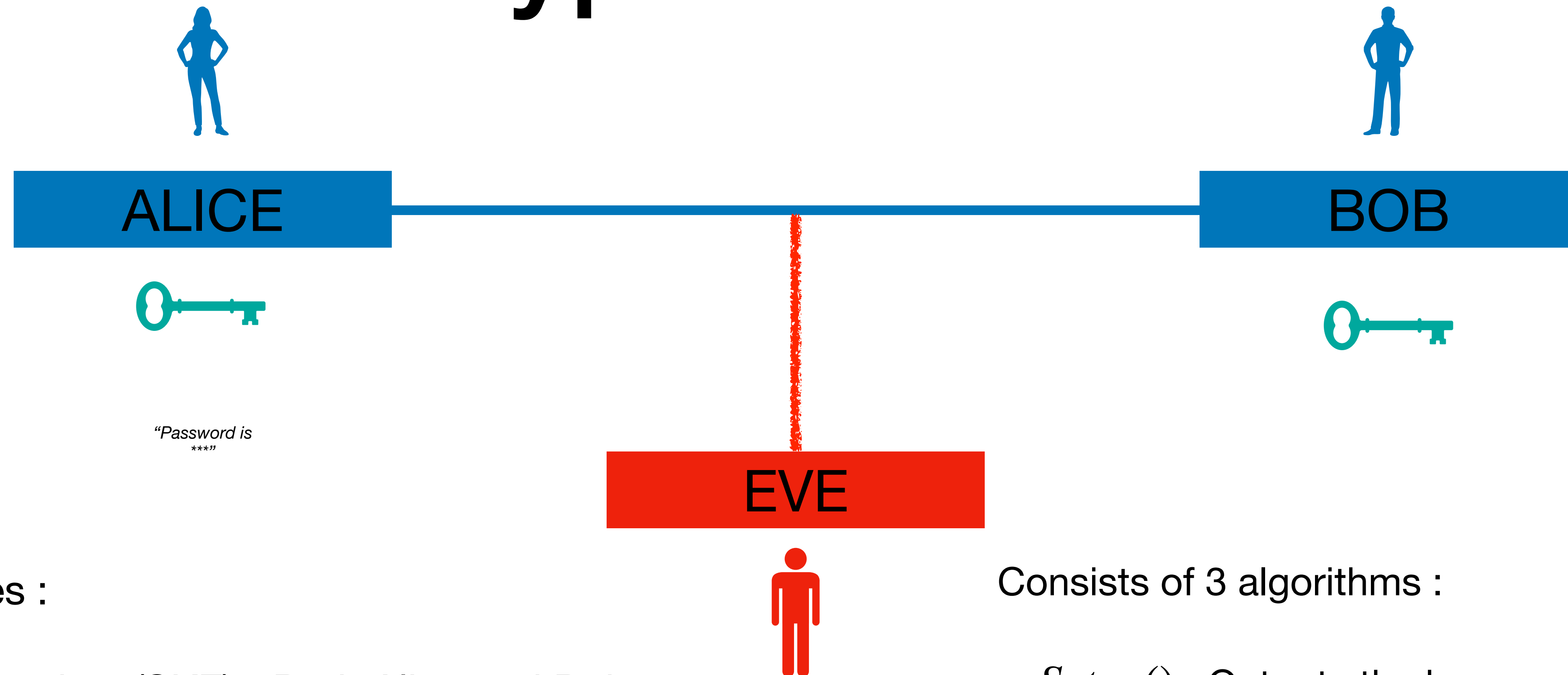
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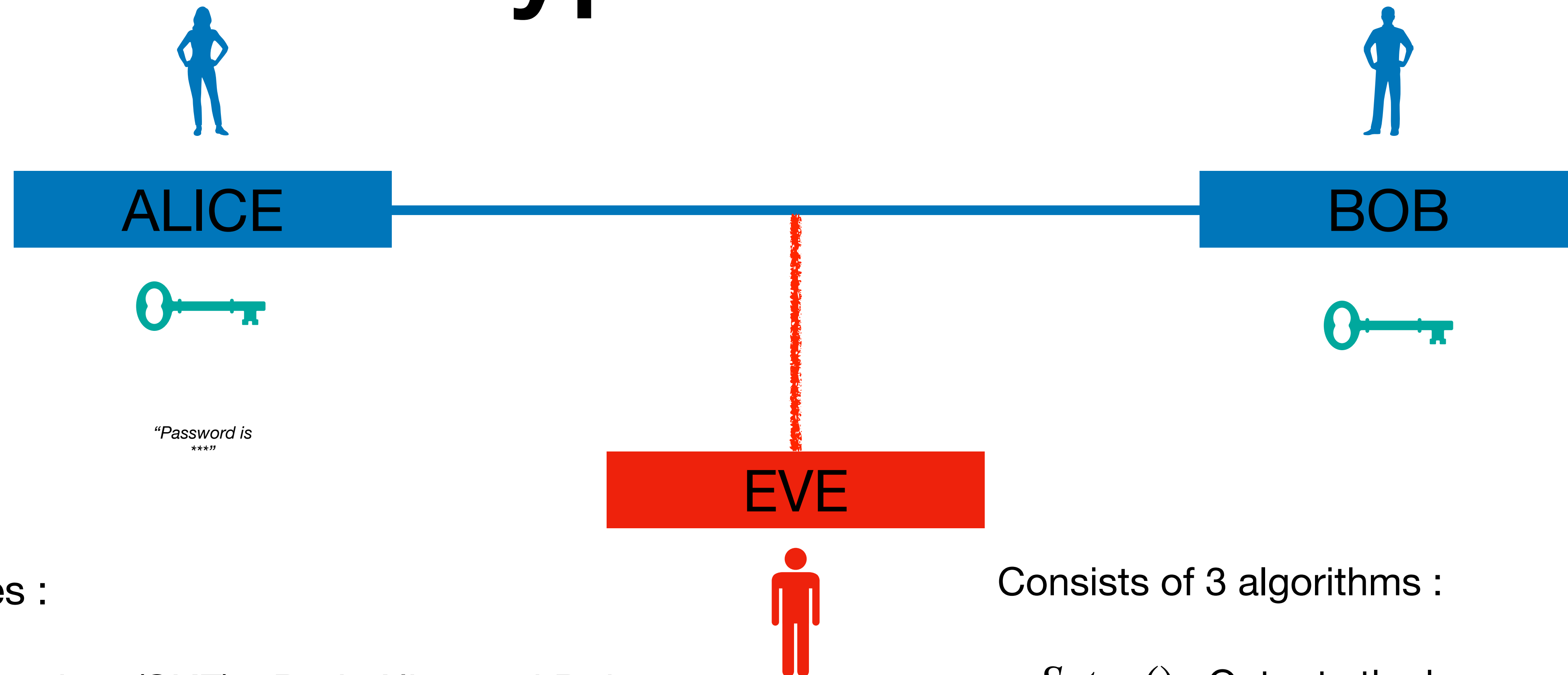
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Consists of 3 algorithms :

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- $Enc(pk/sk, m)$: Outputs ciphertext

Encryption Scheme



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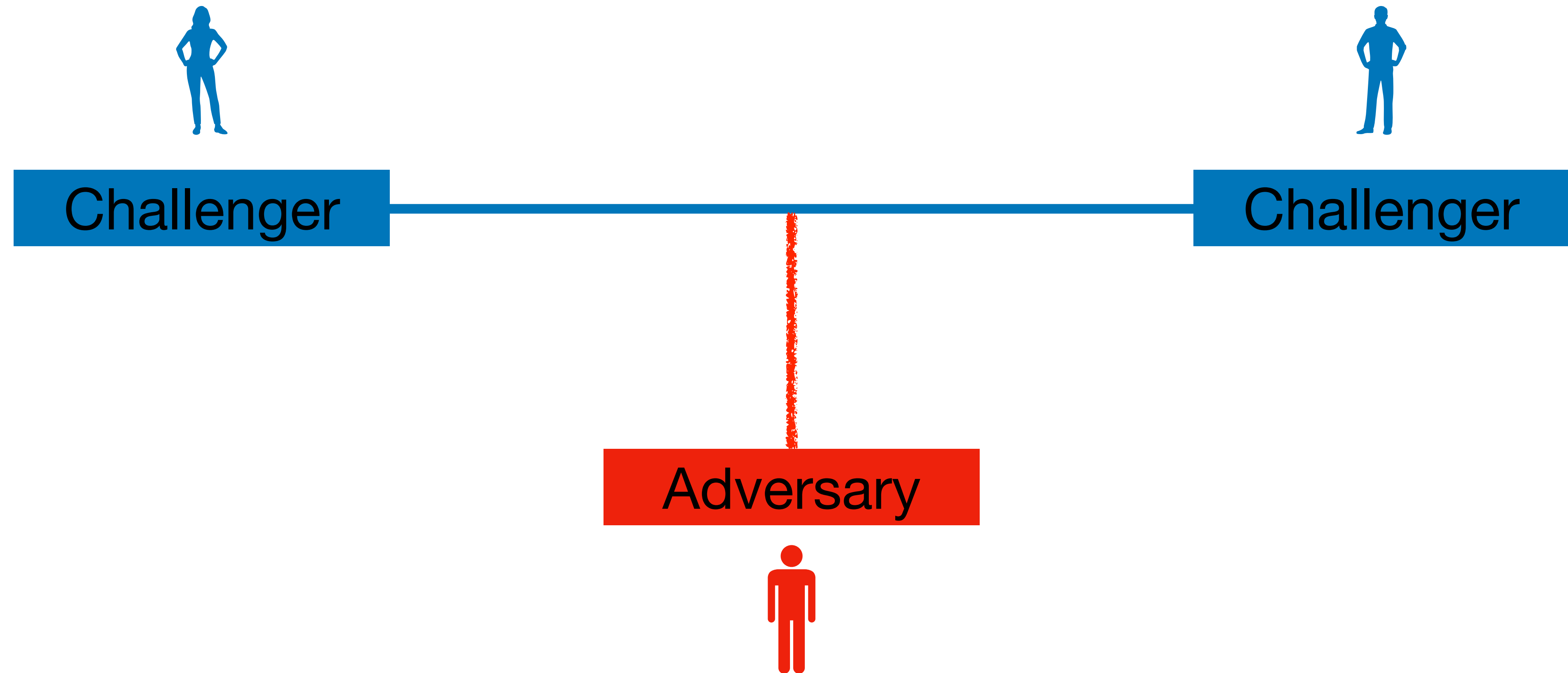
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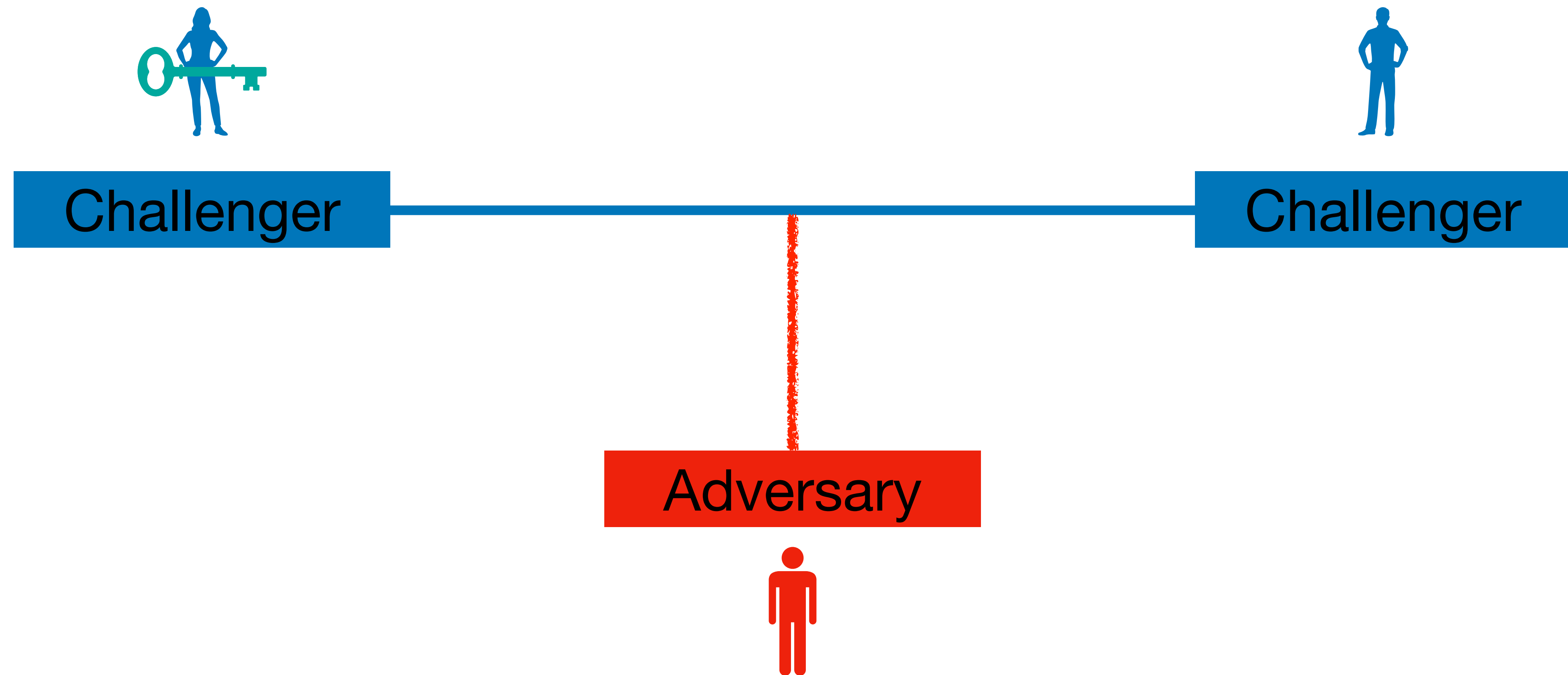
- $Setup()$: Outputs the keys
- $Enc(pk/sk, m)$: Outputs ciphertext
- $Dec(sk, c)$: Outputs message or error

Security Definitions

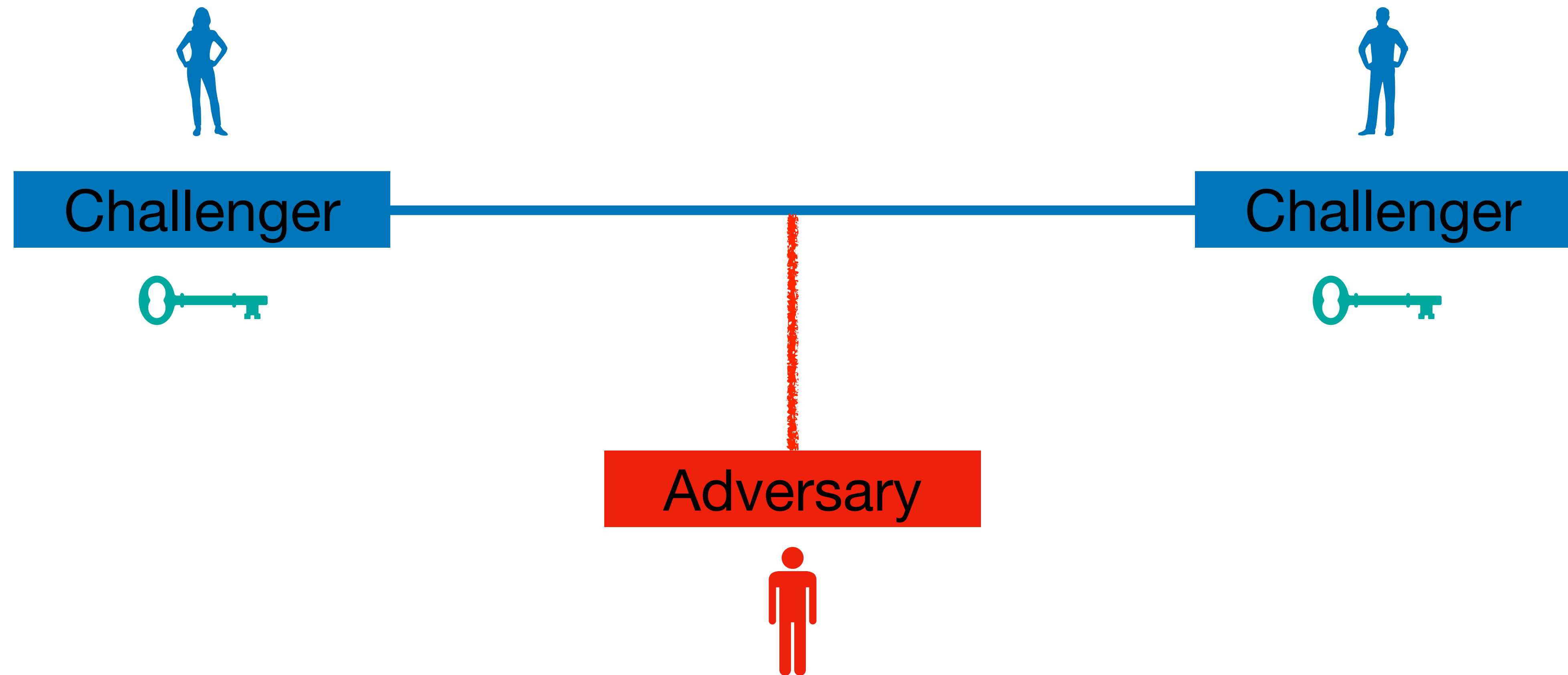
Standard Security [Goldwaser,Micali84]



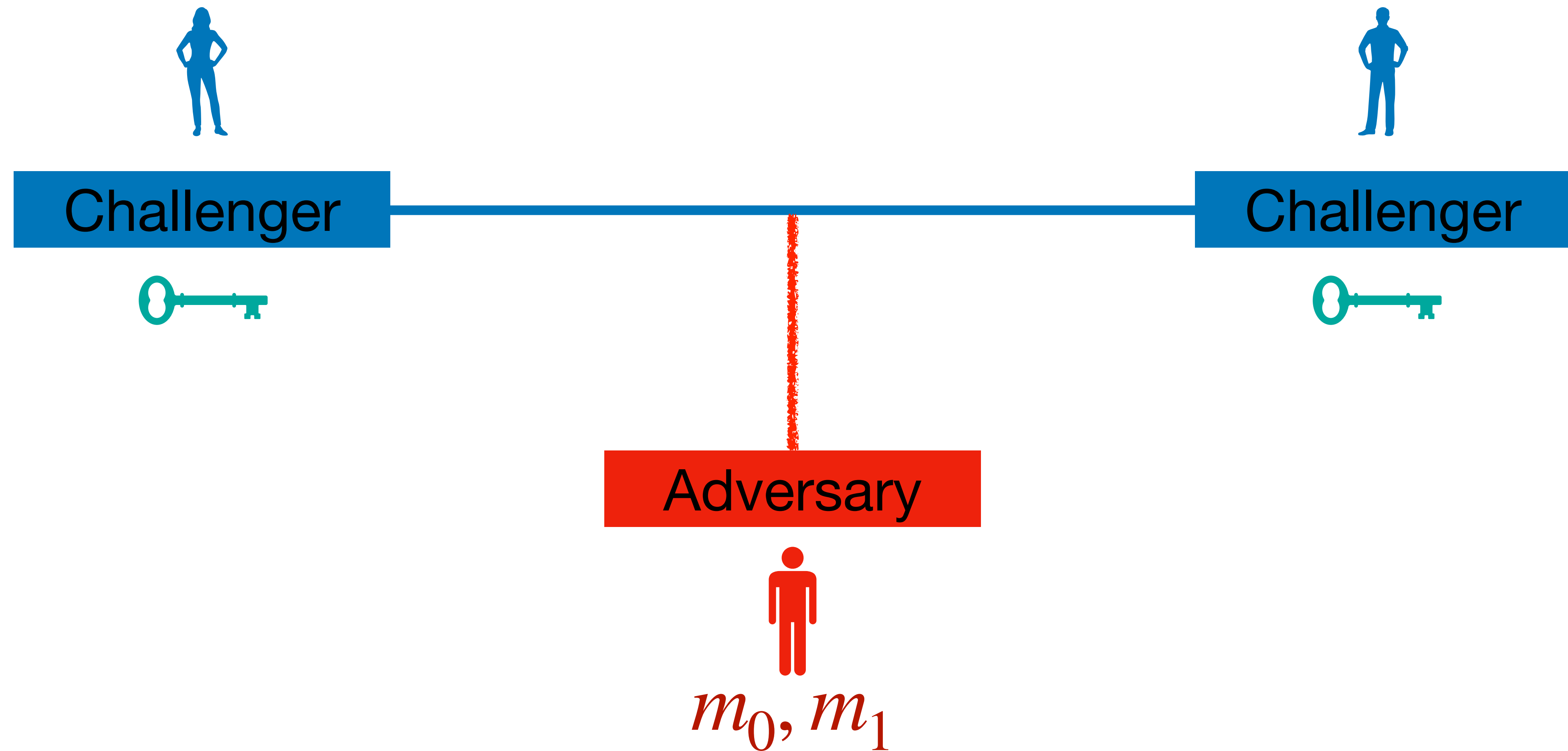
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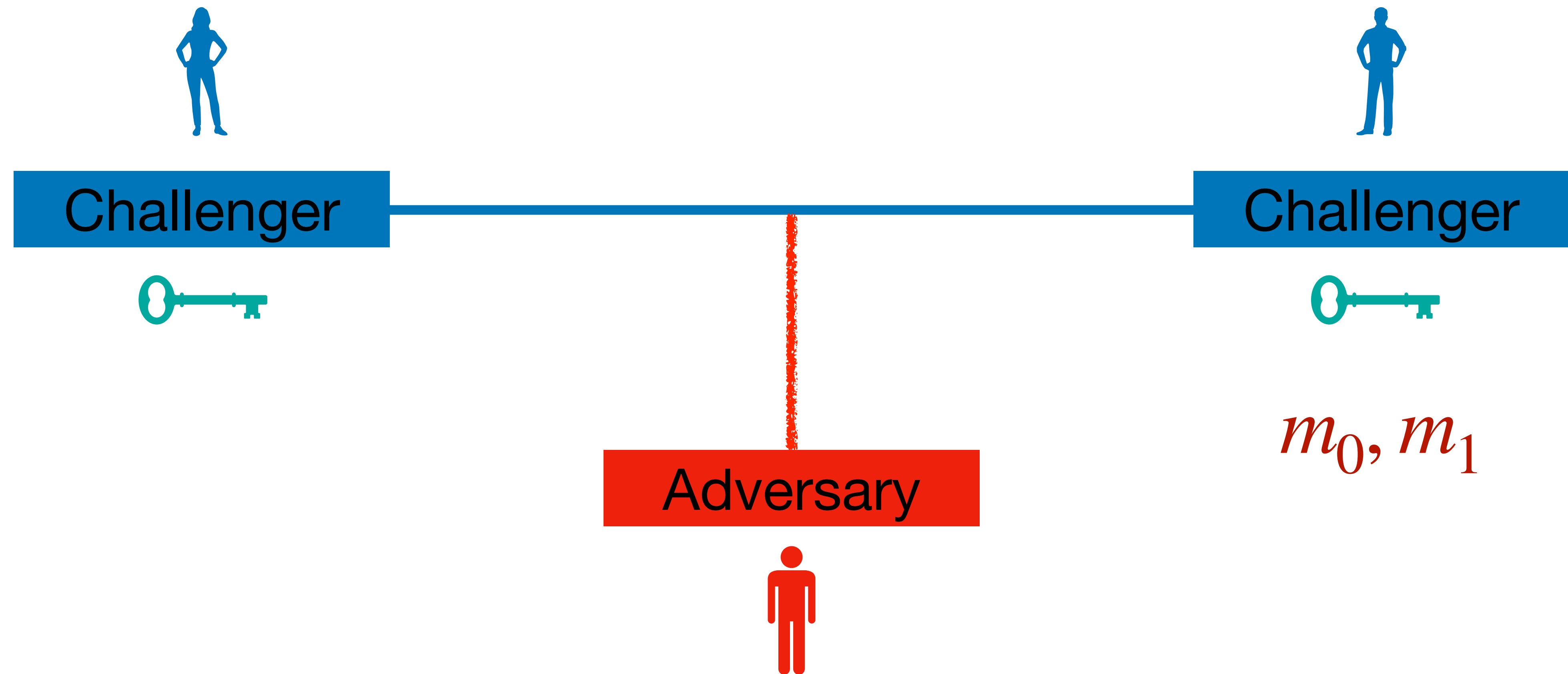
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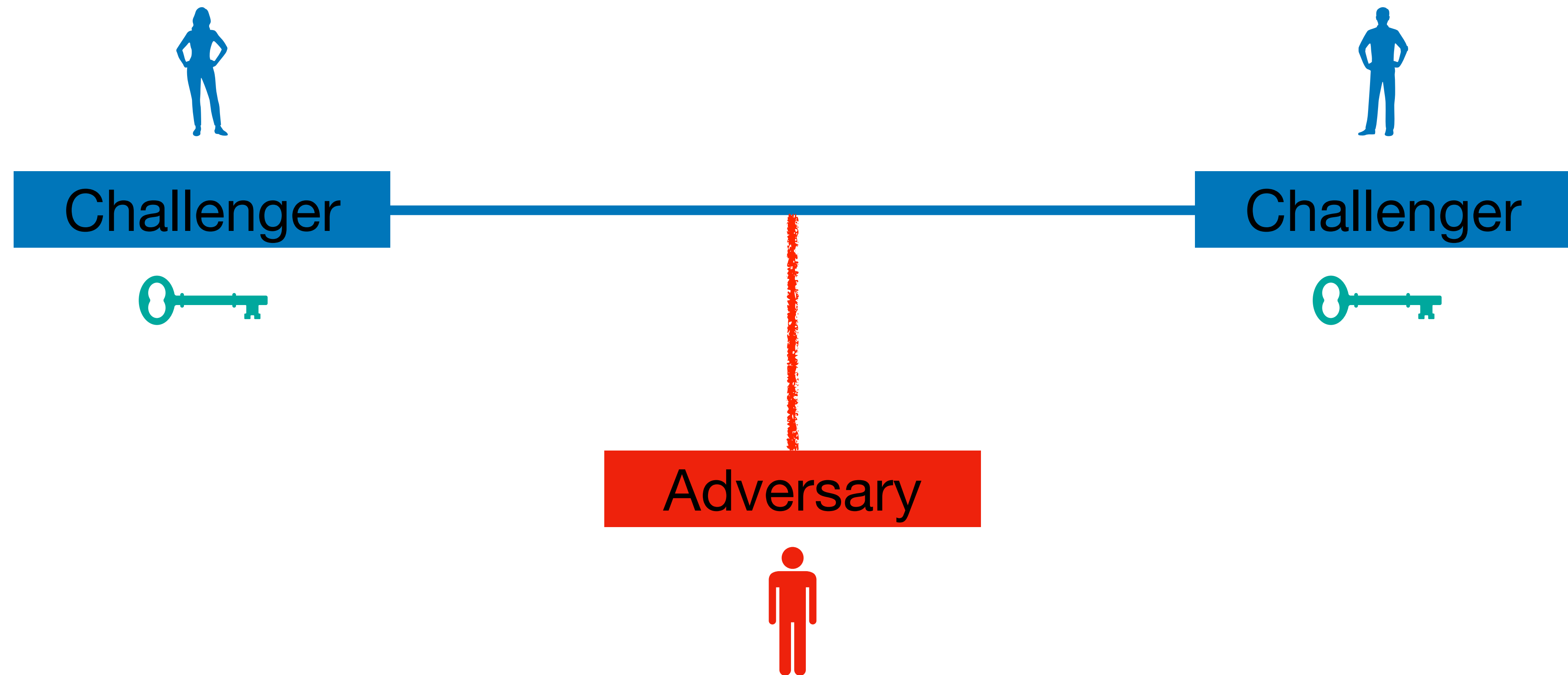
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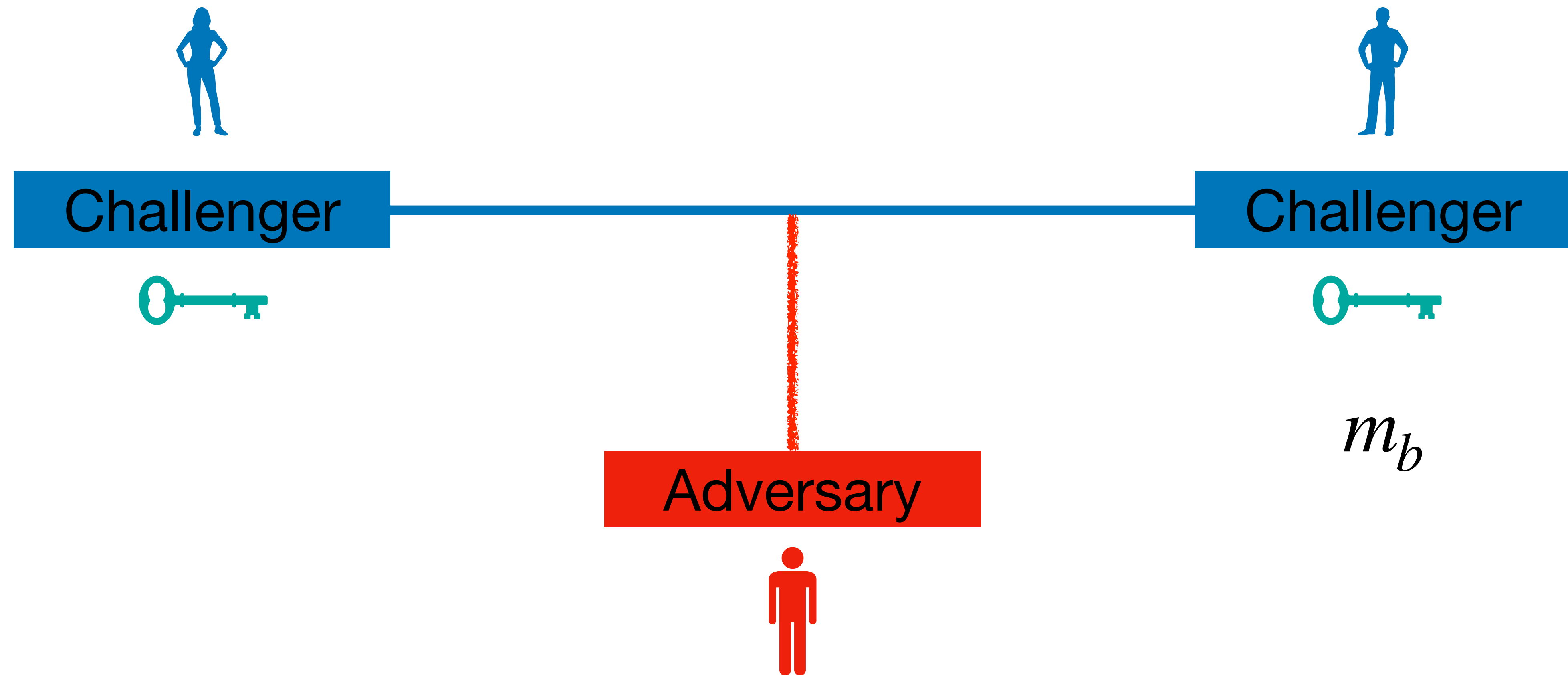
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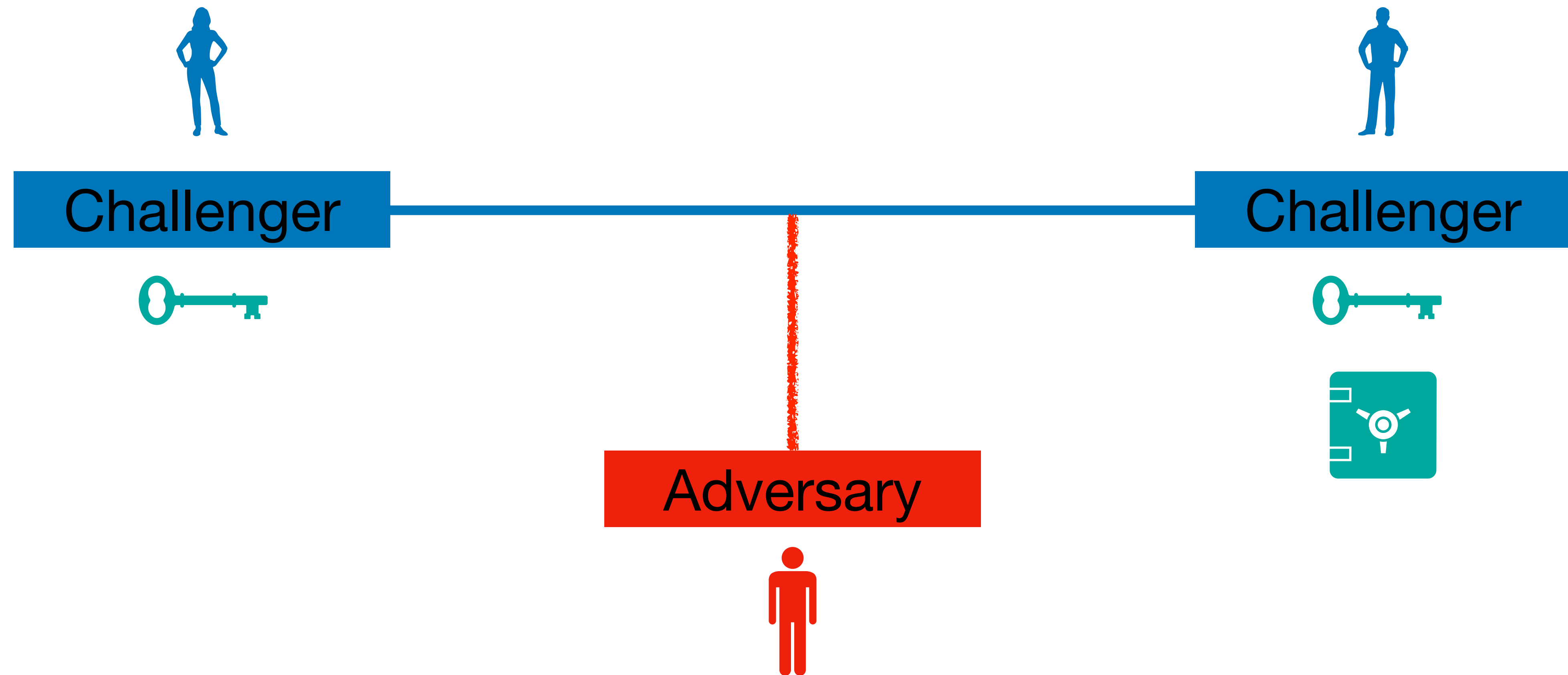
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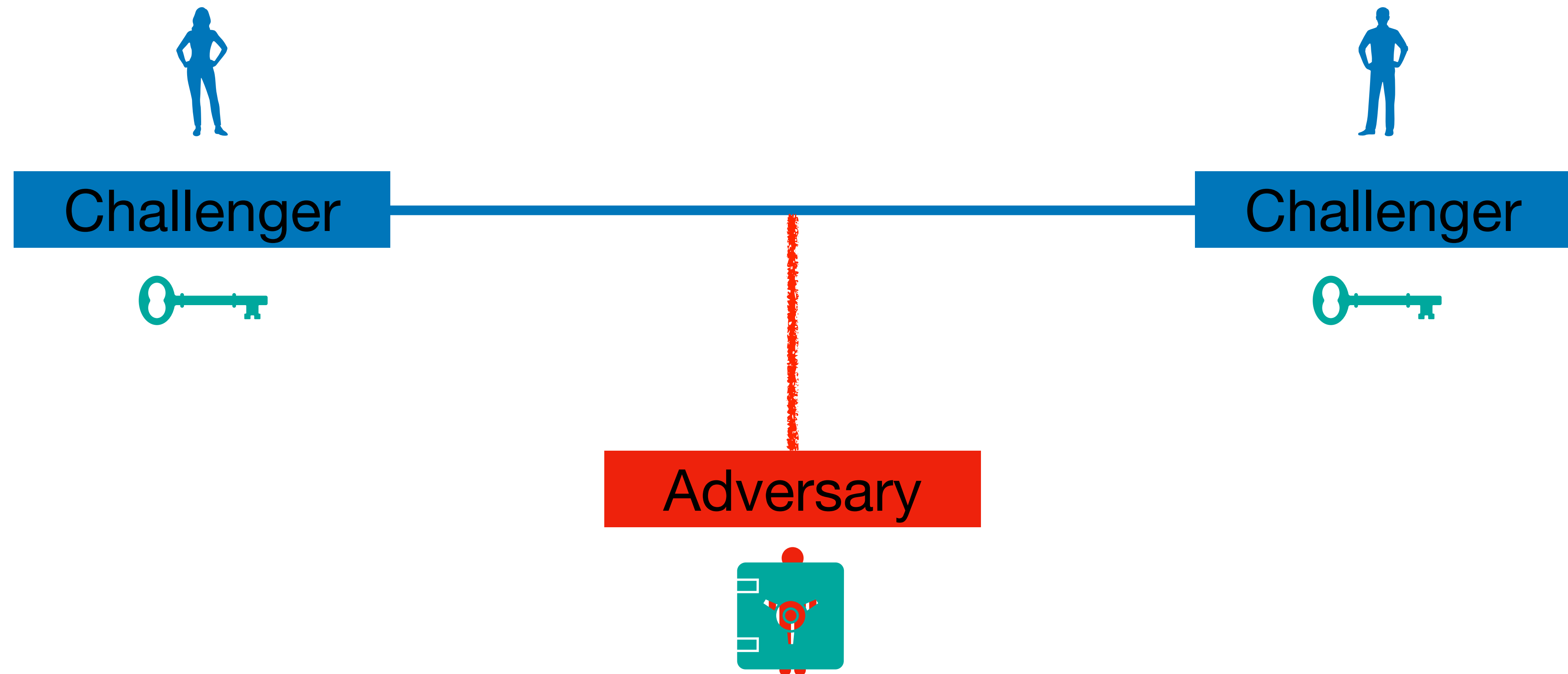
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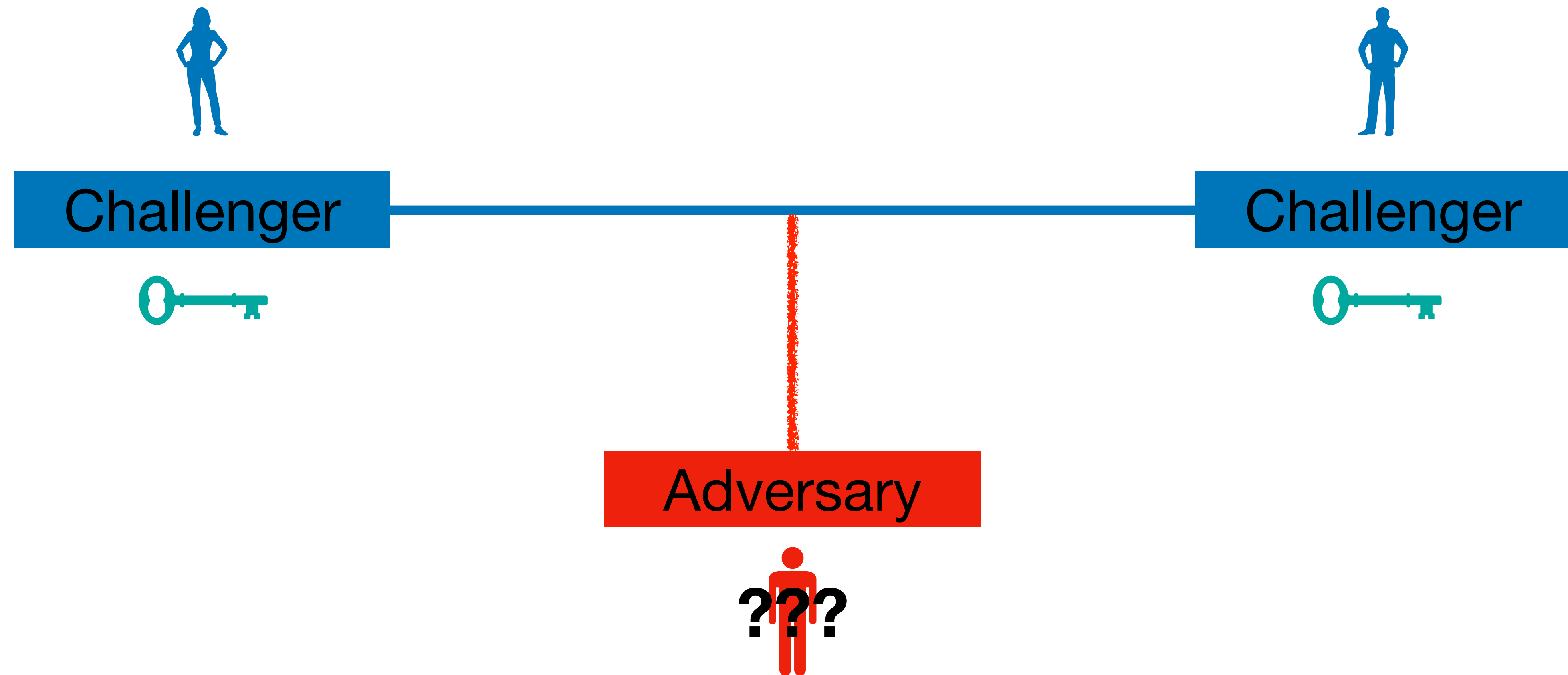
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One-Time Pad

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- $Setup(1^{|m|}) \rightarrow$ Randomly generate $sk \in \{0,1\}^{|m|}$.

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0	0	1	1
$\oplus 0$	$\oplus 1$	$\oplus 0$	$\oplus 1$
<hr/>	<hr/>	<hr/>	<hr/>
0	1	1	0

One-Time Pad

- $Setup(1^{|m|}) \rightarrow$ Randomly generate $sk \in \{0,1\}^{|m|}$.
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- $Dec(sk, ct) \rightarrow$ Return $sk \oplus ct$.

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- $Enc(sk, 11100) \rightarrow$ Returns $\underbrace{11100}_{sk} \oplus \underbrace{11001}_m = \underbrace{00101}_{ct}$.

0	0	1	1
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<hr/>	<hr/>	<hr/>	<hr/>
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One-Time Pad

- $Setup(1^{|m|}) \rightarrow$ Randomly generate $sk \in \{0,1\}^{|m|}$.

- $Enc(sk, m) \rightarrow$ Returns $sk \oplus m$.

0	0	1	1
$\oplus 0$	$\oplus 1$	$\oplus 0$	$\oplus 1$
<hr/>	<hr/>	<hr/>	<hr/>
0	1	1	0

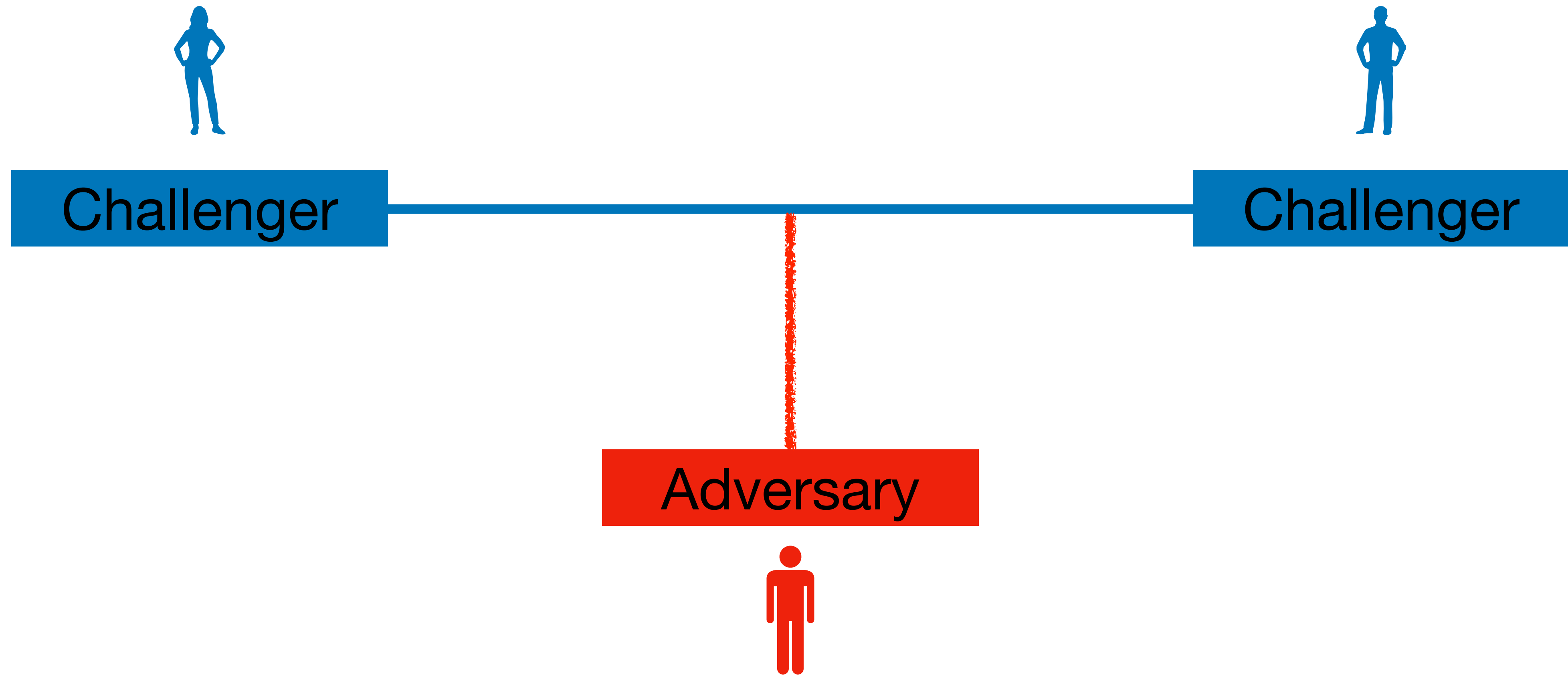
- $Dec(sk, ct) \rightarrow$ Return $sk \oplus ct$.

- $Setup(1^5) \rightarrow$ Generated $\underbrace{11001}_{sk}$.

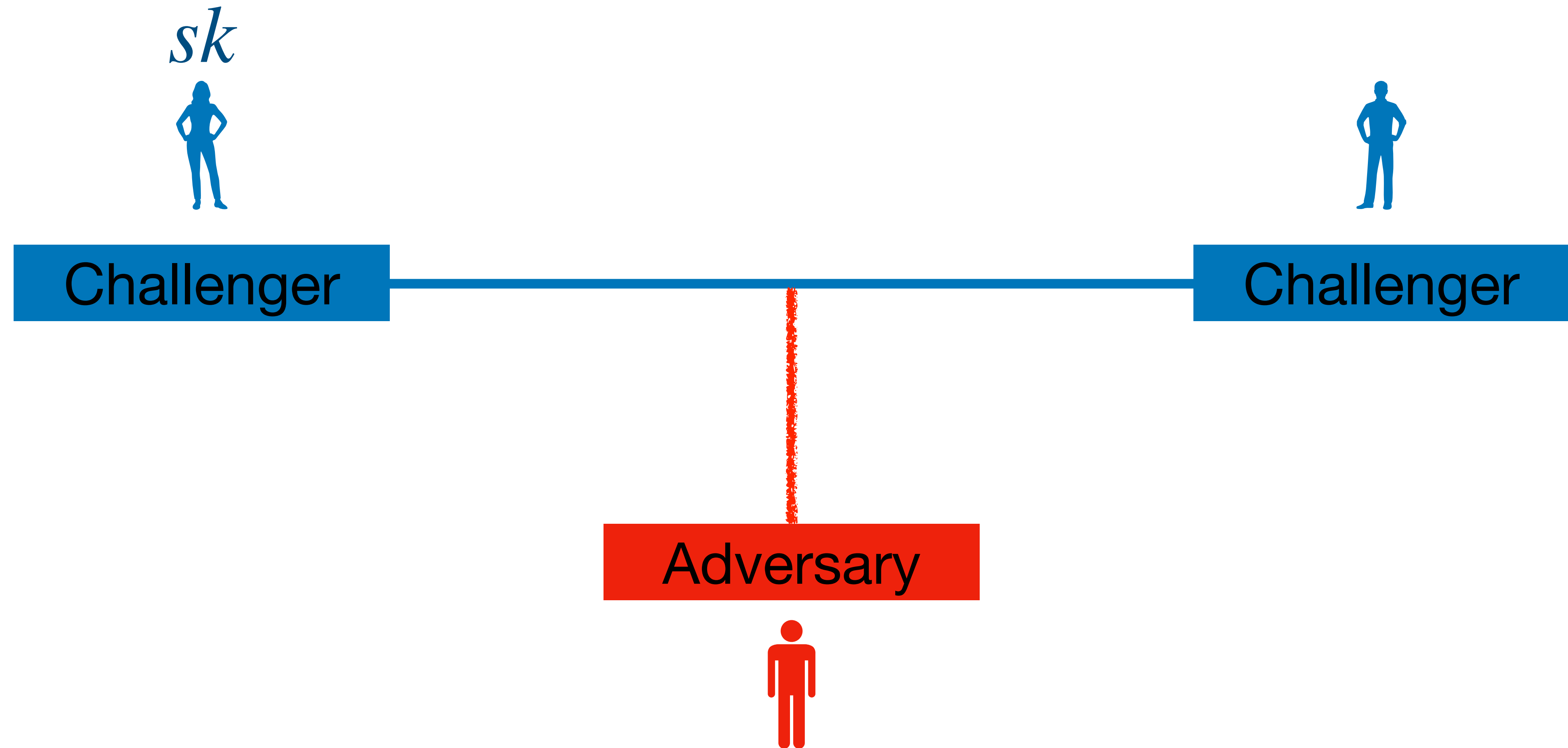
- $Enc(sk, 11100) \rightarrow$ Returns $\underbrace{11100}_{sk} \oplus \underbrace{11001}_m = \underbrace{00101}_{ct}$.

- $Dec(sk, ct) \rightarrow$ Return $\underbrace{11001}_{sk} \oplus \underbrace{00101}_{ct} = \underbrace{11100}_m$.

One Time Pad



One Time Pad



One Time Pad

0100...011



Challenger

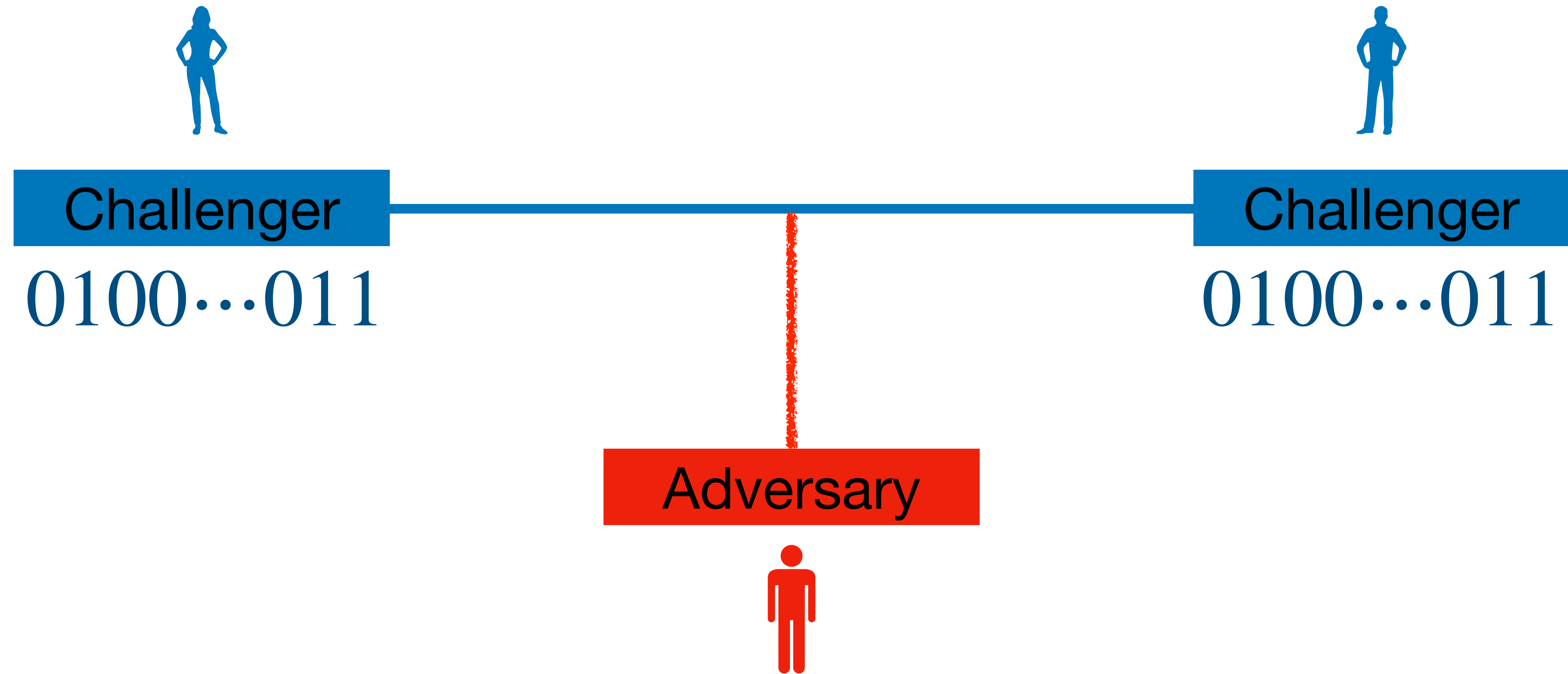


Challenger

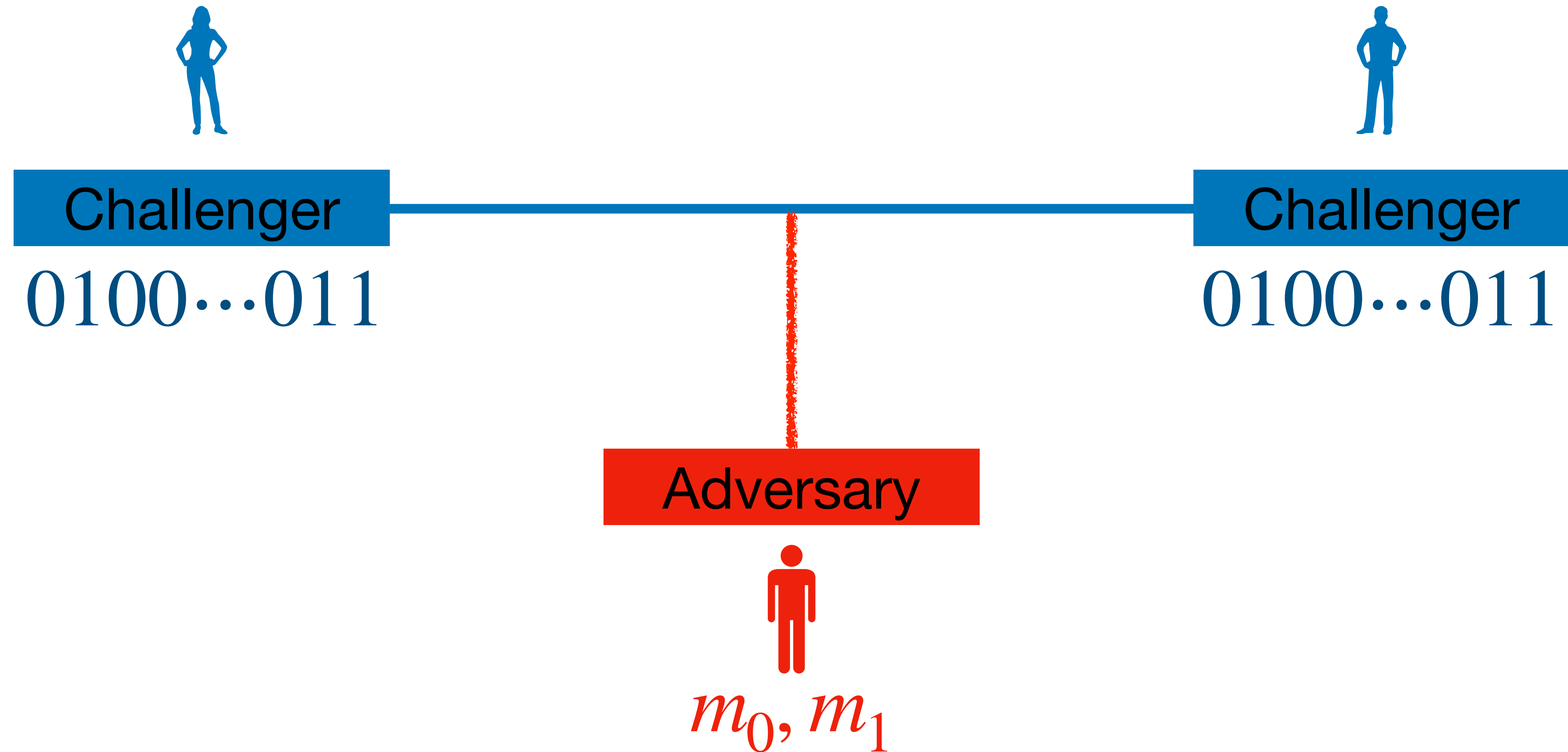
Adversary



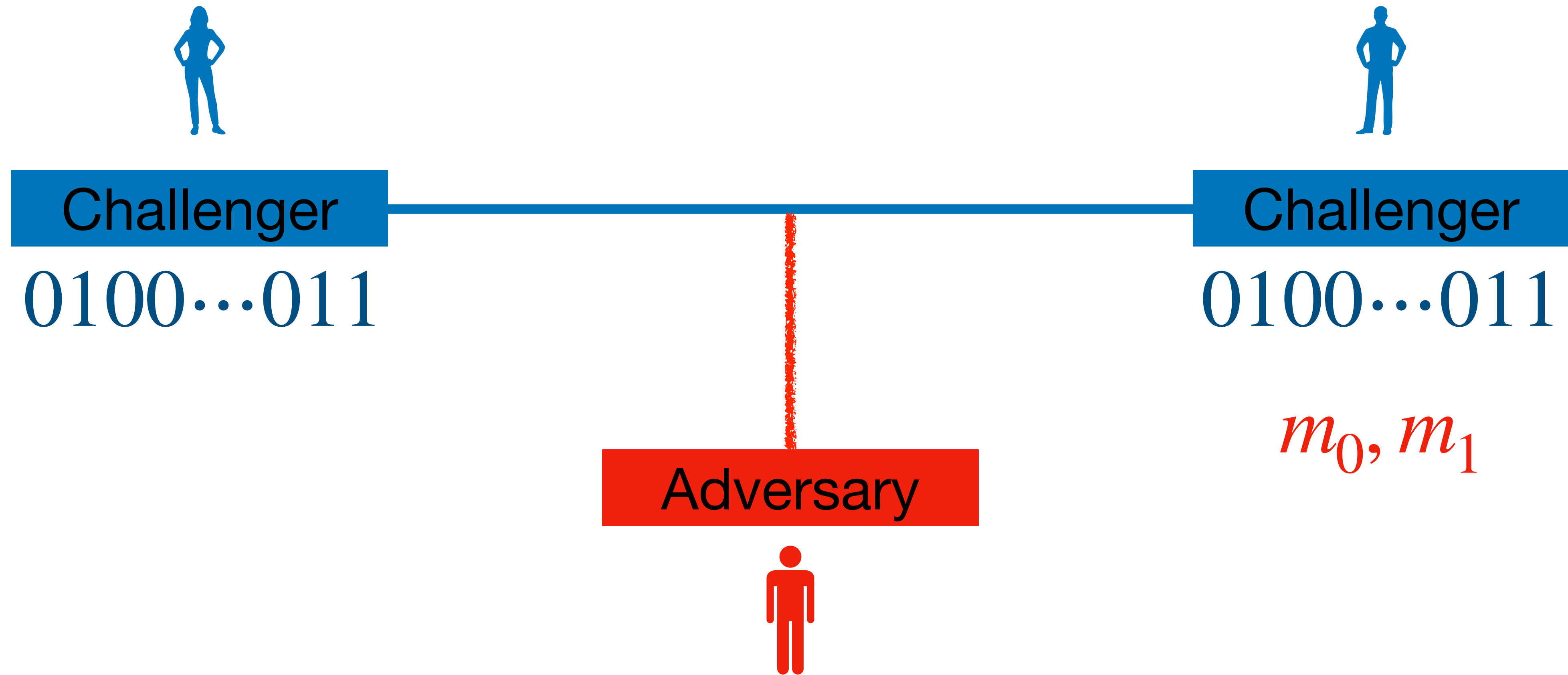
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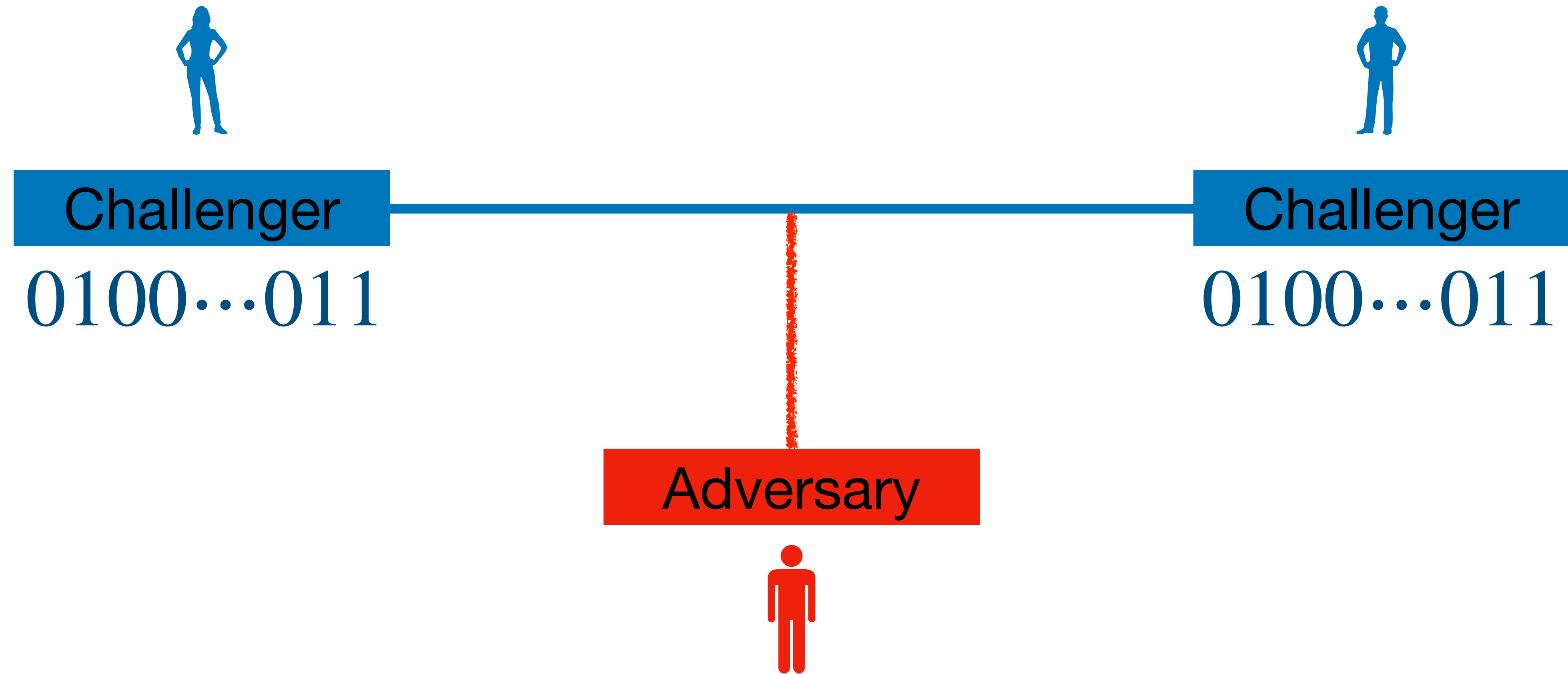
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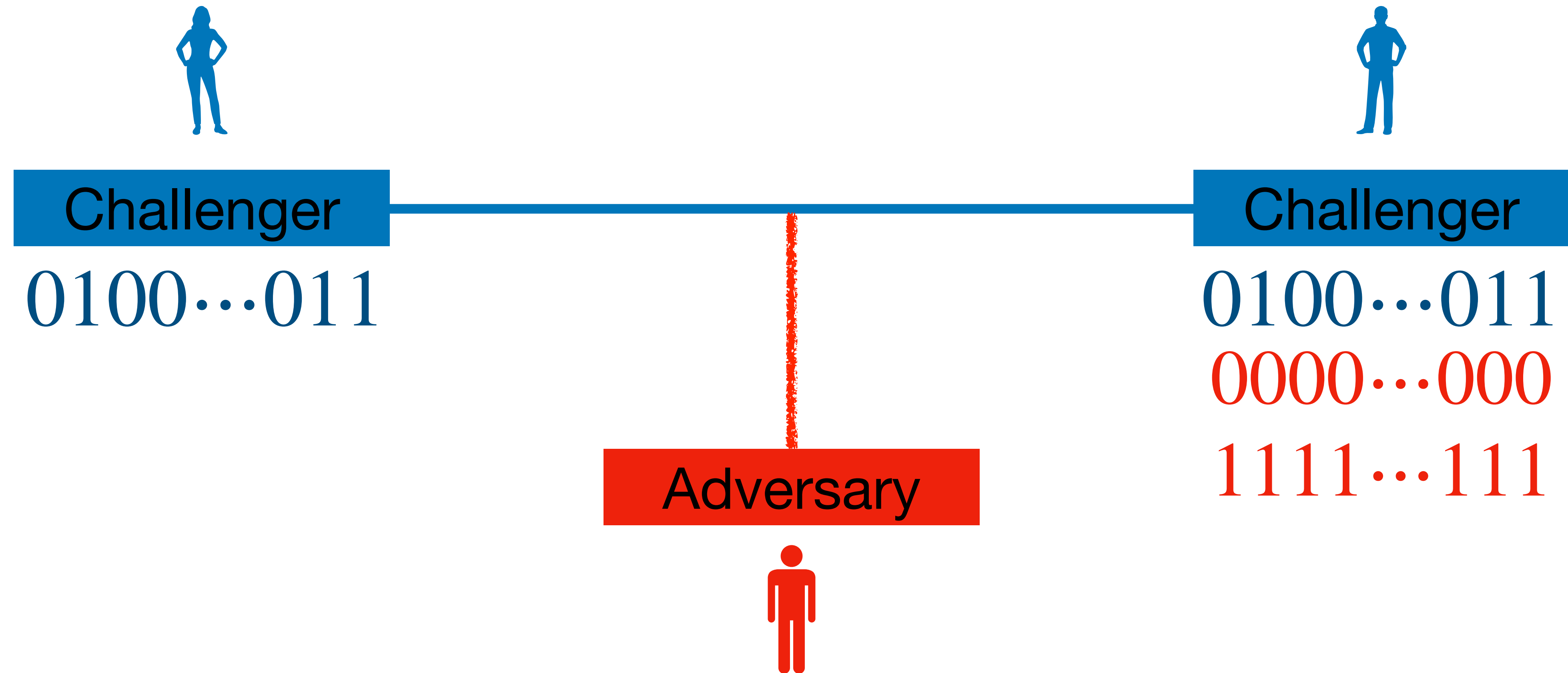
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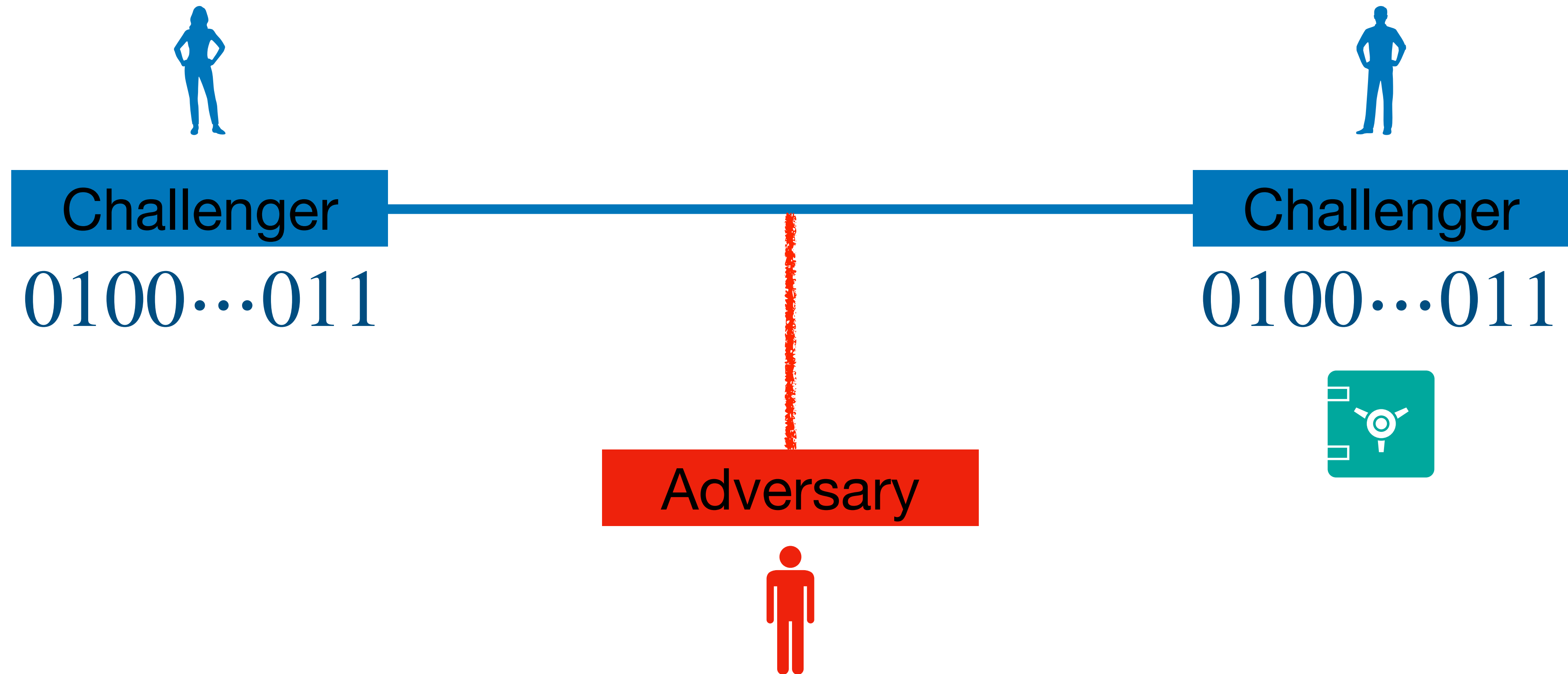
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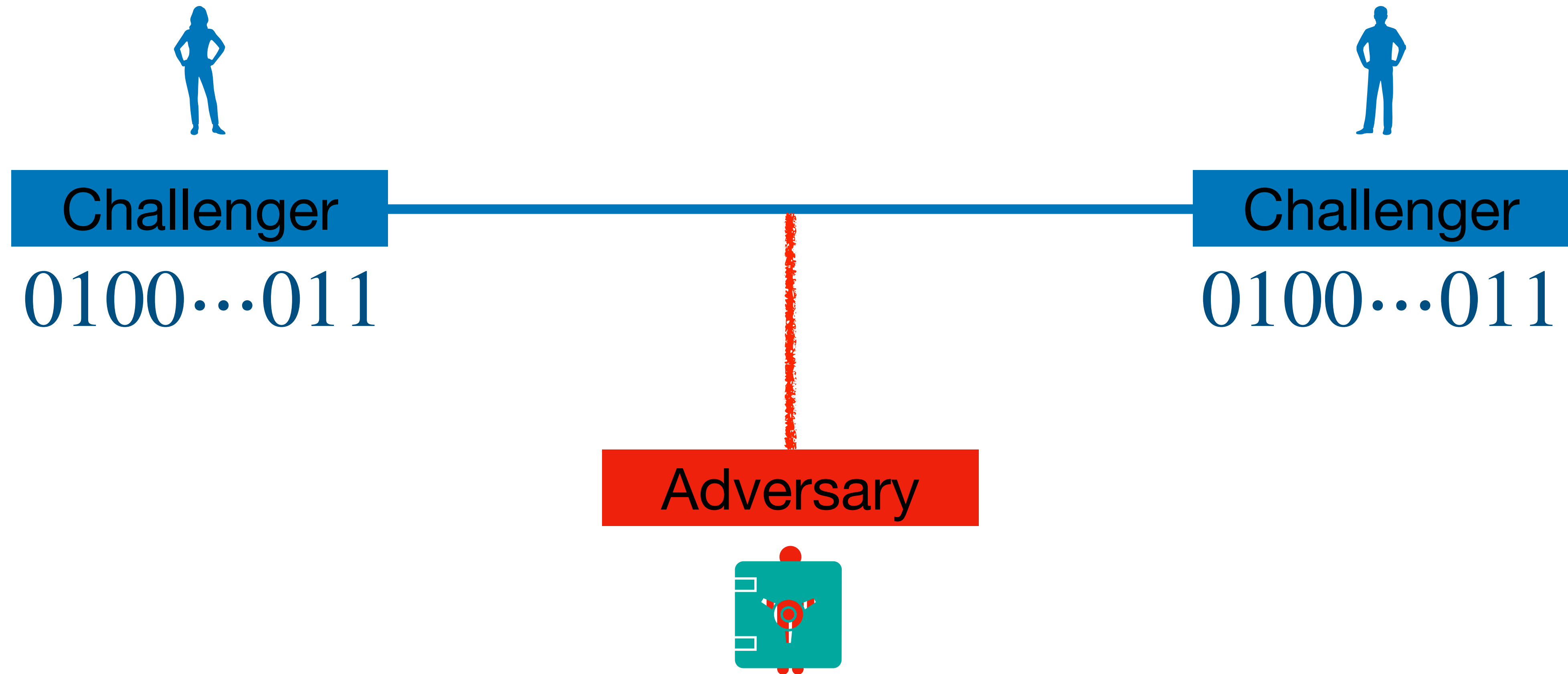
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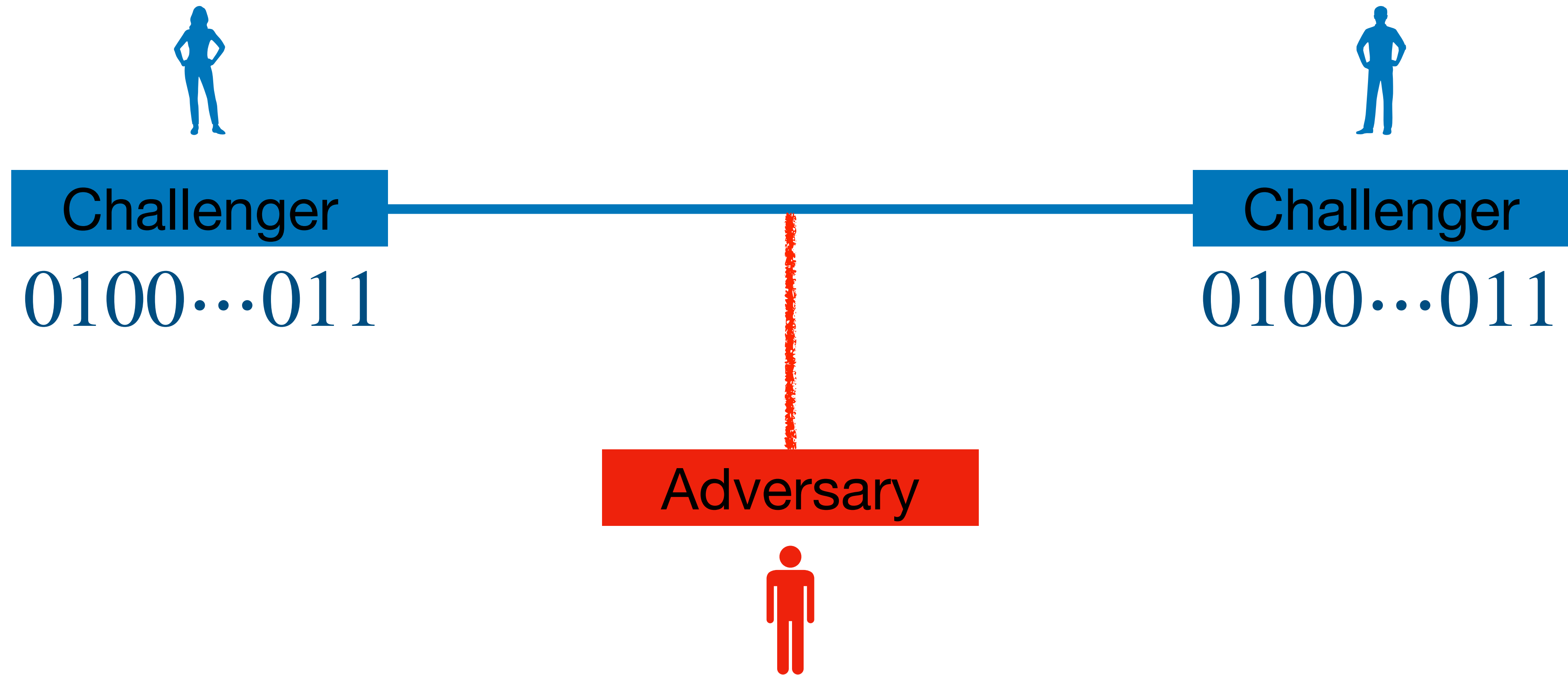
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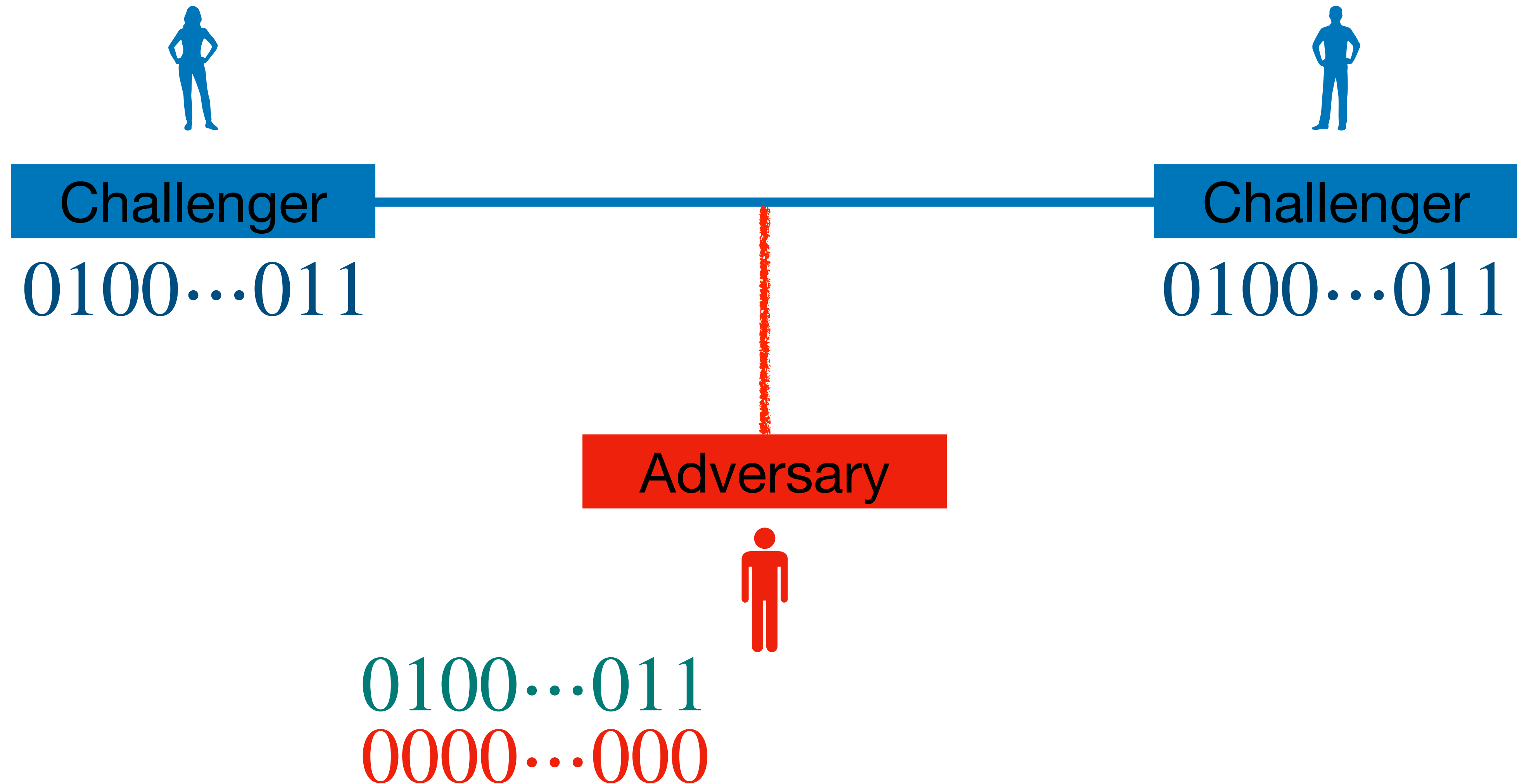
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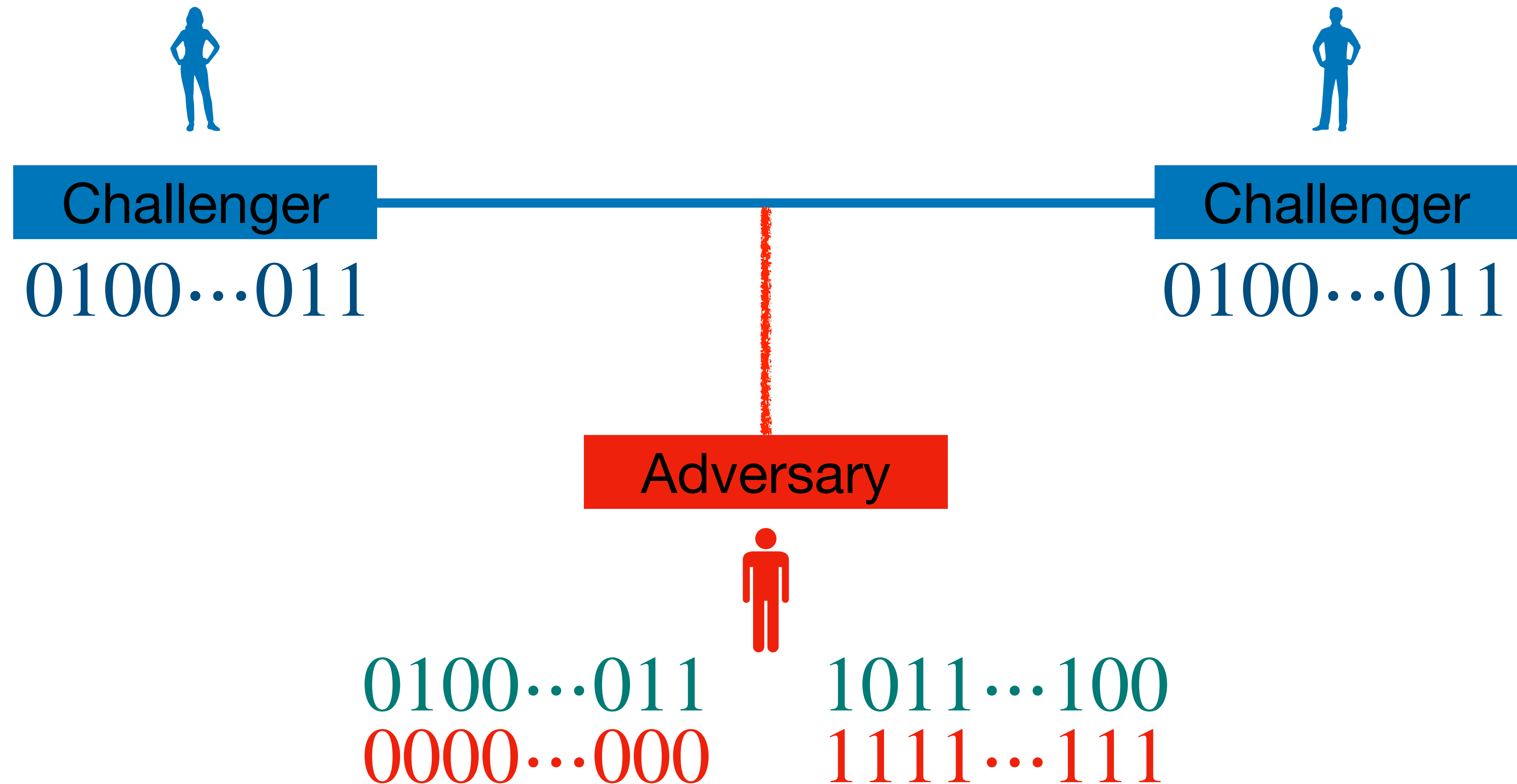
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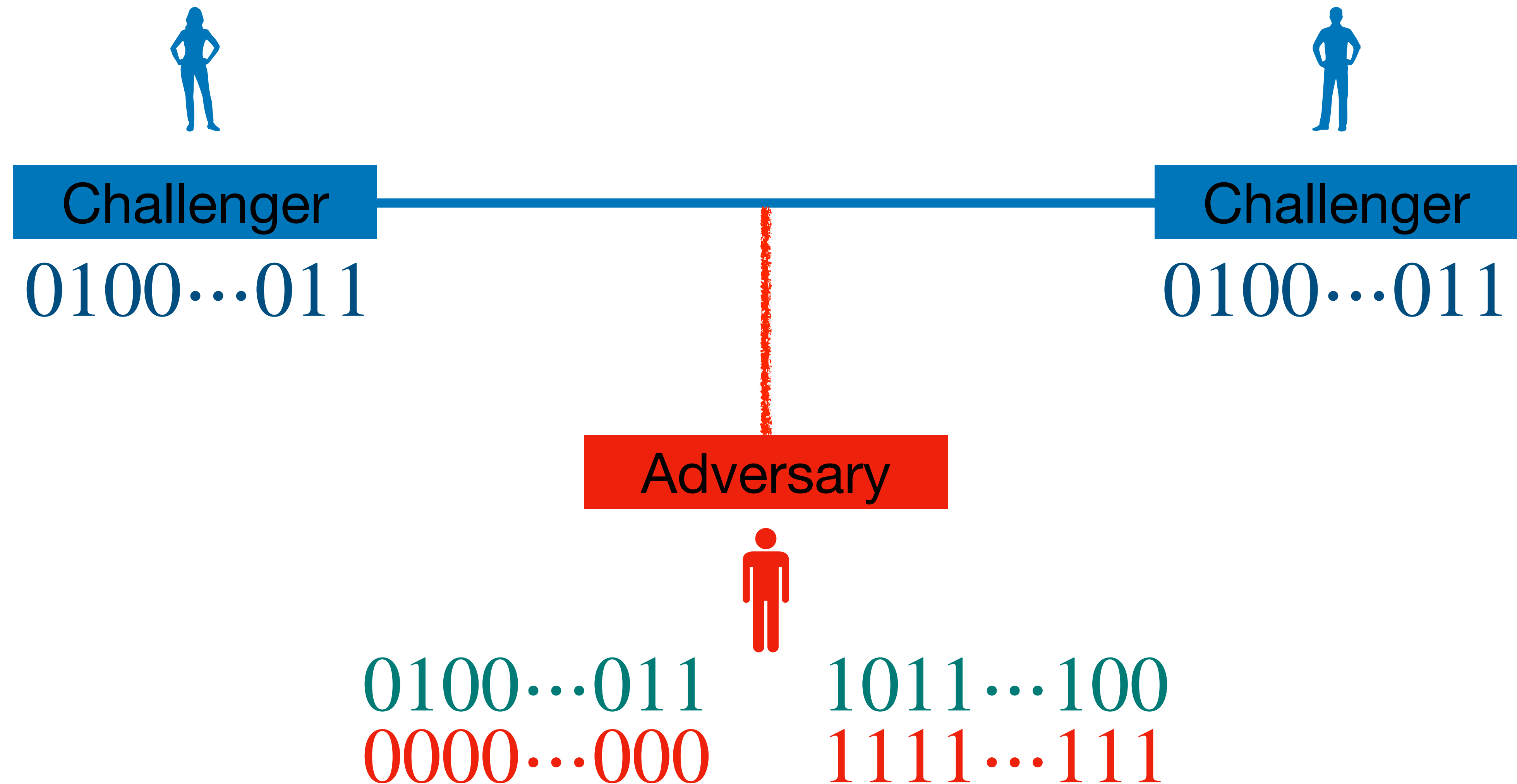
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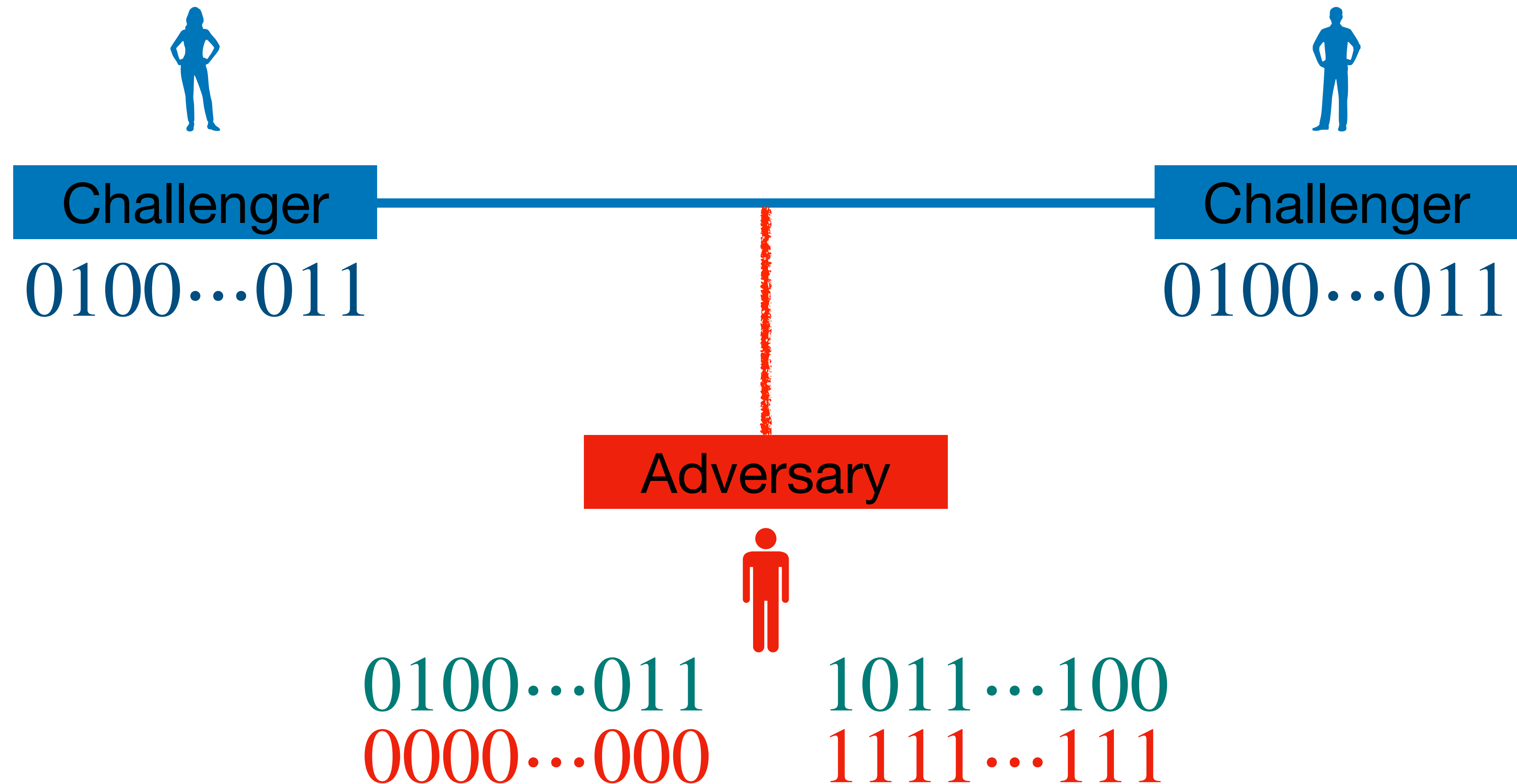
One Time Pad



One Time Pad



One Time Pad



One Time Pad



Challenger

0100...011



Challenger

0100...011

**Shannon
showed that
this is perfectly
secure!!!**

Adversary



0100...011
0000...000

1011...100
1111...111

Can Secret Key be leaked?

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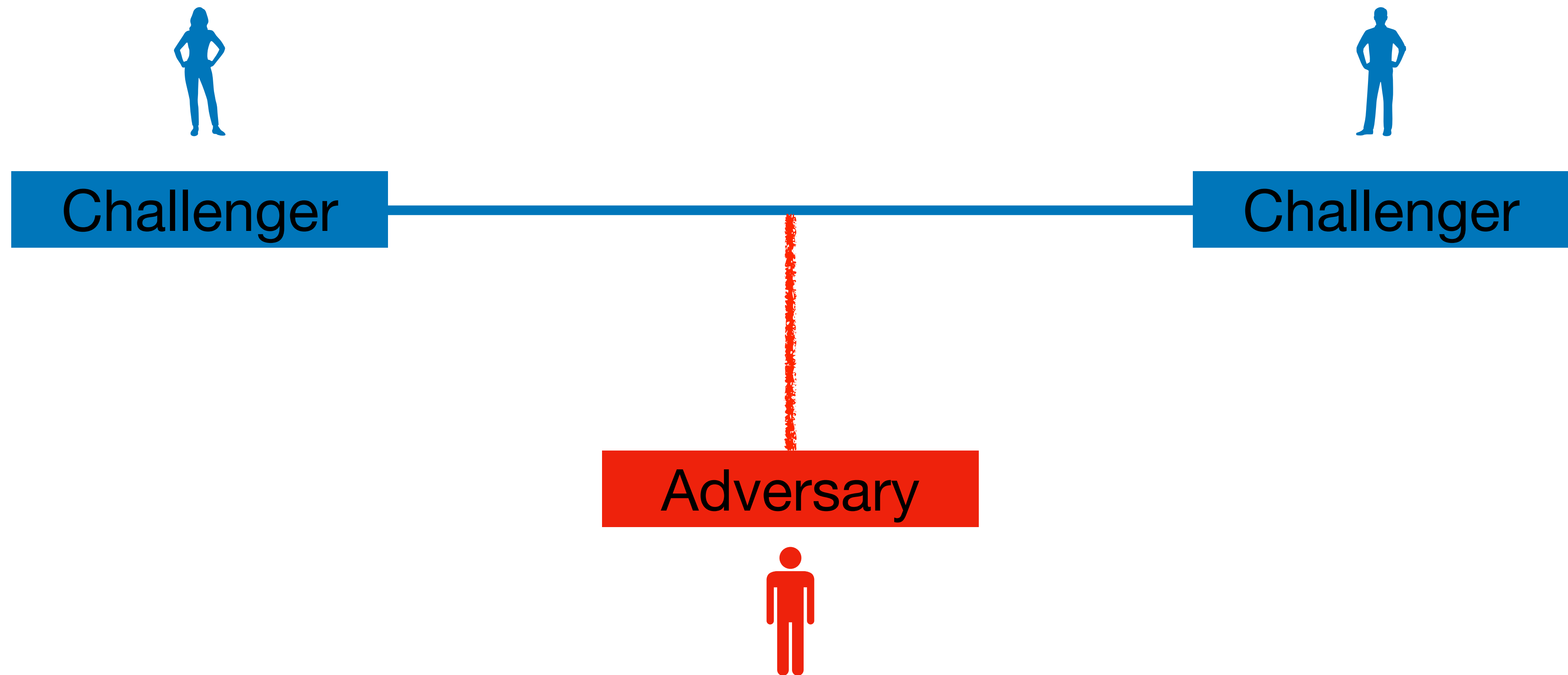
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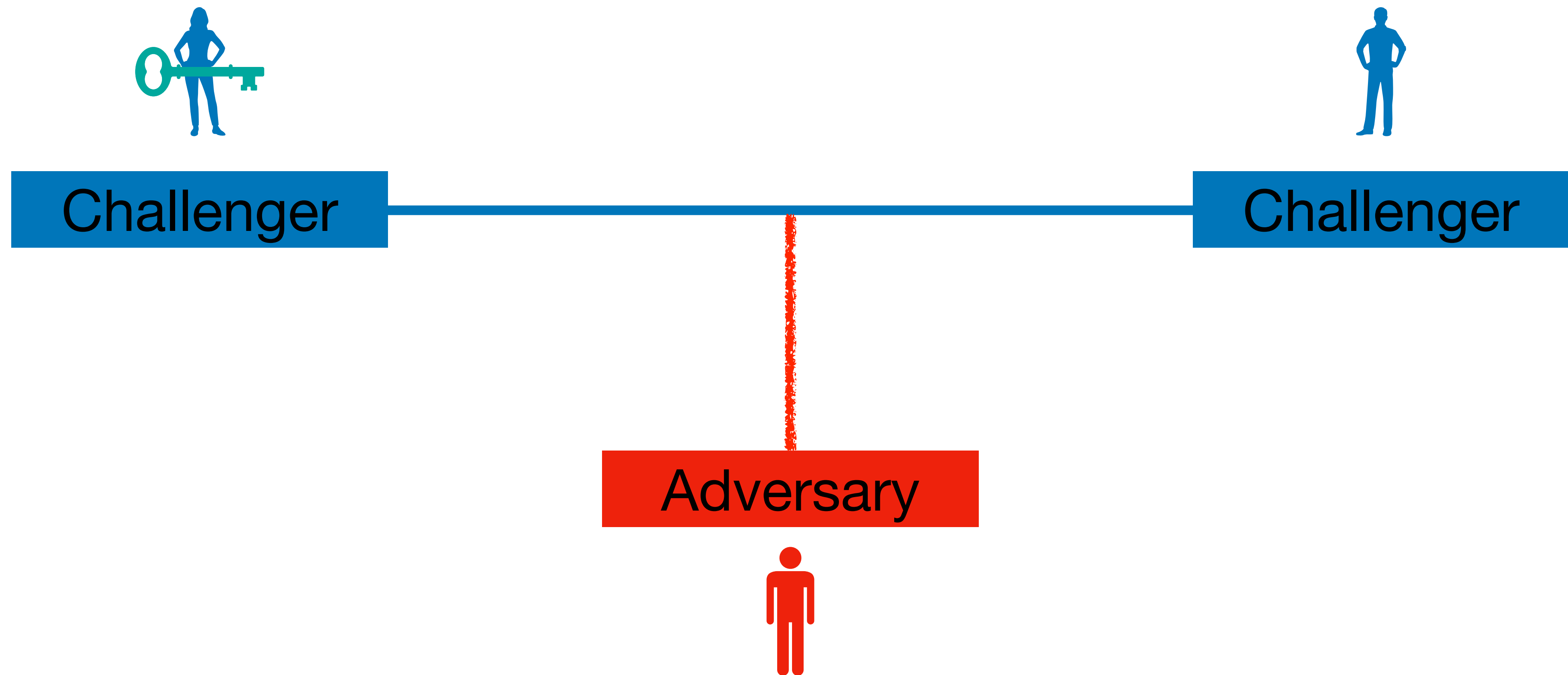
- Standard security says that adversary cannot distinguish between encryptions of two different message provided **no** information of secret key is leaked.
- In practice, secret key can be leaked using side-channel attacks.

Leakage-Resilience

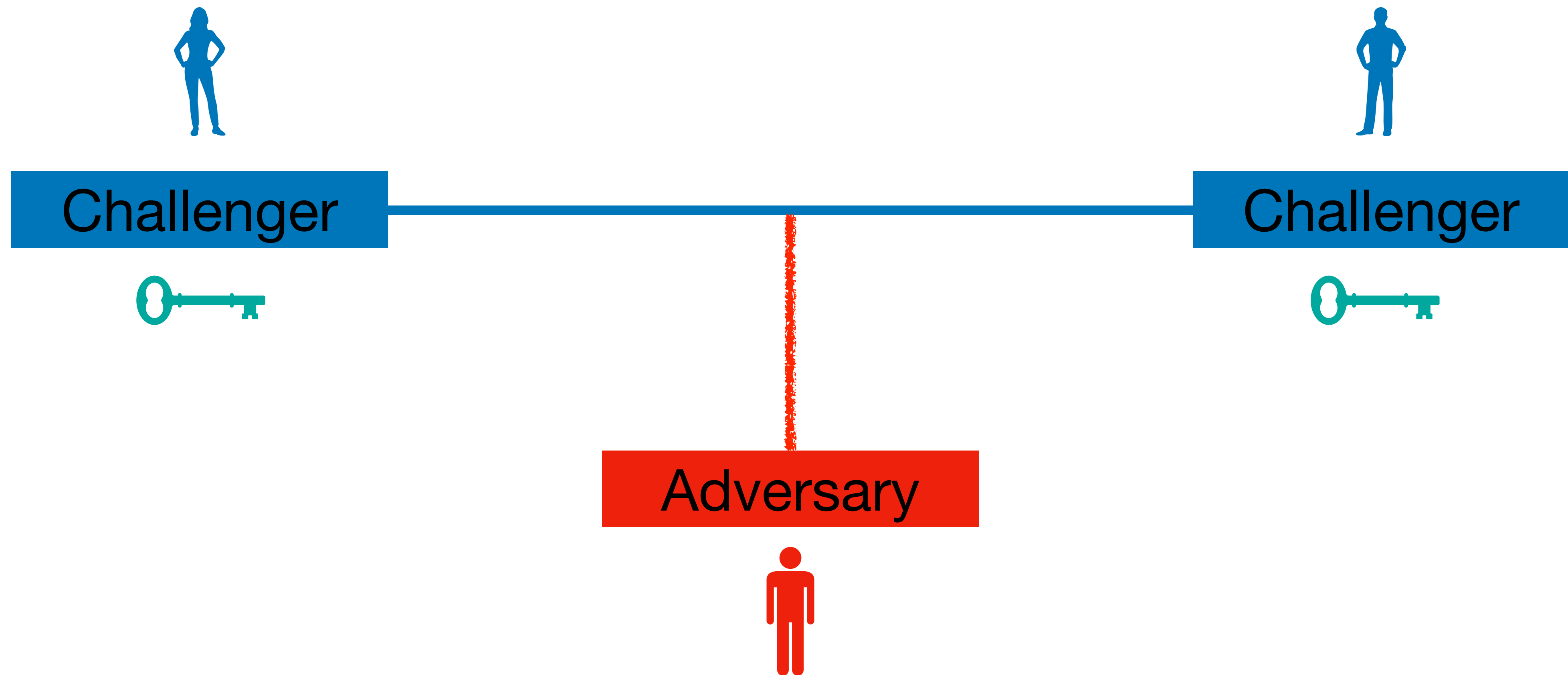
Security against Leakage



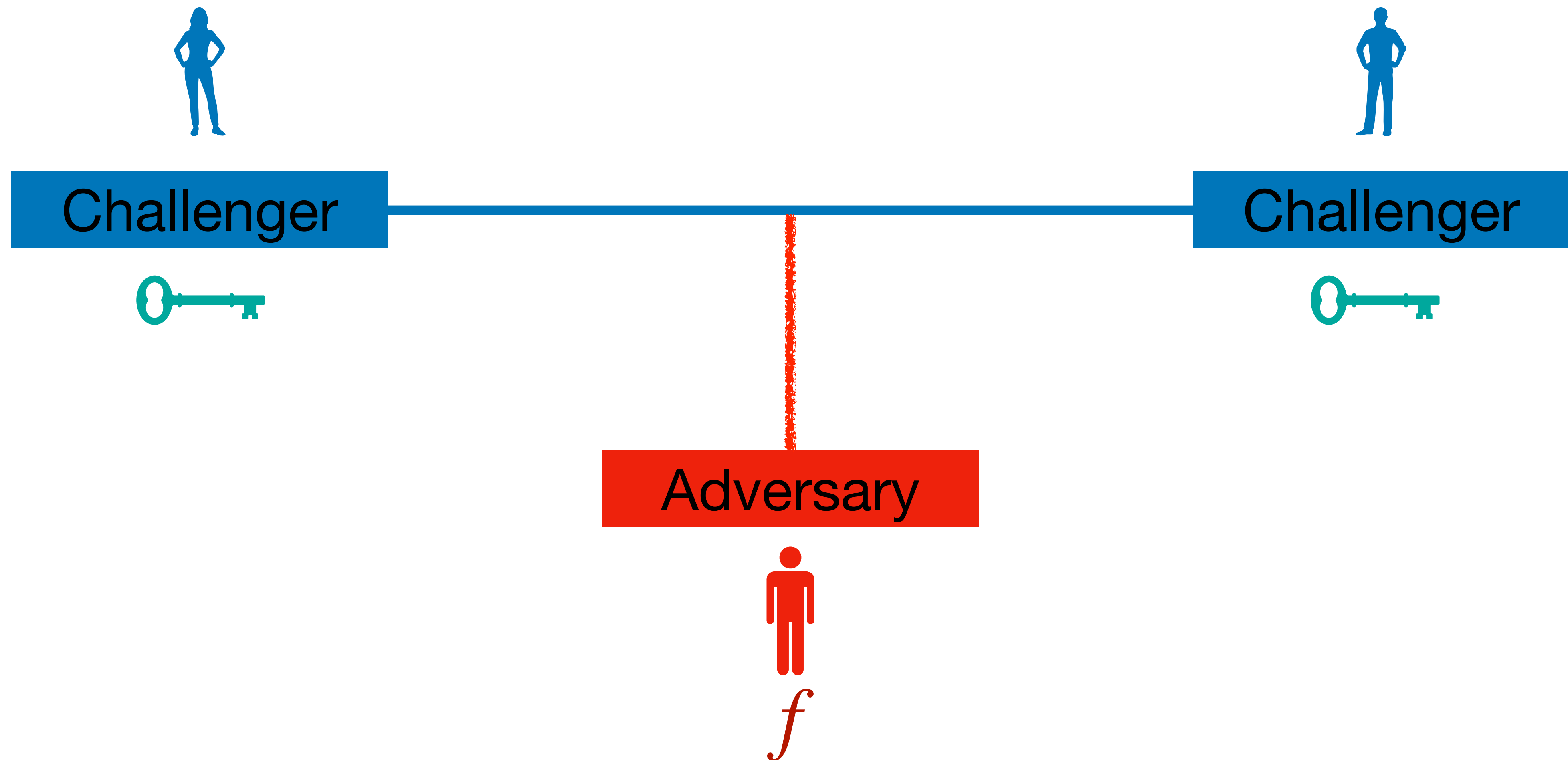
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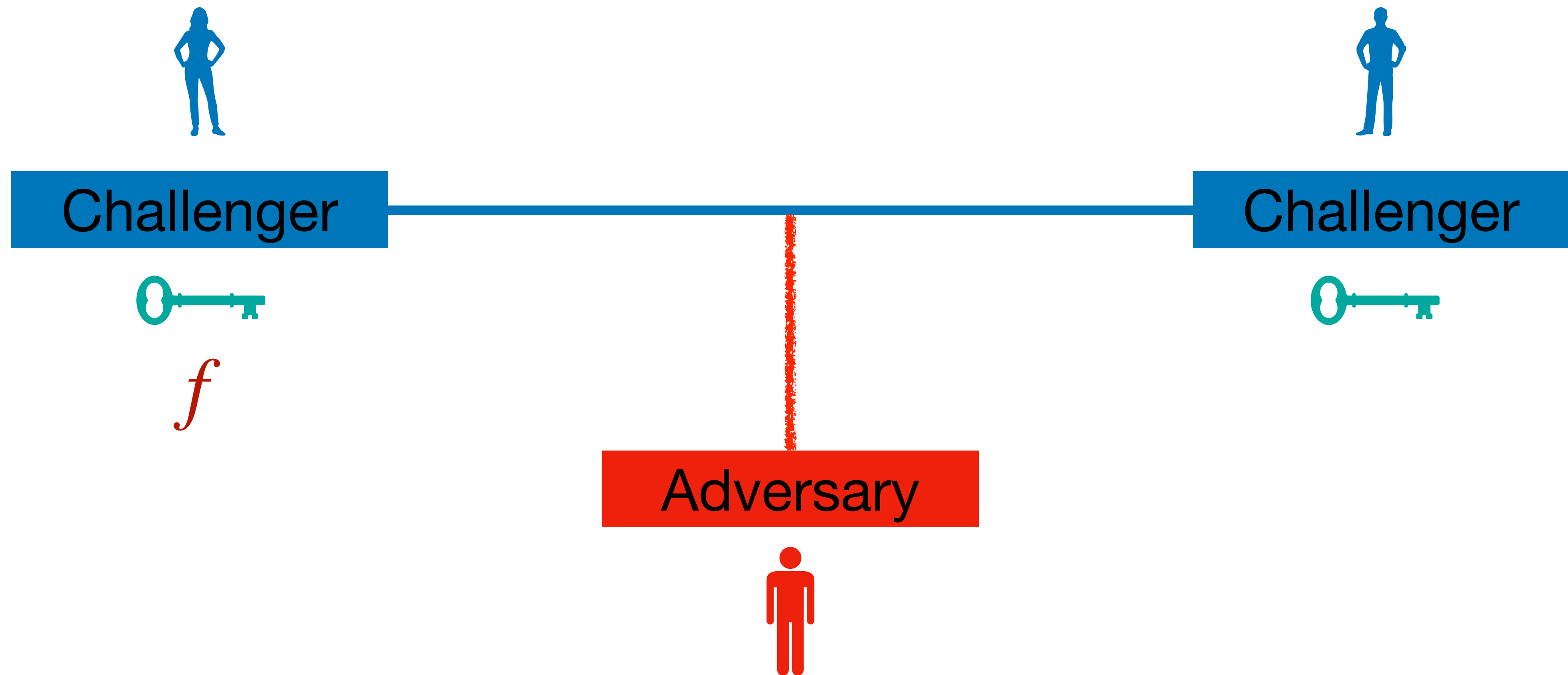
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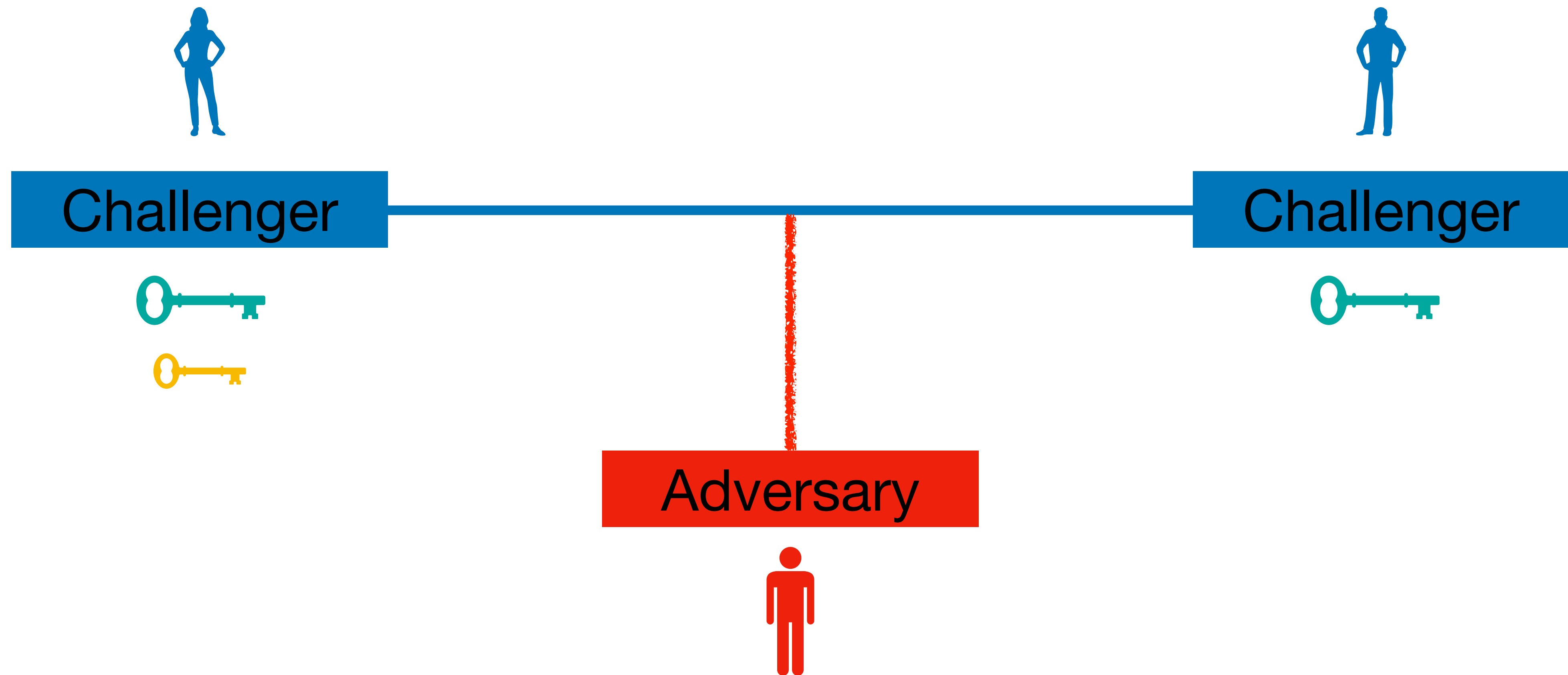
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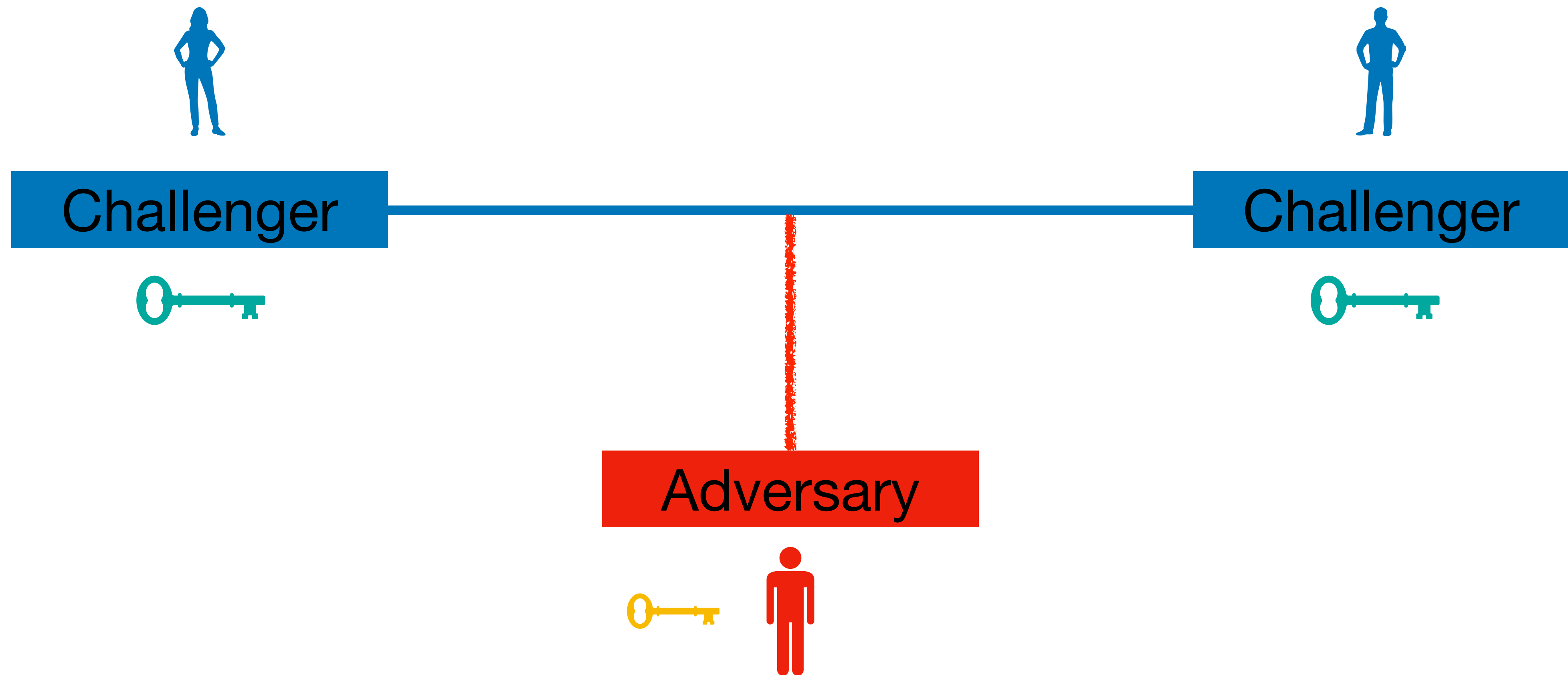
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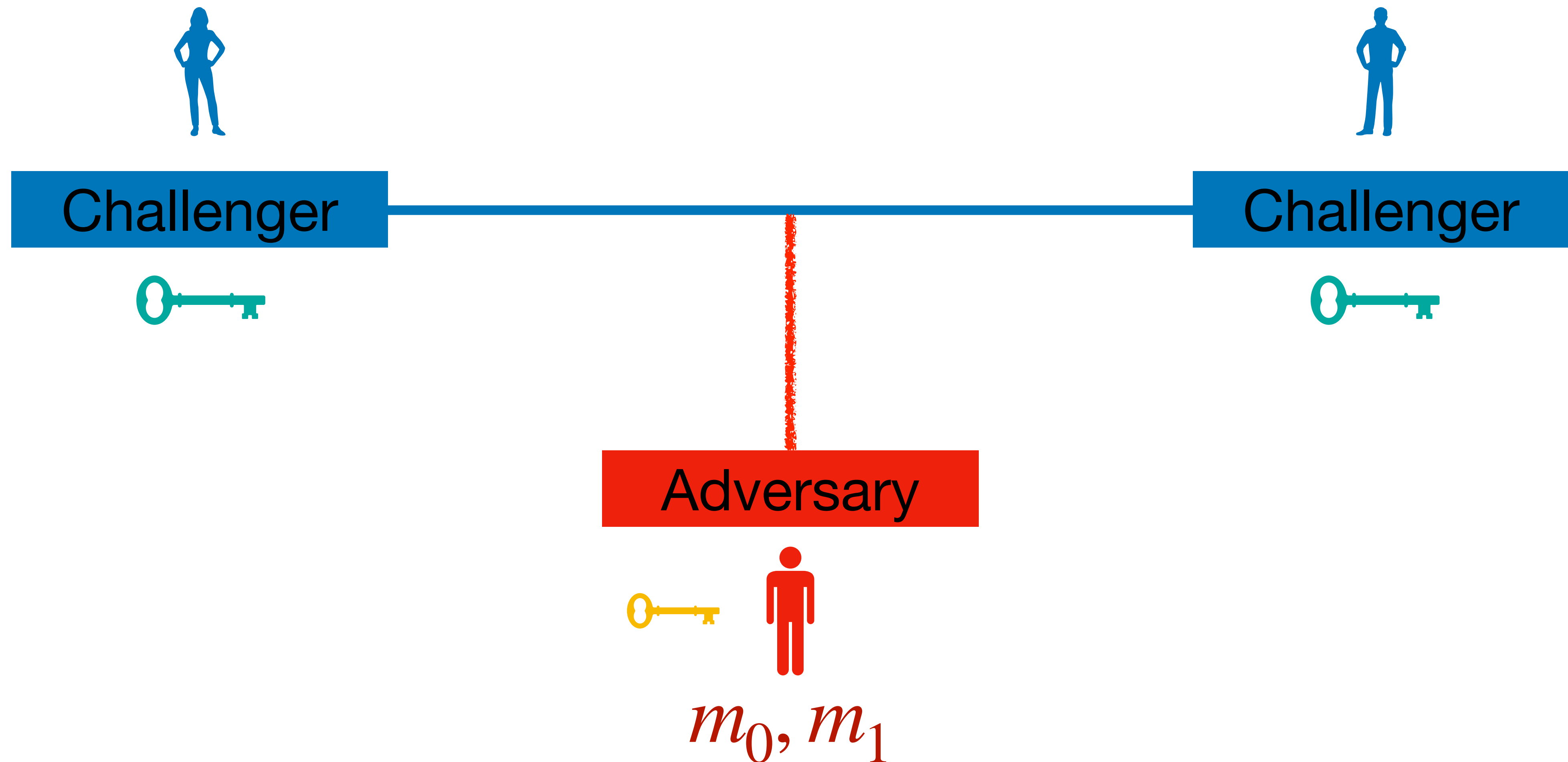
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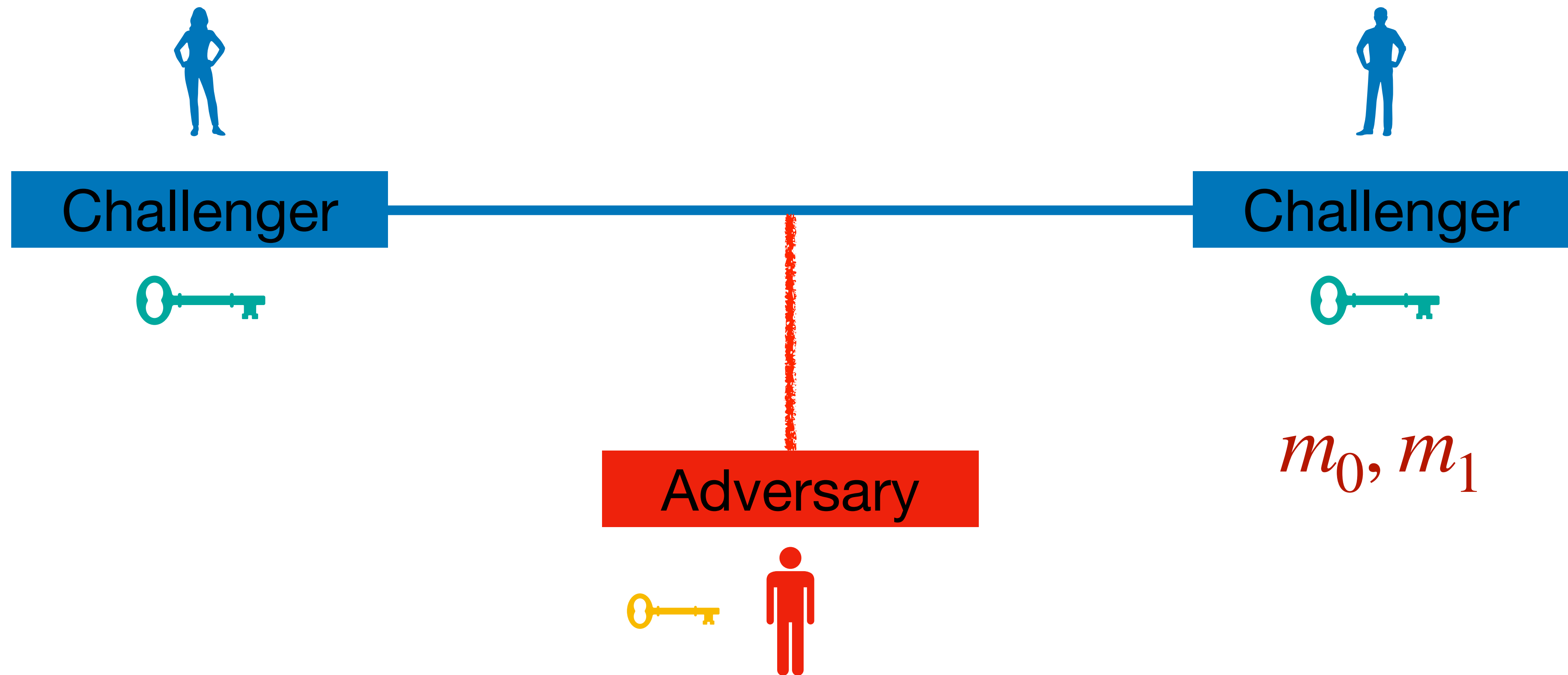
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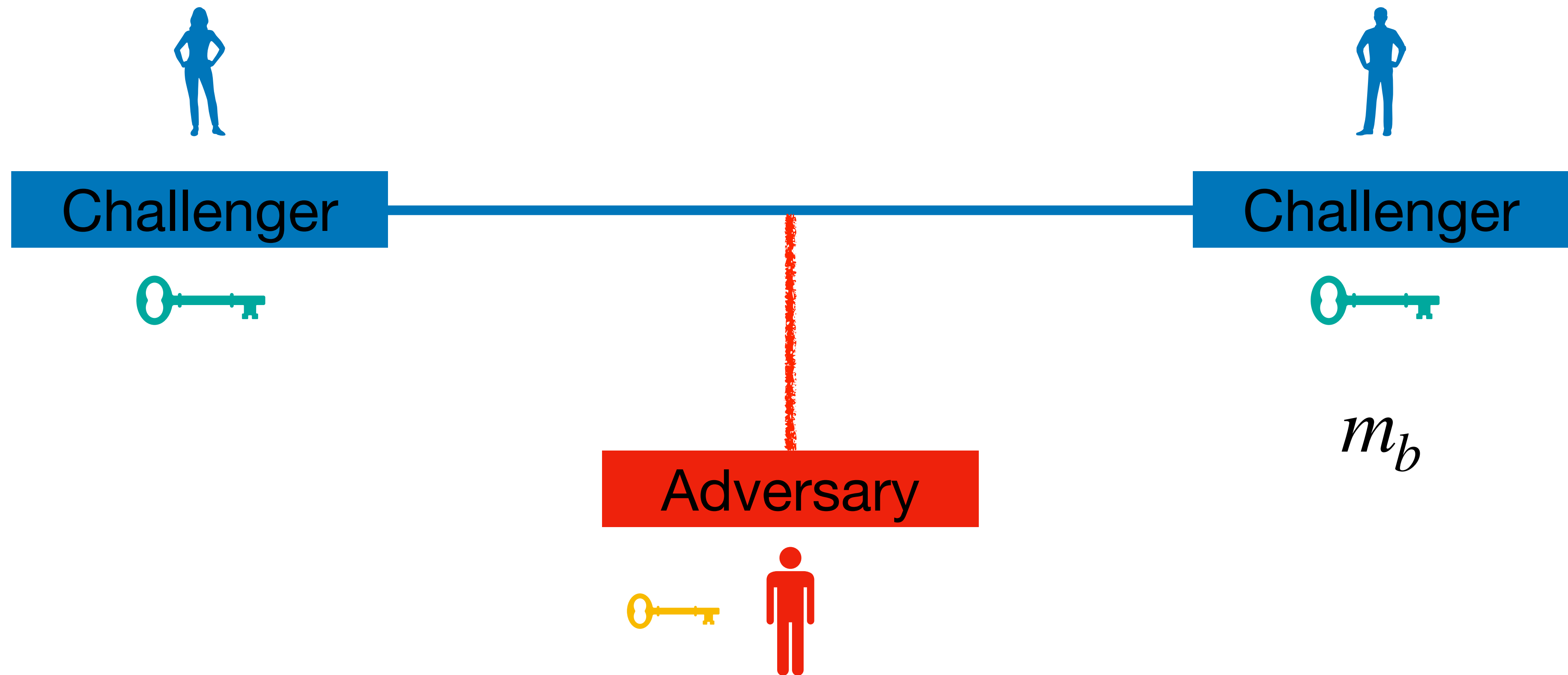
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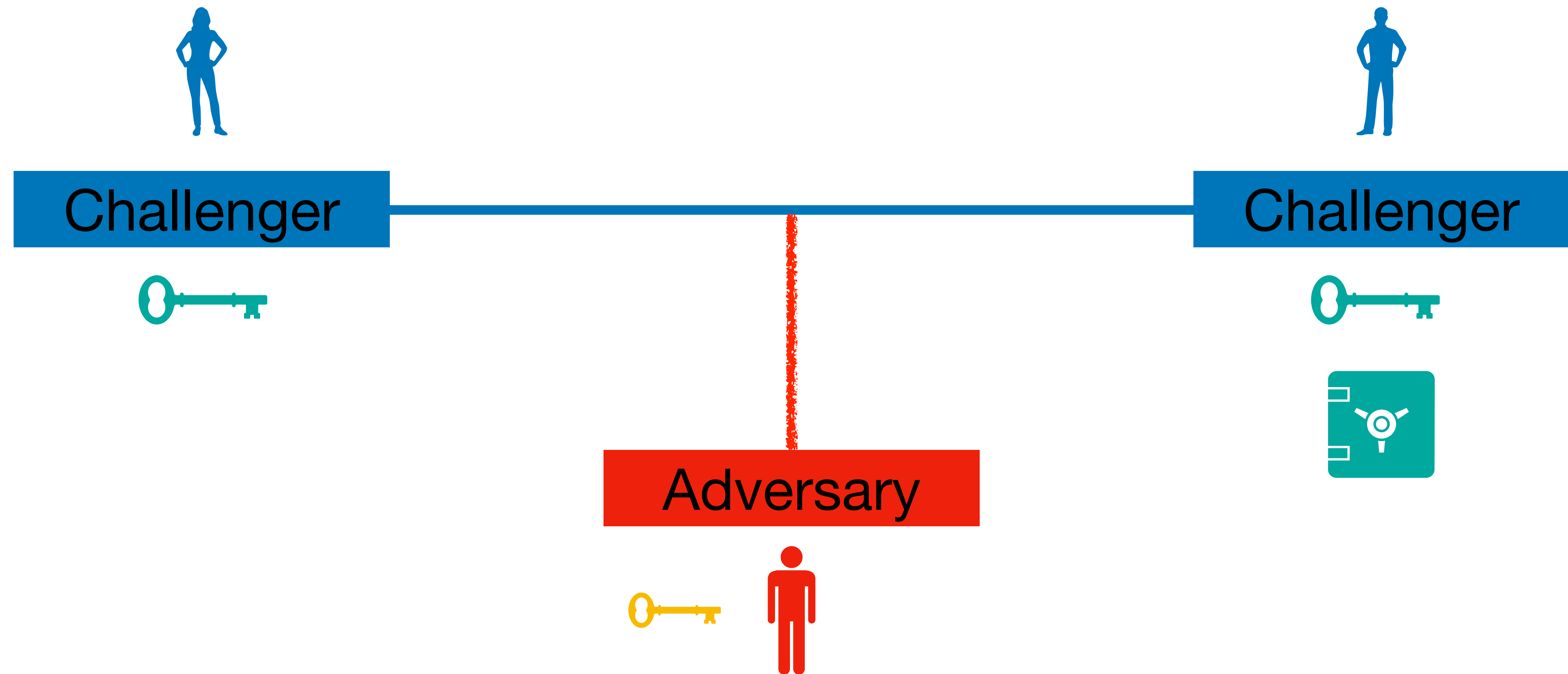
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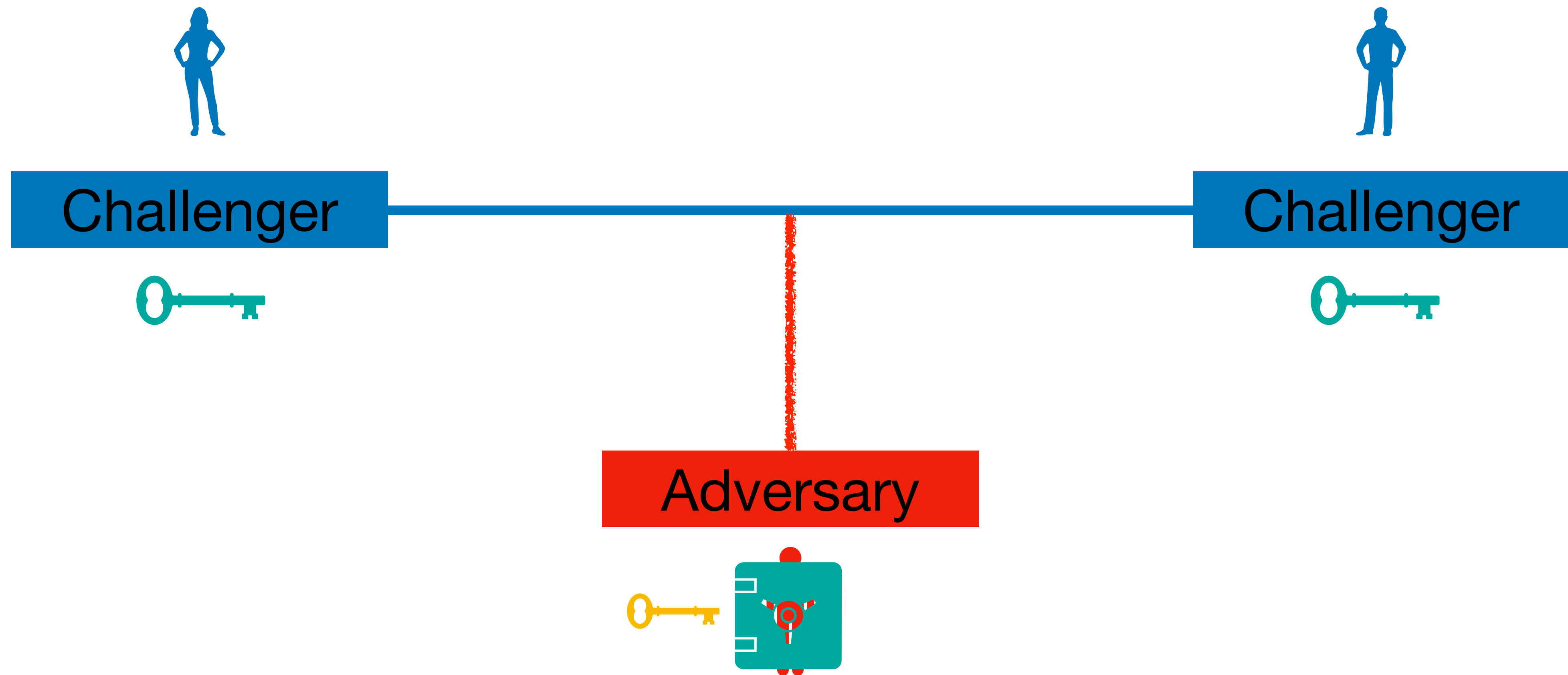
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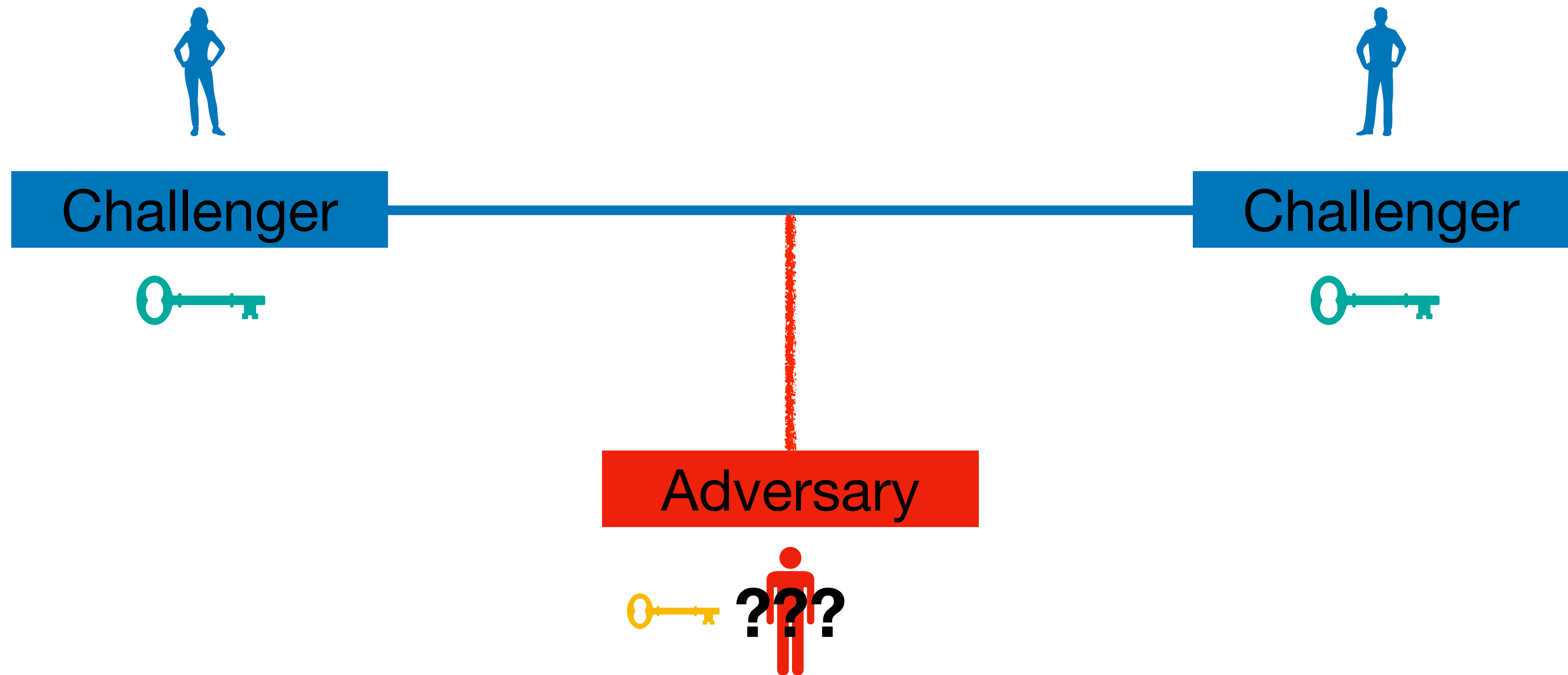
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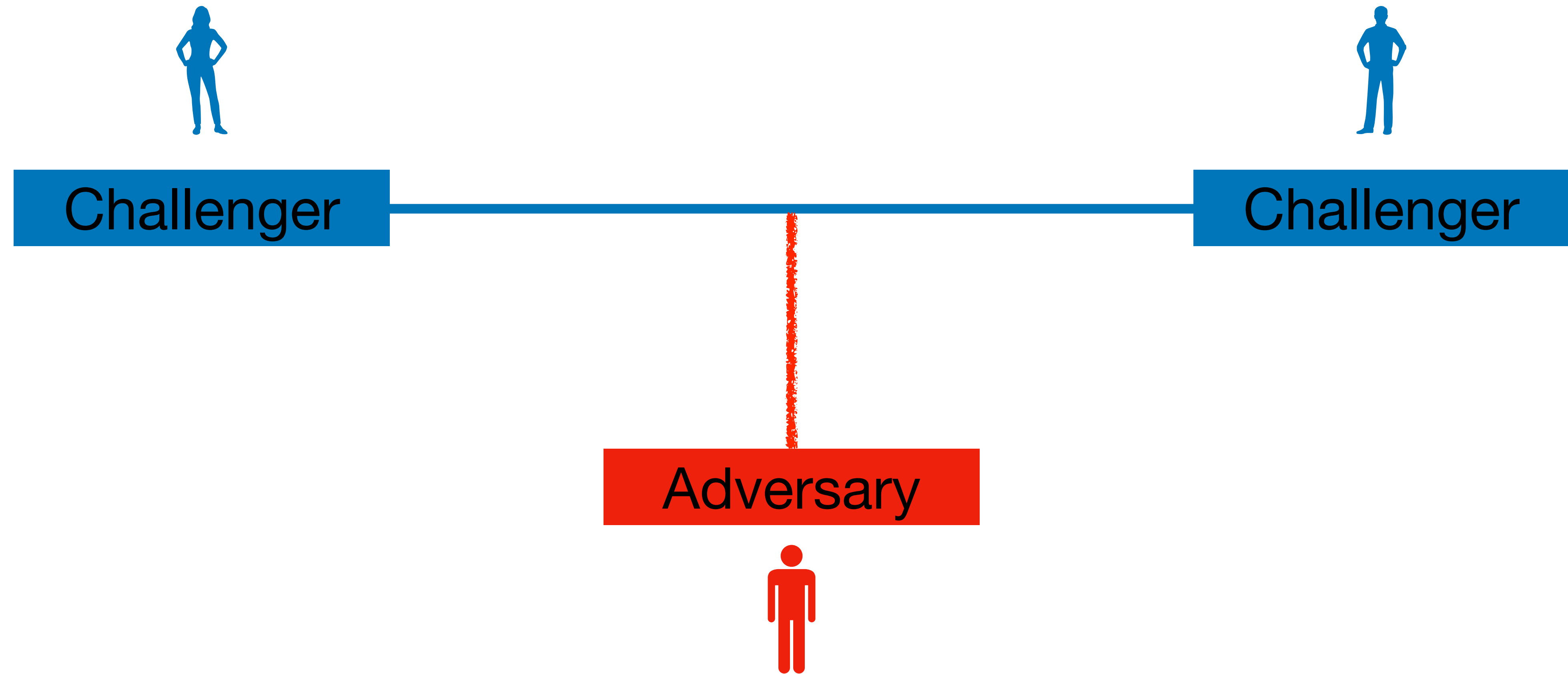
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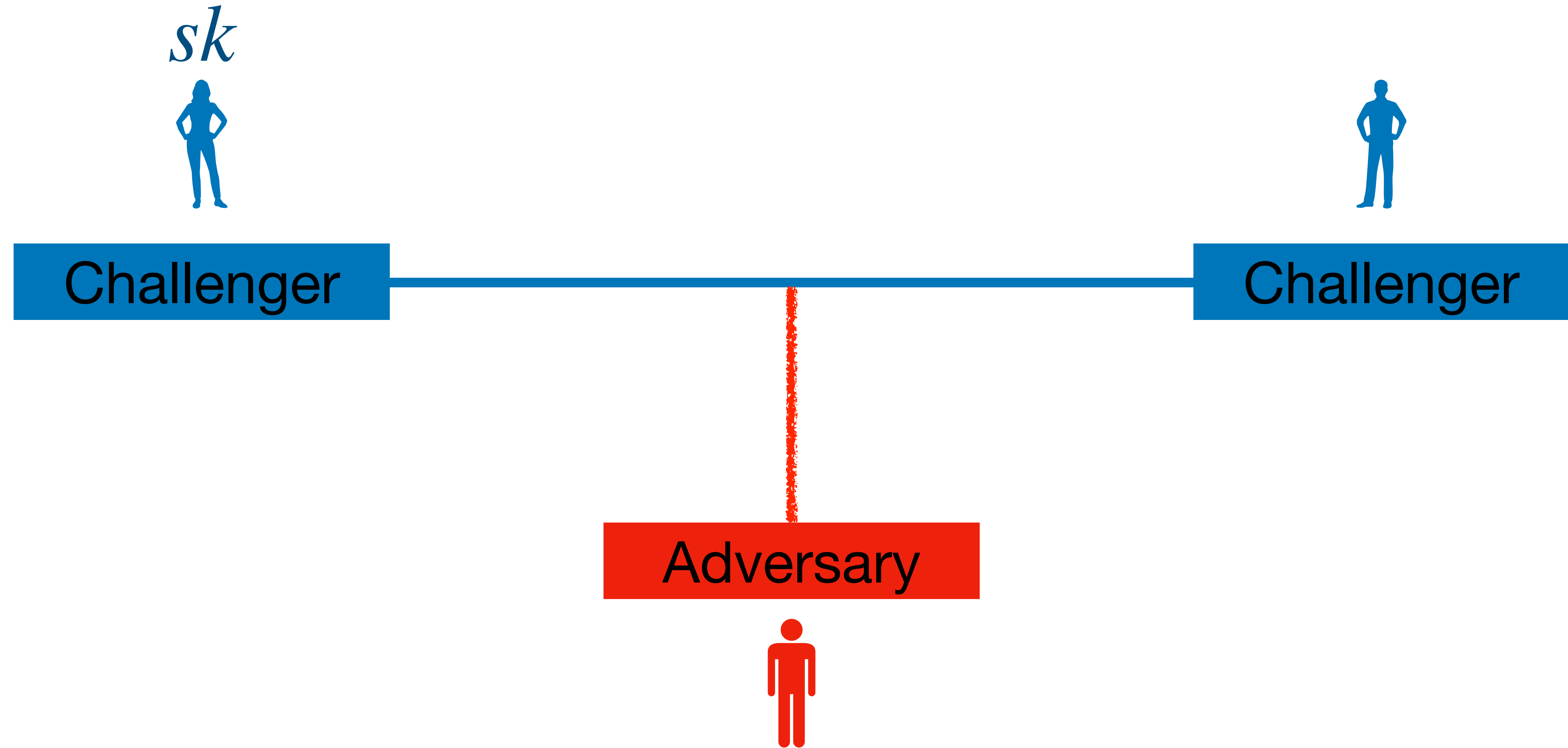
Security against Leakage



One Time Pad is not LR



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0100...011



Challenger

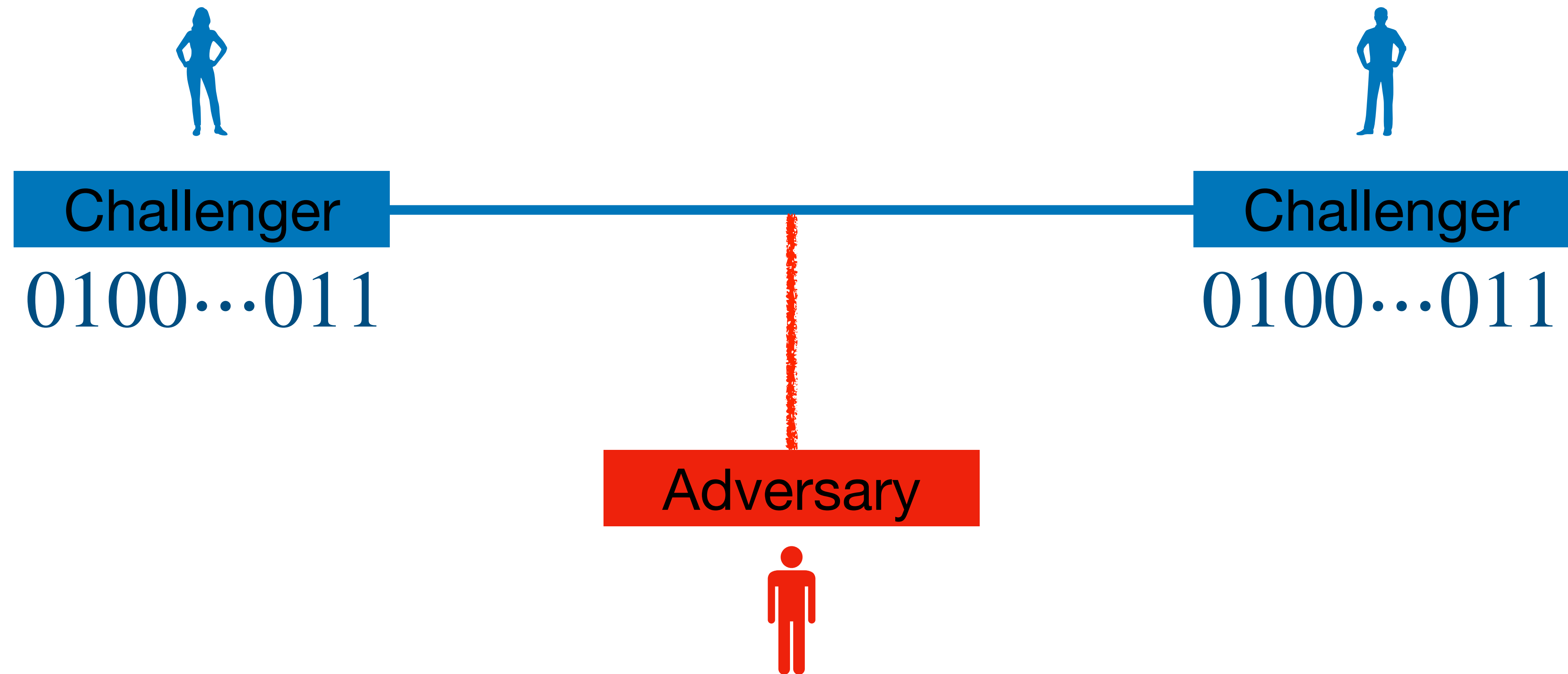


Challenger

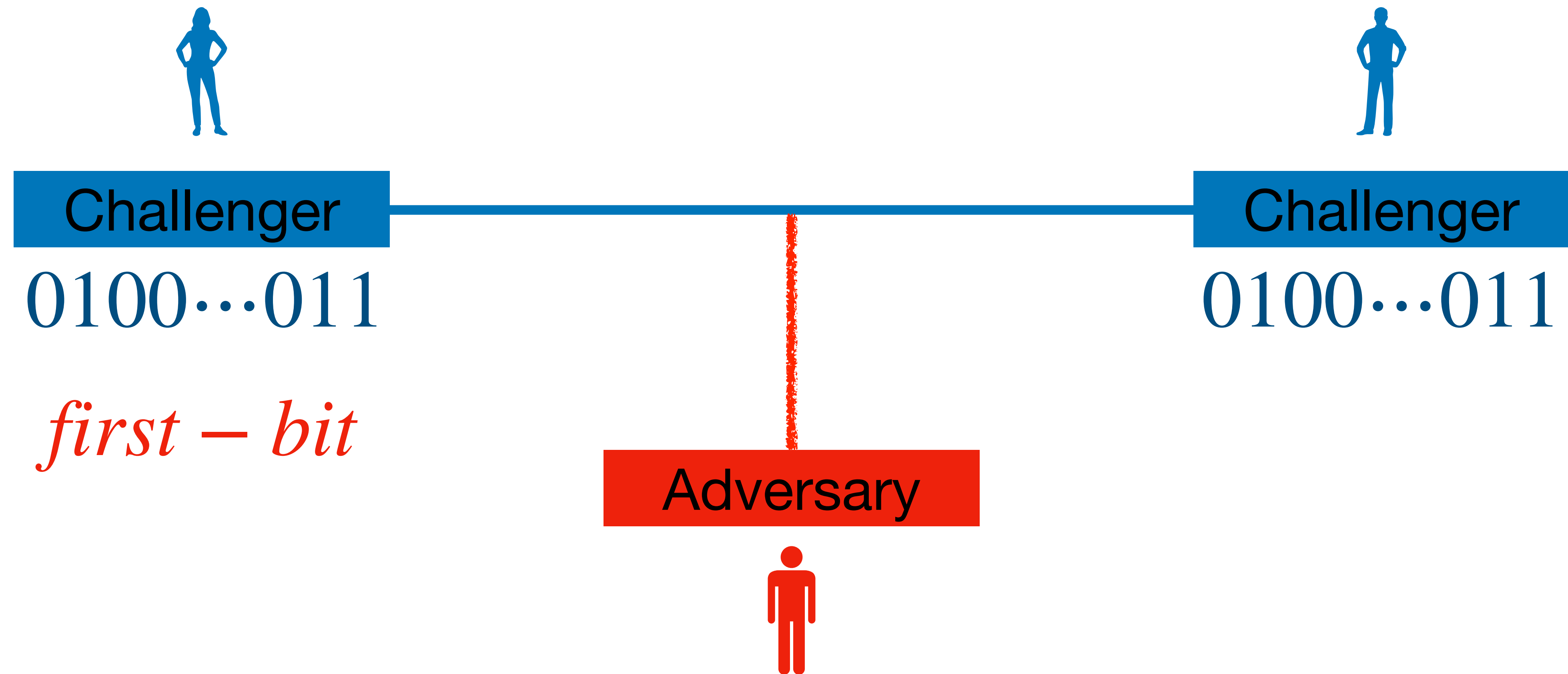
Adversary



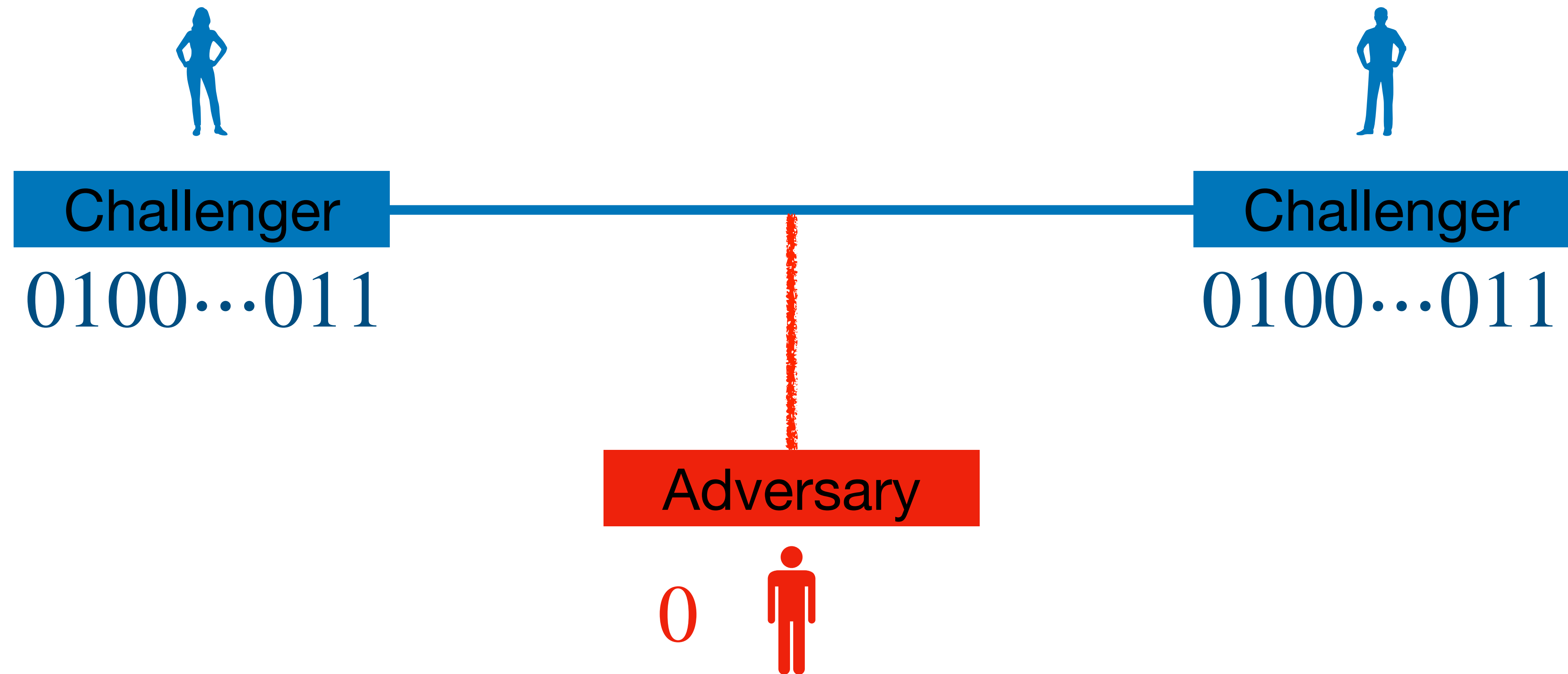
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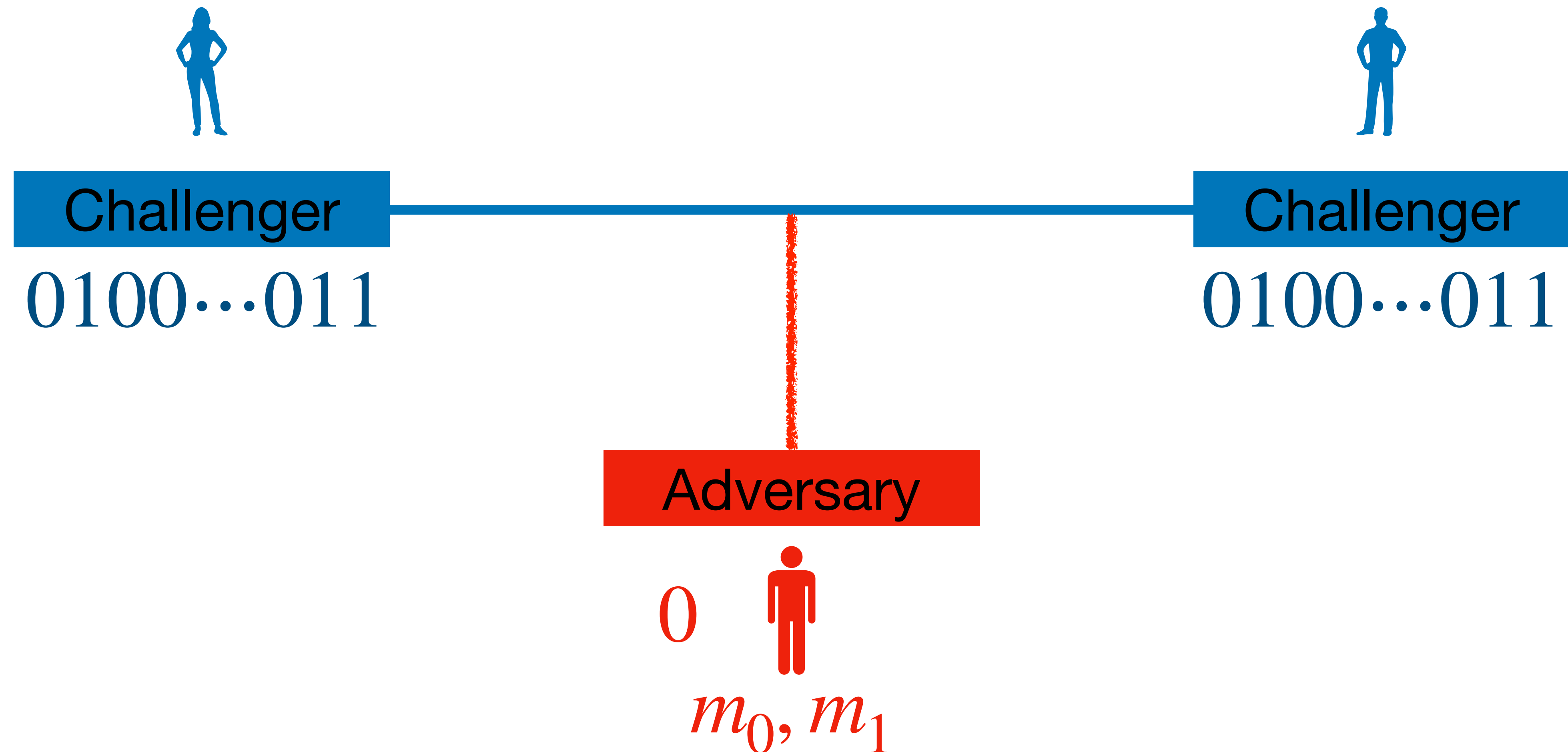
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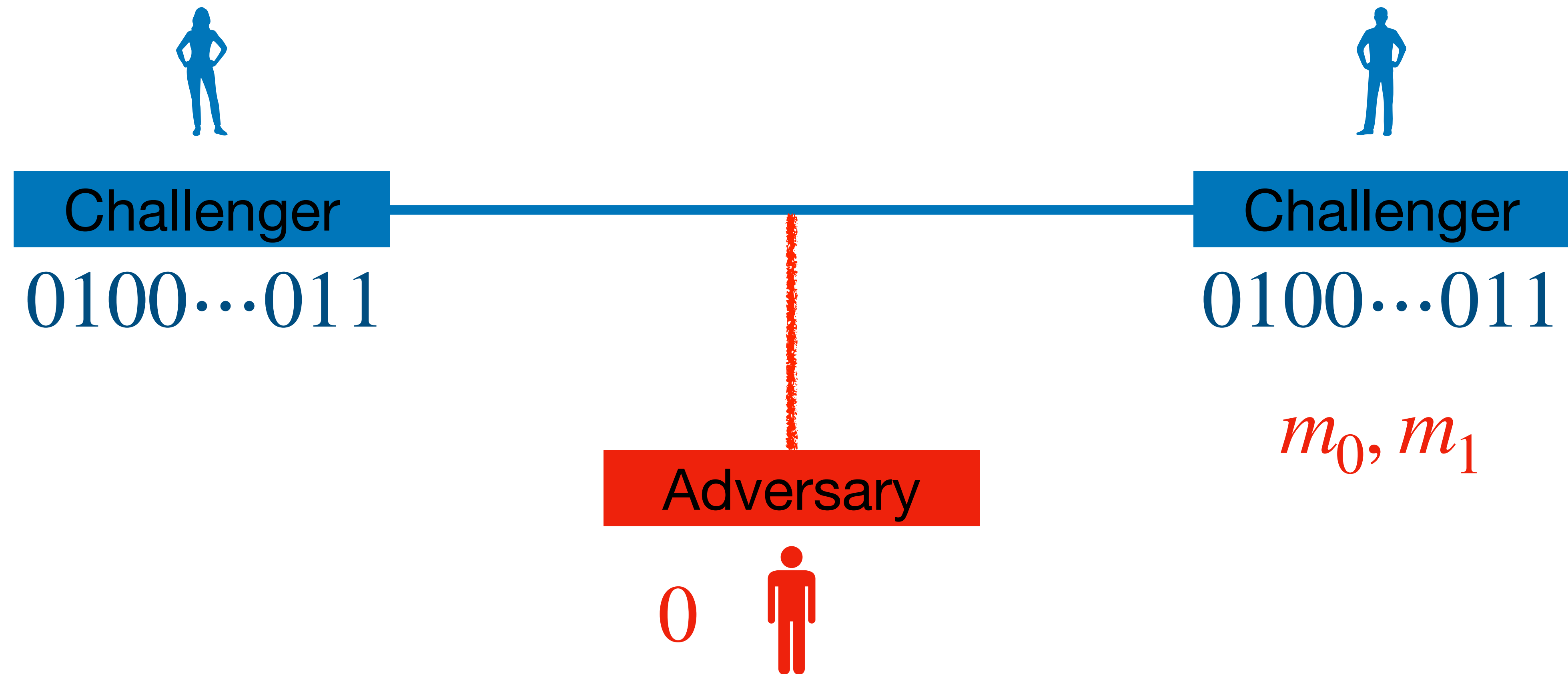
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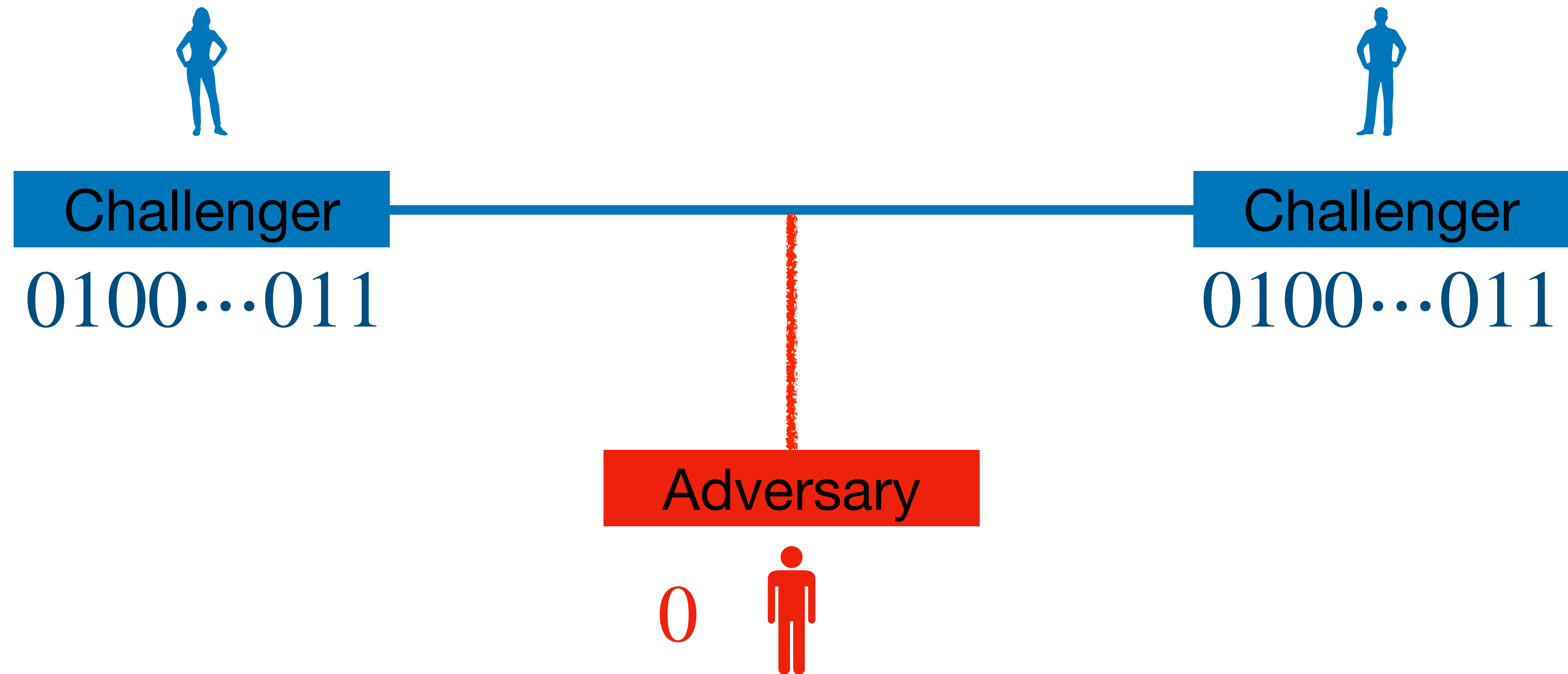
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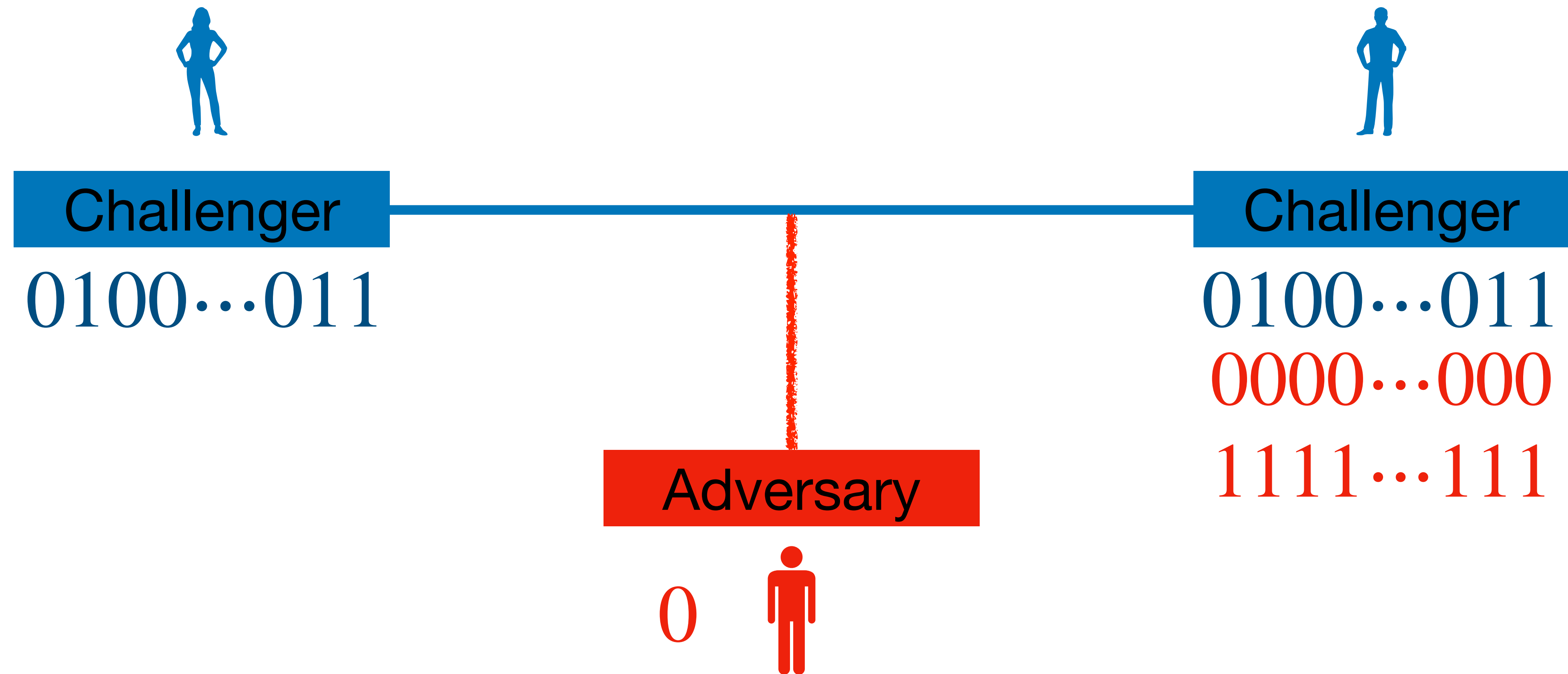
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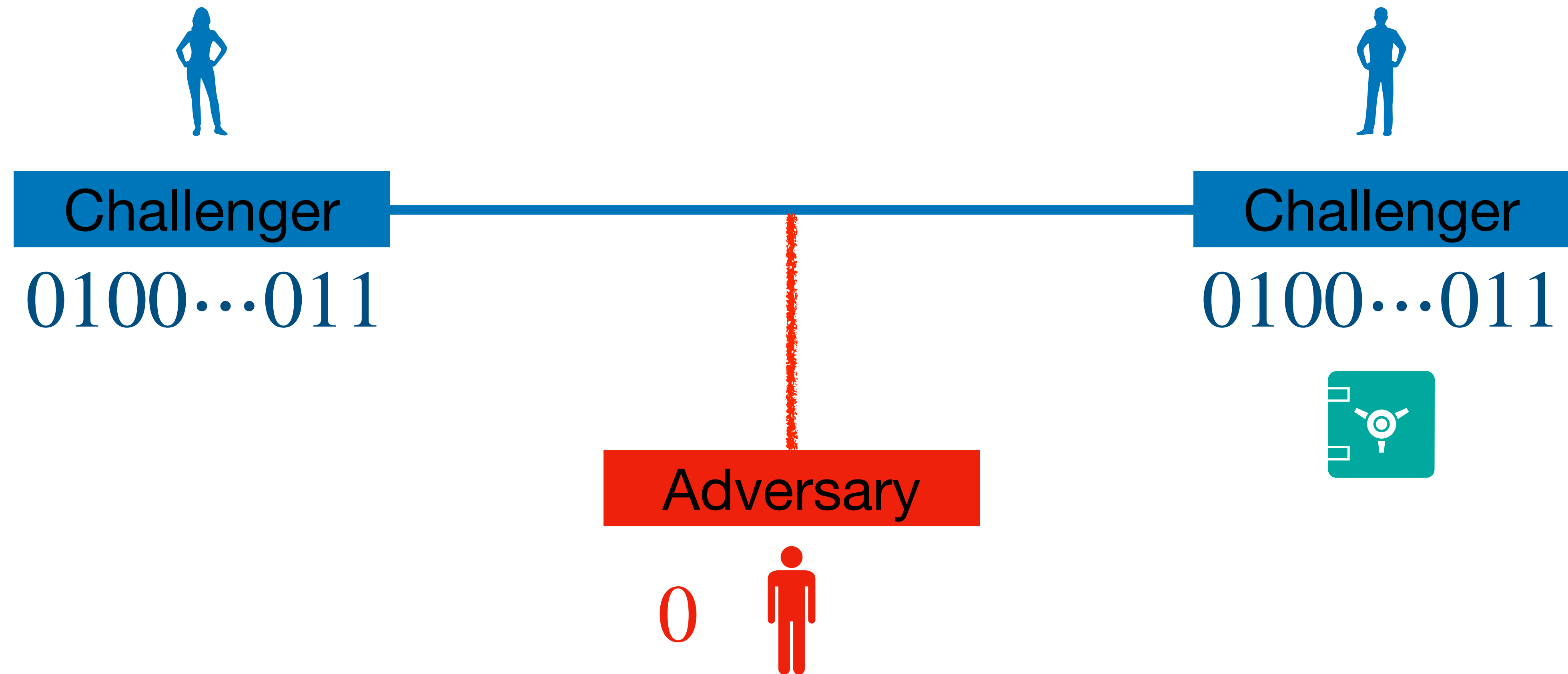
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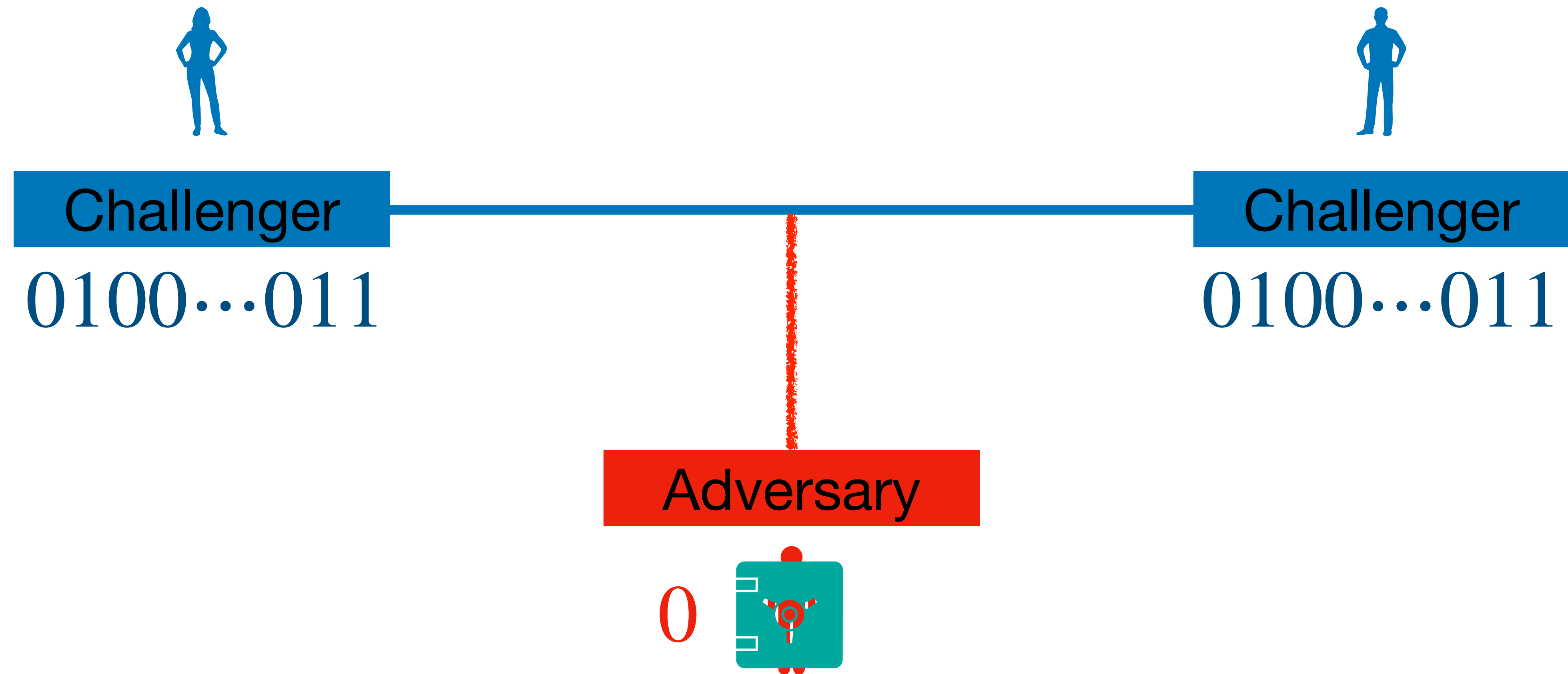
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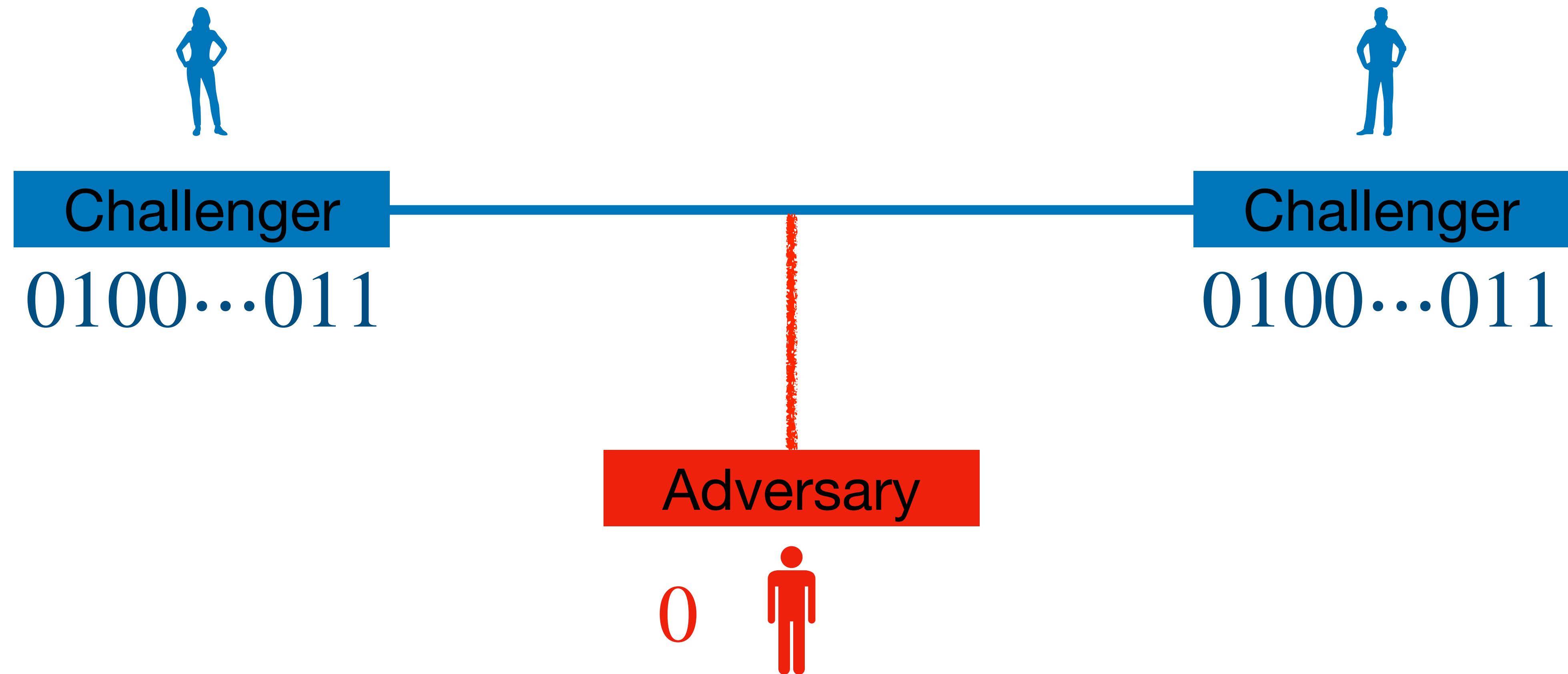
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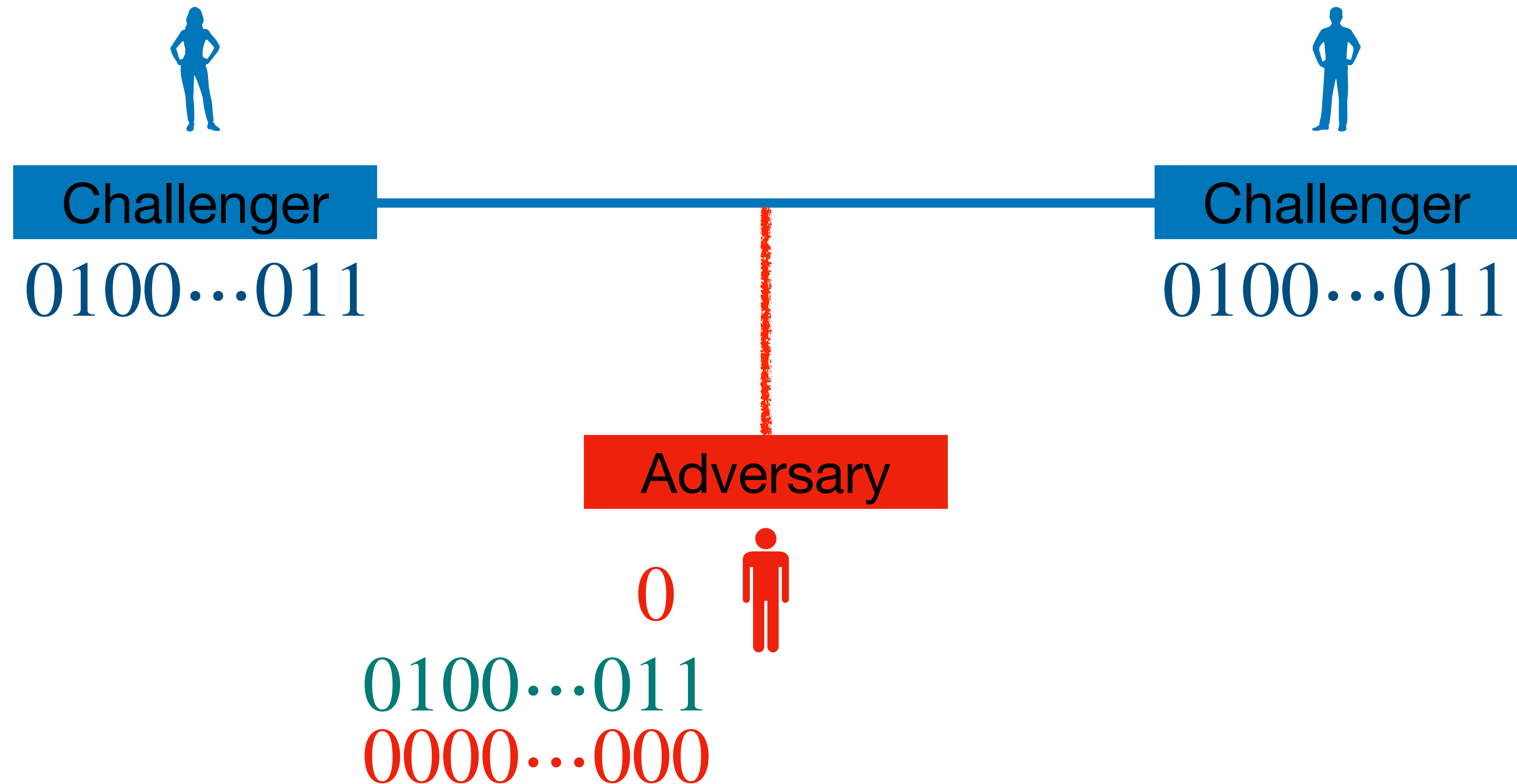
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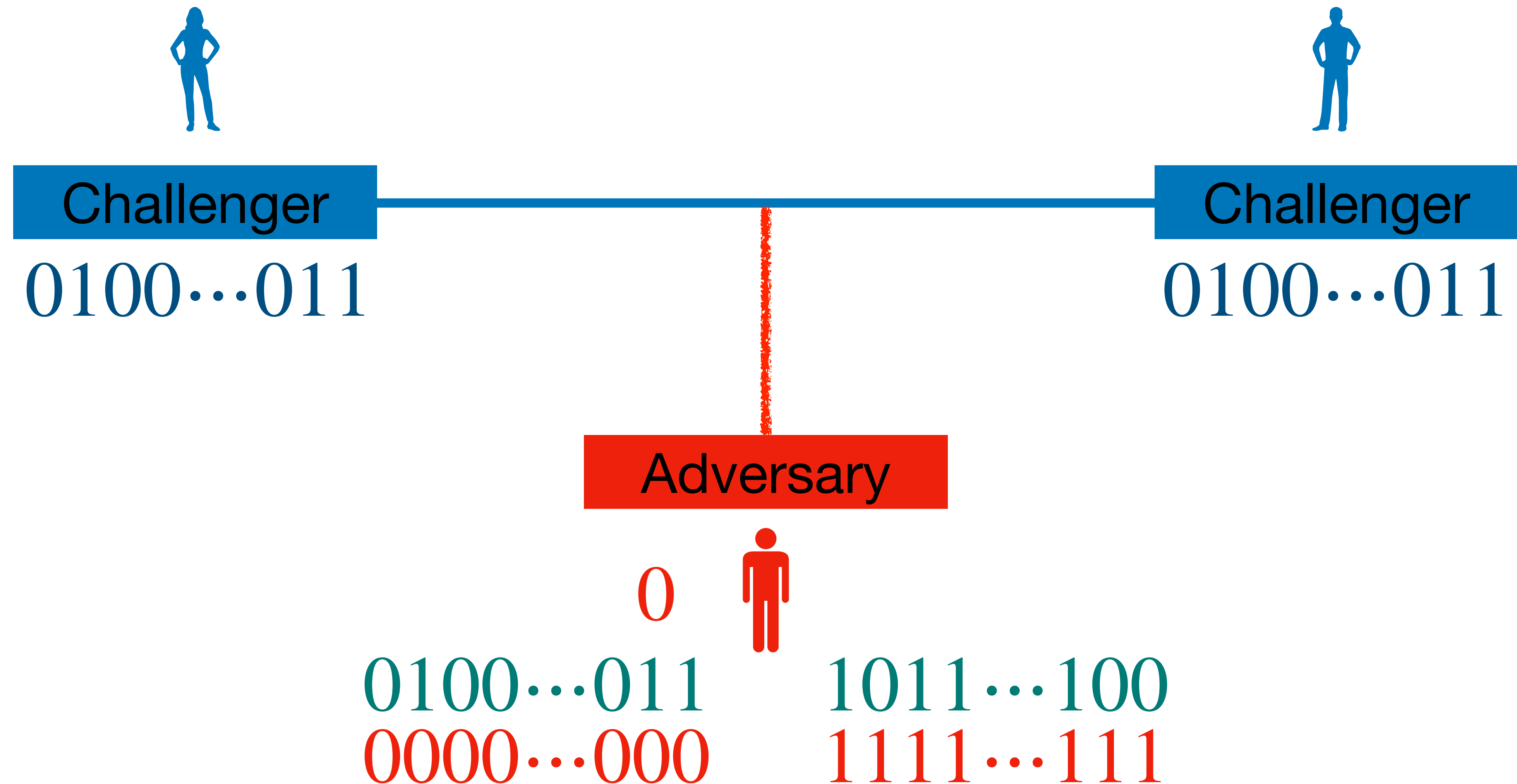
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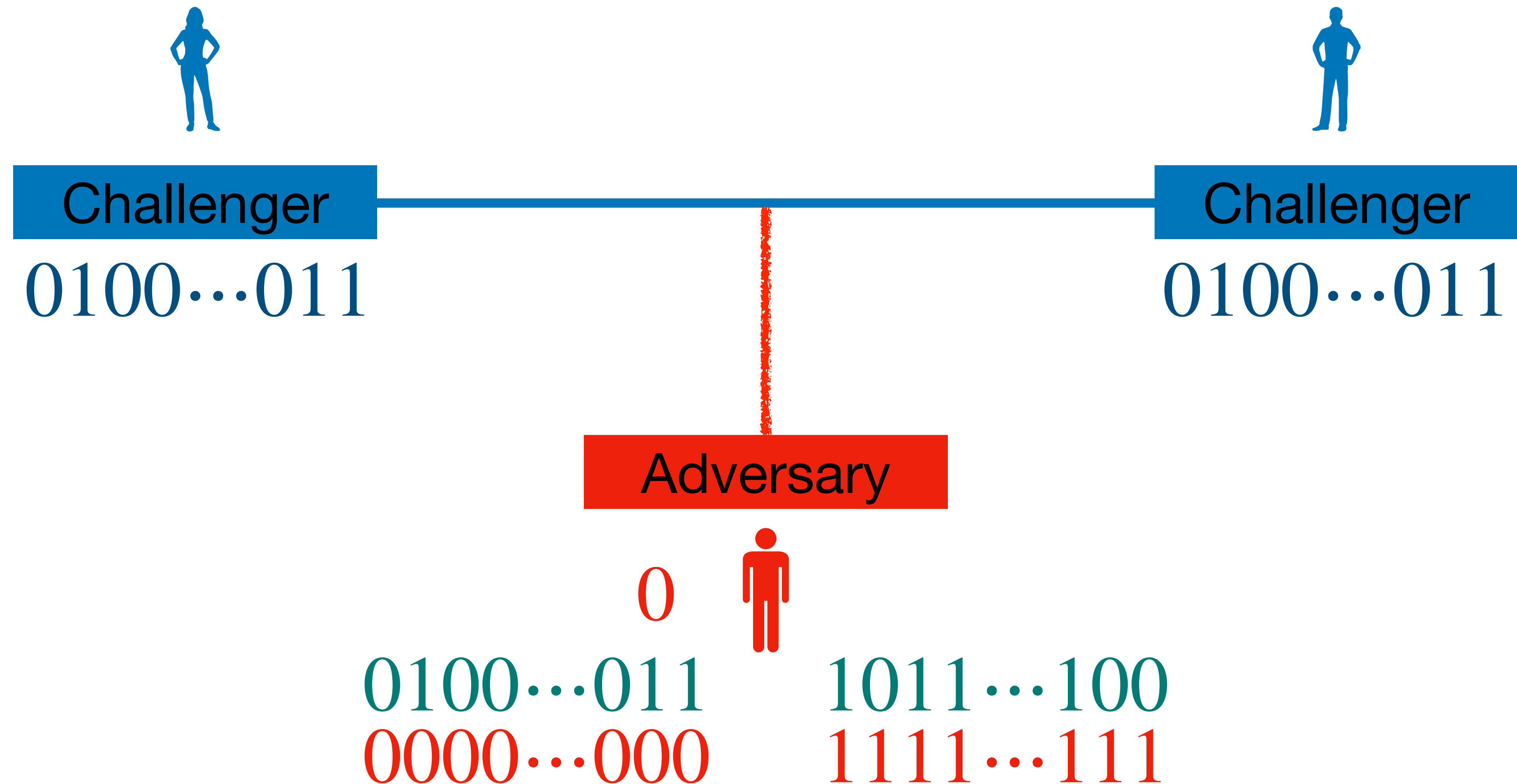
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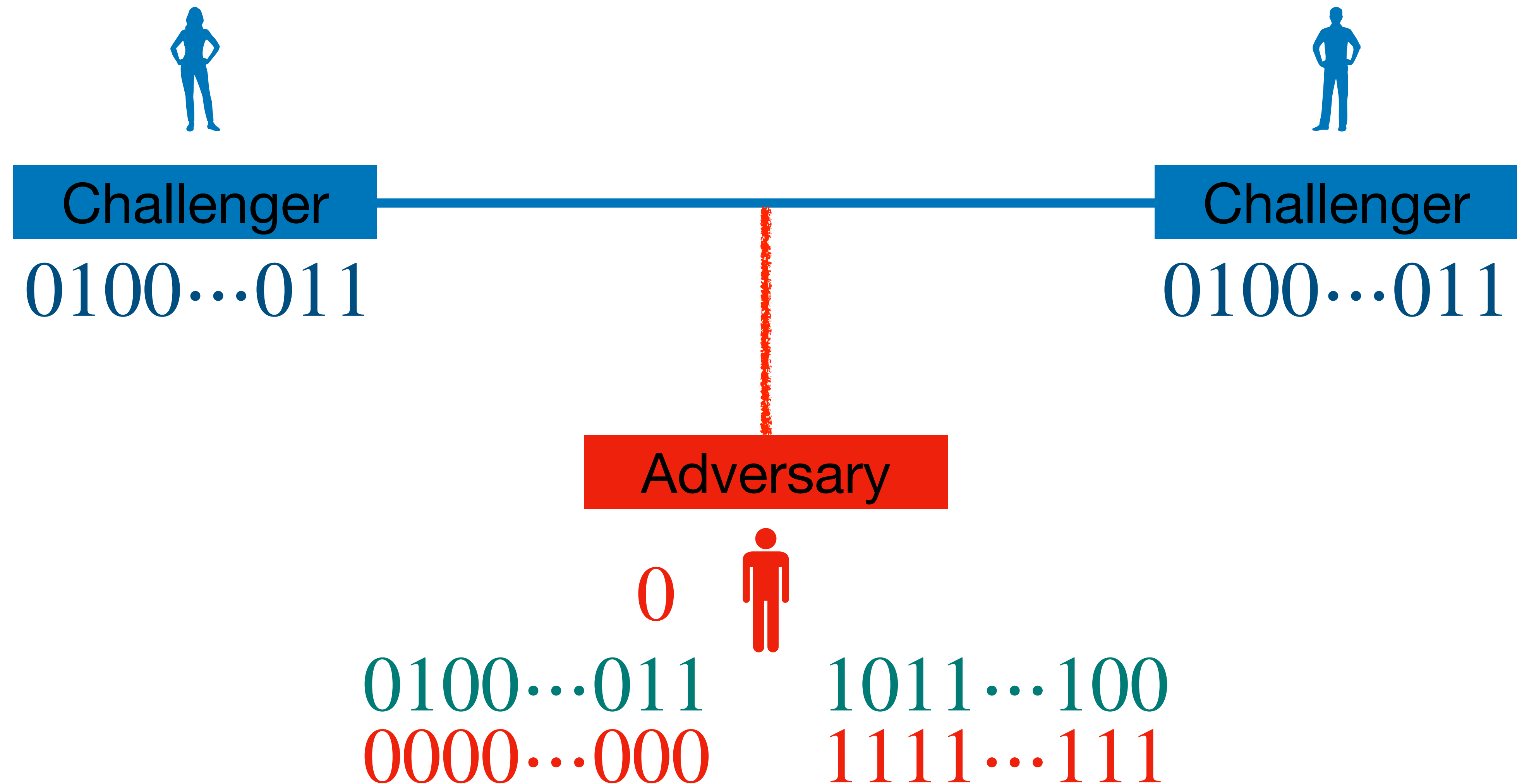
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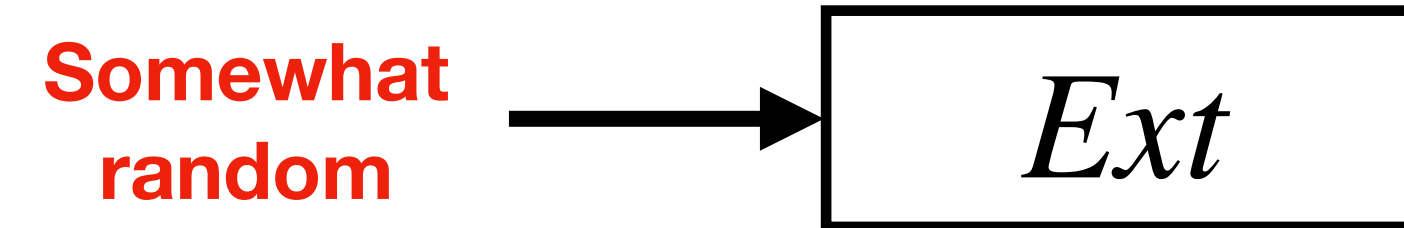
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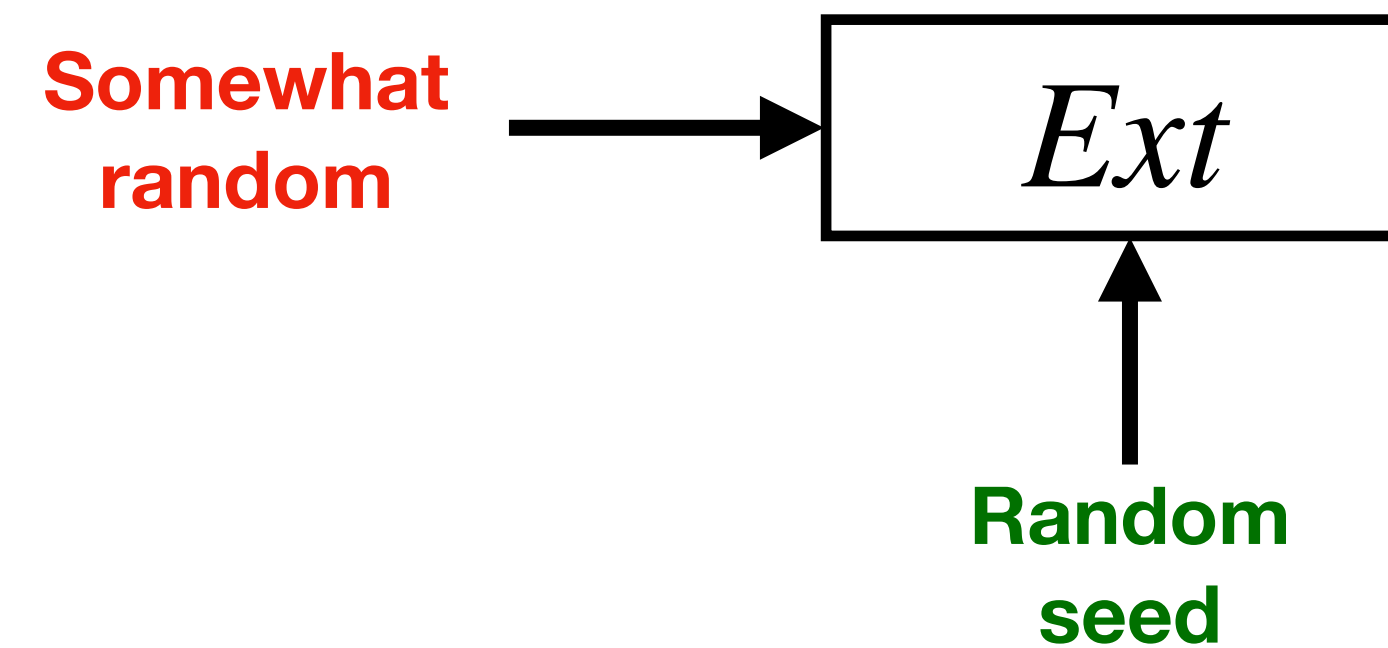
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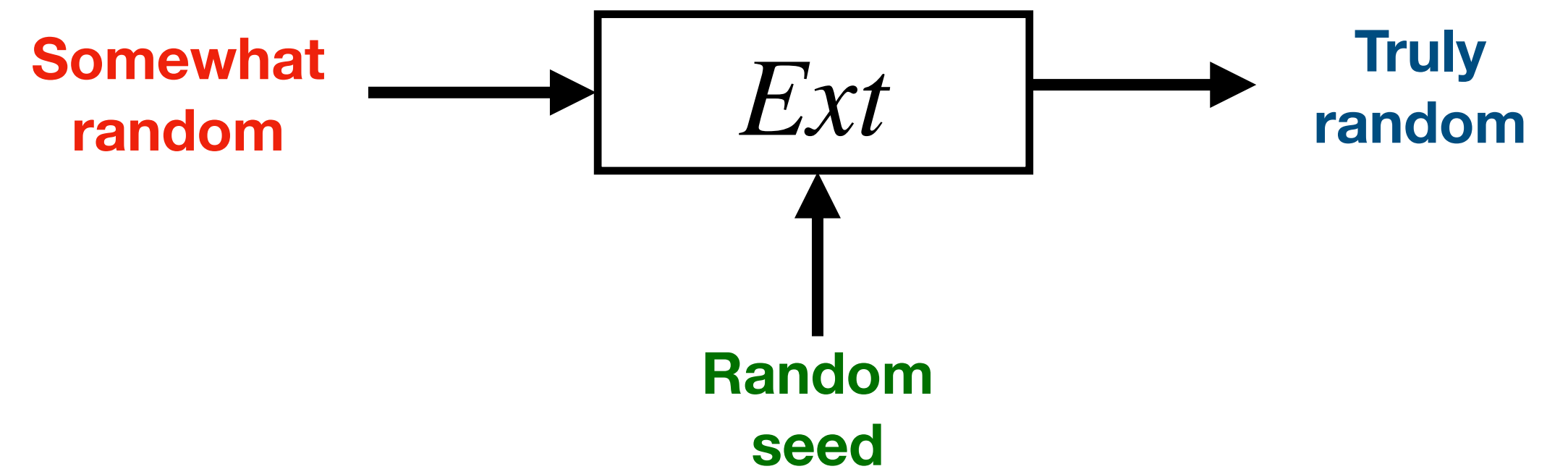
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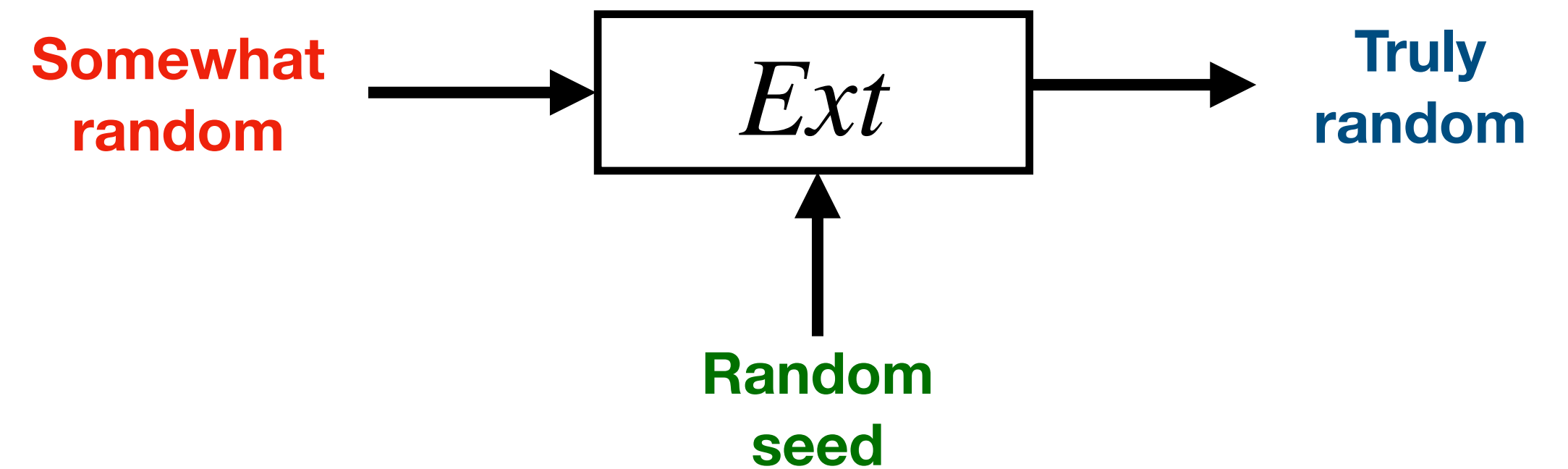


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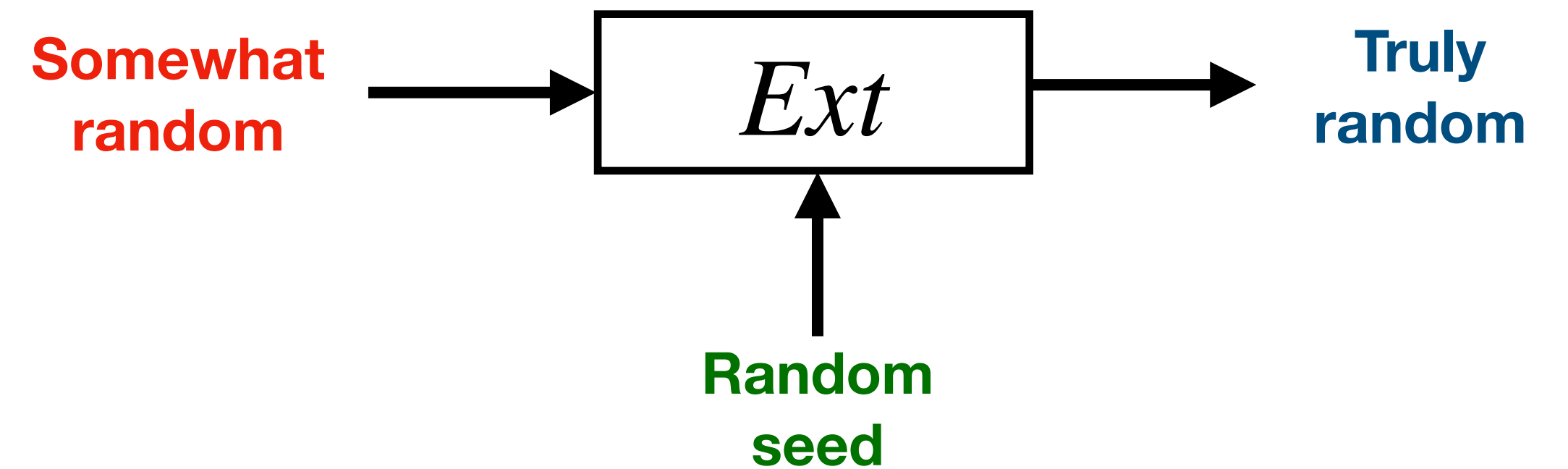


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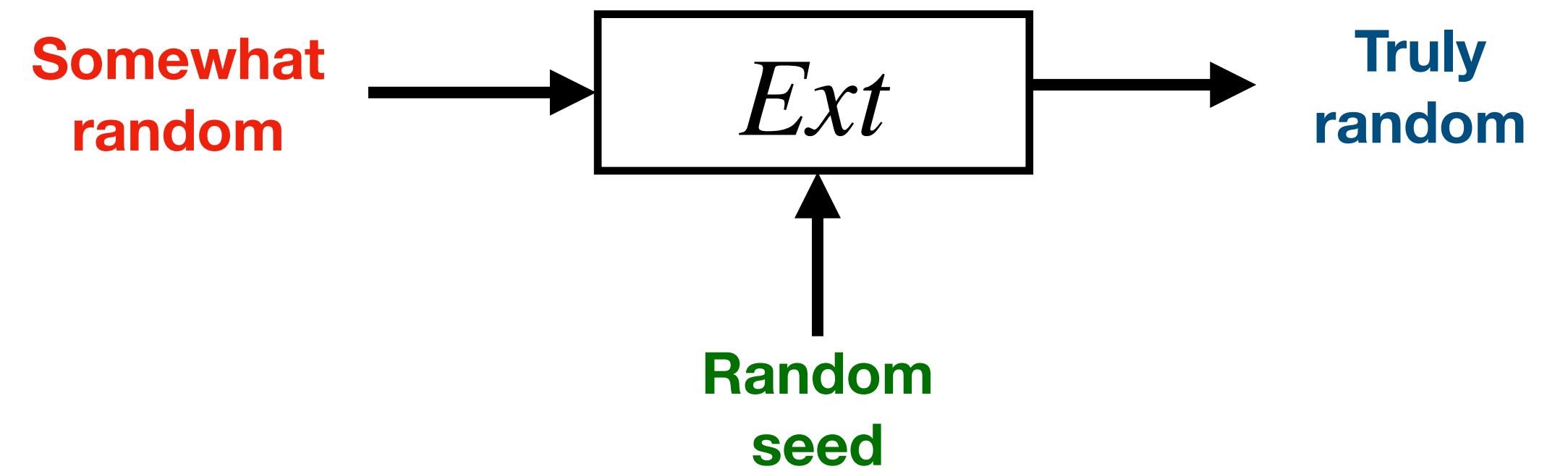
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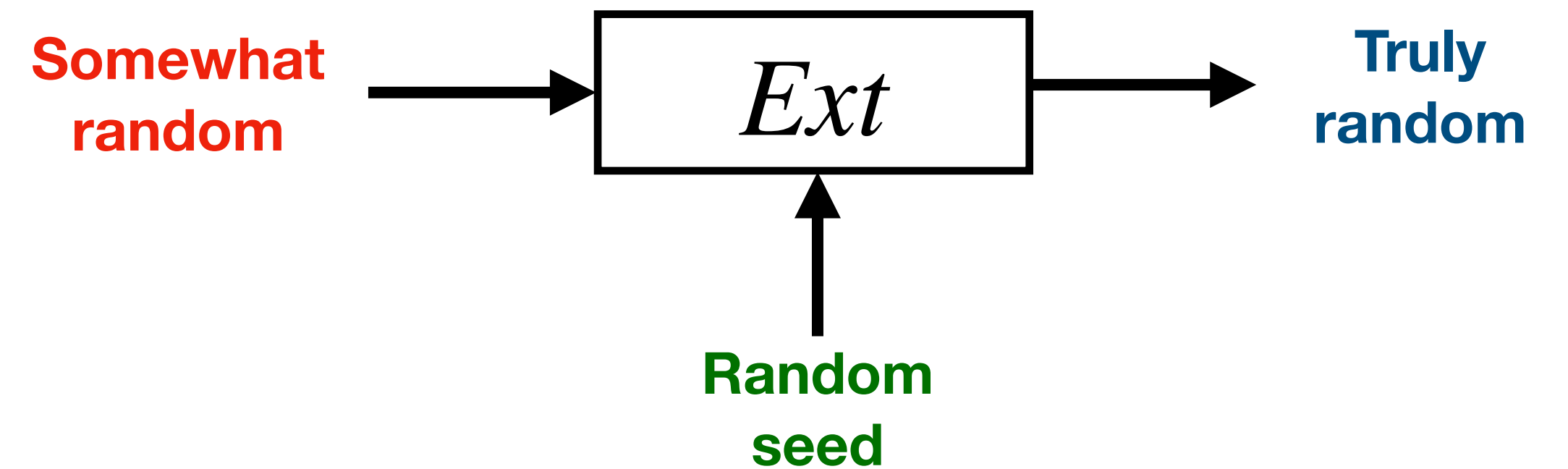
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- $Dec(sk, ct) \rightarrow$ Run $s = Ext_{c_0}(sk)$ and return $s \oplus ct$.



$$(c_0, Ext_{c_0}(sk), f(sk)) \approx (c_0, U, f(sk))$$

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- Other works include [Dodis et al.09], [Brakerski et al.10], [Dodis et al.10], [Faonio et al.15] and many more.

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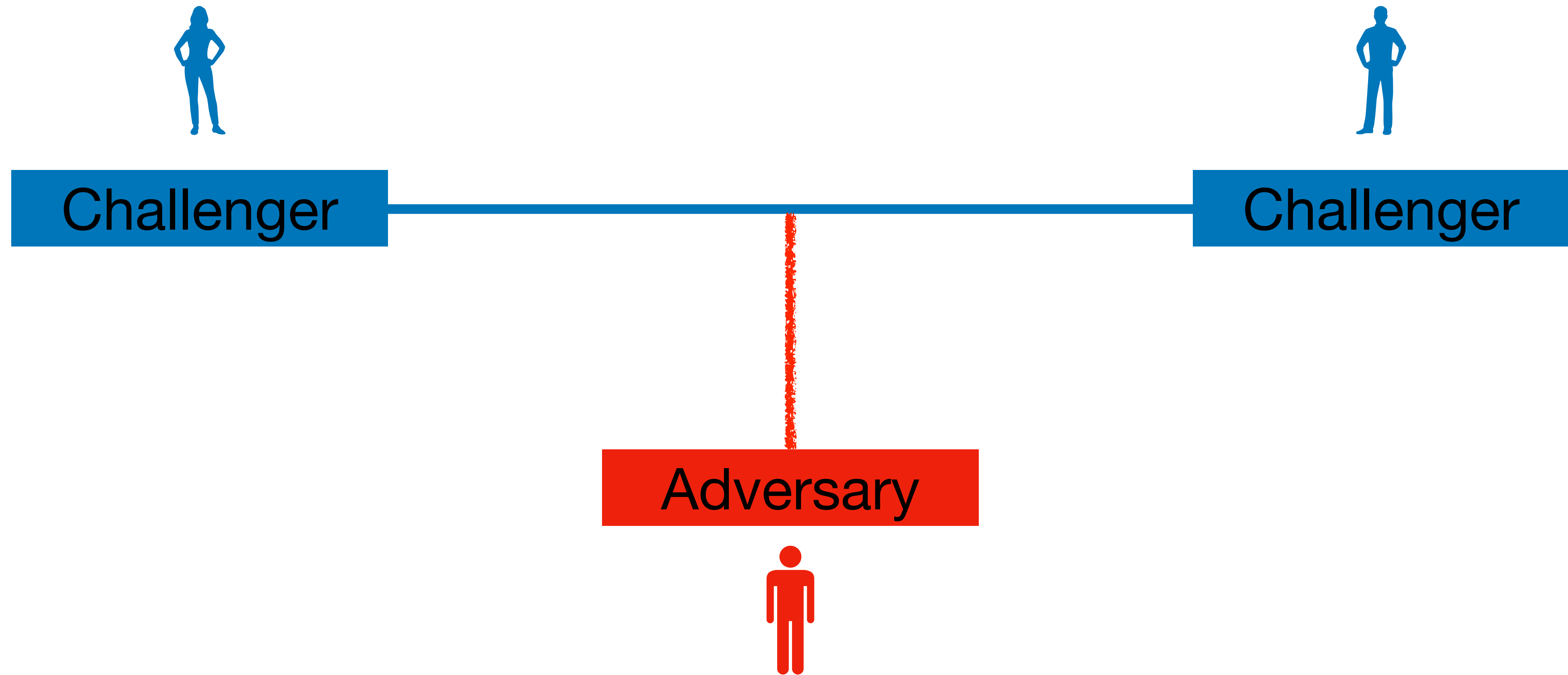
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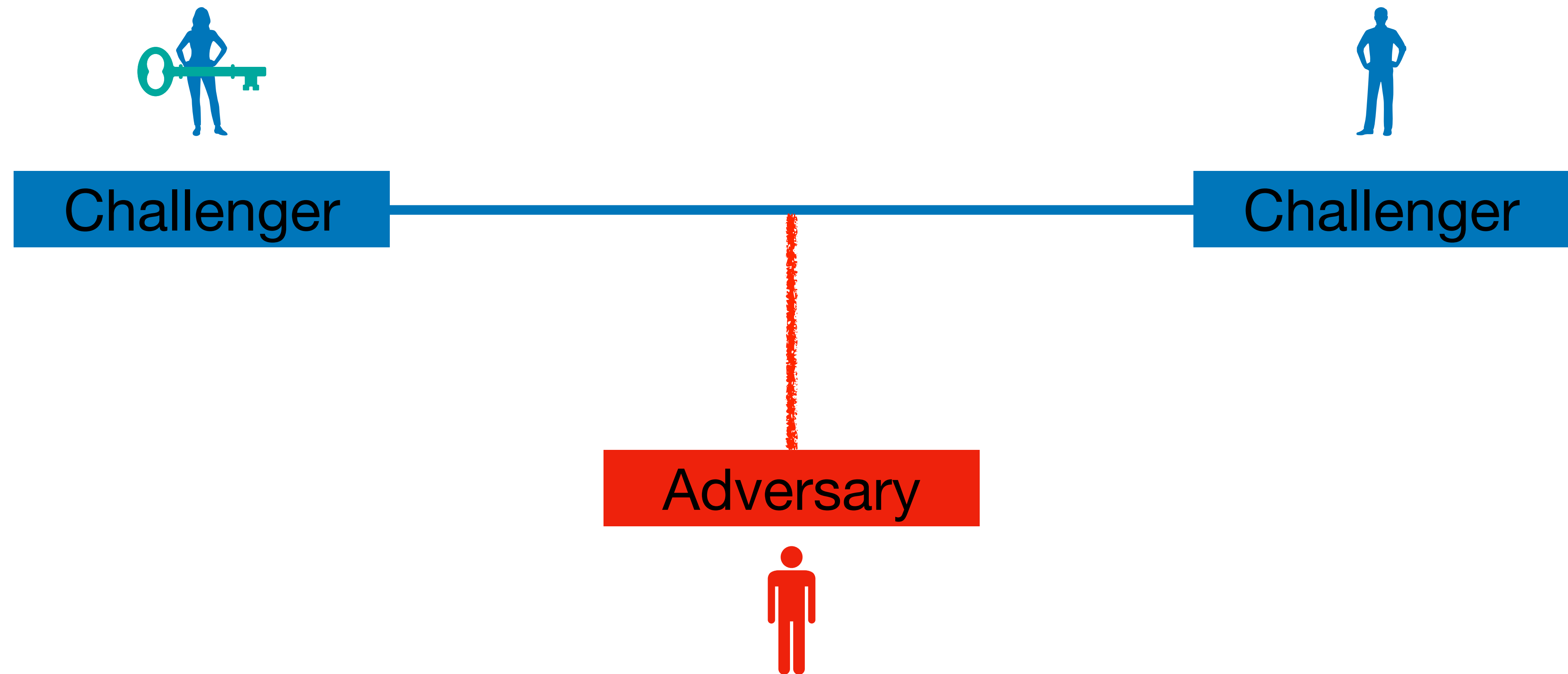
- Does not make sense if **entire secret key and ciphertext** is given to adversary.
- May be possible for adversary to attain the **entire secret key** but store **only a part of the ciphertext**. For example, cloud storage.

Incompressibility

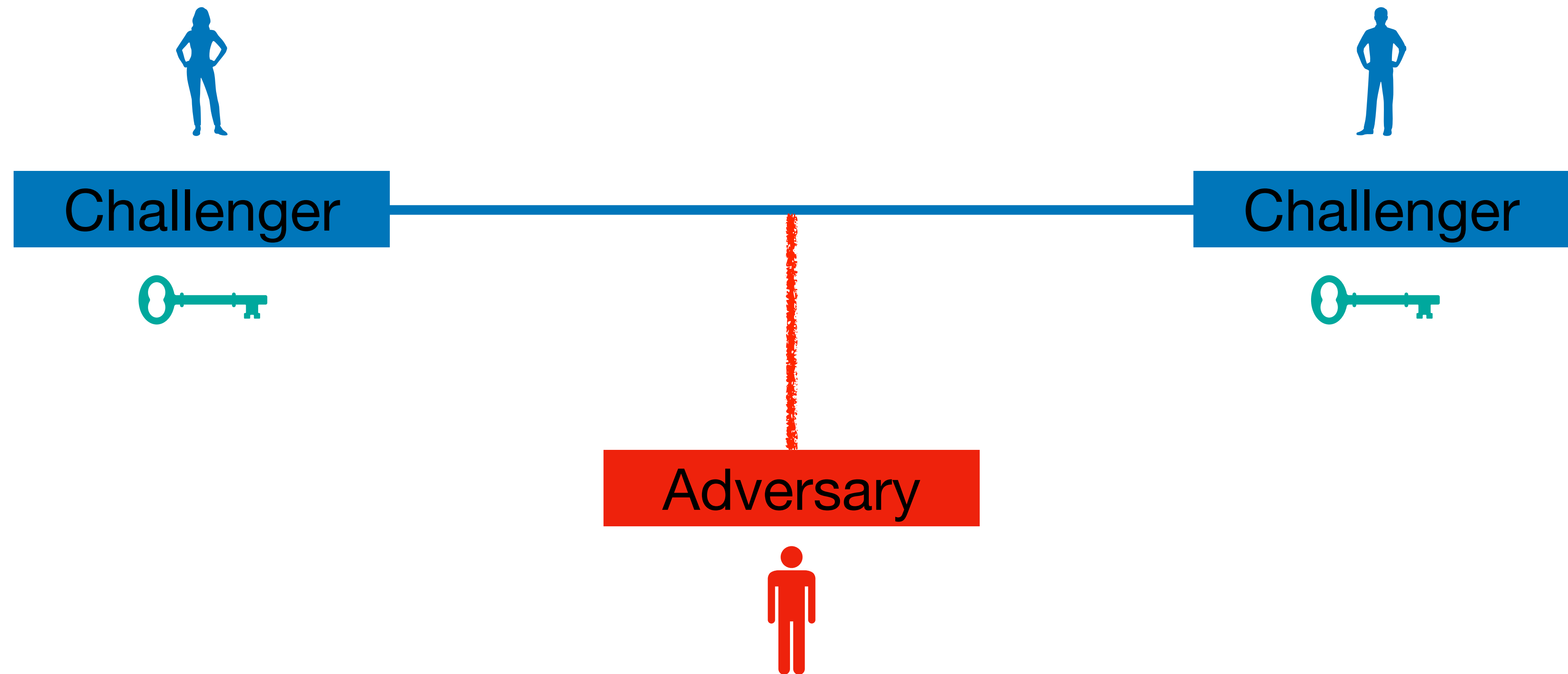
Incompressible Security



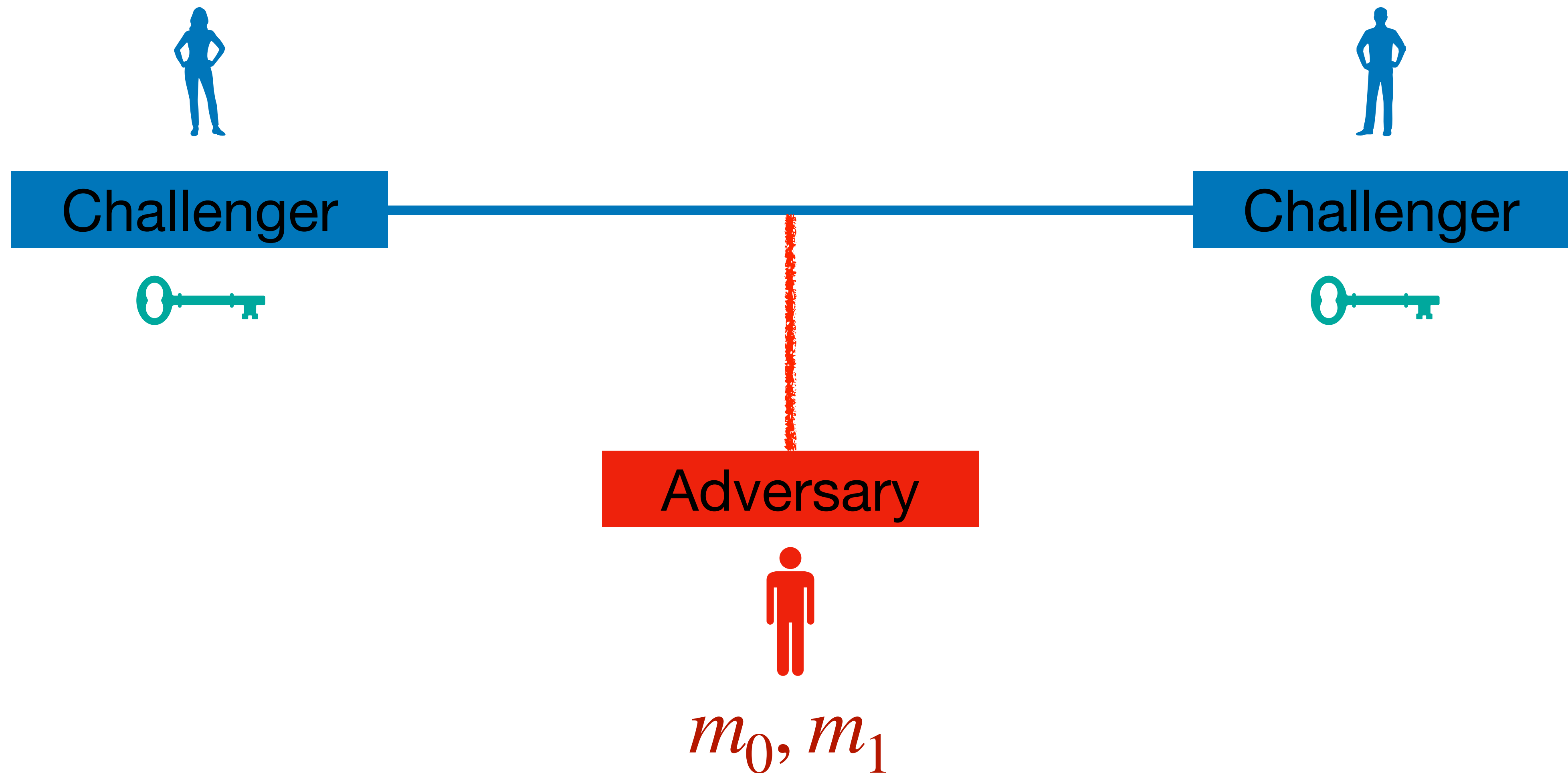
Incompressible Security



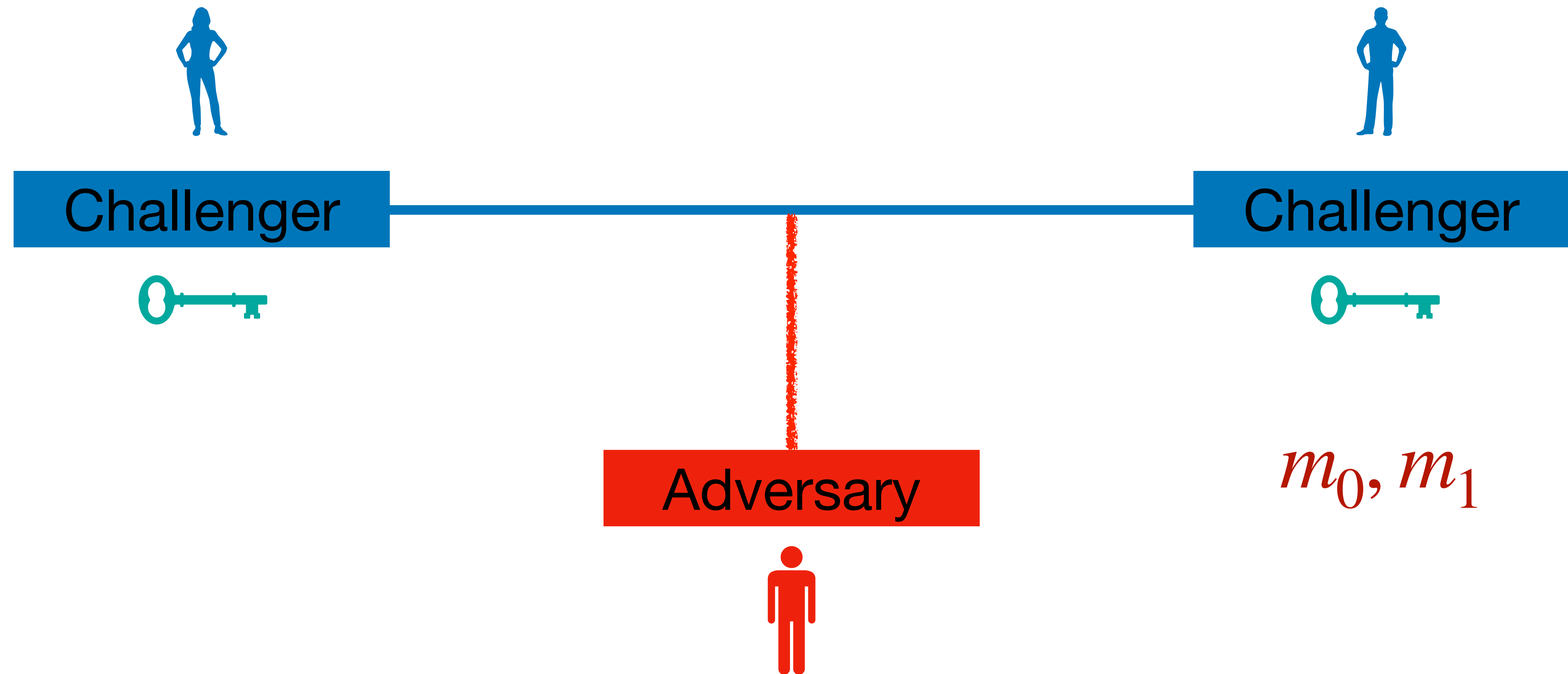
Incompressible Security



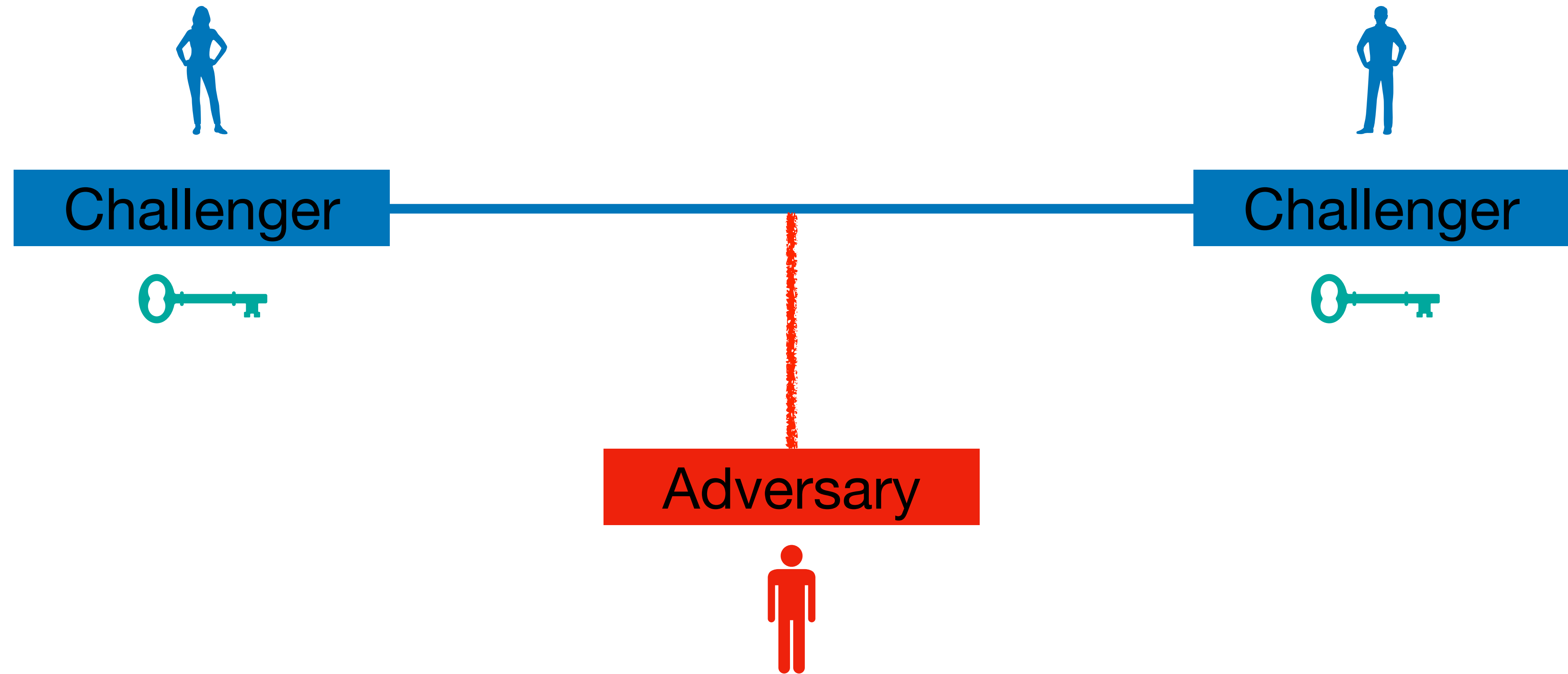
Incompressible Security



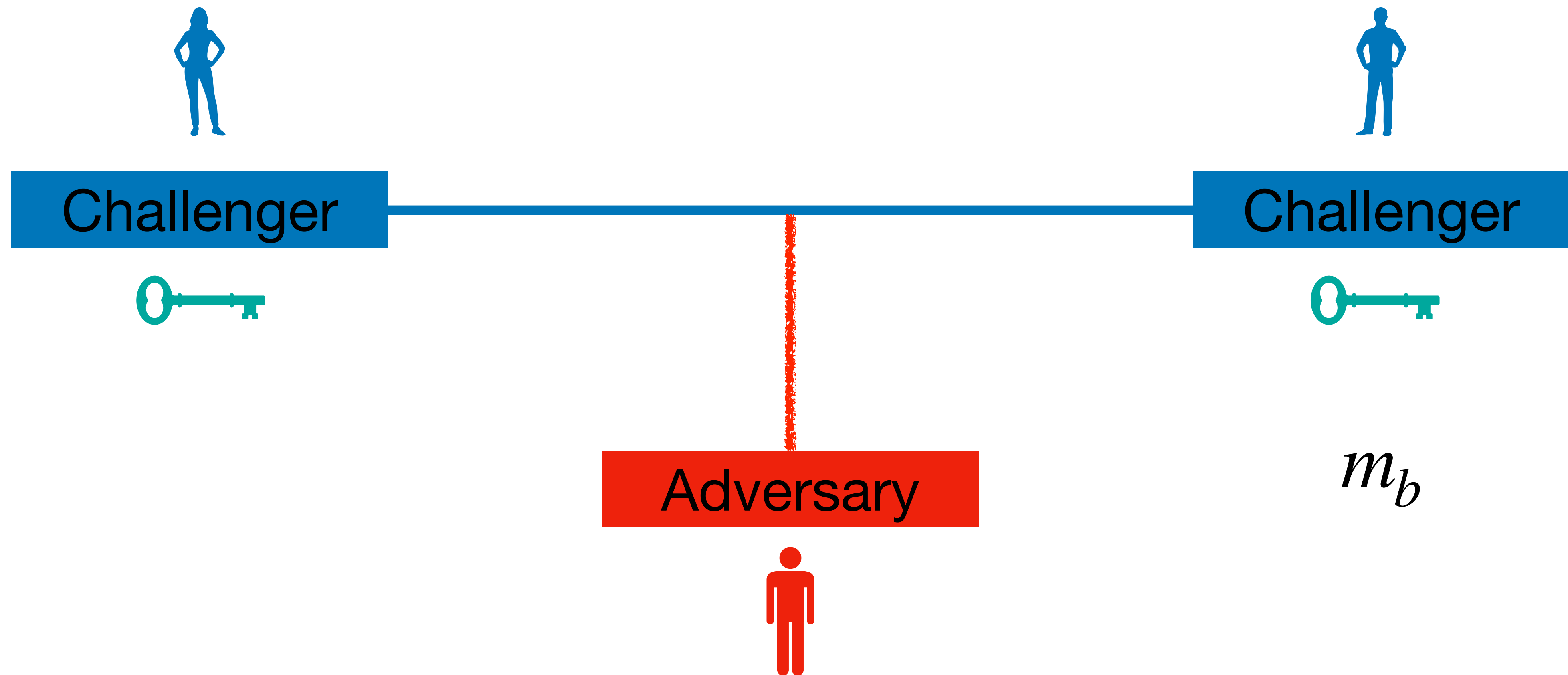
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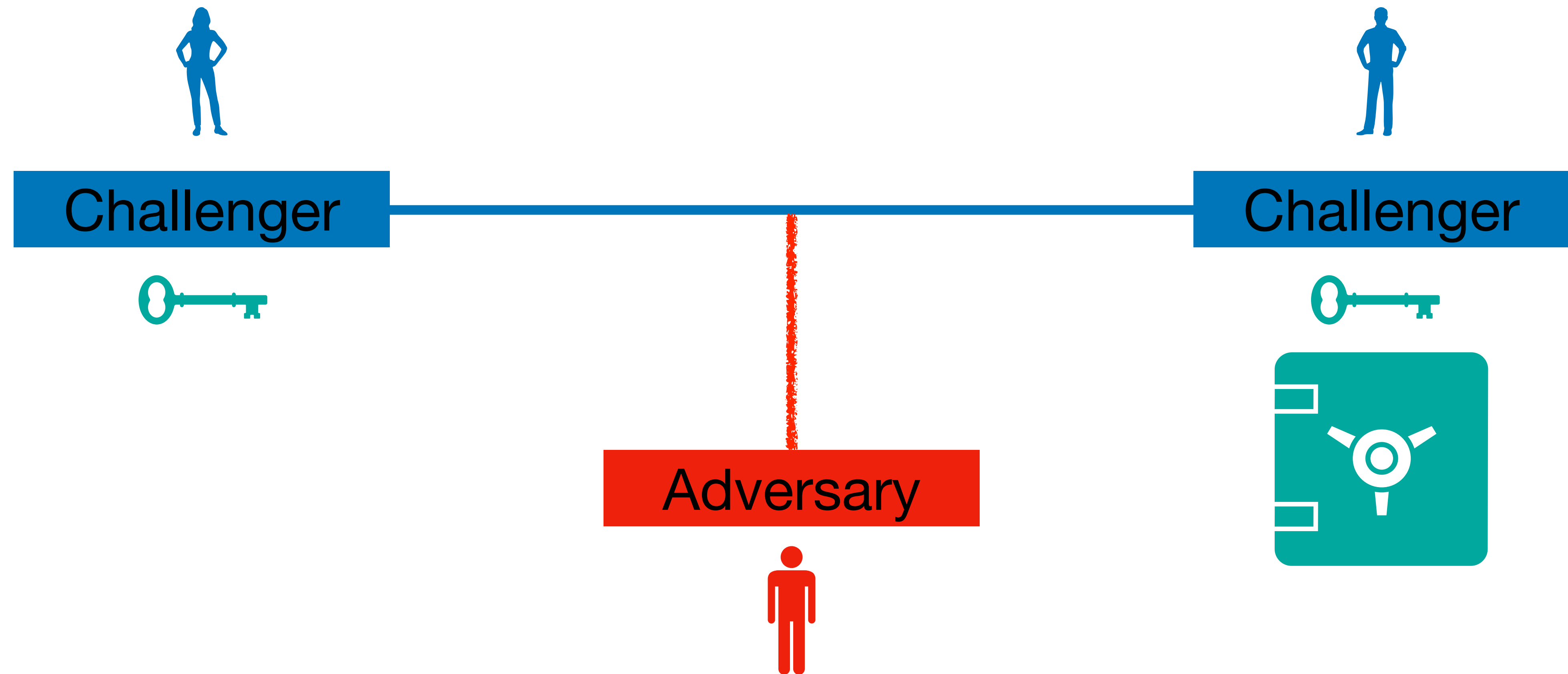
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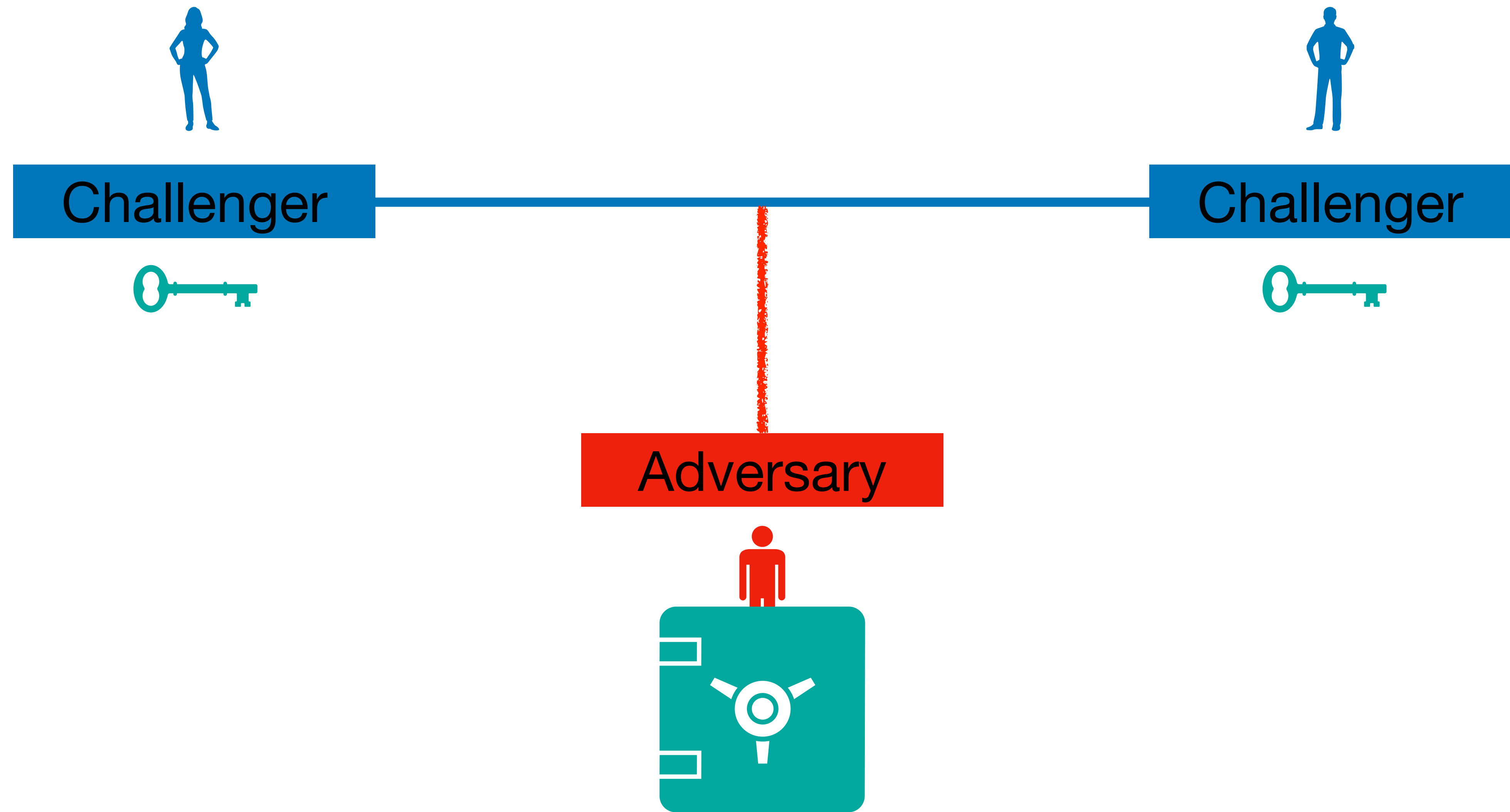
Incompressible Security



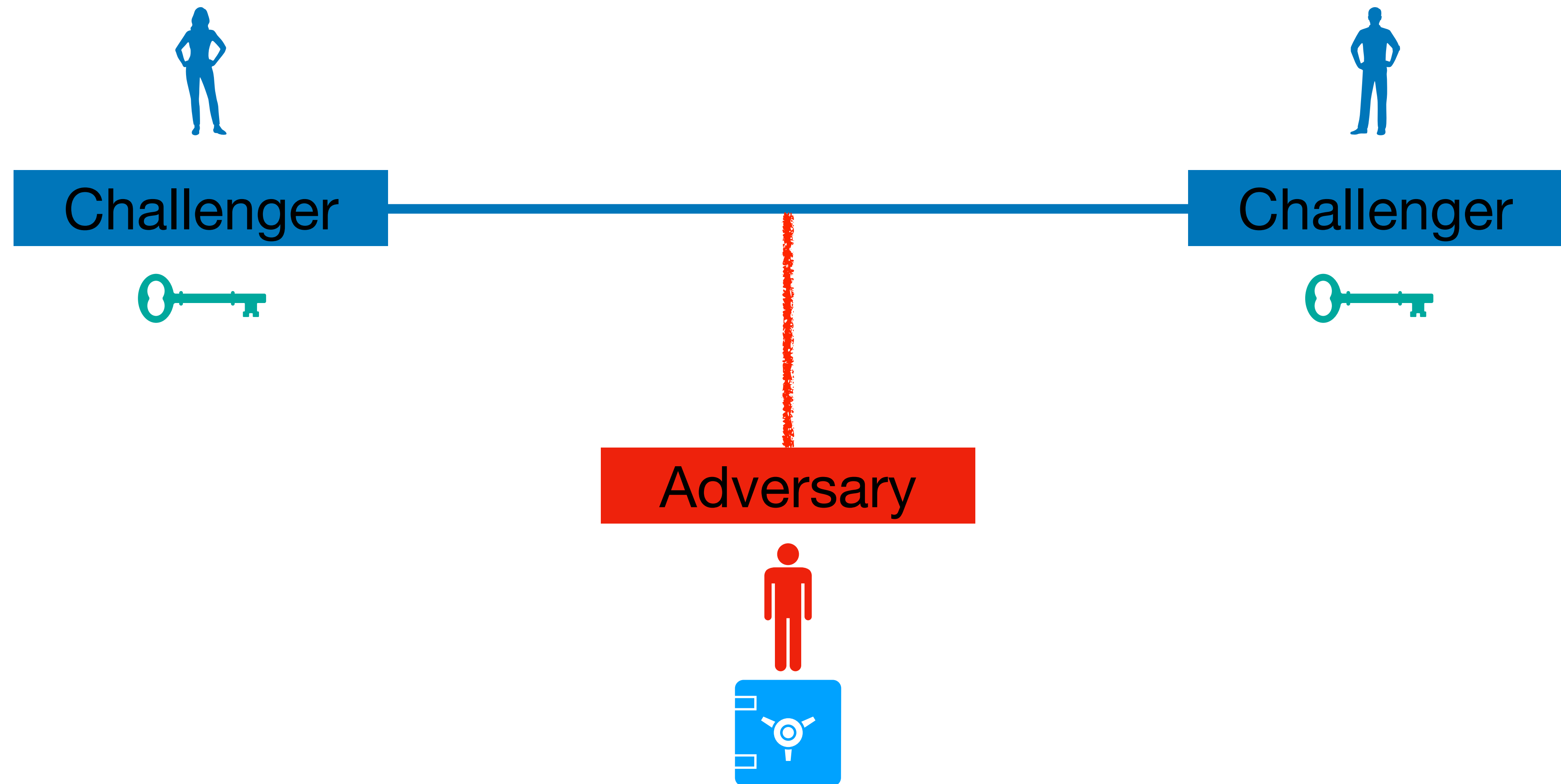
Incompressible Security



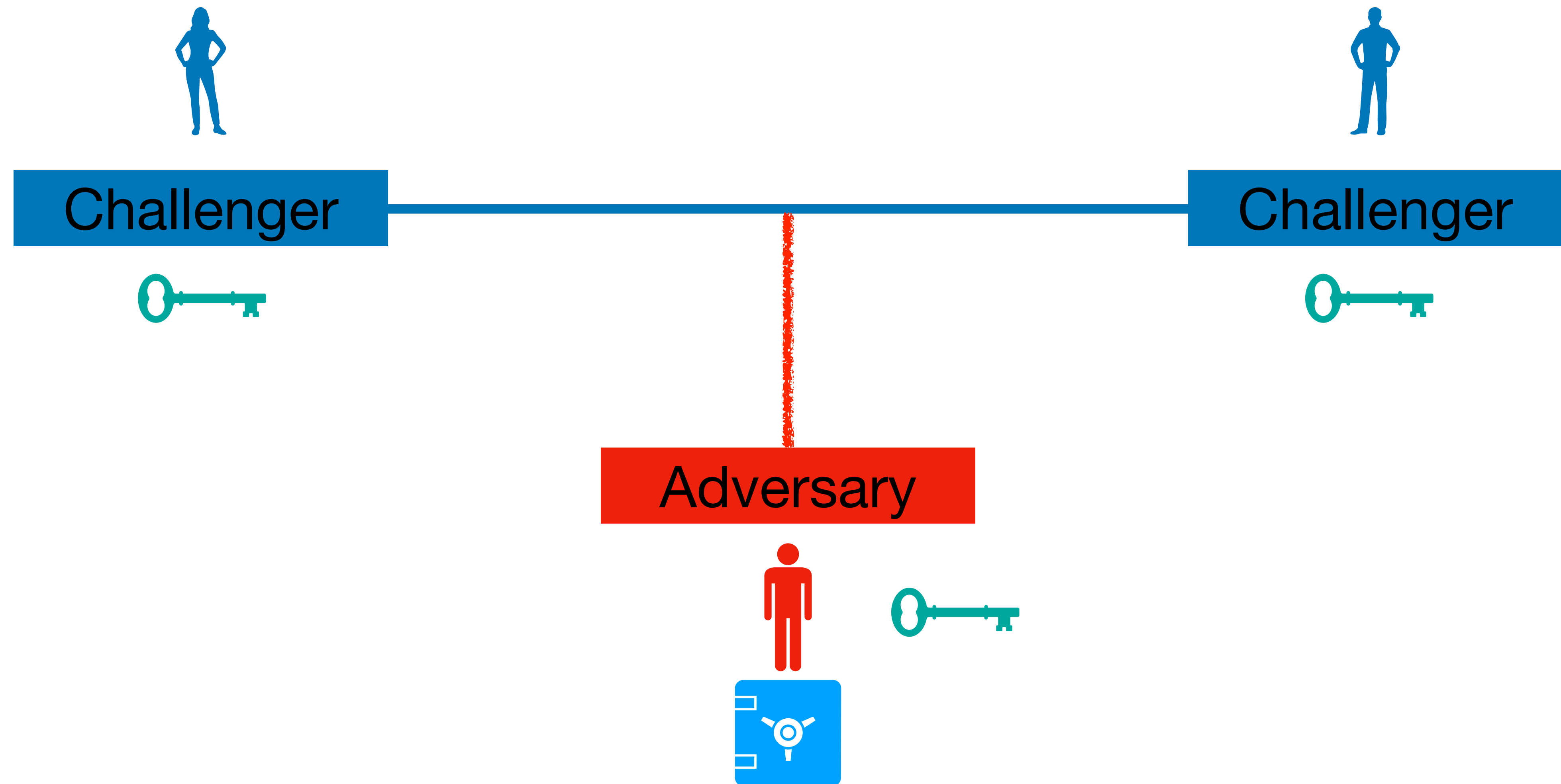
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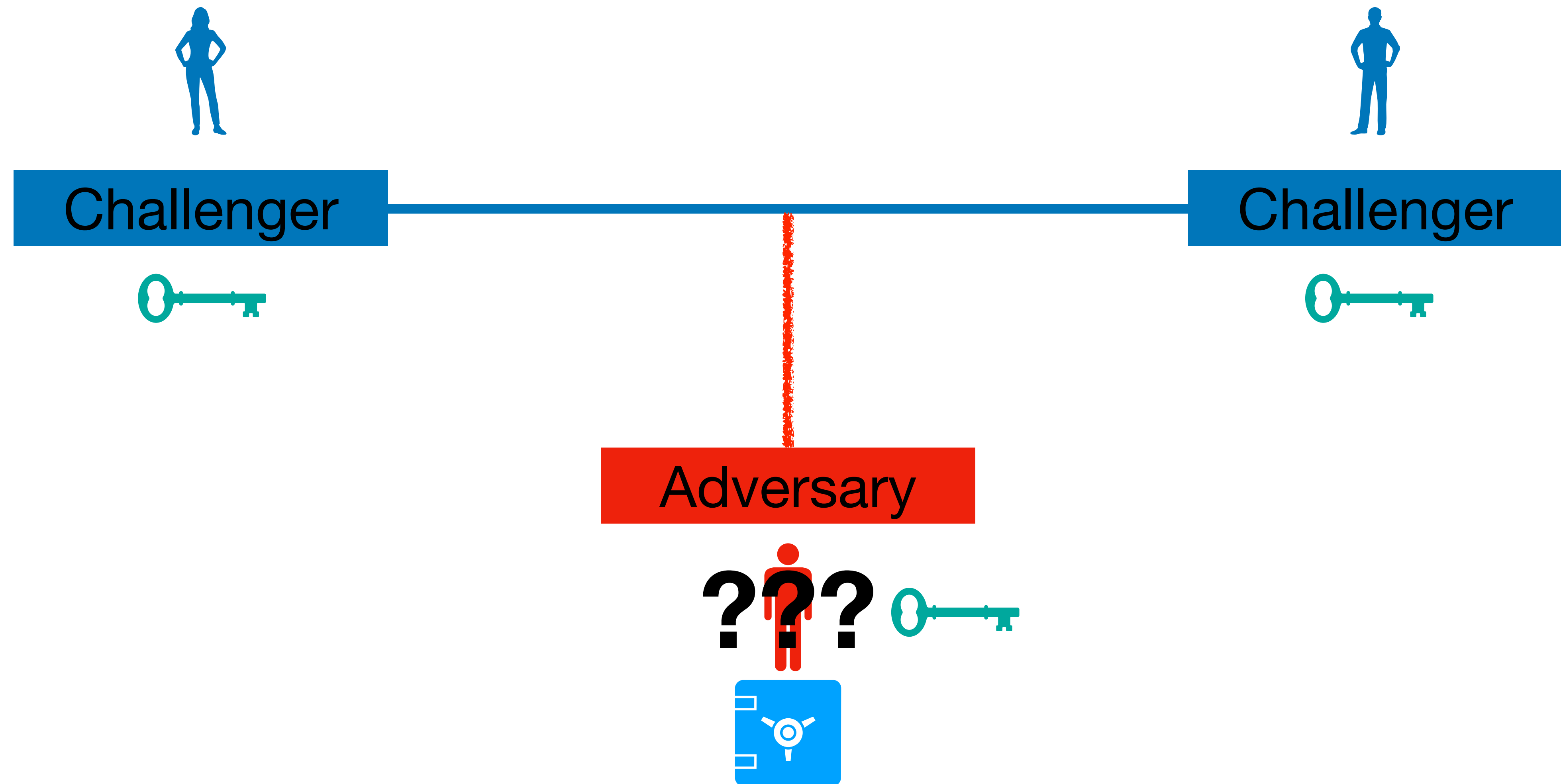
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LR vs Incompressibility

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- Adversary leaks a part of **secret key**.

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LR vs Incompressibility

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LR vs Incompressibility

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Incompressible SKE Schemes

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Incompressible SKE Schemes

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- Dziembowski gave the first construction under standard assumptions (bad rate)
- Guan et al. gave a **rate-1** construction based on LWE and DCR (using incompressible encoding)

Dziembowski's Incompressible One-Time Pad

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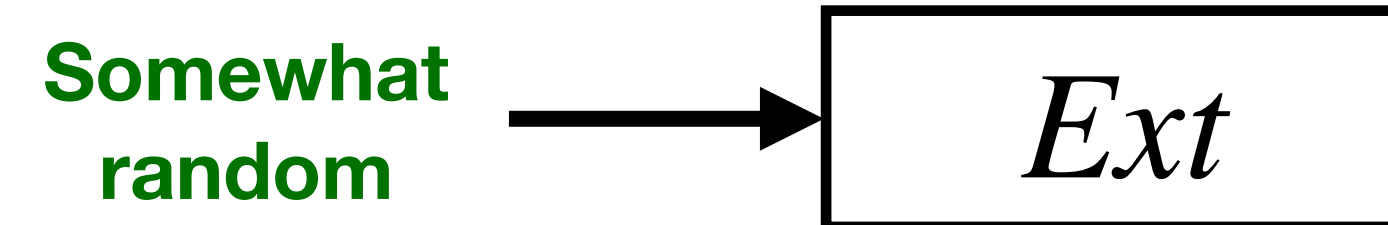
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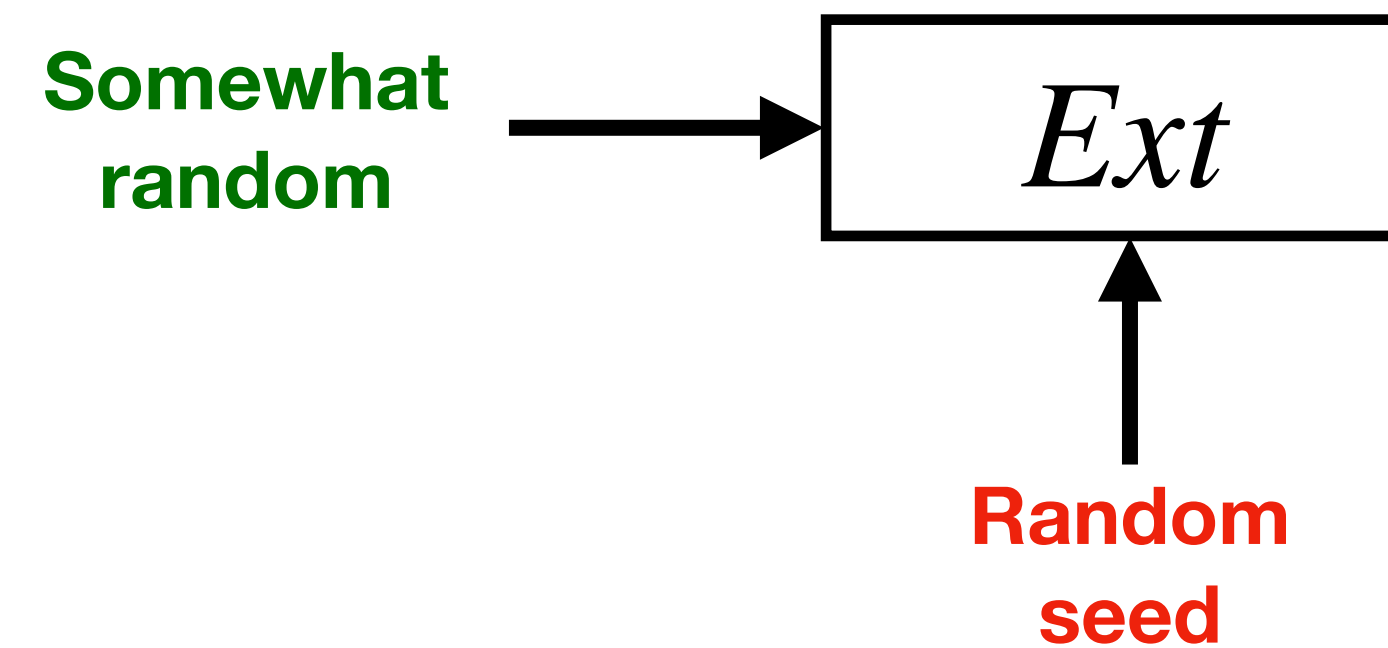
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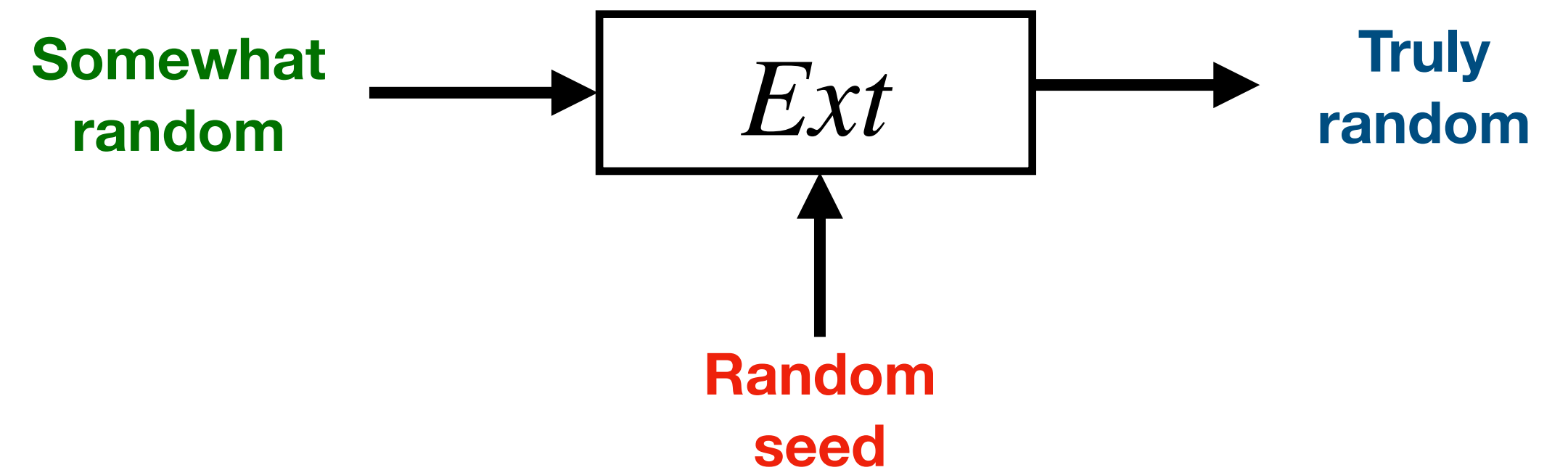
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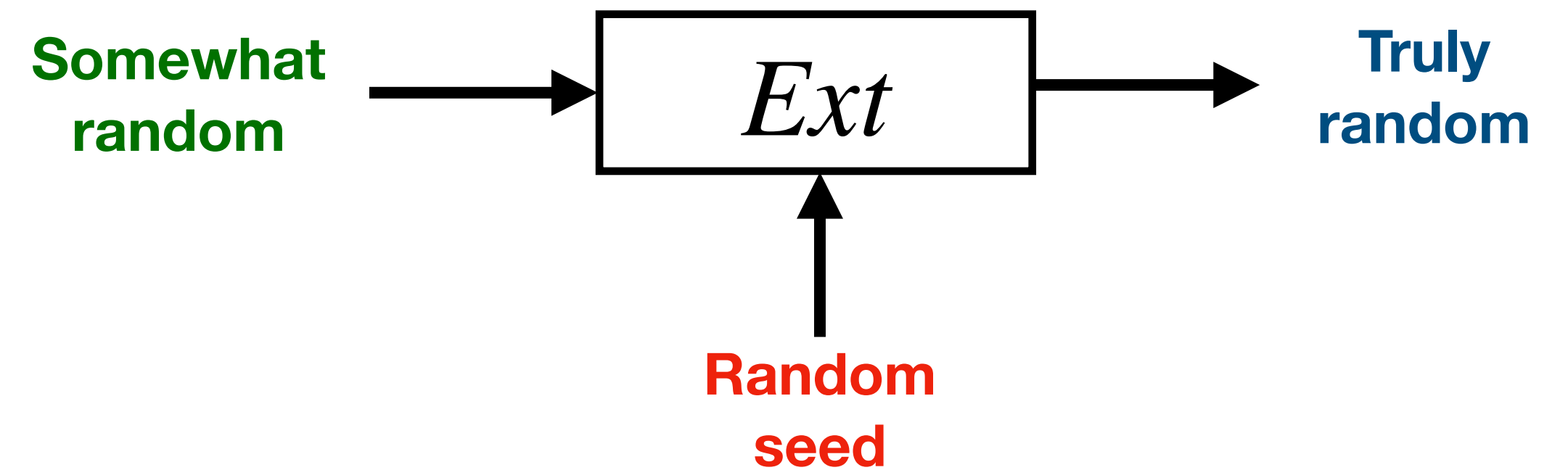
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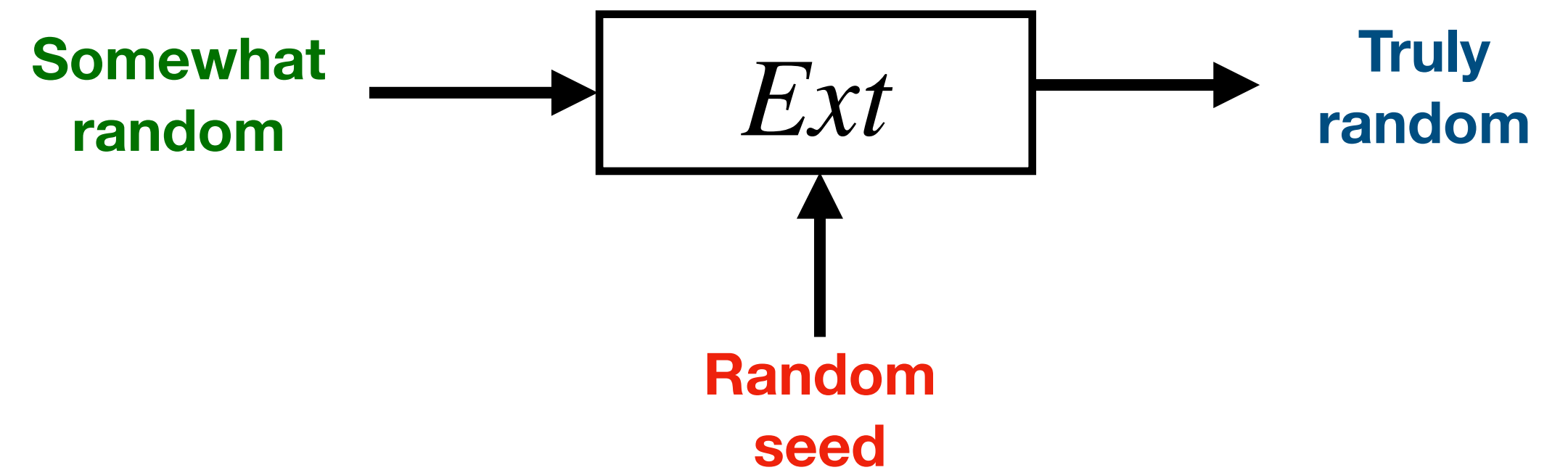


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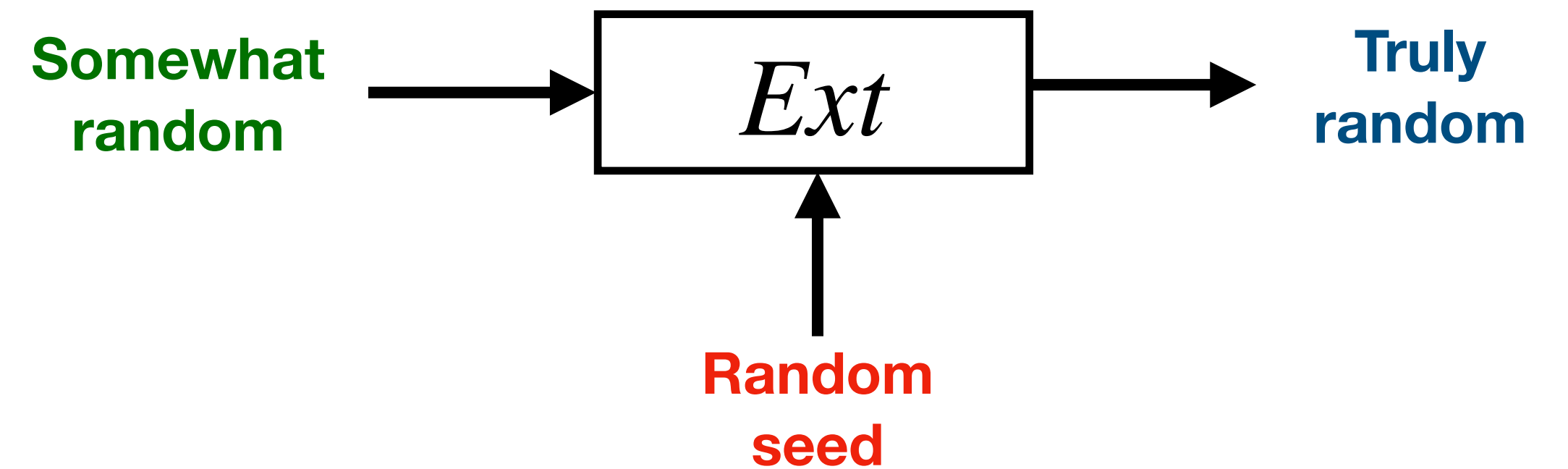
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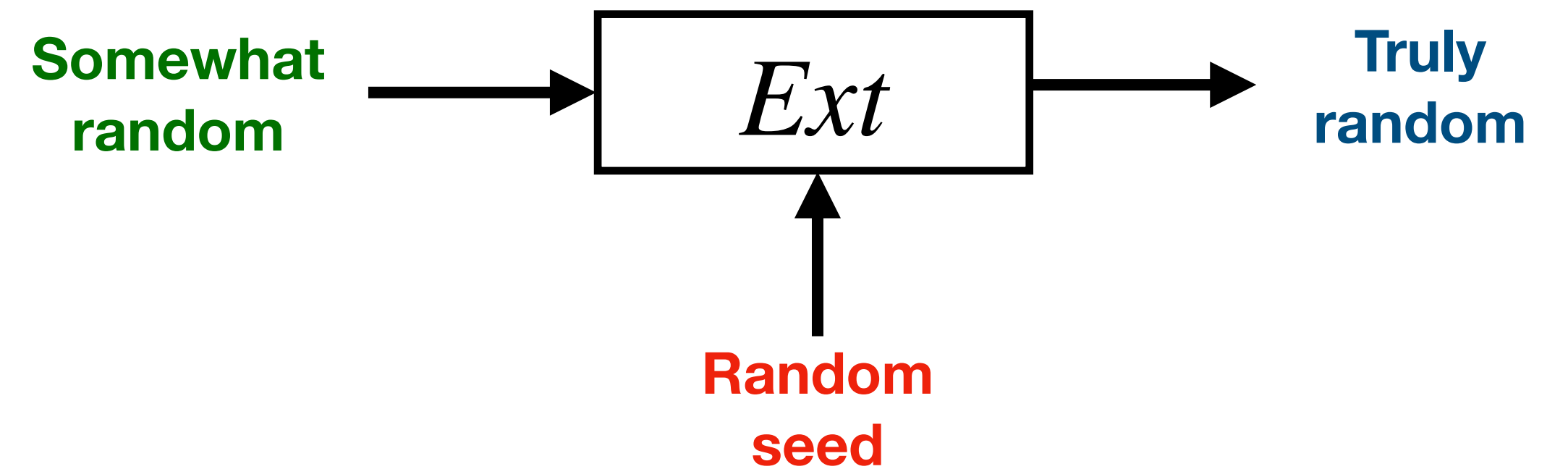
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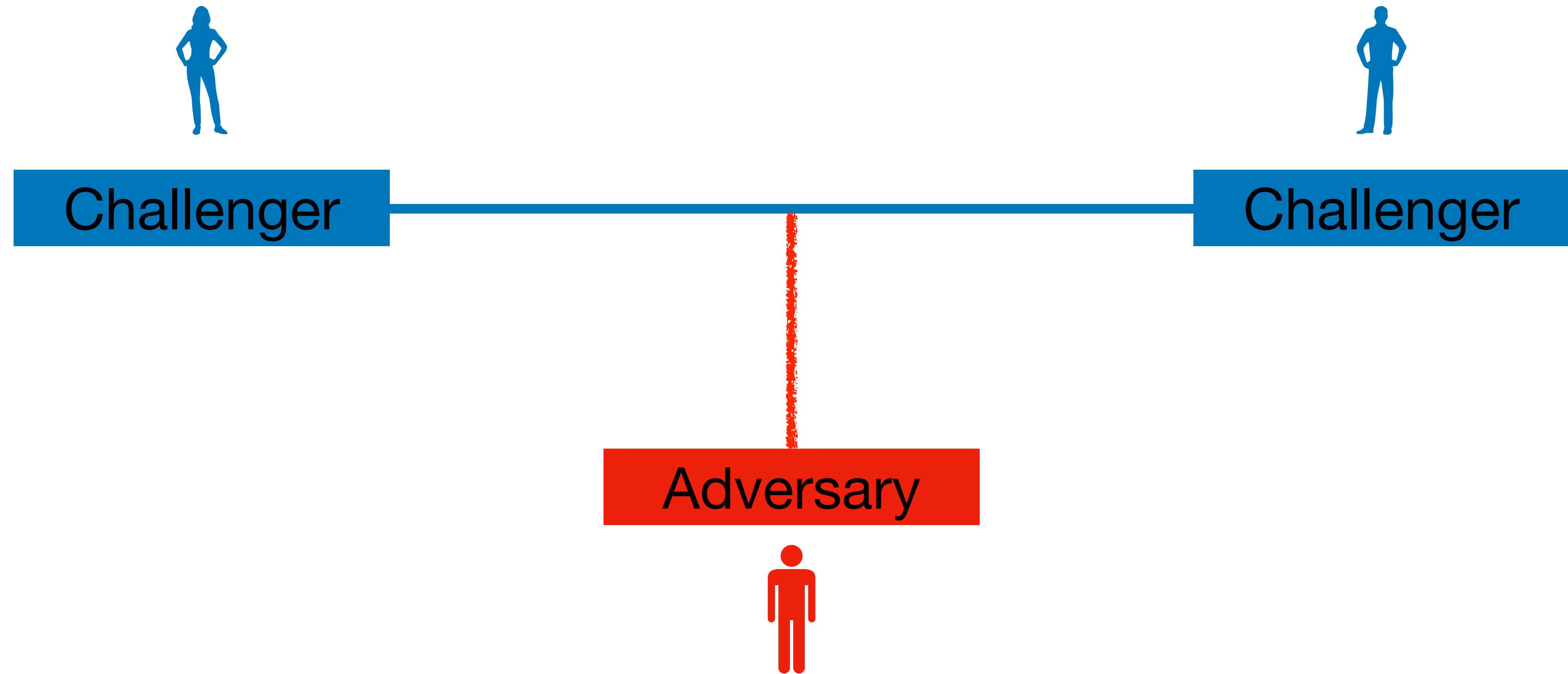
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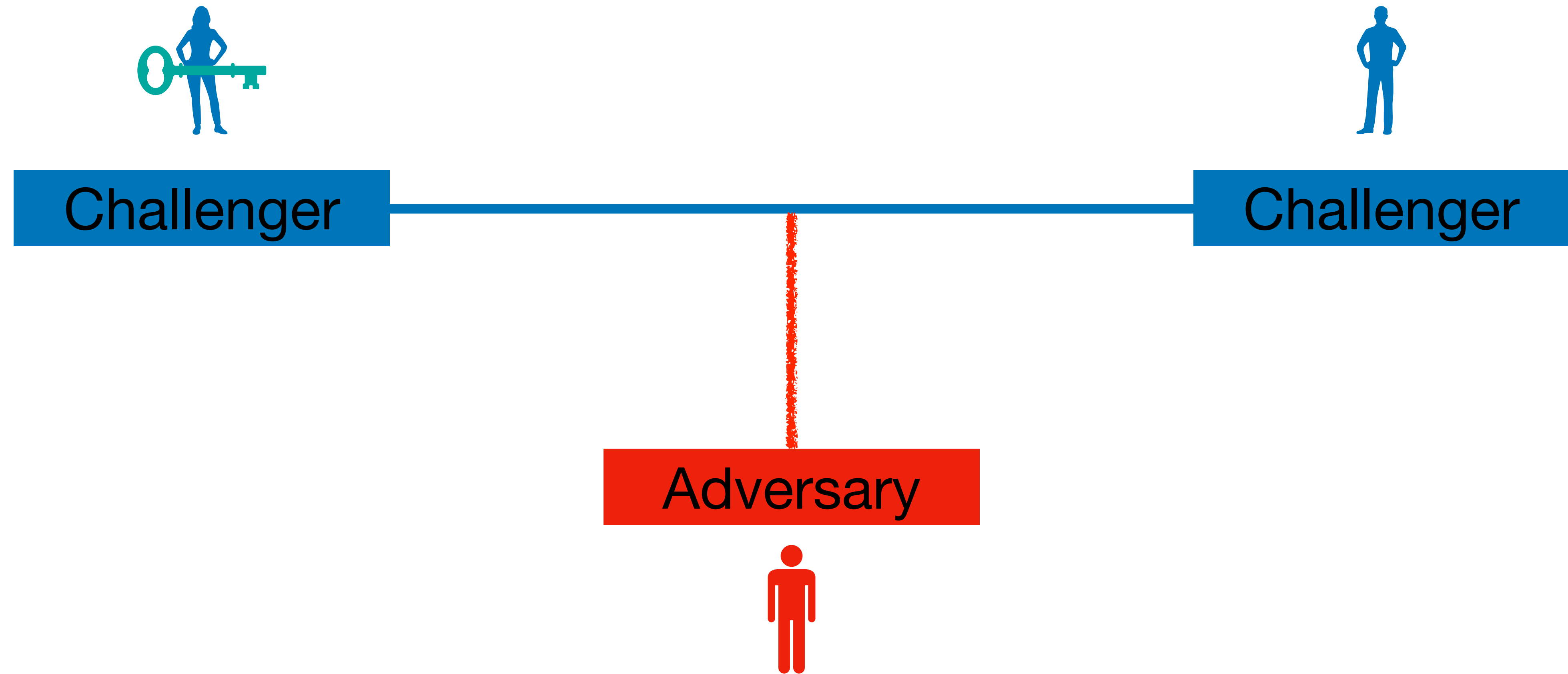
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Leakage-Resilient Incompressibility

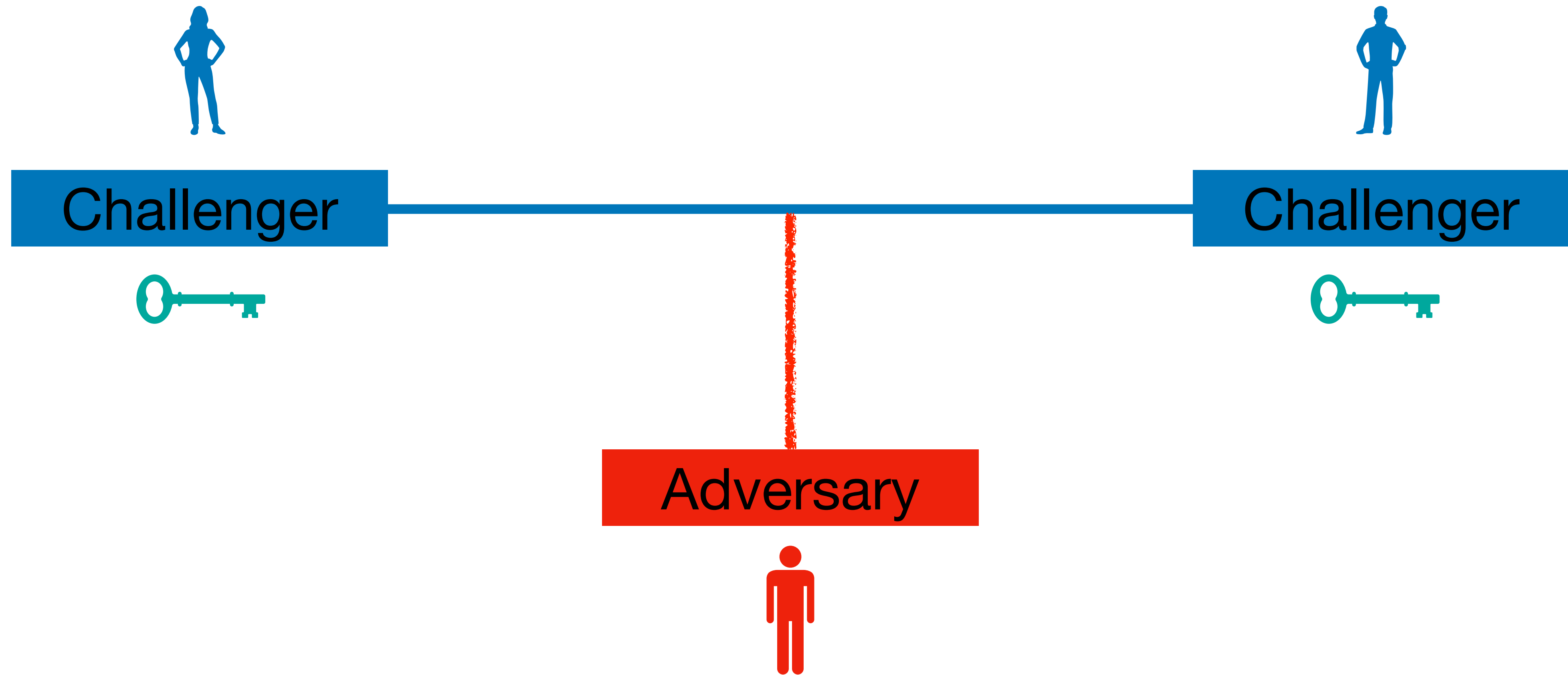
LRI Security



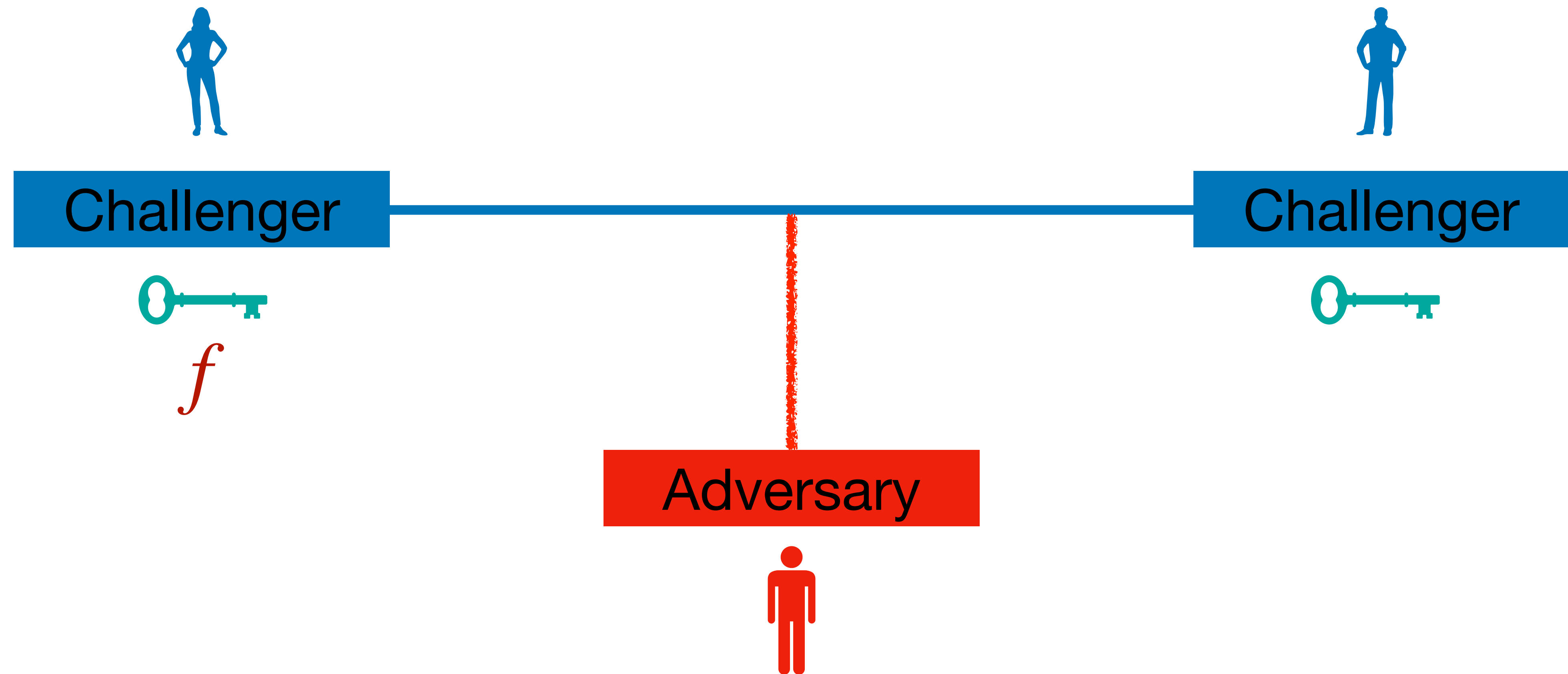
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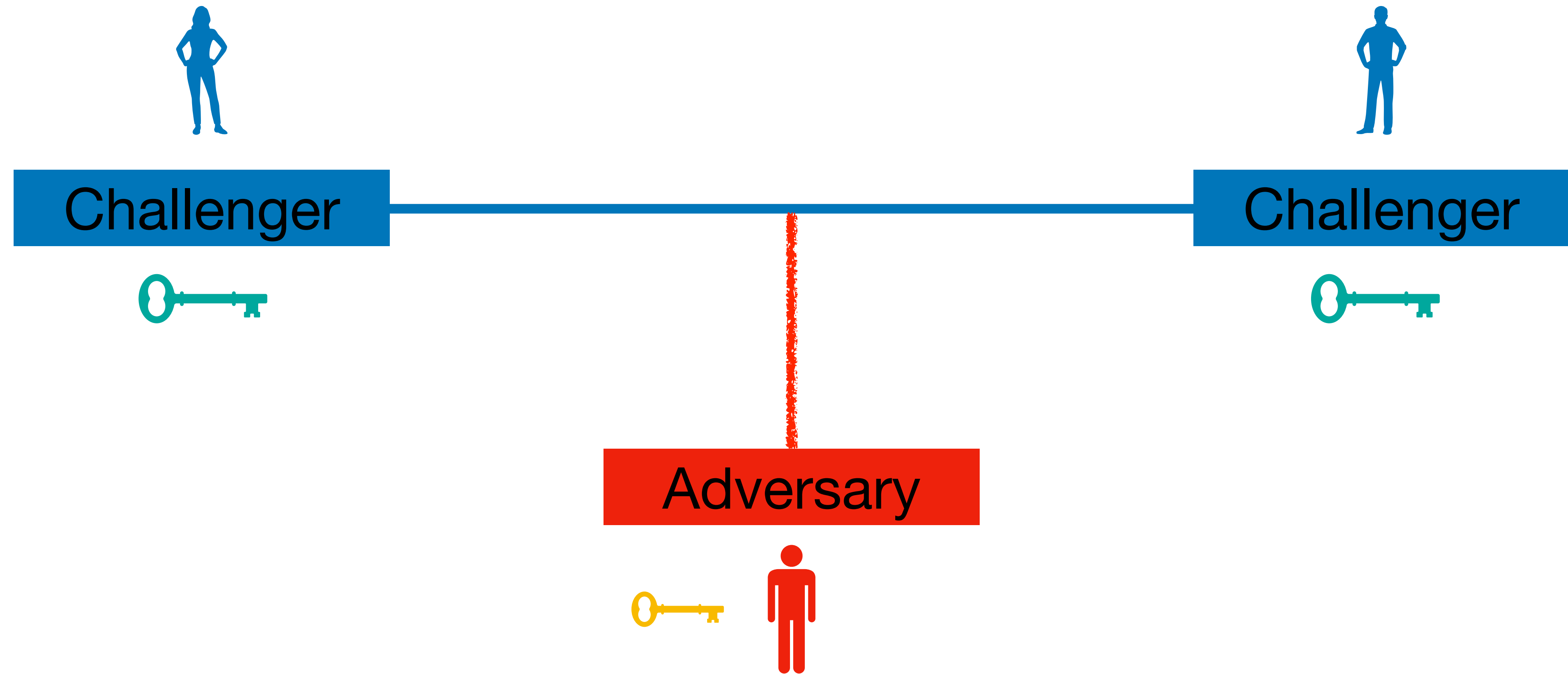
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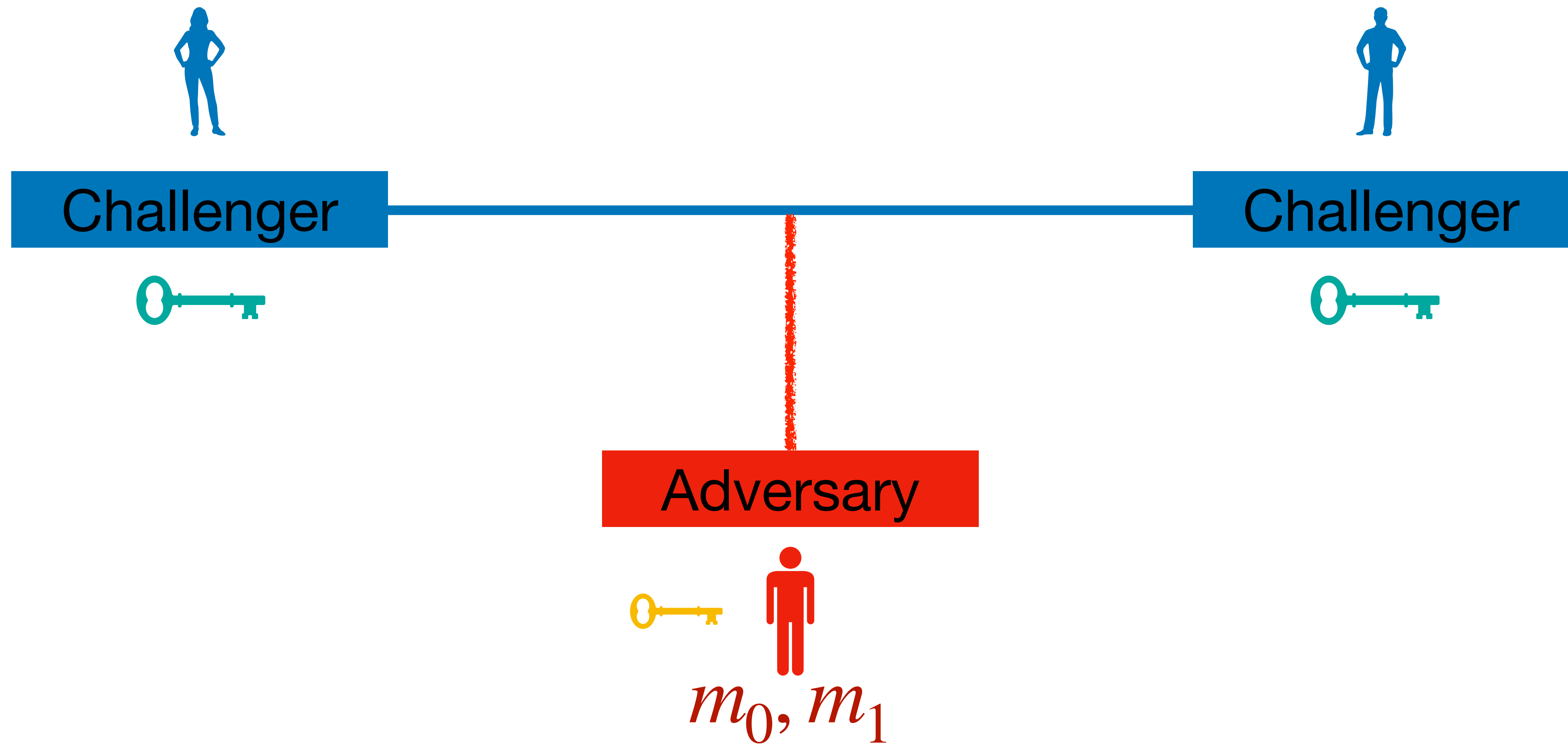
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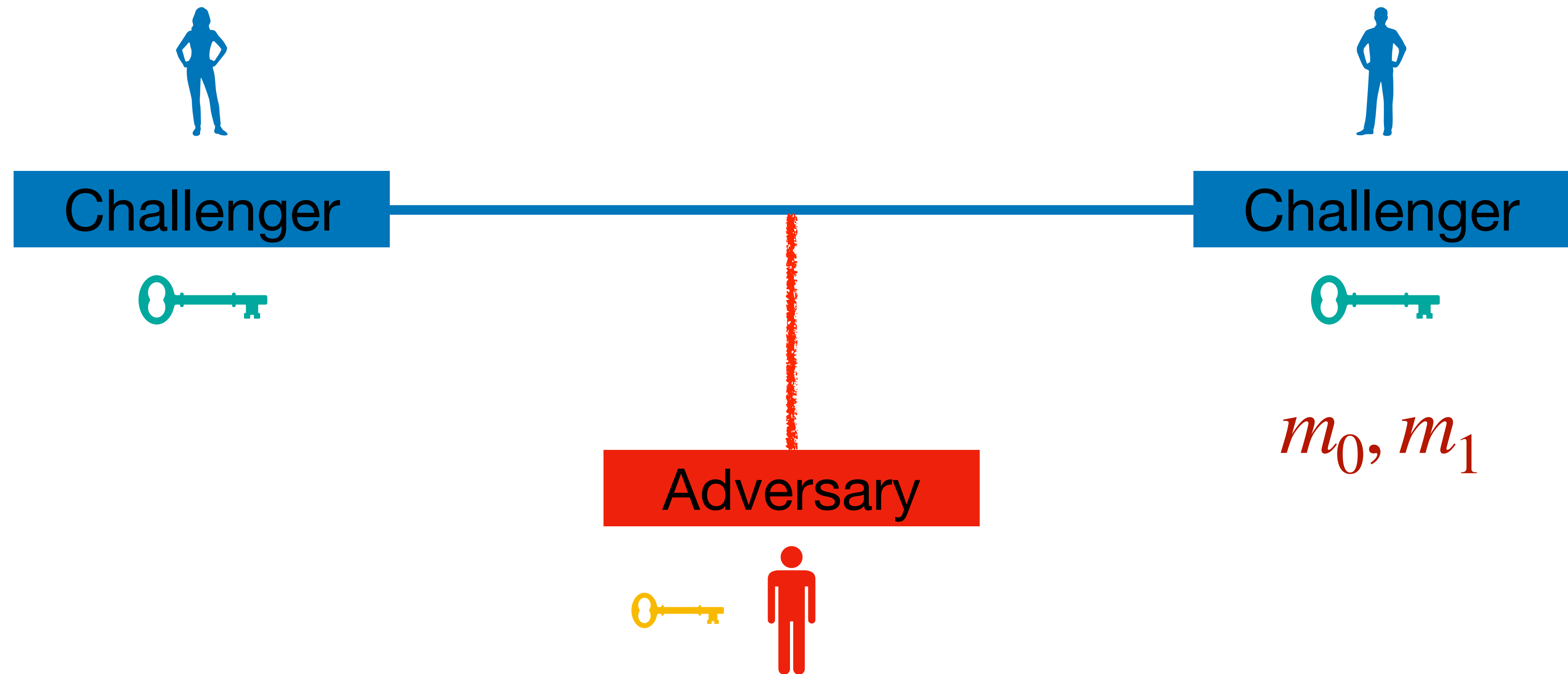
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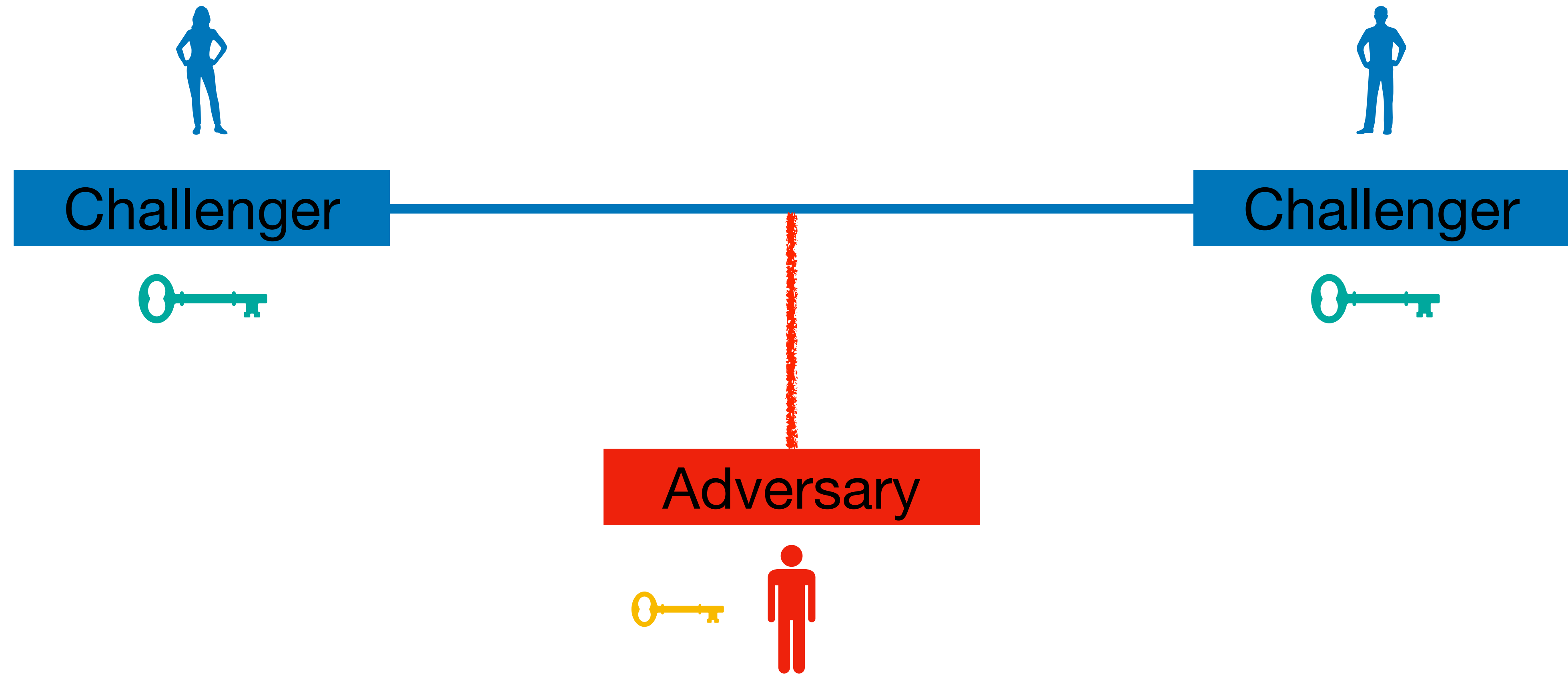
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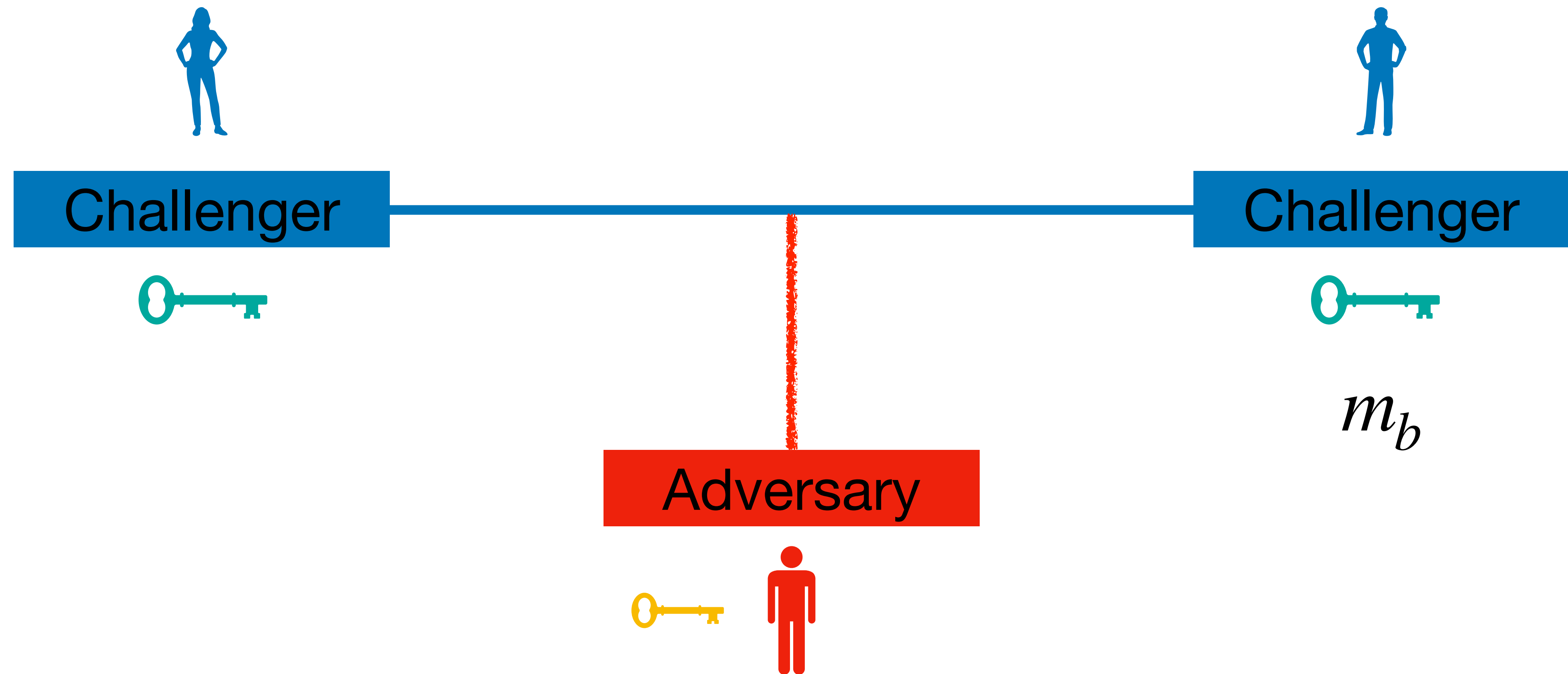
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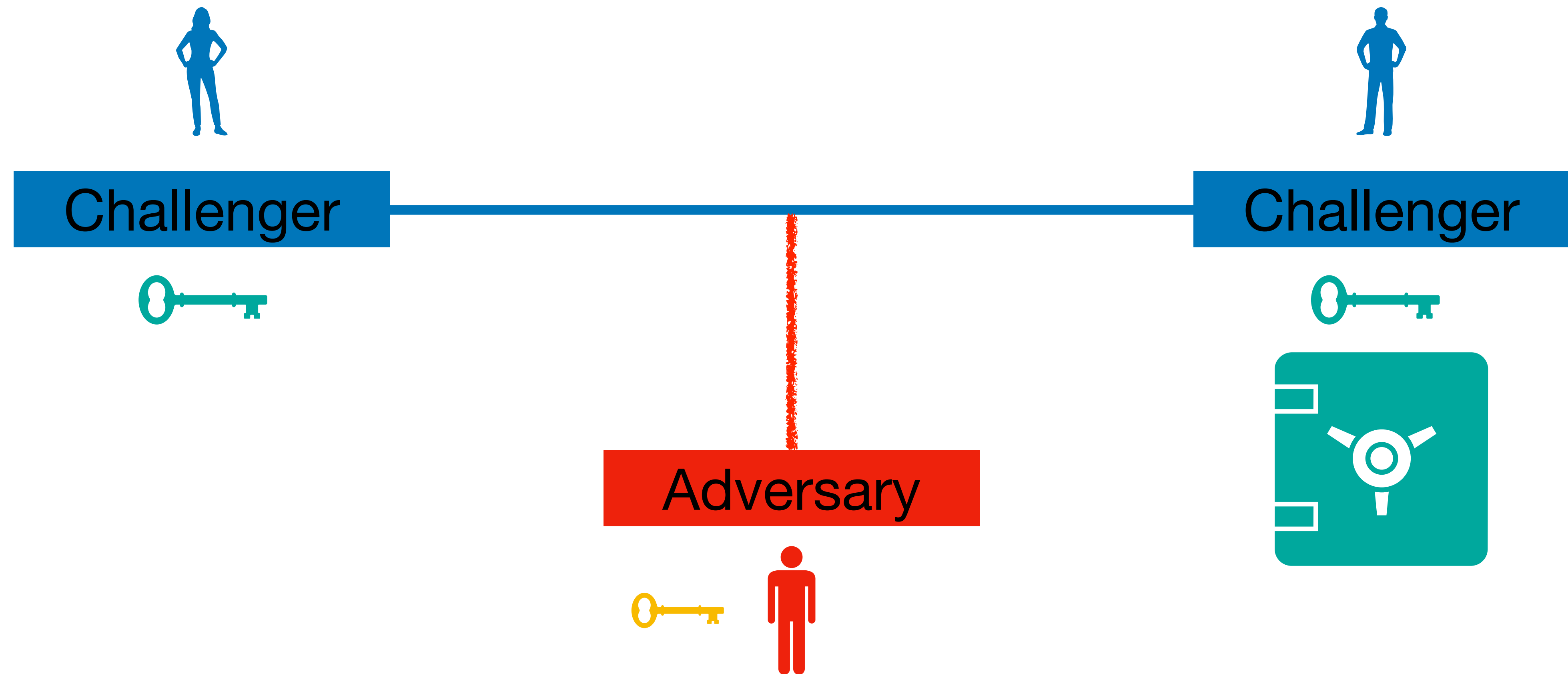
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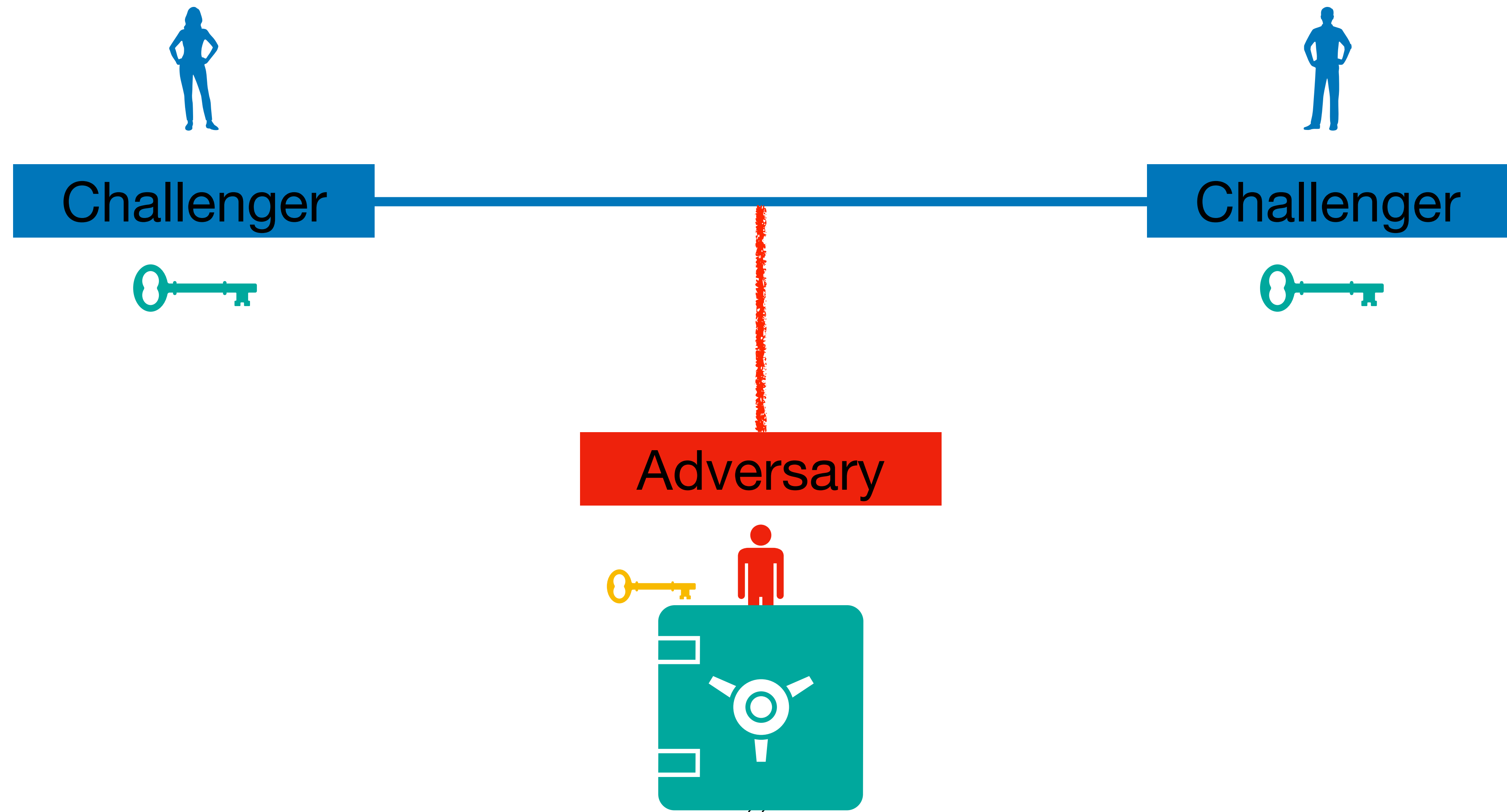
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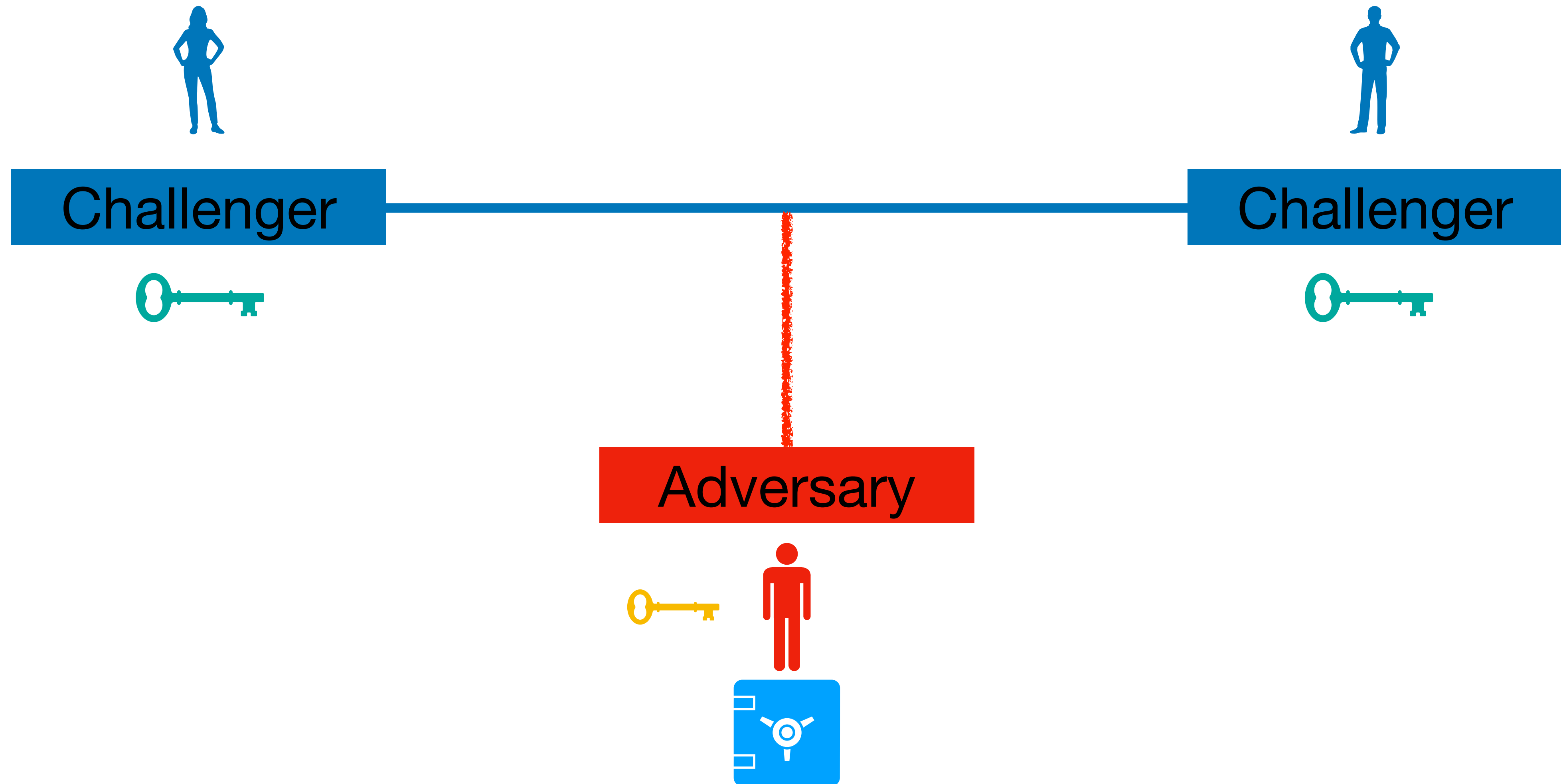
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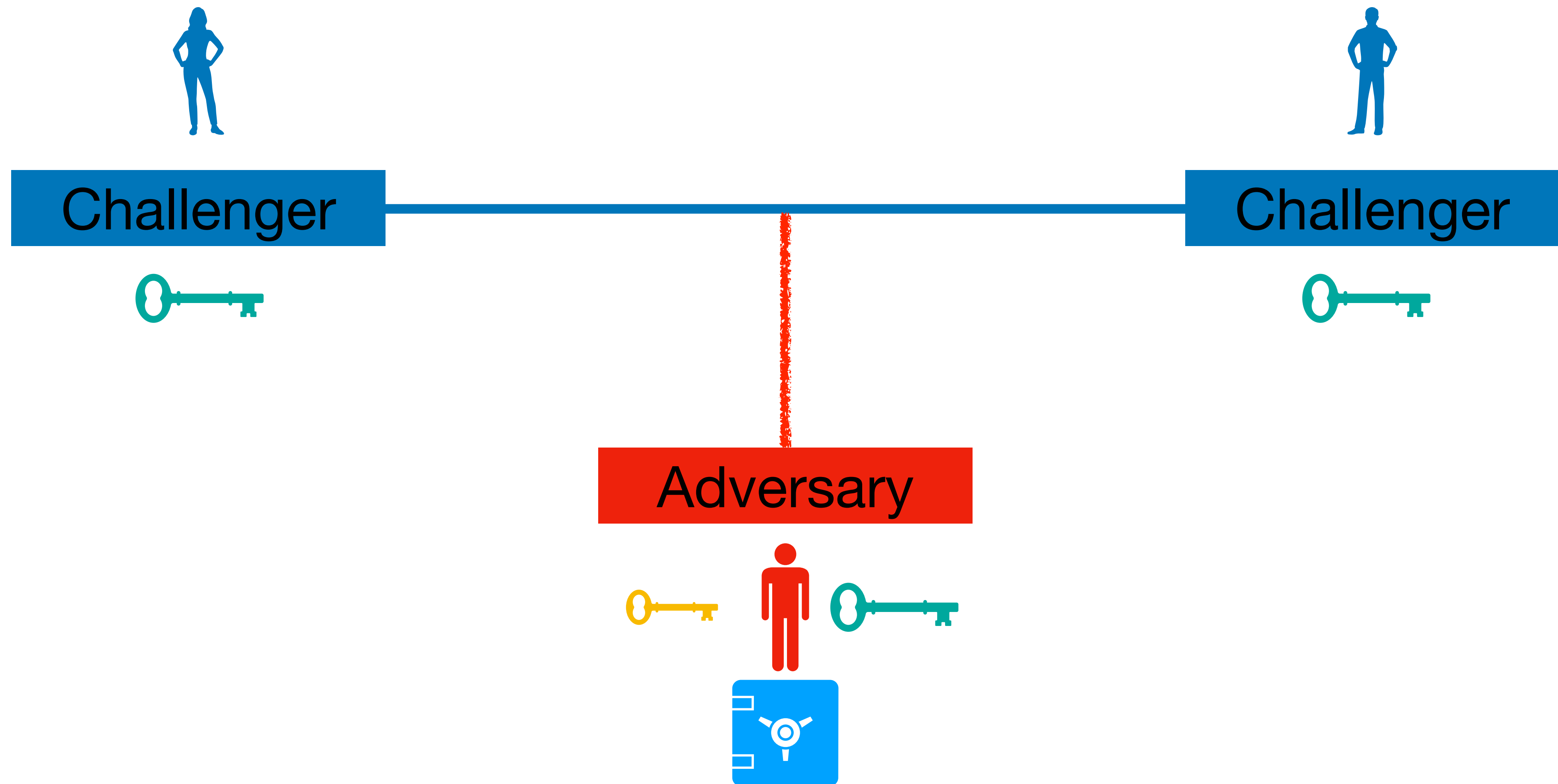
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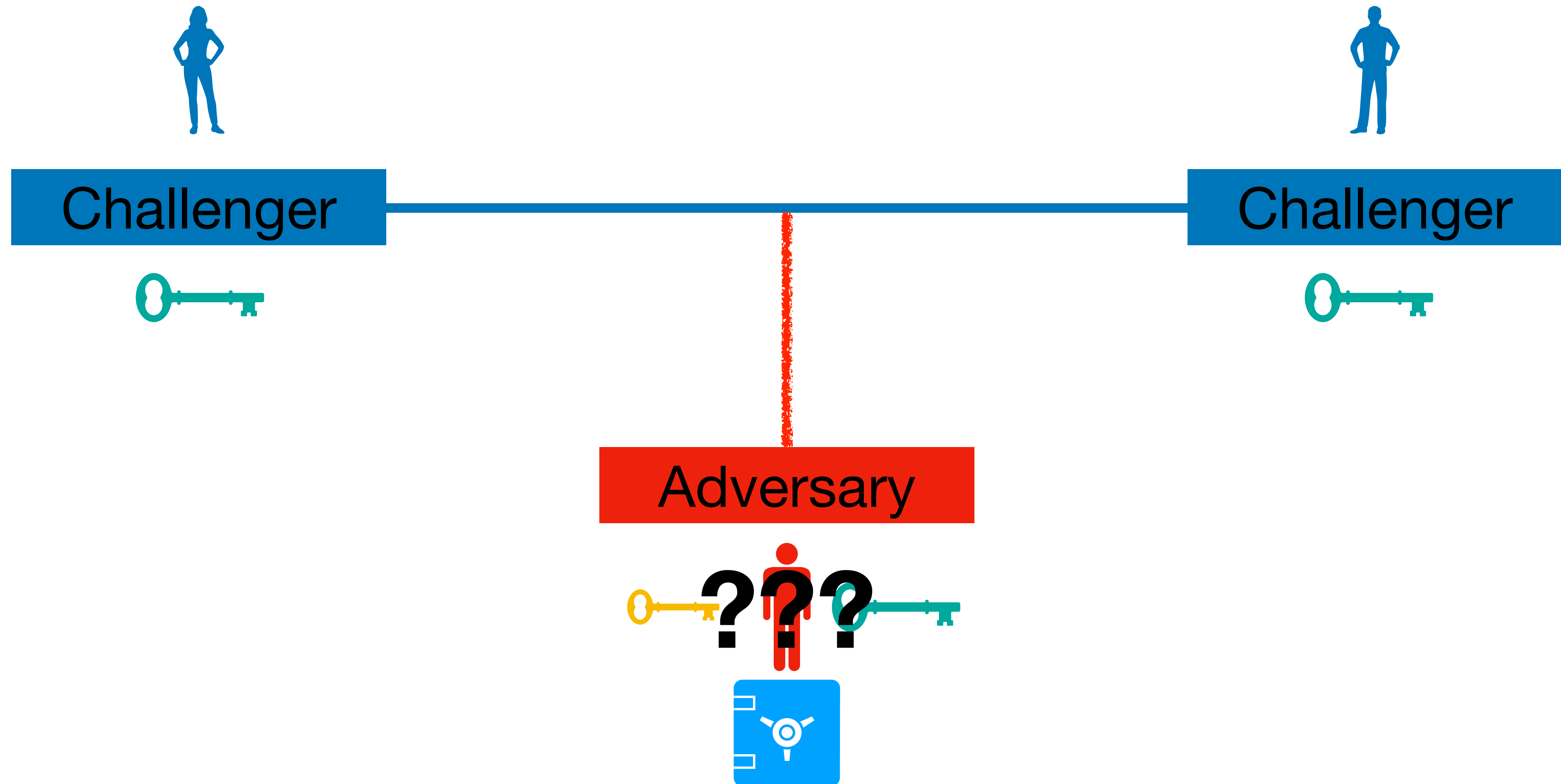
LRI Security



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LRI Security



BGKNPR LRI One-Time Pad

BGKNP^R LRI One-Time Pad

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- $Dec(sk, (c_0, c_1)) \rightarrow$ Run $s = Ext_{c_0}(sk)$ and return $IncompDec(s, c_1)$.

BGKNP **R** Results

BGKNP^R Results

- Transformation from LRI SKE + PKE to LRI PKE using garbling techniques.

BGKNP_R Results

- Transformation from LRI SKE + PKE to LRI PKE using garbling techniques.
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- **Impossibility** of building provably secure **Incomp SKE/PKE** with **small keys** and **small ciphertexts**.

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- **Impossibility** of building provably secure **Incomp SKE/PKE** with **small keys** and **small ciphertexts**.
- **Impossibility** of building provably secure **LRI SKE/PKE** with **large secret key leakage** and **small cipher texts**.

Incompressible Functional Encryption

(Public Key) Identity Based Encryption

(Public Key) Identity Based Encryption



(Public Key) Identity Based Encryption



(Public Key) Identity Based Encryption



sk_A



(Public Key) Identity Based Encryption



sk_A



pk_A

(Public Key) Identity Based Encryption



sk_A



pk_A
 sk_B

(Public Key) Identity Based Encryption



sk_A
 pk_B



pk_A
 sk_B

(Public Key) Identity Based Encryption



sk_A
 pk_B



pk_A
 sk_B



(Public Key) Identity Based Encryption



sk_A
 pk_B



pk_A
 sk_B



pk_A
 pk_B

(Public Key) Identity Based Encryption



sk_A
 pk_B



pk_A
 sk_B



pk_A
 pk_B
 sk_C

(Public Key) Identity Based Encryption



sk_A
 pk_B
 pk_C



pk_A
 sk_B
 pk_C



pk_A
 pk_B
 sk_C

(Public Key) Identity Based Encryption



sk_A
 pk_B
 pk_C



pk_A
 sk_B
 pk_C

In a system of n users, if a new user joins, it needs to perform $2n$ communications.

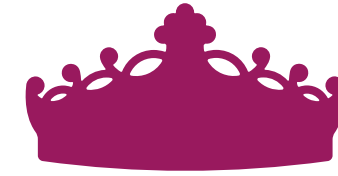


pk_A
 pk_B
 sk_C

Identity Based Encryption (IBE)



Identity Based Encryption (IBE)



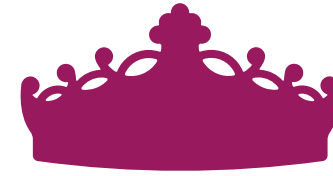
Identity Based Encryption (IBE)



mpk



Identity Based Encryption (IBE)



mpk

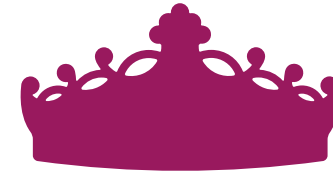


mpk



mpk

Identity Based Encryption (IBE)



sk_E



mpk

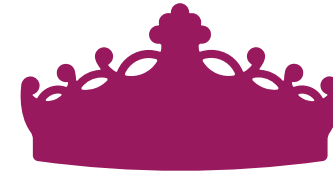


mpk



mpk

Identity Based Encryption (IBE)



mpk
 sk_A



mpk
 sk_B



mpk
 sk_C

Identity Based Encryption (IBE)



mpk
 sk_A

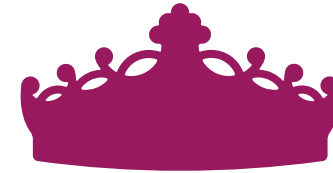


mpk
 sk_B



mpk
 sk_C

Identity Based Encryption (IBE)



mpk
 sk_A

$$ct_A = Enc(mp_k, B, message_A)$$

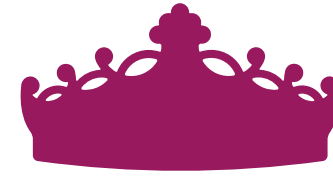


mpk
 sk_B



mpk
 sk_C

Identity Based Encryption (IBE)



mpk
 sk_A



$$ct_A = Enc(mp_k, B, message_A)$$

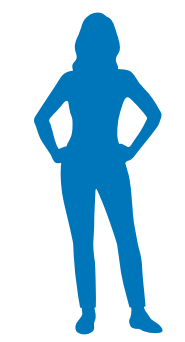
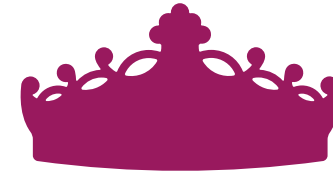


mpk
 sk_B



mpk
 sk_C

Identity Based Encryption (IBE)



mpk
 sk_A



$$ct_A = Enc(mp_k, B, message_A)$$

$$message_A = Dec(sk_B, ct_A)$$

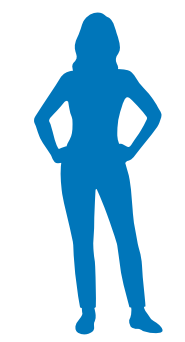


mpk
 sk_B



mpk
 sk_C

Identity Based Encryption (IBE)



mpk
 sk_A



$$ct_A = \text{Enc}(mpk, B, \text{message}_A)$$

$$\text{message}_A = \text{Dec}(sk_B, ct_A)$$



mpk
 sk_B



mpk
 sk_D



mpk
 sk_C

Identity Based Encryption (IBE)



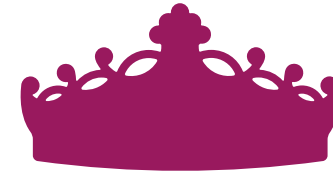
mpk
 sk_D



mpk
 sk_C

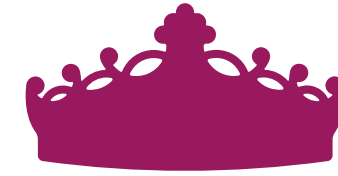
In a system of n users, if a new user joins, it needs to perform 2 communications.

Functional Encryption (FE)



mpk

Functional Encryption (FE)



mpk



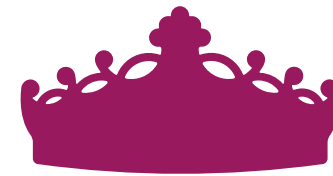
Functional Encryption (FE)



mpk



Functional Encryption (FE)



mpk



mpk

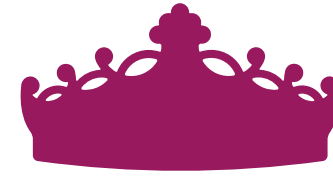


mpk



mpk

Functional Encryption (FE)



mpk
 sk_{f_E}



mpk

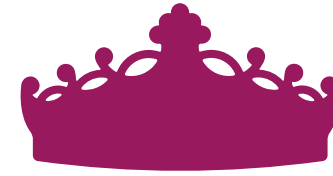


mpk



mpk

Functional Encryption (FE)



mpk



mpk

sk_{f_A}



mpk

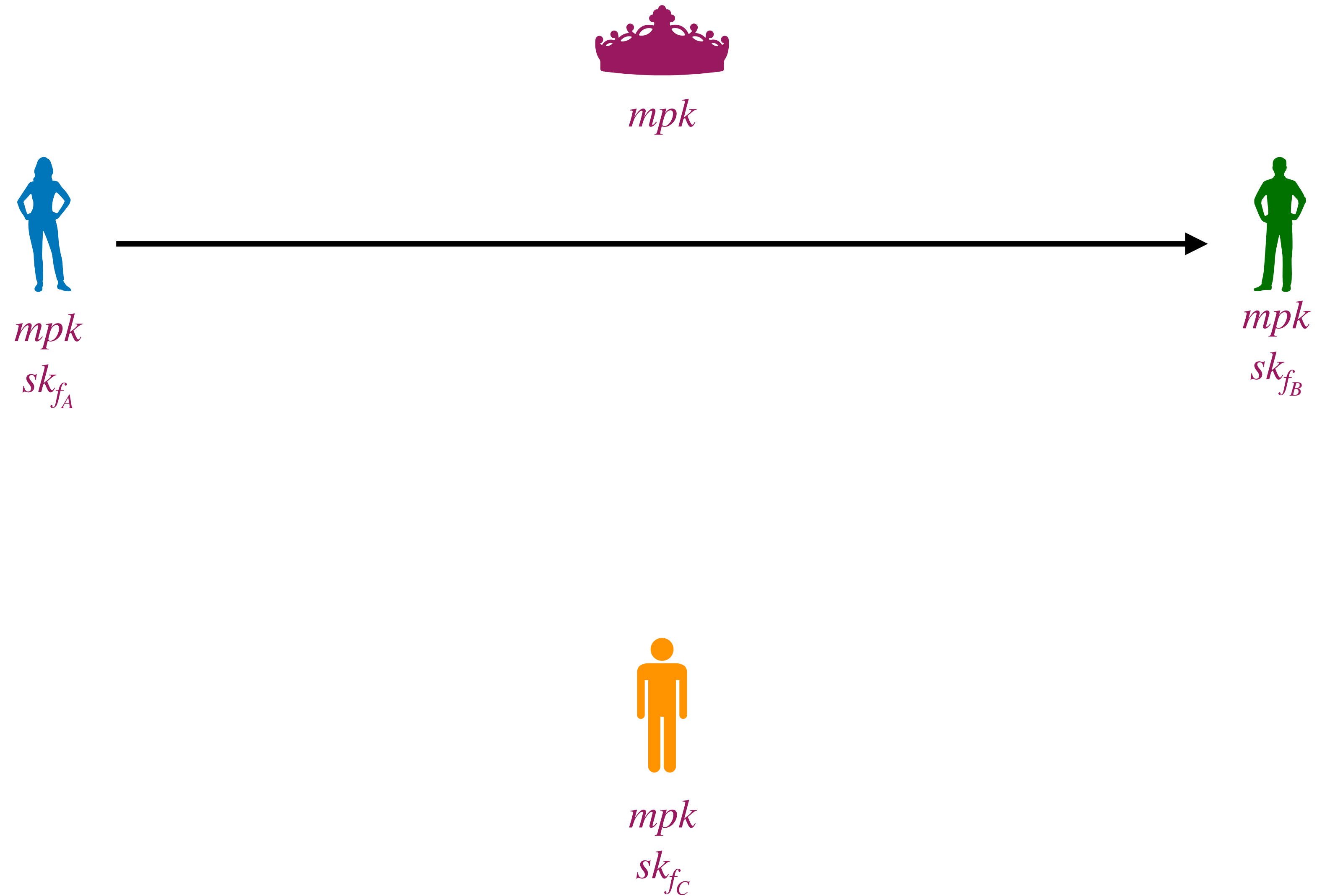
sk_{f_B}



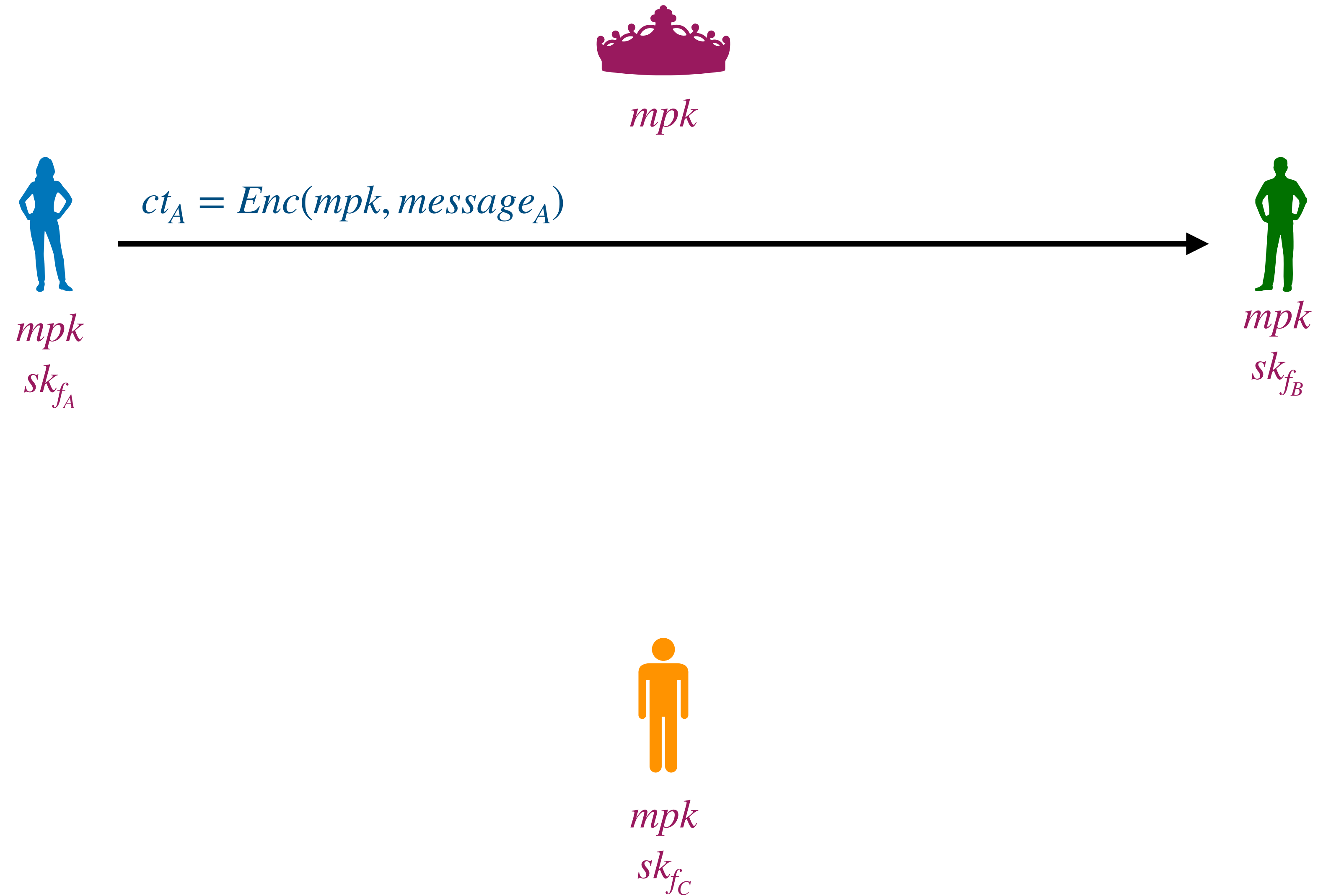
mpk

sk_{f_C}

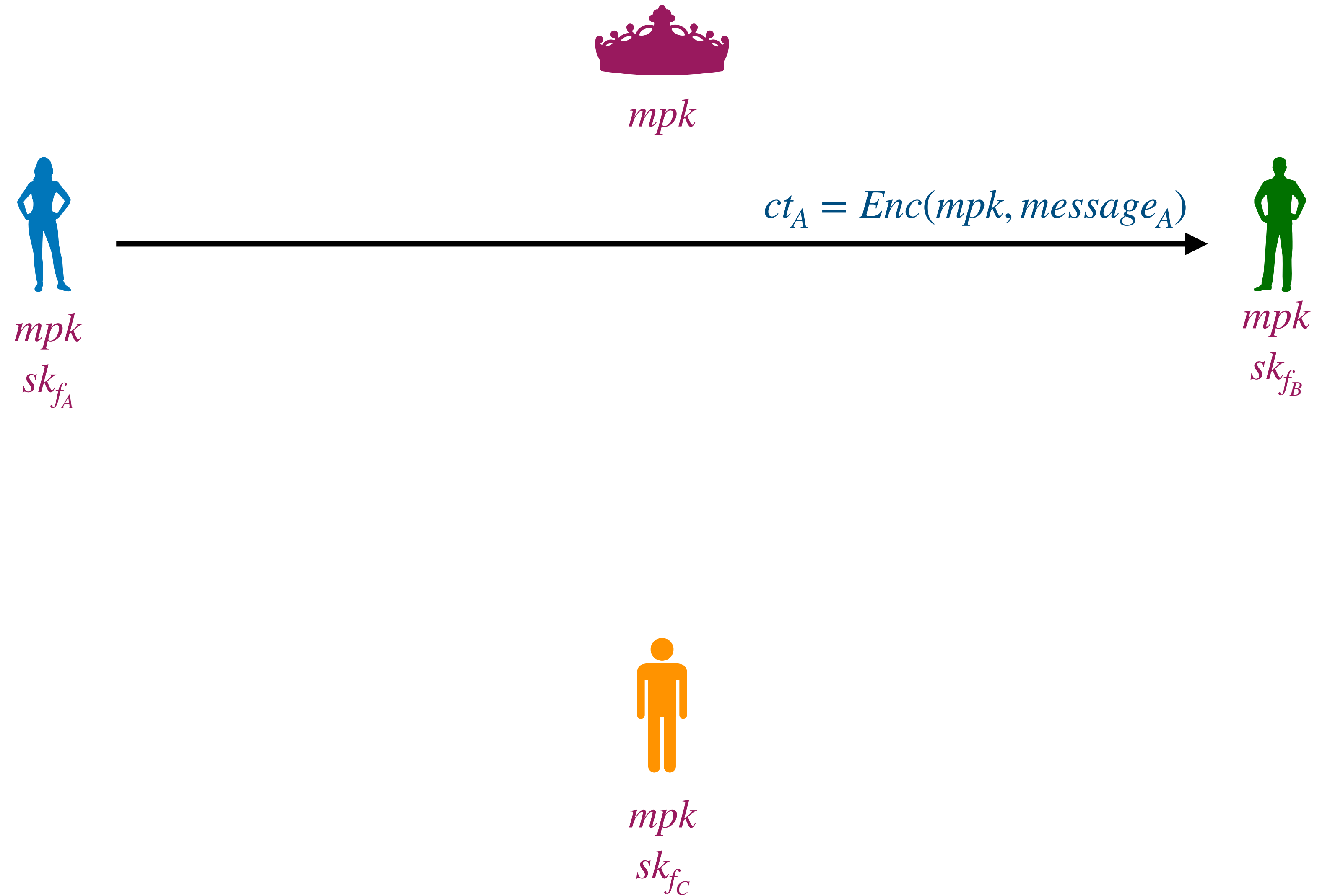
Functional Encryption (FE)



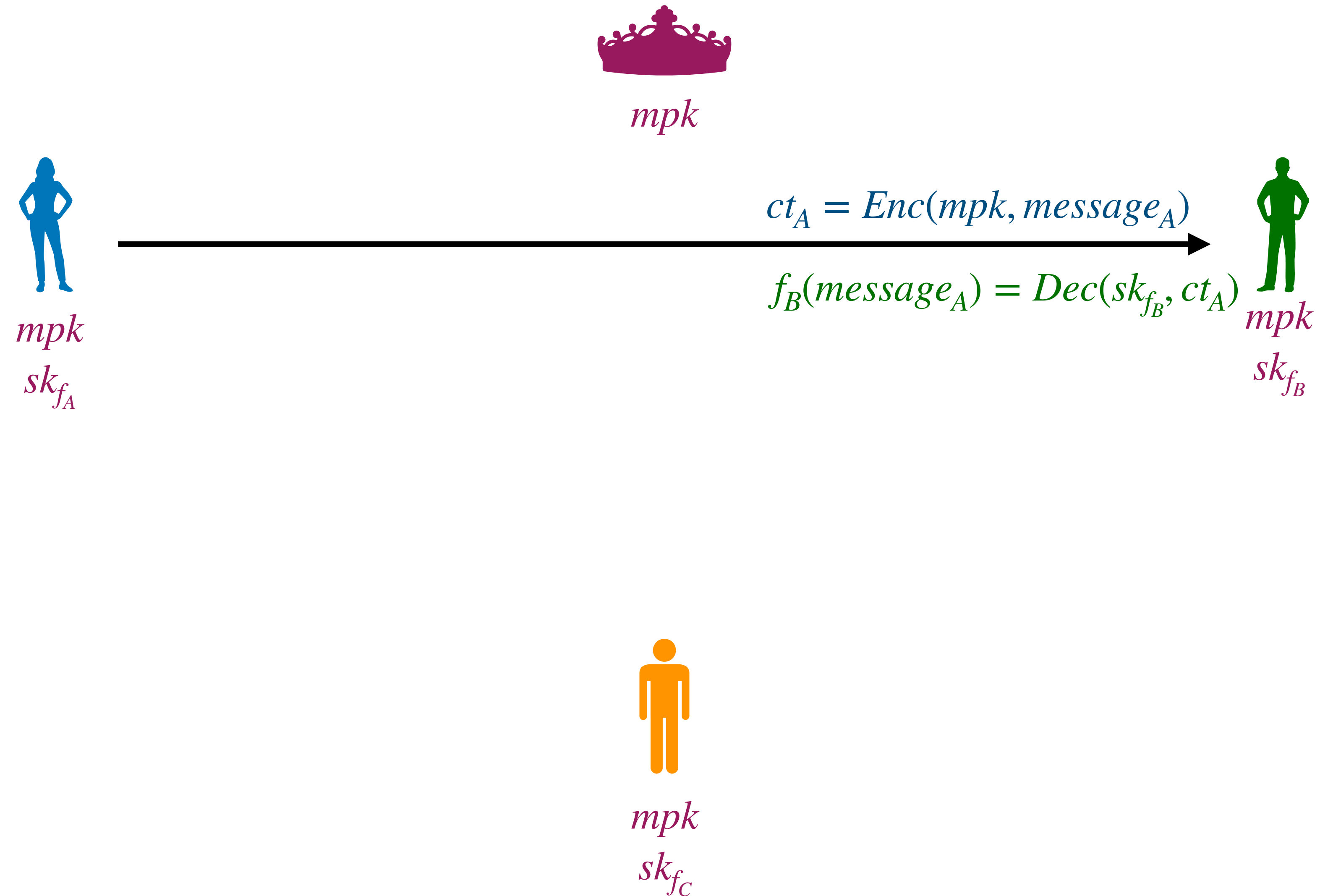
Functional Encryption (FE)



Functional Encryption (FE)



Functional Encryption (FE)



GKRV Results

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- Formally defined Incompressible FE (IBE) security.

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- Transformation from IBE + Incomp PKE to Incomp IBE.

GKRV Results

- Formally defined **Incompressible FE (IBE)** security.
- Transformation from **IBE + Incomp PKE** to **Incomp IBE**.
- Provided novel constructions for **Incomp FE** with (almost) optimal parameter.

Conclusion

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- We saw standard, leakage-resilient, incompressible, LRI security.
- **Constructions** for the above.
- Presented **IBE** and **FE**.
- Mentioned **possibilities** and **impossibilities** in LRI and incompressibility settings.

Thank You!!!

Personal Webpage - <https://mahe94.github.io/>

Incompressible Functional Encryption - <https://eprint.iacr.org/2024/798>

Leakage-Resilient Incompressible Cryptography: Constructions and Barriers -