



# **LAB V**

## **Introduction to Fading Channel and Computer Simulation**

teamwork

# Agenda

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- Introduction to fading channel
- Types of fading
- Generation and statistics of fading samples
- Channel Estimation
- Link level simulation in fading channel
- LAB Assignment+Quiz

# Radio Propagation

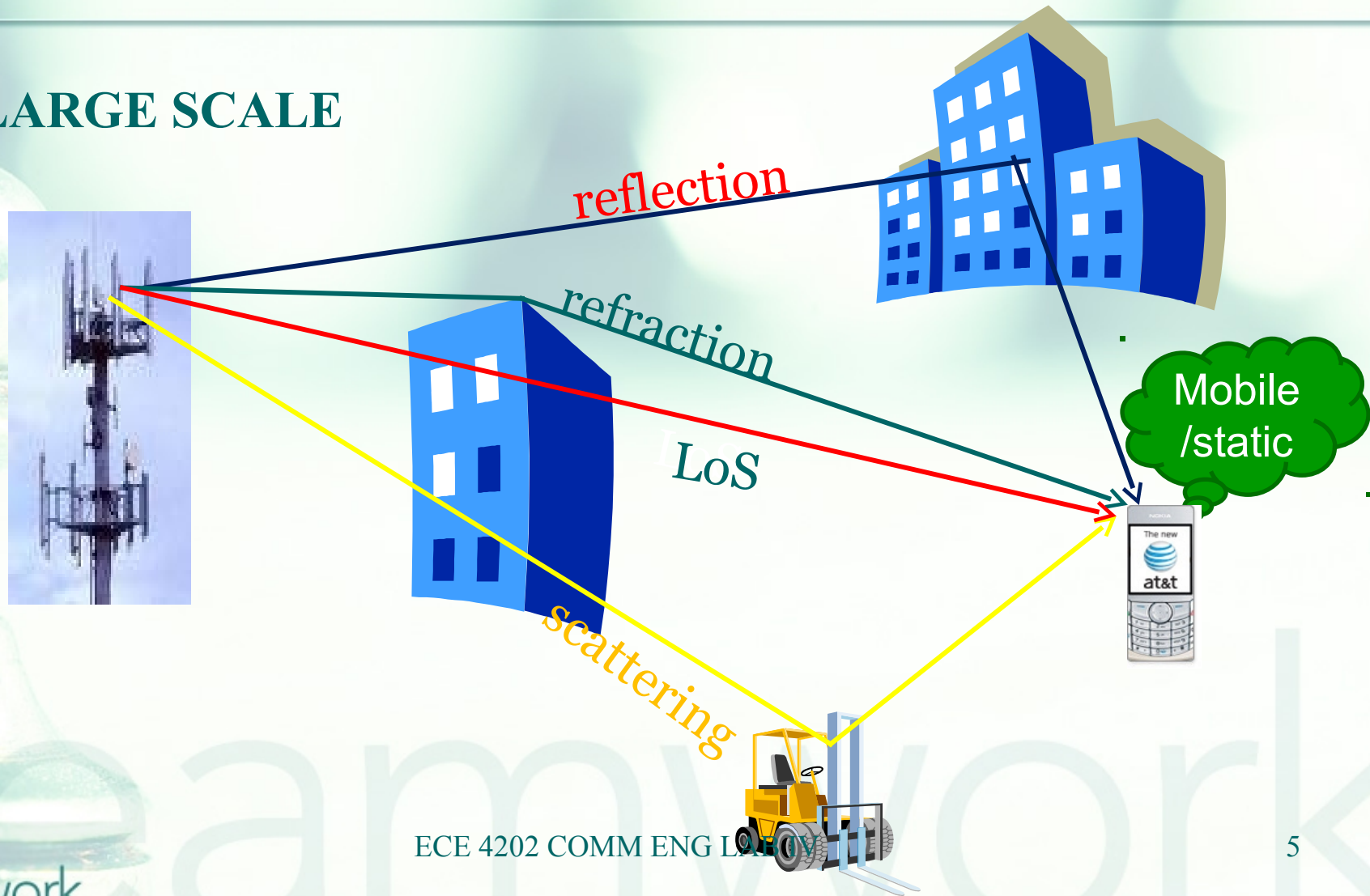
- Radio propagation is classified into
  - Large-scale propagation (path loss)
  - Small-scale propagation (fading)
- Large-scale propagation
  - Behavior of radio waves over 'long' distance (several tens to hundreds of meters)
- Small-scale propagation
  - Behavior of radio waves over 'short' distance (5 to 40 wavelengths)
- **THIS LAB IS ABOUT SMALL-SCALE FADING**

# Introduction to Fading Channel

- Fading is the time variation of received signal as observed by a receiver antenna
  - Multiple paths exist between the transmitter and receiver. Relative delay differences between paths can't be resolved
  - Movement of mobile terminal. Received signals have random phases.
  - Random superposition creates largely fluctuating resultant vector

# Radio wave propagation scenario

LARGE SCALE



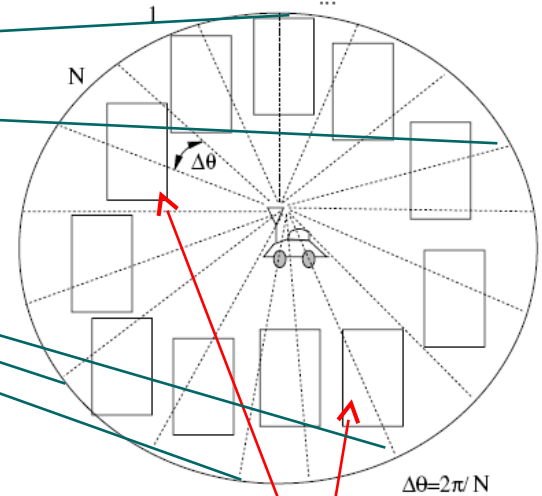


# Cont'd

## SMALL SCALE

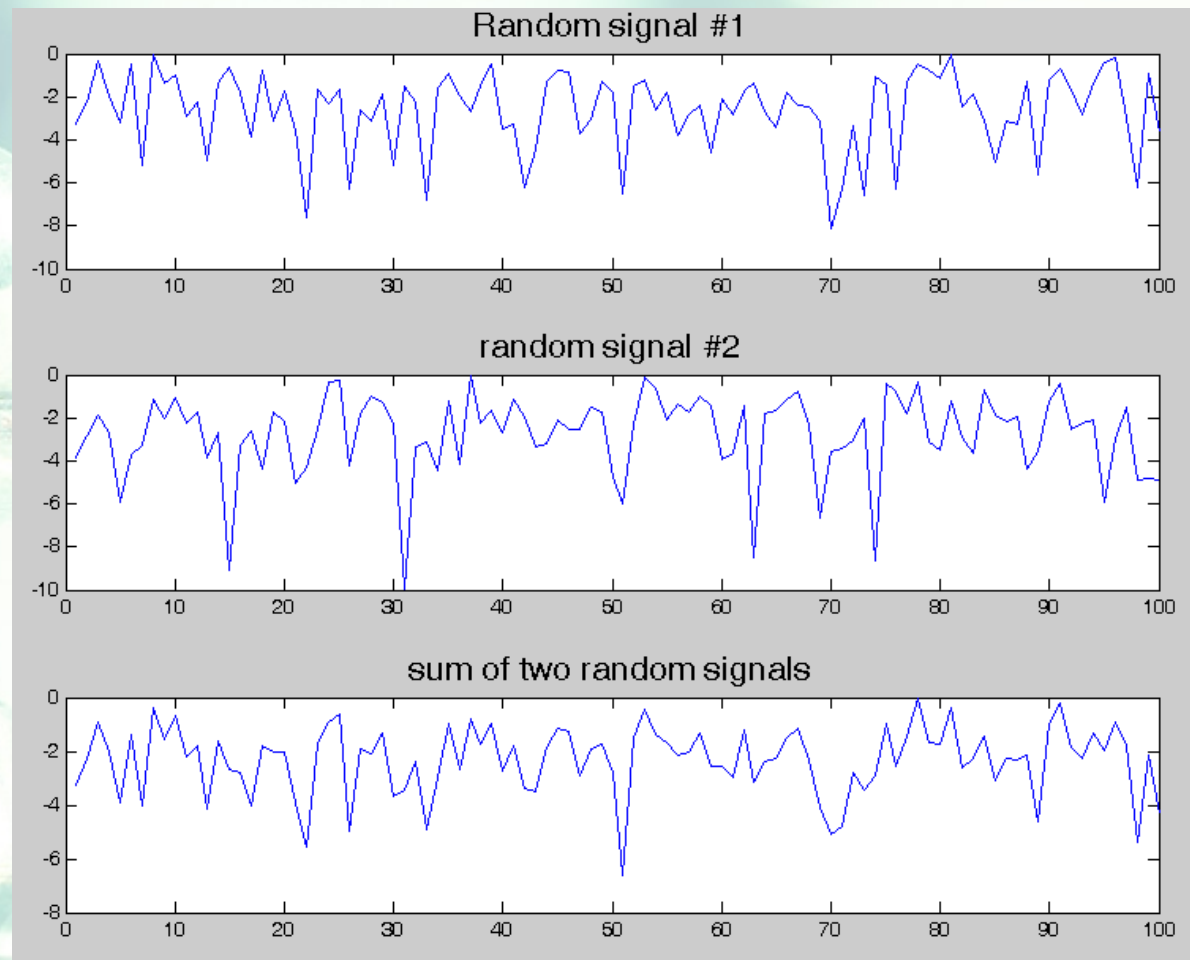


Non-resolvable;  
Seen as a single path by receiver



Each of the wave has random phase and amplitude.  
All are randomly superpositioned.

# Random superposition

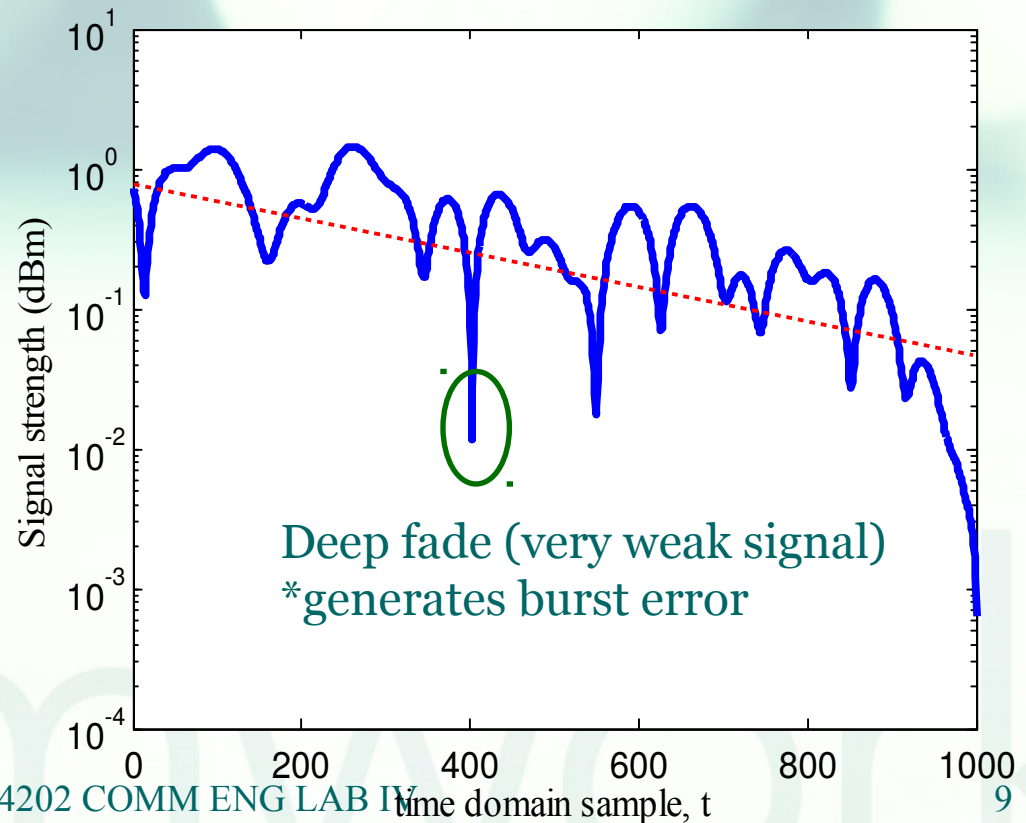
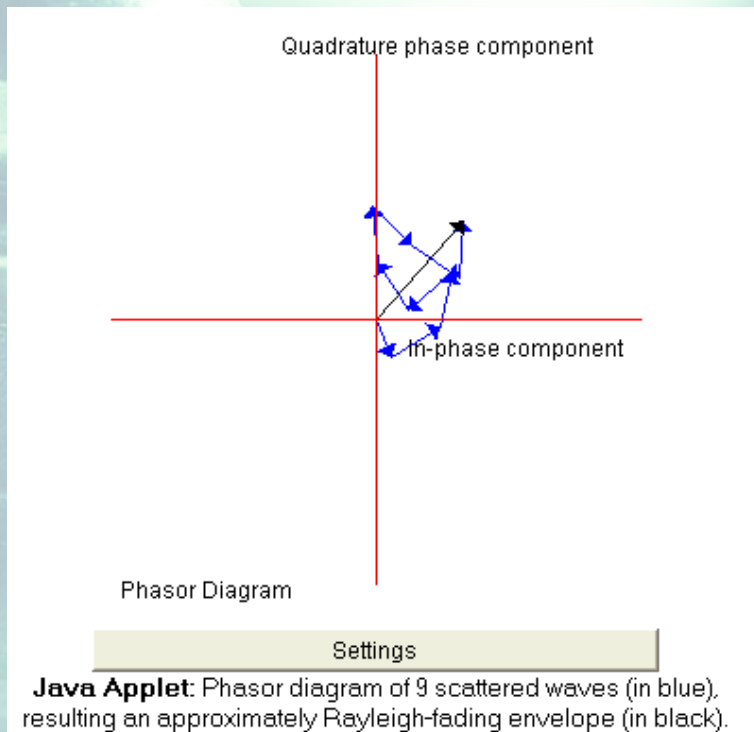


# Fading statistics

- Rayleigh fading
  - No Line of Sight (LoS) component presents
- Rician fading
  - Line of Sight (LoS) component presents
  - Deterministic component, contributes significantly to the total received power

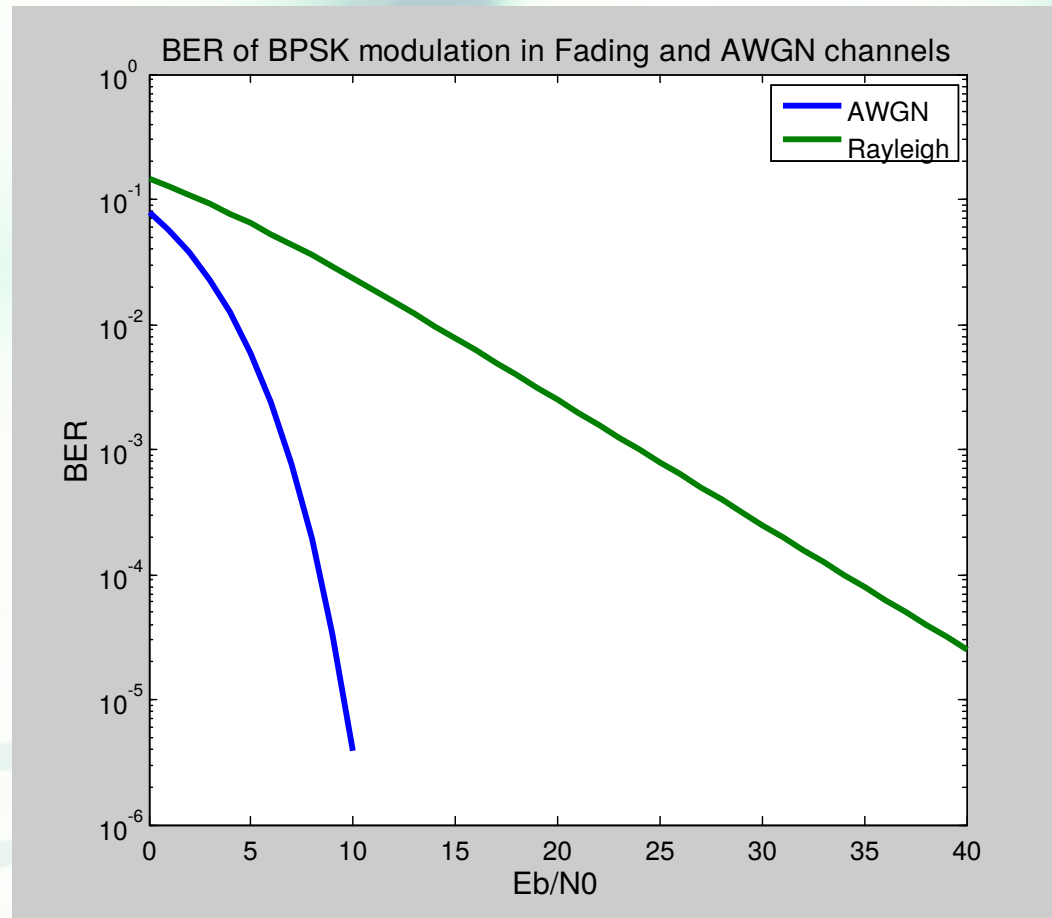


# Cont'd

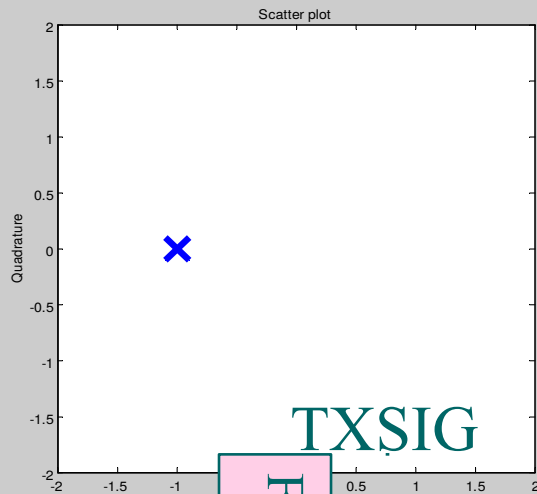


# Fading Effect to BER

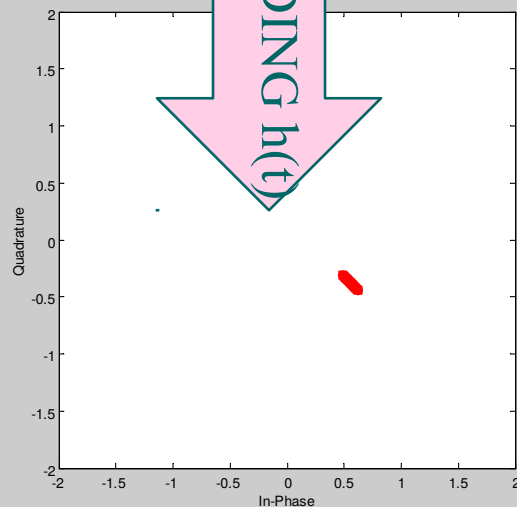
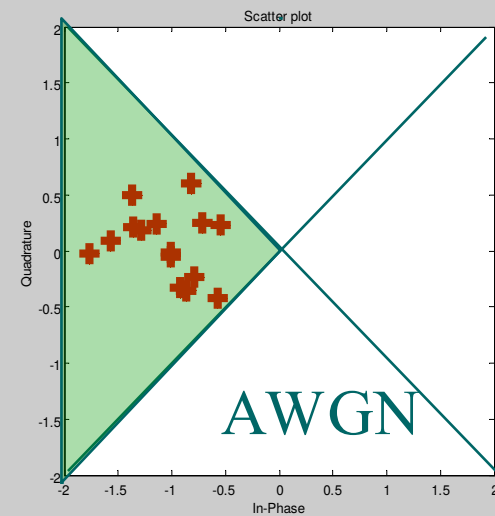
- Fading makes BER decreases only linearly with SNR/ $E_b/N_0$



# What happen to the tx signal?

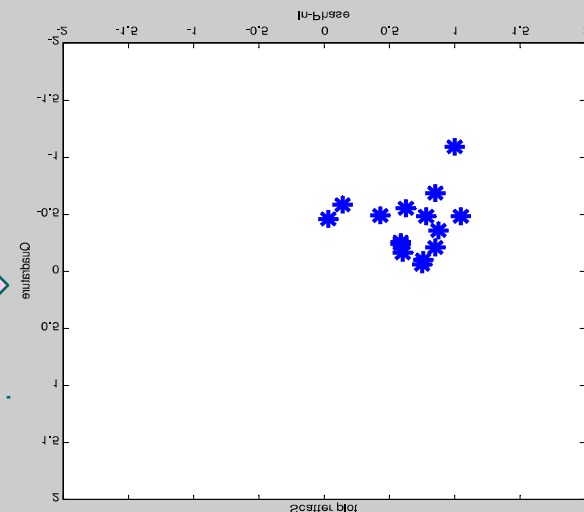


AWGN  $n(t)$



AWGN  $n(t)$

COMM EN



# Cont'd

- Fading effect is multiplicative to the transmit signal

$$y(t) = s(t) * h(t) + n(t)$$

- It causes rotation to the transmit signal
- If we do not “undo” the rotation caused by fading, the whole information will be detected erroneously

# Generating fading samples

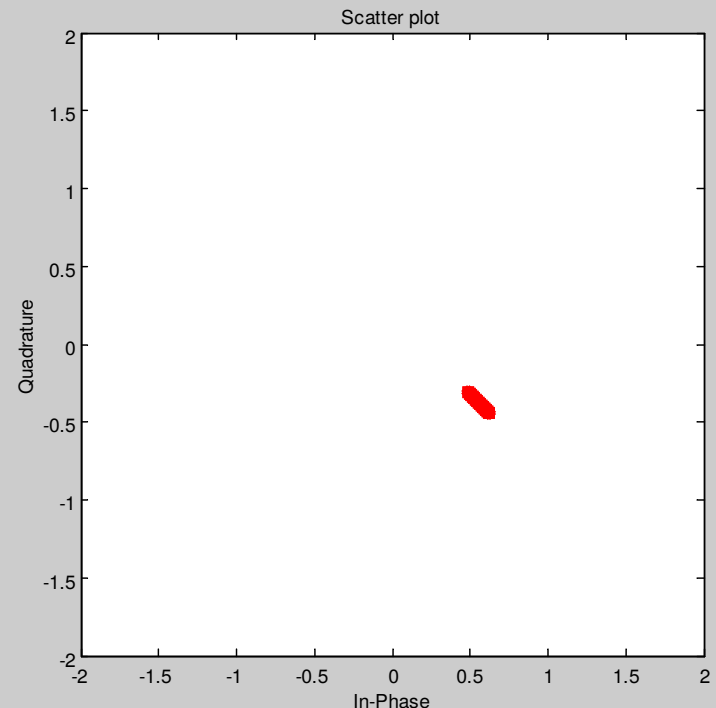
- Create a fading object
  - Generate a transmit signal
  - use filter() which does not require generation of fading sample
- Create a fading object
  - Generate fading samples by filtering all one sequence with the fading object as above
  - Generate a transmit signal
  - Convolve the fading sample with the transmit signal
    - In case of no multipath, it reduces to multiplication



```
%create fading object with sampling period of 0.1ms,  
     $f_D=50\text{Hz}$   
channel= rayleighchan(1e-4,50);  
%generate transmit signal (BPSK)  
data=randint(1,50);  
txsig=pskmod(data,2);  
scatterplot(txsig);  
%generate faded signal (before adding noise)  
fadesig=filter(channel, txsig);  
scatterplot(fadesig);  
%add noise  
rxsig=awgn(fadesig,15);  
%demodulate  
recsig=pskdemod(rxsig,2);  
%calculate the number of errors  
sum(recsig~=data)
```

# “undo” the fading

- How can we undo the fading effect???
- Fading is caused by the (radio) channel. Fading is not known by transmitter and receiver
- What observed by a receiver is  $y(t)$



# Cont'd

- Assume noise free condition

$$y(t) = s(t) * h(t)$$

- *Note that, when  $h(t)=d(t)$ , the convolution reduces to multiplication*
- Frequency domain representation (after Fourier transform)

$$Y(f) = S(f) \bullet H(f)$$

$$H(f) = \frac{Y(f)}{S(f)}$$

# Channel Estimation

- The process of estimating  $H(f)$  from  $Y(f)$ 
  - In case of delta function is equivalent to estimating  $h(t)$  from  $y(t)$
- How do we know  $H(f)$ ?
  - The receiver needs to know  $S(f)$
  - Transmitter must send sequence which is known to the receiver : **pilot sequence**
  - How many pilot symbols are enough (provide good channel estimate)?

# Cont'd

- Pilot sequence can be any sequence which is known to both transmitter and receiver
- Pilot sequence
  - $p = 1 \ 1 \ 1 \ 1$
  - $p = 1 \ -1 \ 1 \ -1$
  - $p = 1 \ 1 \ -1 \ -1$



# Cont'd

- In digital communication, user's information/data is grouped into blocks/frames before transmission
  - Add pilot sequence to each frame before modulation
  - Pilot sequence is known to the receiver and hence does not carry information

# Cont'd

$$\tilde{h}(t) = \frac{1}{N_p} \sum_{n=0}^{N_p-1} y(n) \bullet p(n)$$

- $\tilde{h}(t)$  : Channel estimate  
 $N_p$  : number of pilot symbols  
 $y(n)$  : received signal samples  
 $p(n)$  : n-th pilot symbol

# demodulation

- Before we perform demodulation on the user information carrying signal we need to compensate for the fading effect

$$y'(t) = y(t) \star \text{conj}(\tilde{h}(t))$$

- $y'(t)$  is the input to the demodulator, not  $y(t)$

```

%create fading object with sampling period of 0.1ms,  $f_d=20\text{Hz}$ 
channel= rayleighchan(1e-4,20);
%generate transmit signal (BPSK)
data=randint(1,50);
%BPSK modulation
modsig=pskmod(data,2);
%generate pilot signal
pilot= [1 1 -1 -1] ;
txsig =[pilot modsig];
scatterplot(txsig);
%generate faded signal (before adding noise)
fadesig=filter(channel, txsig);
scatterplot(fadesig);
%add noise
rxsig=awgn(fadesig,15);
%scatterplot(rxsig);
%channel estimation and compensation
h_tilde = channelestimate(pilot, rxsig(1:4))
modemin= rxsig(5:end)*conj(h_tilde);
%scatterplot(modemin);
%demodulate
recsig=pskdemod(modemin,2);
%calculate the number of errors
sum(recsig~=data)

```

```
%function to perform channel estimation on  
%bpsk modulated sequence  
%[h_tilde]=channelestimate(pilot,rxsig)  
function [h]=channelestimate(pilot, rxsig)  
h = mean(rxsig.*pilot); %element wise multiplication followed by averaging
```



# Cautions

- Simulating fading channel requires much more samples compared to AWGN channel
  - Insufficient number of samples may lead to incorrect results