

GATE XE 2023

AI25BTECH11003- Bhavesh Gaikwad

GENERAL APTITUDE

- 1) The village was nestled in a green spot, _____ the ocean and the hills.
(GATE 2023 XE)
a) through b) in c) at d) between
- 2) Disagree : Protest :: Agree : _____ (By word meaning)
(GATE 2023 XE)
a) Refuse b) Pretext c) Recommend d) Refute
- 3) A 'frabjous' number is defined as a 3 digit number with all digits odd, and no two adjacent digits being the same. For example, 137 is a frabjous number, while 133 is not. How many such frabjous numbers exist?
(GATE 2023 XE)
a) 125 b) 720 c) 60 d) 80
- 4) Which one among the following statements must be TRUE about the mean and the median of the scores of all candidates appearing for GATE 2023?
(GATE 2023 XE)
a) The median is at least as large as the mean. is larger than the median.
b) The mean is at least as large as the median. d) At most half the candidates have a score that
c) At most half the candidates have a score that is larger than the mean.
- 5) In the given diagram, ovals are marked at different heights (h) of a hill. Which one of the following options P, Q, R, and S depicts the top view of the hill?

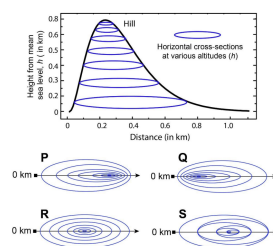


Fig. 5: Diagram

(GATE 2023 XE)

- a) P b) Q c) R d) S

- 6) Residency is a famous housing complex with many well-established individuals among its residents. A recent survey conducted among the residents of the complex revealed that all of those residents who are well established in their respective fields happen to be academicians. The survey also revealed that most of these academicians are authors of some best-selling books. Based only on the information provided above, which one of the following statements can be logically inferred with certainty?

(GATE 2023 XE)

- | | |
|--|--|
| a) Some residents of the complex who are well established in their fields are also authors of some best-selling books. | c) Some authors of best-selling books are residents of the complex who are well established in their fields. |
| b) All academicians residing in the complex are well established in their fields. | d) Some academicians residing in the complex are well established in their fields. |

- 7) Ankita has to climb 5 stairs starting at the ground, while respecting the following rules: 1. At any stage, Ankita can move either one or two stairs up. 2. At any stage, Ankita cannot move to a lower step. Let $F(n)$ denote the number of possible ways in which Ankita can reach the N th stair. For example, $F(1) = 1$, $F(2) = 2$, $F(3) = 3$. The value of $F(5)$ is _____.

(GATE 2023 XE)

- | | | | |
|------|------|------|------|
| a) 8 | b) 7 | c) 6 | d) 5 |
|------|------|------|------|

- 8) The information contained in DNA is used to synthesize proteins that are necessary for the functioning of life. DNA is composed of four nucleotides: Adenine (A), Thymine (T), Cytosine (C), and Guanine (G). The information contained in DNA can then be thought of as a sequence of these four nucleotides: A, T, C, and G. DNA has coding and non-coding regions. Coding regions—where the sequence of these nucleotides are read in groups of three to produce individual amino acids—constitute only about 2% of human DNA. For example, the triplet of nucleotides CCG codes for the amino acid glycine, while the triplet GGA codes for the amino acid proline. Multiple amino acids are then assembled to form a protein. Based only on the information provided above, which of the following statements can be logically inferred with certainty? (i) The majority of human DNA has no role in the synthesis of proteins. (ii) The function of about 98% of human DNA is not understood.

(GATE 2023 XE)

- | | |
|--------------|-------------------------|
| a) only (i) | c) both (i) and (ii) |
| b) only (ii) | d) neither (i) nor (ii) |

- 9) Which one of the given figures P, Q, R and S represents the graph of the following $f(x) = ||x + 2| - |x - 1||$ function?

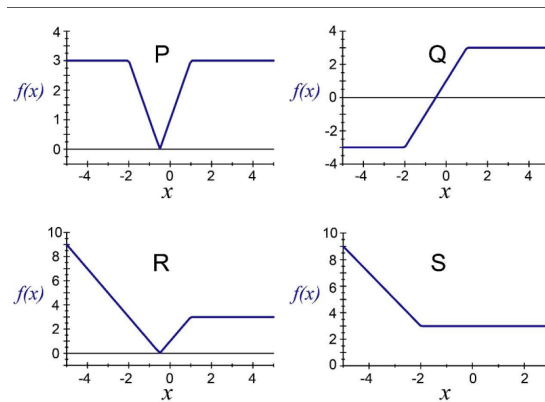


Fig. 9: (Graphs)

(GATE 2023 XE)

- a) P b) Q c) R d) S

- 10) An opaque cylinder (shown below) is suspended in the path of a parallel beam of light, such that its shadow is cast on a screen oriented perpendicular to the direction of the light beam. The cylinder can be reoriented in any direction within the light beam. Under these conditions, which one of the shadows P, Q, R, and S is NOT possible?

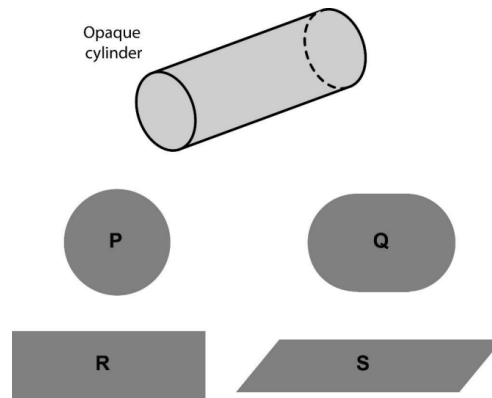


Fig. 10: Cylinder and Its Shadows

(GATE 2023 XE)

- a) P b) Q c) R d) S

END OF SECTION- GA

ENGINEERING MATHEMATICS

1) Let A be a 3×3 real matrix having eigenvalues 1, 2, and 3. If $B = A^2 + 2A + I$, where I is the 3×3 identity matrix, then the eigenvalues of B are

(GATE 2023 XE)

- a) 4, 9, 16
b) 1, 2, 3

- c) 1, 4, 9
d) 4, 16, 25

2) Let $f : \mathbb{R}^2 \rightarrow \mathbb{R}$ be a function defined by $f(x, y) = \begin{cases} \frac{x, y}{|x| + y} & \text{if } y \neq -|x| \\ 0, & \text{otherwise} \end{cases}$

Then which one of the following statement is TRUE?

(GATE 2023 XE)

- f is NOT continuous at $(0, 0)$.
- $\frac{\partial f}{\partial x}(0, 0) = 0$, and $\frac{\partial f}{\partial y}(0, 0) = 1$.

- c) $\frac{\partial f}{\partial x}(0,0) = 1$, and $\frac{\partial f}{\partial y}(0,0) = 0$.
d) $\frac{\partial f}{\partial x}(0,0) = 1$, and $\frac{\partial f}{\partial y}(0,0) = 1$.

3) If the quadrature formula

$$\int_{-1}^1 f(x)dx \approx \frac{1}{9} \left(c_1 f(-1) + c_2 f\left(\frac{1}{2}\right) + c_3 f(1) \right)$$

is exact for all polynomials of degree less than or equal to 2, then

(GATE 2023 XE)

- $$\begin{array}{l} \text{a) } c_1 + \frac{c_2}{4} + c_3 = 6 \\ \text{b) } c_1 + \frac{c_2}{3} + c_3 = 4 \end{array}$$

- c) $c_1 + \frac{c_2}{2} + c_3 = 2$
d) $c_1 + c_2 + c_3 = 5$

4) The second smallest eigenvalue of the eigenvalue problem

$$\frac{d^2 y}{dx^2} + (\lambda - 3)y = 0, \quad y(0) = y(\pi) = 0,$$

(GATE 2023 XE)

- a) 4
b) 3

- c) 7
d) 9

5) Which one of the following functions is differentiable at $z = 0$ but NOT differentiable at any other point in the complex plane \mathbb{C} ?

(GATE 2023 XE)

- $f(z) = z|z|, z \in \mathbb{C}$
- $f(z) = \sin(z), z \in \mathbb{C}$

- $$\begin{aligned} \text{c) } f(z) &= \begin{cases} e^{1/z} & , z \neq 0, \\ 0 & , z = 0 \end{cases} \\ \text{d) } f(z) &= e^{-z^2}, z \in \mathbb{C} \end{aligned}$$

6) If the polynomial

$$P(x) = a_0 + a_1x + a_2x(x-1) + a_3x(x-1)(x-2)$$

interpolates the points $(0, 2), (1, 3), (2, 2)$ and $(3, 5)$, then the value of $P(\frac{5}{2})$ is _____ (round off to 2 decimal places).

(GATE 2023 XE)

- 7) The value of m for which the vector field
 $\vec{F}(x, y) = (4x^m y^2 - 2xy^m)\hat{i} + (2x^4 y - 3x^2 y^2)\hat{j}$
 is a conservative vector field, is _____ (integer).

(GATE 2023 XE)

8) Let $P = \begin{bmatrix} 4 & -2 & 2 \\ 6 & -3 & 4 \\ 3 & -2 & 3 \end{bmatrix}$ and $Q = \begin{bmatrix} 3 & -2 & 2 \\ 4 & -4 & 6 \\ 2 & -3 & 5 \end{bmatrix}$.

The eigenvalues of both P and Q are 1, 1, 2. Which one of the following statements is TRUE?

(GATE 2023 XE)

- a) Both P and Q are diagonalizable
 b) P is diagonalizable but Q is NOT diagonalizable
 c) P is NOT diagonalizable but Q is diagonalizable
 d) Both P and Q are NOT diagonalizable

- 9) The surface area of the portion of the paraboloid
 $z = x^2 + y^2$
 that lies between the planes $z = 0$ and $z = 1/4$ is

(GATE 2023 XE)

- a) $\frac{\pi}{6}(2\sqrt{2} - 1)$
 b) $\frac{\pi}{2}(2\sqrt{2} - 1)$
 c) $\pi(2\sqrt{2} - 1)$
 d) $\frac{\pi}{3}(2\sqrt{2} - 1)$

- 10) The probability of a person telling the truth is $\frac{4}{6}$. An unbiased die is thrown twice by the same person and the person reports that the numbers appeared in both throws are same. Then the probability that actually the numbers appeared in both throws are same is _____ (round off to 2 decimal places).

(GATE 2023 XE)

- 11) Let $u(x, t)$ be the solution of the initial boundary value problem
 $\frac{\partial u}{\partial t} - \frac{\partial^2 u}{\partial x^2} = 0$, for $x \in (0, 2), t > 0$ with initial condition $u(x, 0) = \sin(\pi x)$ for $x \in (0, 2)$ and
 boundary conditions $u(0, t) = u(2, t) = 0$
 Then the value of $e^{\pi^2}(u(\frac{1}{2}, 1) - u(\frac{3}{2}, 1))$ is _____ (integer).

(GATE 2023 XE)

END OF SECTION-A

FLUID MECHANICS

1) Match the following measuring instruments with the appropriate figures.

I – Pitot probe II – Pitot-static probe III – Piezometer

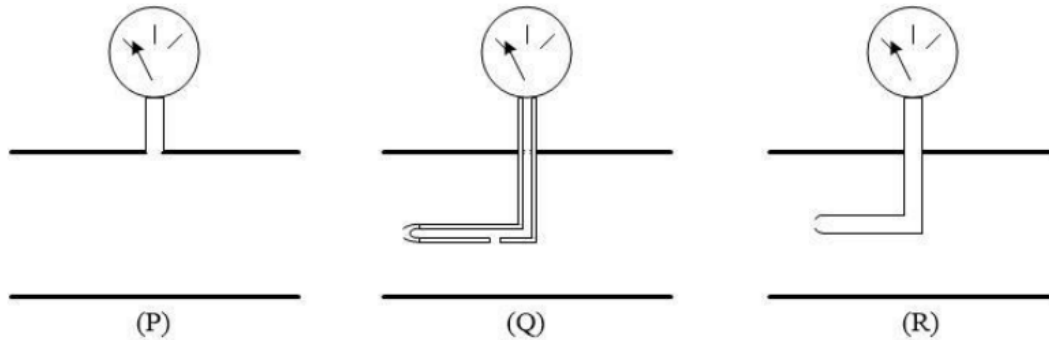


Fig. 1: Figures for matching instruments

(GATE 2023 XE)

a) I – P; II – Q; III – R

c) I – R; II – P; III – Q

b) I – R; II – Q; III – P

d) I – Q; II – P; III – R

2) Among the following non-dimensional numbers, which one characterizes periodicity present in a transient flow? (GATE 2023 XE)

a) Froude number

c) Peclet number

b) Strouhal number

d) Lewis number

3) For an incompressible boundary layer flow over a flat plate shown in the figure, the momentum thickness is expressed as

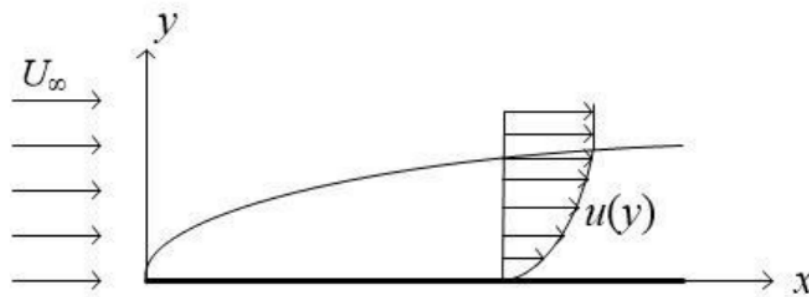


Fig. 3: Flat plate boundary layer schematic

(GATE 2023 XE)

a) $\int_0^\infty \frac{u}{U_\infty} dy$

c) $\int_0^\infty \frac{u}{U_\infty} \left(1 - \frac{u}{U_\infty}\right) dy$

b) $\int_0^\infty \left(1 - \frac{u}{U_\infty}\right) dy$

d) $\int_0^\infty \left(1 - \frac{u^2}{U_\infty^2}\right) dy$

- 4) Among the shear stress versus shear strain rate curves shown in the figure, which one corresponds to a shear thinning fluid?

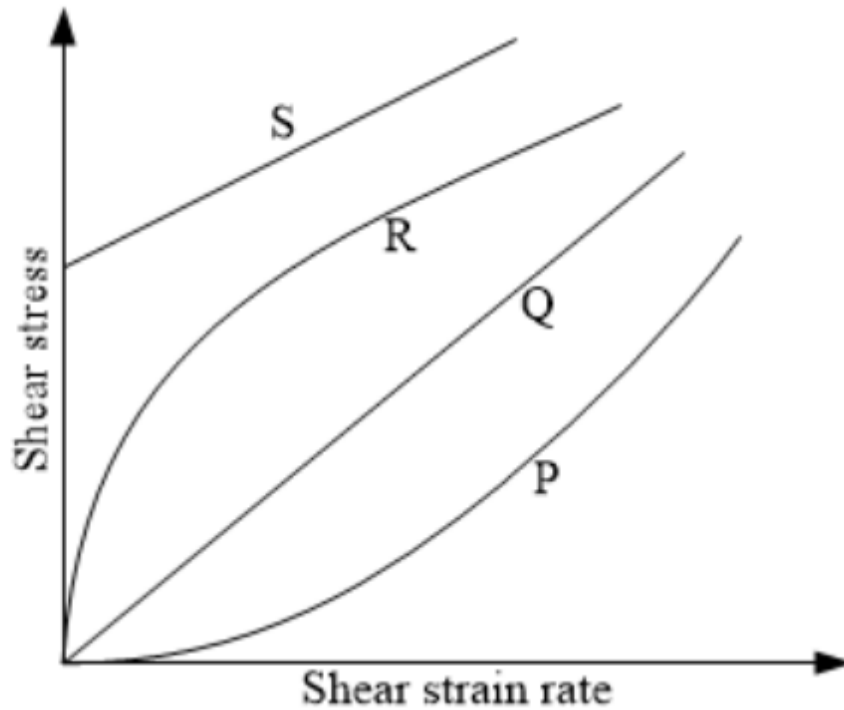


Fig. 4: Shear stress vs. shear rate curves

(GATE 2023 XE)

- a) P
b) Q
c) R
d) S

- 5) Consider steady incompressible flow over a flat plate, where the dashed line represents the edge of the boundary layer, as shown in the figure. Which one among the following statements is true?



Fig. 5: Regions relative to boundary layer

(GATE 2023 XE)

- a) Bernoulli's equation can be applied in Region I between any two arbitrary points. c) Bernoulli's equation cannot be applied in Region II.
- b) Bernoulli's equation can be applied in Region I only along a streamline. d) Bernoulli's equation cannot be applied in Region I.
- 6) An inviscid steady incompressible flow is formed by combining a uniform flow with velocity U_∞ and a clockwise vortex of strength K at the origin, as shown in the figure. Velocity potential (ϕ) for the combined flow in polar coordinate (r, θ) is

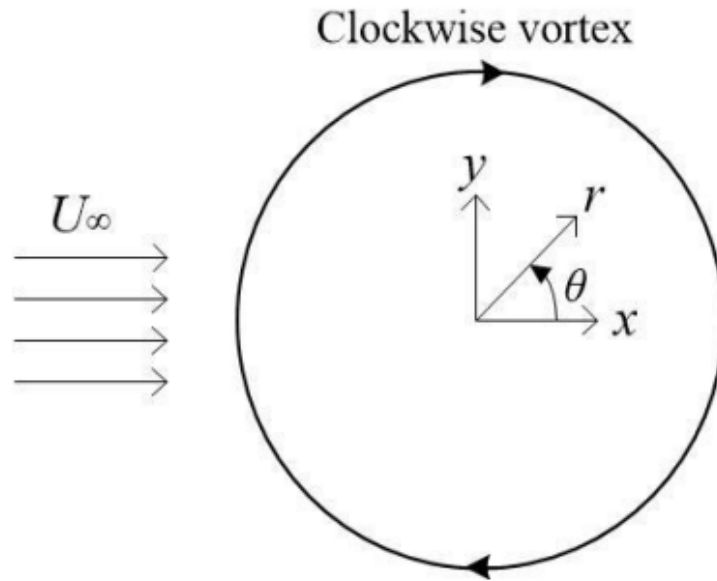


Fig. 6: Uniform flow plus vortex

(GATE 2023 XE)

- a) $\phi = \frac{K\theta}{2\pi} - U_\infty r \cos \theta$ c) $\phi = K \ln r + U_\infty r \cos \theta$
- b) $\phi = \frac{K\theta}{2\pi} - U_\infty r \sin \theta$ d) $\phi = -K \ln r + U_\infty r \sin \theta$

7) Which of the following statements are true?

- (i) Conservation of mass for an unsteady incompressible flow can be represented as $\nabla \cdot \vec{V} = 0$, where \vec{V} denotes velocity vector.
- (ii) Circulation is defined as the line integral of vorticity about a closed curve.
- (iii) For some fluids, shear stress can be a nonlinear function of the shear strain rate.
- (iv) Integration of the Bernoulli's equation along a streamline under steady-state leads to the Euler's equation.

(GATE 2023 XE)

- a) (i), (ii) and (iv) only c) (i) and (iii) only
- b) (i), (ii) and (iii) only d) (ii) and (iv) only

- 8) For a two-dimensional flow field given as $\vec{V} = -x\hat{i} + y\hat{j}$, a streamline passes through points $(2, 1)$ and $(5, p)$. The value of p is (GATE 2023 XE)

- a) 5
b) $5/2$
c) $2/5$
d) 2

- 9) A stationary object is fully submerged in a static fluid, as shown in the figure. Here, CG and CB stand for center of gravity and center of buoyancy, respectively. Which one(s) among the following statements is/are true? (GATE 2023 XE)

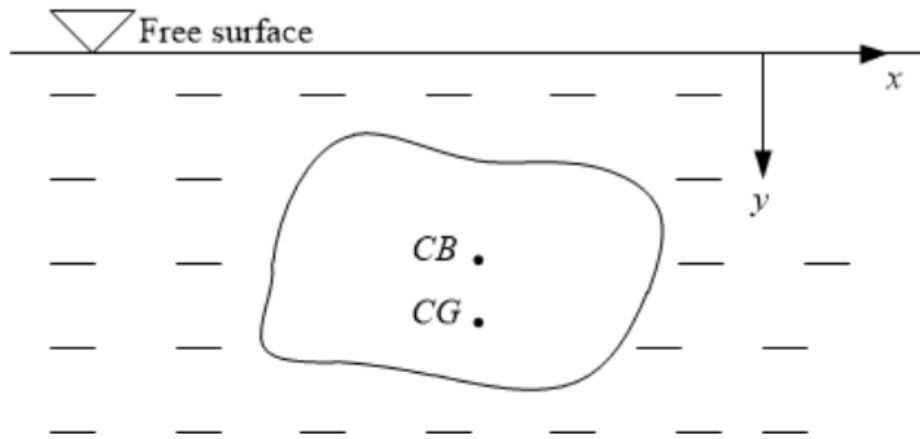


Fig. 9: Submerged object with CG and CB

- a) The object is in stable equilibrium if $y_{CG} > y_{CB}$.
b) The object is in stable equilibrium if $y_{CG} < y_{CB}$.
c) The object is in neutral equilibrium if $y_{CG} = y_{CB}$.
d) The object is in unstable equilibrium if $y_{CG} = y_{CB}$.
- 10) Consider steady fully-developed incompressible flow of a Newtonian fluid between two infinite parallel flat plates. The plates move in the opposite directions, as shown in the figure. In the absence of body force and pressure gradient, the ratio of shear stress at the top surface ($y = H$) to that at the bottom surface ($y = 0$) is

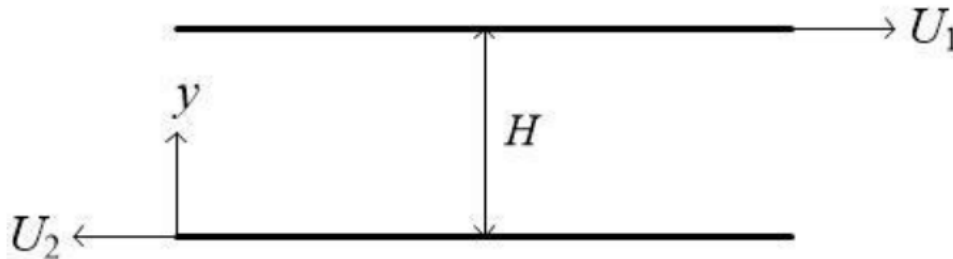


Fig. 10: Couette flow between plates

(GATE 2023 XE)

- a) 1
b) U_1/U_2
c) $(U_1 - U_2)/U_2$
d) $(U_1 + U_2)/U_2$

11) A two-dimensional incompressible flow field is defined as, $\vec{V}(x, y) = (Axy)\hat{i} + (By^2)\hat{j}$ where, A and B are constants. The dynamic viscosity of the Newtonian fluid is μ . In the absence of body force, which among the following expressions represents the pressure gradient at the location $(5, 0)$ in the concerned flow field? (GATE 2023 XE)

- a) $\mu A(5\hat{i} + \hat{j})$
b) $\mu(-5B\hat{i} + A\hat{j})$
c) $\mu A(-\hat{j})$
d) $\mu A(5\hat{i})$

12) For a potential flow, the fluid velocity is given by $\vec{V}(x, y) = u\hat{i} + v\hat{j}$. The slope of the potential line at (x, y) is (GATE 2023 XE)

- a) u/v
b) v/u
c) $-u/v$
d) $-v/u$

13) Consider steady incompressible flow of a Newtonian fluid over a horizontal flat plate, as shown in the figure. The boundary layer thickness is proportional to

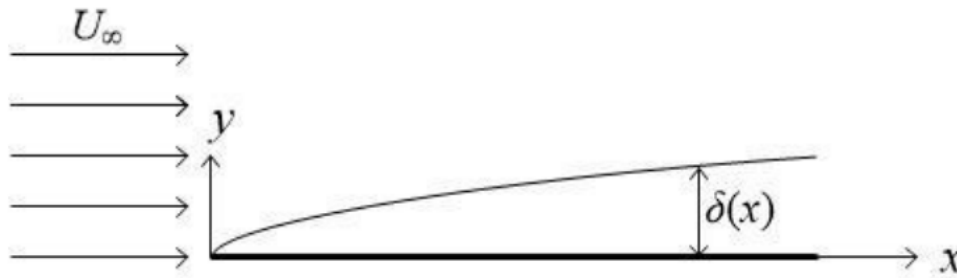


Fig. 13: Flat plate boundary layer growth

(GATE 2023 XE)

- a) $x^{1/4}$
b) $x^{1/2}$
c) $x^{-1/2}$
d) x^2

14) In a steady two-dimensional compressible flow, u and v are the x - and y - components of flow velocity, respectively and ρ is the fluid density. Among the following pairs of relations, which one(s) perfectly satisfies/satisfy the definition of stream function, ψ , for this flow? (GATE 2023 XE)

- a) $u = \frac{\partial \psi}{\partial y}$ and $v = -\frac{\partial \psi}{\partial x}$
b) $u = -\frac{\partial \psi}{\partial x}$ and $v = -\frac{\partial \psi}{\partial y}$
c) $\rho u = \frac{\partial \psi}{\partial y}$ and $\rho v = -\frac{\partial \psi}{\partial x}$
d) $\rho u = -\frac{\partial \psi}{\partial y}$ and $\rho v = \frac{\partial \psi}{\partial x}$

- 15) A water jet (density = 1000 kg/m^3) is approaching a vertical plate, having an orifice at the center, as shown in the figure. While a part of the jet passes through the orifice, remainder flows along the plate. Neglect friction and assume both the inlet and exit jets to have circular cross-sections. If $V = 5 \text{ m/s}$, $D = 100 \text{ mm}$ and $d = 25 \text{ mm}$, magnitude of the horizontal force (in N, rounded off to one decimal place) required to hold the plate in its position is _____.

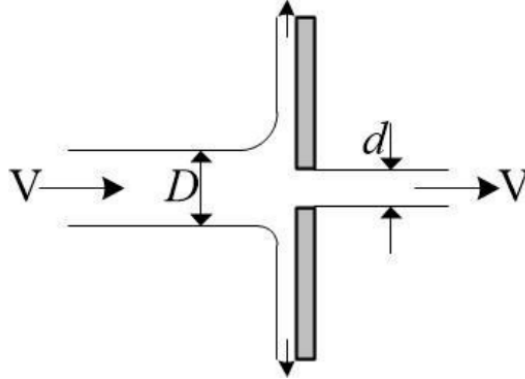


Fig. 15: Jet impacting perforated plate

(GATE 2023 XE)

- 16) Water (density = 1000 kg/m^3) and alcohol (specific gravity = 0.7) enter a Y-shaped channel at flow rates of $0.2 \text{ m}^3/\text{s}$ and $0.3 \text{ m}^3/\text{s}$, respectively. Their mixture leaves through the other end of the channel, as shown in the figure. The average density (in kg/m^3) of the mixture is _____.

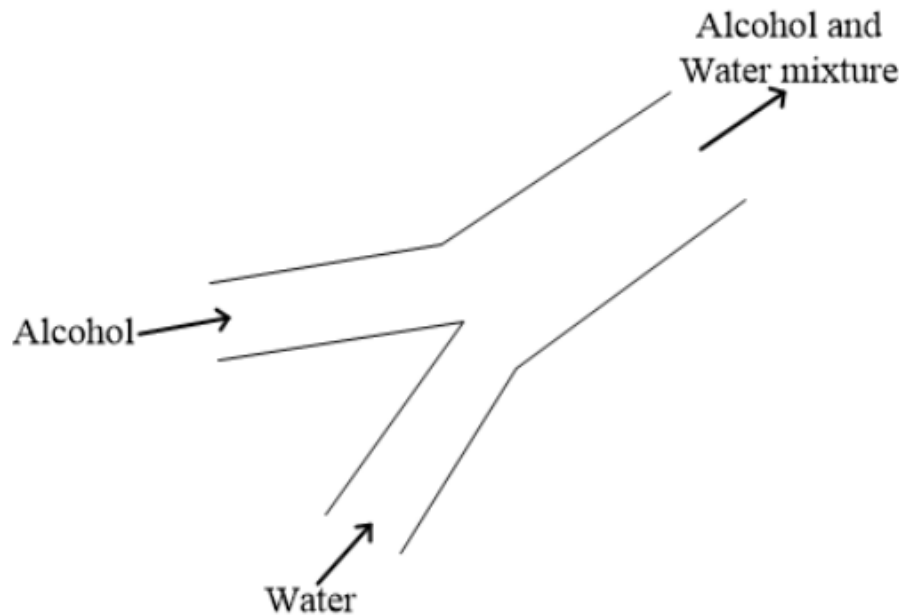


Fig. 16: Mixing in Y-channel

(GATE 2023 XE)

- 17) The velocity and acceleration of a fluid particle are given as $\vec{V} = (-\hat{i} + 2\hat{j}) \text{ m/s}$ and $\vec{a} = (-2\hat{i} - 4\hat{j}) \text{ m/s}^2$, respectively. The magnitude of the component of acceleration (in m/s^2 , rounded off to two decimal places) of the fluid particle along the streamline is _____.
- (GATE 2023 XE)

- 18) A hydraulic turbine with rotor diameter of 100 mm produces 200 W of power while rotating at 300 rpm. Another dynamically-similar turbine rotates at a speed of 1500 rpm. Consider both turbines to operate with the same fluid (identical density and viscosity), and neglect any gravitational effect. Then the power (in W, rounded off to nearest integer) produced by the second turbine is _____.
(GATE 2023 XE)
- 19) Water (density = 1000 kg/m^3) flows steadily with a flow rate of $0.05 \text{ m}^3/\text{s}$ through a venturimeter having throat diameter of 100 mm. If the pipe diameter is 200 mm and losses are negligible, the pressure drop (in kPa, rounded off to one decimal place) between an upstream location in the pipe and the throat (both at the same elevation) is _____.
(GATE 2023 XE)
- 20) Water flows around a thin flat plate (0.25 m long, 2 m wide) with a free stream velocity (U_∞) of 1 m/s, as shown in the figure. Consider linear velocity profile $\left(\frac{u}{U_\infty} = \frac{y}{\delta}\right)$ for which the laminar boundary layer thickness is expressed as $\delta = \frac{3.5x}{\sqrt{Re_x}}$. For water, density = 1000 kg/m^3 and dynamic viscosity = 0.001 kg/m.s . Net drag force (in N, rounded off to two decimal places) acting on the plate, neglecting the end effects, is _____.

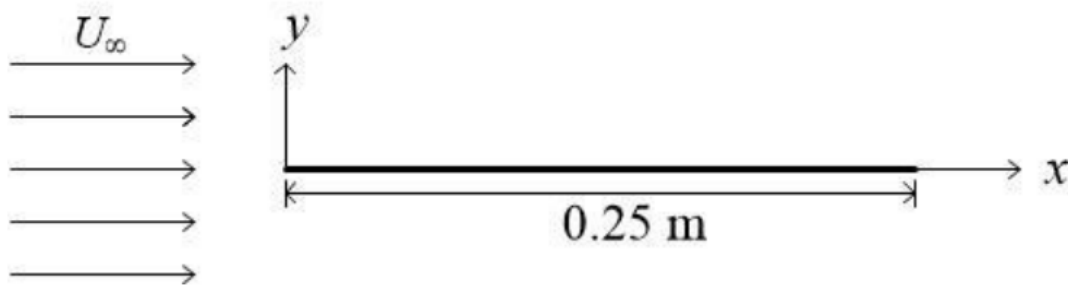


Fig. 20: Flow over thin flat plate

(GATE 2023 XE)

- 21) Axial velocity profile $u(r)$ for an axisymmetric flow through a circular tube of radius R is given as, $\frac{u(r)}{U} = \left(1 - \frac{r}{R}\right)^{1/n}$ where U is the centerline velocity. If V refers to the area-averaged velocity (volume flow rate per unit area), then the ratio V/U for $n = 1$ (rounded off to two decimal places) is _____.
(GATE 2023 XE)

- 22) A stationary circular pipe of radius $R = 0.5$ m is half filled with water (density = 1000 kg/m^3), whereas the upper half is filled with air at atmospheric pressure, as shown in the figure. Acceleration due to gravity is $g = 9.81 \text{ m/s}^2$. The magnitude of the force per unit length (in kN/m, rounded off to one decimal place) applied by water on the pipe section AB is _____.

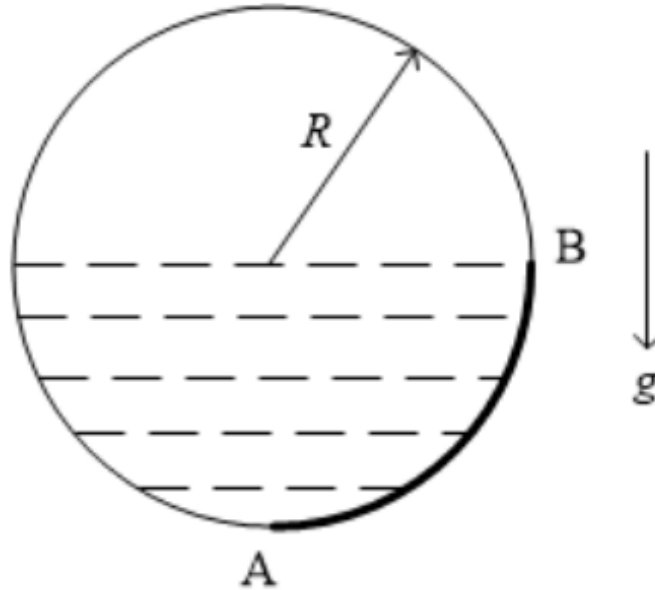


Fig. 22: Hydrostatic force on pipe section AB

(GATE 2023 XE)

END OF SECTION-B

SOLID MECHANICS

- 1) A plane truss is simply supported at P and R as shown. A downward force F is applied at hinge Q. The axial force developed in member PS is

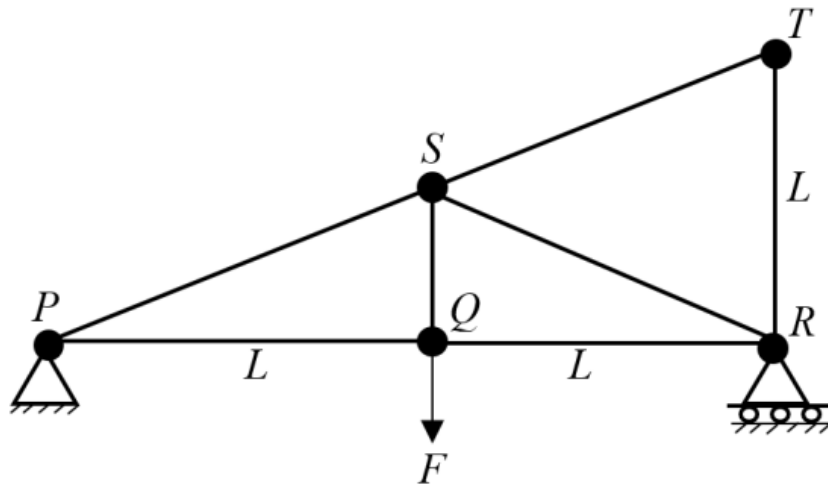


Fig. 1: Plane truss with supports at P and R, load at Q

(GATE 2023 XE)

- a) $\frac{\sqrt{5}}{2} F$ Tensile
 b) $\frac{\sqrt{5}}{2} F$ Compressive
 c) $\sqrt{5} F$ Tensile
 d) $\sqrt{5} F$ Compressive
- 2) A massless rigid rod OP of length L is hinged frictionlessly at O. A concentrated mass m is attached to end P of the rod. Initially, the rod OP is horizontal. Then, it is released from rest. There is gravity as shown. The rod acquires an angular velocity as it swings. The clockwise angular velocity of the rod, when it first reaches the vertical position as shown, is

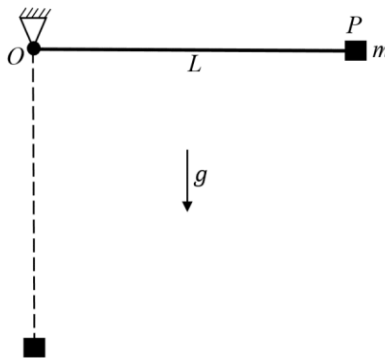


Fig. 2: Pendulum-like rigid rod OP with mass m at P

(GATE 2023 XE)

- a) $2\sqrt{\frac{g}{L}}$
 b) $\sqrt{\frac{2g}{L}}$
 c) $\sqrt{\frac{g}{L}}$
 d) $\frac{1}{2}\sqrt{\frac{g}{L}}$

- 3) Two equivalent descriptions of the state of stress at a point are shown in the figure. The normal stresses σ_1 and σ_2 as shown on the right must be, respectively,

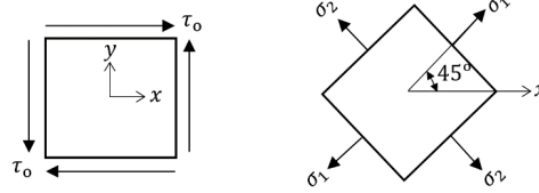


Fig. 3: Equivalent stress states at a point

(GATE 2023 XE)

- a) τ_0 and $-\tau_0$
 b) $-\tau_0$ and τ_0
 c) $\frac{\tau_0}{\sqrt{2}}$ and $-\frac{\tau_0}{\sqrt{2}}$
 d) $-\frac{\tau_0}{\sqrt{2}}$ and $\frac{\tau_0}{\sqrt{2}}$
- 4) The state of strain at a point in a machine component is given as $\varepsilon_{xx} = 2.5 \times 10^{-4}$, $\varepsilon_{yy} = 2.0 \times 10^{-4}$, $\varepsilon_{zz} = -1.5 \times 10^{-4}$, $\varepsilon_{xy} = 2.5 \times 10^{-4}$, $\varepsilon_{yz} = -0.5 \times 10^{-4}$, $\varepsilon_{zx} = -1.0 \times 10^{-4}$. The volumetric strain at this point is
 (GATE 2023 XE)
- a) 4×10^{-4}
 b) 3×10^{-4}
 c) -5×10^{-4}
 d) -3×10^{-4}
- 5) A thin walled, closed cylindrical vessel of inside diameter d and wall thickness t contains a fluid under pressure p . The figure below shows a part of the cylindrical vessel; end caps are not shown. Consider the small element shown with sides parallel and perpendicular to the axis of the cylinder. The stresses σ_1 and σ_2 are
 (GATE 2023 XE)

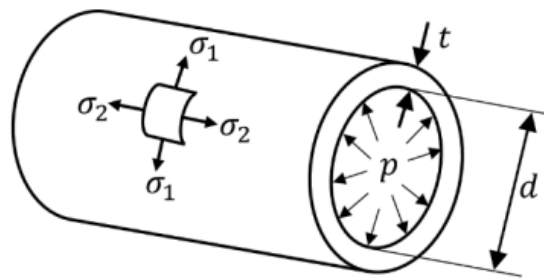


Fig. 5: Thin-walled cylinder element and stresses

- a) $\sigma_1 = \frac{pd}{2t}$; $\sigma_2 = \frac{pd}{4t}$
 b) $\sigma_1 = \frac{pd}{t}$; $\sigma_2 = \frac{pd}{2t}$
 c) $\sigma_1 = \frac{pd}{4t}$; $\sigma_2 = \frac{pd}{2t}$
 d) $\sigma_1 = \frac{pd}{2t}$; $\sigma_2 = 0$

- 6) A spring mass system is shown in the figure below. Take the acceleration due to gravity as $g = 9.81 \text{ m/s}^2$. The static deflection due to weight and the time period of oscillations, respectively, are (GATE 2023 XE)

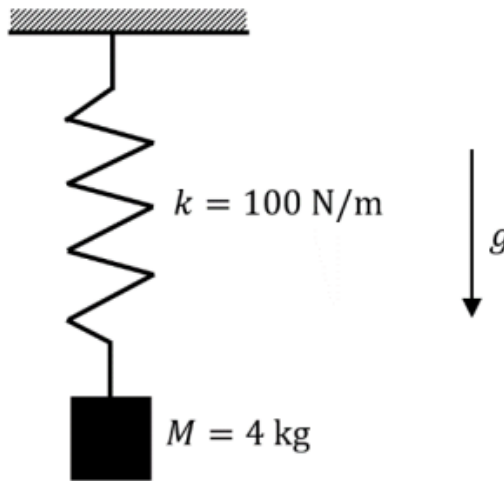


Fig. 6: Spring-mass system

- a) 0.392 m and 1.26 s
 b) 0.392 m and 3.52 s
 c) 0.626 m and 1.26 s
 d) 0.626 m and 3.52 s
- 7) A rod is subjected to three forces as shown in the figure on the left. An equivalent force system with forces F_1 , F_2 and moment M is shown in the figure on the right. The value of M (in N-m) is _____ (rounded off to one decimal place). (GATE 2023 XE)

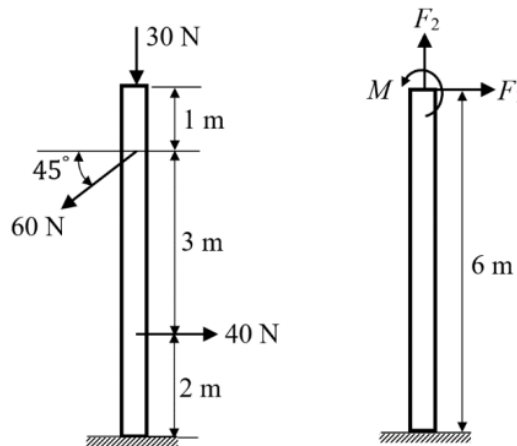


Fig. 7: Original and equivalent force systems on a rod

- 8) A simply supported beam of length 3 m is loaded as shown in the figure. The magnitude of the shear force (in kN) at the mid-point of the beam is _____(rounded off to one decimal place).

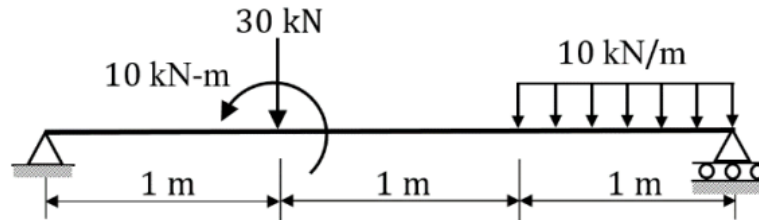


Fig. 8: Simply supported beam with loading

(GATE 2023 XE)

- 9) For a plane stress problem, the principal stresses are 100 MPa and 50 MPa. The magnitude of maximum shear stress (in MPa) in the material is _____(rounded off to one decimal place).
(GATE 2023 XE)
- 10) A solid uniform rigid disk of mass m and radius R rolls without slipping along a horizontal surface PQ. The speed of the center of the disk is v . The disk then strikes a hurdle of height $\frac{3R}{20}$ at point S. During the impact, there is no rebound or slip at S and no impulse from the surface PQ. The magnitude of the velocity of the center of the disk immediately after the impact is

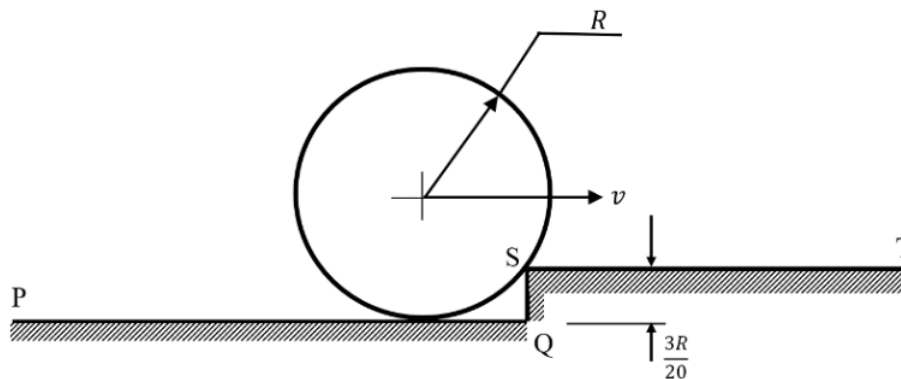


Fig. 10: Rolling disk striking a hurdle

(GATE 2023 XE)

- | | |
|-----------|-----------|
| a) $0.1v$ | c) $0.7v$ |
| b) $0.3v$ | d) $0.9v$ |

- 11) A cylinder made of rubber (length = L and diameter = d) is inserted in a rigid container as shown in the figure. The rubber cylinder fits snugly in the rigid container. There is no wall friction. The modulus of elasticity of the rubber is E and its Poisson's ratio is ν . The cylinder is subjected to a small uniform pressure p as shown in the figure. The resulting axial strain (ϵ_{zz}) is

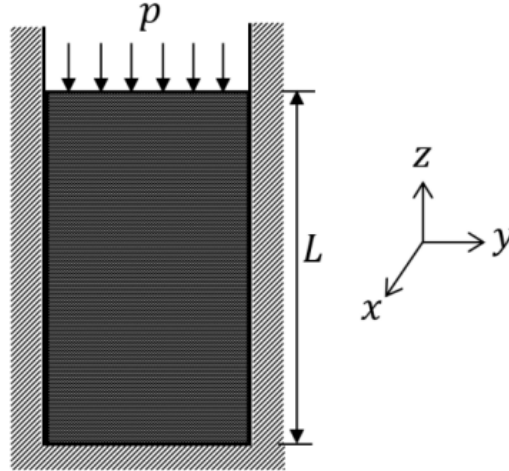


Fig. 11: Rubber cylinder confined in rigid container under pressure

(GATE 2023 XE)

- a) $-\frac{p}{E}$
b) $-\frac{p}{E(1-2\nu)}$
c) $-\frac{p}{E} \frac{(1+\nu)(1-2\nu)}{(1-\nu)}$
d) $-\frac{p}{E} \frac{(1-\nu)(1-2\nu)}{(1+\nu)}$

- 12) The state of stress at the critical location in a structure is $\sigma_{xx} = 420$ MPa, $\sigma_{yy} = 100$ MPa, $\sigma_{zz} = \sigma_{xy} = \sigma_{yz} = \sigma_{zx} = 0$. The yield stress of the material in uniaxial tension is 400 MPa. Select the correct statement among the following. (GATE 2023 XE)

- a) The structure is safe by both Tresca (maximum shear stress) theory and von-Mises (distortion energy) theory.
b) The structure is safe by Tresca (maximum shear stress) theory and unsafe by von-Mises (distortion energy) theory.
c) The structure is unsafe by Tresca (maximum shear stress) theory and safe by von-Mises (distortion energy) theory.
d) The structure is unsafe by both Tresca (maximum shear stress) theory and von-Mises (distortion energy) theory.

- 13) The figure shows a column of rectangular cross section $100 \text{ mm} \times 80 \text{ mm}$. It carries a load of 60 kN at a point 30 mm from the edge PQ . The values of stress component σ_{zz} on surfaces $PQQ'P'$ and $SRR'S'$, at points far away from both ends of the column, are respectively

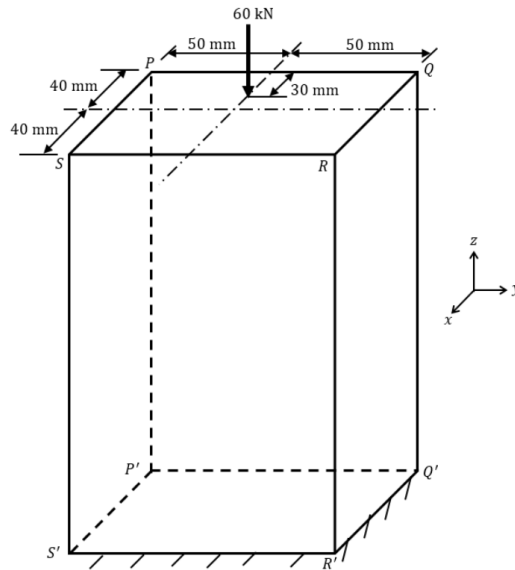


Fig. 13: Eccentrically loaded rectangular column

(GATE 2023 XE)

- a) 18.75 N/mm^2 (Compressive) and 3.75 N/mm^2 (Tensile) c) 13.13 N/mm^2 (Compressive) and 1.88 N/mm^2 (Tensile)
 b) 18.75 N/mm^2 (Compressive) and 3.75 N/mm^2 (Compressive) d) 13.13 N/mm^2 (Compressive) and 1.88 N/mm^2 (Compressive)
- 14) Consider an electric pole with dimensions as shown in the figure. Let the end R be subjected to a vertical force F . The flexural rigidity of both vertical and horizontal bars is EI . Neglect the axial deflection of the vertical bar, and all effects of self-weight. The vertical deflection at end R is

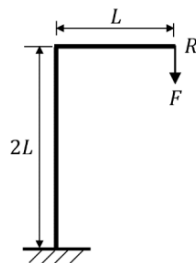


Fig. 14: Frame representing an electric pole under load at R

(GATE 2023 XE)

- a) $\frac{7FL^3}{3EI}$ c) $\frac{5FL^3}{3EI}$
 b) $\frac{10FL^3}{3EI}$ d) $\frac{8FL^3}{3EI}$

- 15) A uniform cantilever beam has flexural rigidity EI and length L . It is subjected to a concentrated force F and moment $M = 2FL$ at the free end as shown. The deflection (δ) at the free end is

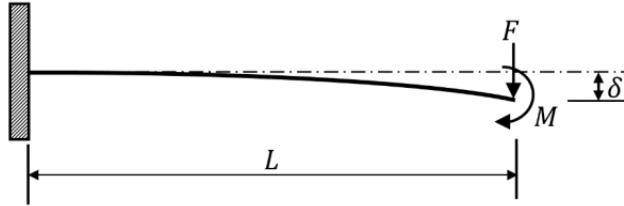


Fig. 15: Cantilever with end force F and end moment $2FL$

(GATE 2023 XE)

- a) $\frac{11FL^3}{12EI}$ c) $\frac{4FL^3}{3EI}$
 b) $\frac{8FL^3}{9EI}$ d) $\frac{7FL^3}{6EI}$

- 16) A steel ball of mass $m = 10$ kg is suspended from the ceiling of a moving carriage by two inextensible strings making 60° with the horizontal as shown. The carriage has an acceleration a such that the tension in the string on the right is double the tension in the string on the left. Take the acceleration due to gravity (g) as 10 m/s^2 . The acceleration a (in m/s^2) is _____(rounded off to one decimal place).

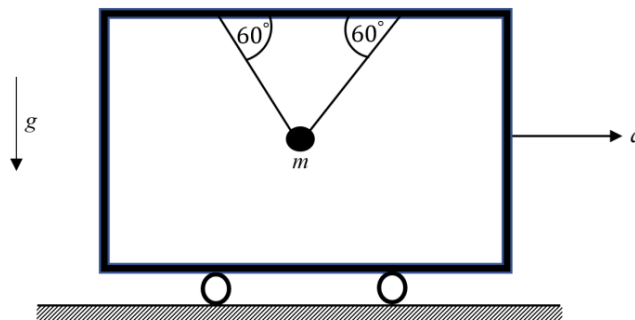


Fig. 16: Mass suspended by two strings in an accelerating carriage

(GATE 2023 XE)

- 17) A block of mass $m = 10 \text{ kg}$ is lying on an inclined plane PQ. The mass is restrained from sliding down the inclined plane by a force F . The coefficient of friction between the block and the inclined plane is 0.3. Take the acceleration due to gravity as 10 m/s^2 . The smallest force F (in N) required to prevent the block from sliding down is _____ (rounded off to one decimal place).

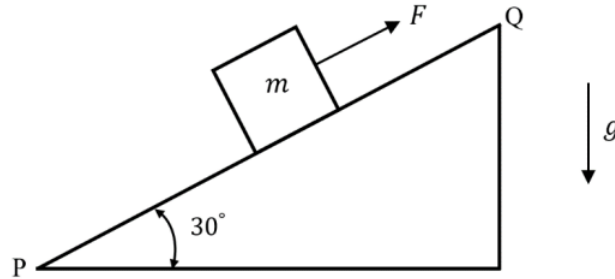


Fig. 17: Block on rough inclined plane held by force F

(GATE 2023 XE)

- 18) A spherical rigid ball of mass 10 kg is moving with a speed of 2 m/s in the direction shown. The ball collides with a rigid frictionless wall and rebounds at an angle α with a speed of v , as shown. The coefficient of restitution is 0.9. The angle α (in degrees) is _____ (rounded off to one decimal place).

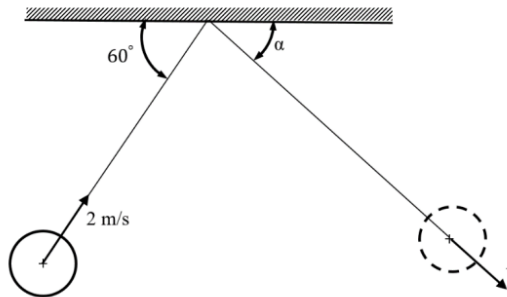


Fig. 18: Oblique impact of a ball with a frictionless wall

(GATE 2023 XE)

- 19) A thin steel plate is loaded in the x-y plane as shown in the figure. Take the Poisson's ratio of steel to be 0.3 and the modulus of elasticity of steel to be 200 GPa. The strain along the z-direction is $\varepsilon_{zz} = -3 \times 10^{-4}$. The value of σ_{yy} (in MPa) is _____ (rounded off to one decimal place).

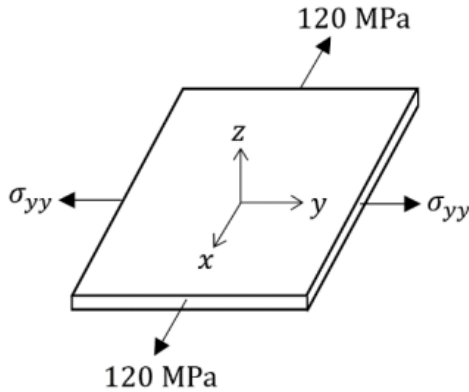


Fig. 19: In-plane loading of a thin steel plate

(GATE 2023 XE)

- 20) A composite rod made of steel and copper is fixed immovably at its ends as shown in the figure. The length of each portion of the rod is 1 m as shown. The cross-sections of both portions are the same. The moduli of elasticity of steel and copper are 200 GPa and 100 GPa, respectively. The coefficients of thermal expansion of steel and copper are $12 \times 10^{-6}/^{\circ}C$ and $18 \times 10^{-6}/^{\circ}C$, respectively. The composite rod is initially stress free. Then, the temperature of the composite rod is increased by $100^{\circ}C$. The magnitude of axial stress (in MPa) developed in the steel rod is _____ (rounded off to one decimal place).

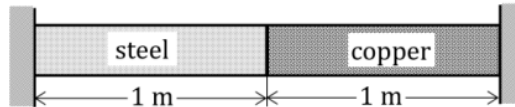


Fig. 20: Bi-material composite rod fixed at ends

(GATE 2023 XE)

- 21) A slender uniform elastic rod of length 1 m and of solid circular cross-section of diameter 50 mm is originally straight. It is then loaded by equal and opposite end moments as indicated in the figure. The resulting lateral displacement of the mid-point of the rod is 10 mm (displacements are exaggerated in the figure). The maximum longitudinal strain in the rod is $p \times 10^{-3}$, where p is _____ (rounded off to one decimal place).

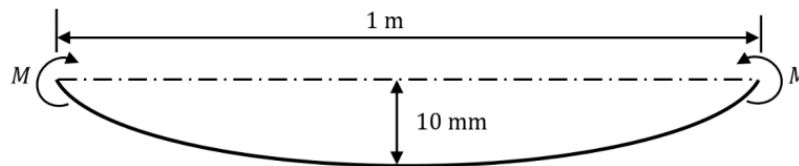


Fig. 21: Slender elastic rod under equal and opposite end moments

(GATE 2023 XE)

- 22) Consider a solid cylindrical shaft and a hollow cylindrical shaft. Both shafts are axisymmetric and elastic, and have the same cross-sectional area. The hollow shaft has an outside diameter of 150 mm and an inside diameter of 120 mm. When both the shafts are twisted by the same twisting moment, the ratio of maximum shear stress developed in the hollow shaft (τ_h) to maximum shear stress developed in the solid shaft (τ_s) will be _____ (rounded off to three decimal places).
(GATE 2023 XE)

END OF SECTION-C

THERMODYNAMICS

- 1) A: The number of properties required to fix the state of a system is given by 'state postulate'.
 R: The state of a simple compressible system is completely specified by two independent, intensive properties.
 About the statements A and R applied to a single-phase system, (GATE 2023 XE)
- a) A is correct and R is incorrect. c) Both A and R are incorrect.
 b) A is incorrect and R is correct. d) Both A and R are correct.
- 2) Which of the following is an extensive property of a system? (GATE 2023 XE)
- a) Density c) Temperature
 b) Pressure d) Total mass
- 3) A tank of volume V contains homogeneous mixture of two ideal gases, A and B at a temperature T and a pressure P . The mixture contains n_A moles of gas A and n_B moles of gas B. If P_A and P_B are the partial pressures of gas A and gas B, respectively, then (GATE 2023 XE)
- a) $P_A = \frac{n_A}{n_A + n_B}P$, $P_B = \frac{n_B}{n_A + n_B}P$ c) $P_A = \frac{n_A}{n_B}P$, $P_B = \frac{n_B}{n_A}P$
 b) $P_A = \frac{n_B}{n_A}P$, $P_B = \frac{n_A}{n_B}P$ d) $P_A = \frac{n_B n_B}{n_A + n_B}P$, $P_B = \frac{n_A}{n_A + n_B}P$
- 4) If an ideal air-standard Otto cycle and an ideal air-standard Diesel cycle operate on the same compression ratio, then the relation between the thermal efficiencies (η_{th}) of the cycles is (GATE 2023 XE)
- a) $\eta_{th,Otto} = \eta_{th,Diesel}$ and $\eta_{th,Otto} < 1$ c) $\eta_{th,Otto} < \eta_{th,Diesel}$
 b) $\eta_{th,Otto} > \eta_{th,Diesel}$ d) $\eta_{th,Otto} = \eta_{th,Diesel} = 1$
- 5) The following statements are given:
 (i) The third law of thermodynamics deals with the entropy of a substance at the absolute zero temperature.
 (ii) Entropy of any non-crystalline structure is zero at absolute zero temperature.
 (iii) At the absolute zero temperature, the crystal structure has maximum degree of order.
 (iv) The thermal energy of the substance at absolute zero temperature is maximum.
 The correct option describing these statements is (GATE 2023 XE)
- a) Only (i) is correct c) Both (i) and (iii) are correct
 b) Only (ii) is correct d) Both (i) and (iv) are correct
- 6) Adiabatic bulk modulus of a substance is defined as (GATE 2023 XE)
- a) $-\frac{1}{v} \left(\frac{\partial v}{\partial P} \right)_T$ c) $-\frac{1}{v} \left(\frac{\partial v}{\partial P} \right)_s$
 b) $-v \left(\frac{\partial P}{\partial v} \right)_T$ d) $-v \left(\frac{\partial P}{\partial v} \right)_s$

13) Match the following:

TABLE 13: Matching thermodynamic functions/equations with their corresponding expressions

Thermodynamic function/equation	Expression
A1) Helmholtz function	B1) $\left(\frac{d}{dT} \ln P\right)_{\text{sat}} = \frac{h_g - h_f}{RT^2}$
A2) Gibbs function	B2) $u - Ts$
A3) T-ds equation	B3) $du = Tds - Pdv$
A4) Clapeyron-Clausius equation	B4) $h - Ts$

(GATE 2023 XE)

a) A1→B2, A2→B4, A3→B1, A4→B3

c) A1→B2, A2→B4, A3→B3, A4→B1

b) A1→B4, A2→B2, A3→B1, A4→B3

d) A1→B4, A2→B2, A3→B3, A4→B1

14) A piston-cylinder device initially contains 1 m^3 of air at 200 kPa and 25°C . Air expands at constant pressure while a heater of 250 W is switched on for 10 minutes. There is a heat loss of 4 kJ during this process. Assuming air as an ideal gas, the final temperature of air is _____ $^\circ\text{C}$ (rounded off to one decimal place).

Use the following data for air: $R = 0.287 \text{ kJ/kg}\cdot\text{K}$, $c_p = 1.005 \text{ kJ/kg}\cdot\text{K}$ (GATE 2023 XE)

15) Steam at 2 MPa and 300°C steadily enters a nozzle of inlet diameter of 20 cm. Steam leaves the nozzle with a velocity of 300 m/s. The mass flow rate of steam through the nozzle is 10 kg/s. Assume no work interaction and no change in potential energy. If the heat loss from the nozzle per kg of steam is 3 kJ, the exit enthalpy per kg of steam is _____ kJ (rounded off to nearest integer).

Use the following data for steam: At 2 MPa and 300°C : $v = 0.12551 \text{ m}^3/\text{kg}$, $h = 3024.2 \text{ kJ/kg}$ (GATE 2023 XE)

16) A rigid tank of 2 m^3 internal volume contains 5 kg of water as a saturated liquid-vapor mixture at 400 kPa. Half of the mass of the saturated liquid in the tank is drained-off while maintaining constant pressure of 400 kPa in the tank. The final quality of the mixture remaining in the tank is _____ (rounded off to two decimal places).

(GATE 2023 XE)

17) Consider a spark ignition engine which operates on an ideal air-standard Otto cycle. It uses a fuel which produces 44 MJ/kg of heat in the engine. If the engine requires 40 mg of fuel to produce 1 kJ of work output, then the compression ratio of the Otto cycle is _____ (rounded off to two decimal places).

For the entire cycle, use $c_p/c_v = 1.4$

(GATE 2023 XE)

18) A refrigerator operates on an ideal vapor compression cycle between the pressure limits of 140 kPa and 800 kPa. The working fluid is the refrigerant R-134a. The refrigerant enters the compressor as saturated vapor at 140 kPa and exits at 800 kPa and 60°C . It leaves the condenser as a saturated liquid at 800 kPa. The coefficient of performance (COP) of the refrigerator is _____ (rounded off to two decimal places).

(GATE 2023 XE)

19) A steam power plant operates on a simple ideal Rankine cycle. The condenser pressure is 10 kPa and the boiler pressure is 5 MPa. The steam enters the turbine at 600°C . Mass flow rate of the steam is 50 kg/s. Neglecting the pump work, the net power output of the plant is _____ MW (rounded off to one decimal place).

(GATE 2023 XE)

- 20) In an air-conditioning system, air enters at 20°C and 30% relative humidity at a steady rate of $30\text{ m}^3/\text{min}$ in a humidifier and it is conditioned to 25°C and 60% relative humidity. Assuming entire process takes place at pressure of 100 kPa , the mass flow rate of the steam added to air in the humidifier is _____ kg/min (rounded off to three decimal places).
(GATE 2023 XE)
- 21) An office uses a heat pump to receive 500 kJ/day heat in winter to maintain its temperature at 300 K . The ambient temperature is 280 K . If the COP of the heat pump is 60% of its theoretical maximum value, the ratio of actual work input to the minimum theoretical work input to the heat pump is _____ (rounded off to one decimal place). (GATE 2023 XE)
- 22) In a liquid-vapour phase change process, $\left(\frac{dP}{dT}\right)$ at 100°C for saturated water is 3750 Pa/K . If the resulting change in specific volume $(v_g - v_f)$ is $1.672\text{ m}^3/\text{kg}$, the enthalpy of vaporization (h_{fg}) will be _____ kJ/kg (in integer). (GATE 2023 XE)

END OF SECTION-D

POLYMER SCIENCE AND ENGINEERING

- 1) Which one of the monomers given is used in the synthesis of cellulose? (GATE 2023 XE)
- a) Fructose
b) Lactic acid
c) Galactose
d) Glucose
- 2) A copper wire upon loading instantaneously increases in length to l , and then continues to elongate gradually. Upon unloading, the wire retracts to length l . According to the Maxwell model, which one of the options given correctly relates the total strain E , the applied stress S , the modulus G , the material's resistance to flow η , and the elapsed time t between loading and unloading? (GATE 2023 XE)
- a) $E = (S/G) - (S/\eta)t$
b) $E = (S/G) \times (S/\eta)t$
c) $E = (S/G) + (S/\eta)t$
d) $E = (S/G) / (S/\eta)t$
- 3) Consider the structure of a cross-linked polymer shown in the figure. From the options given, identify the monomers that are used in the synthesis of the polymer. (GATE 2023 XE)

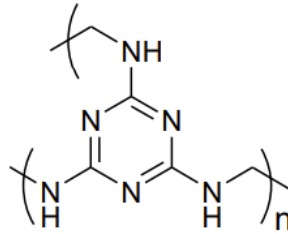


Fig. 3: Structure of a crosslinked polymer used to identify constituent monomers

- a) Melamine and Benzaldehyde
b) Melamine and Acetone
c) Melamine and Formaldehyde
d) Melamine and Ethanol
- 4) Among the options given, choose the most suitable compatibilizer for blending Polyvinylidene fluoride (PVDF) and Acrylonitrile butadiene styrene (ABS). (GATE 2023 XE)
- a) Styrene-acrylonitrile (SAN)
b) Polybutadiene (PB)
c) Polymethyl methacrylate (PMMA)
d) Nylon 6
- 5) A high molecular weight polymer passes through different zones from the hopper to the die in an extruder. Among the options given, identify the correct match between the zones and their key functions. (GATE 2023 XE)

TABLE 5: Matching extruder zones with their key functions

Zones	Key functions
P Metering zone	1 High shear forces for effective mixing
Q Compression zone	2 Receives the charge or feed
R Feed zone	3 Melts the charge or feed through heat conducted by the heating element
S Working zone	4 The charge or feed acquires a constant flow rate imparted by the helical flight of the screw

- a) P-4; Q-3; R-2; S-1
b) P-3; Q-4; R-1; S-2

- c) P-4; Q-1; R-2; S-3
d) P-3; Q-1; R-2; S-4

6) Polymer wetting is improved by the addition of fillers with functional groups. In a typical case-study, natural-clay was modified with hydroxyl groups and compounded with Nylon 6 along with an antioxidant. The resulting composite exhibited poor mechanical properties. Which one among the options given explains this observation? (GATE 2023 XE)

- a) The surface functional groups of the filler reacted with Nylon 6
- b) The antioxidant degraded during the processing
- c) The surface functional groups of the filler formed hydrogen bonds with the antioxidant
- d) The antioxidant reacted with Nylon 6

7) Among the options given, identify the correct match between the polymers and their glass transition temperatures (T_g). (GATE 2023 XE)

TABLE 7: Matching polymers with their glass transition temperatures (T_g)

Polymer	Glass transition temperature (°C)
P. High density polyethylene	1. >200
Q. Poly(vinyl carbazole)	2. 145 to 155
R. Polymethyl methacrylate	3. -100 to -80
S. Polycarbonate	4. 90 to 100

- a) P-2; Q-4; R-3; S-1
b) P-3; Q-1; R-4; S-2

- c) P-3; Q-4; R-1; S-2
d) P-4, Q-2; R-1; S-3

8) What is the correct order of decreasing crystallinity of the given polymers? (GATE 2023 XE)

P atactic-Polypropylene Q syndiotactic-Polystyrene
R Nylon 6 S Polyethylene terephthalate

- a) $P > R > S > Q$
b) $S > Q > P > R$

- c) $Q > S > R > P$
d) $S > R > Q > P$

- 9) Choose the correct option that best correlates the graphs with the polymerization methods. (GATE 2023 XE)

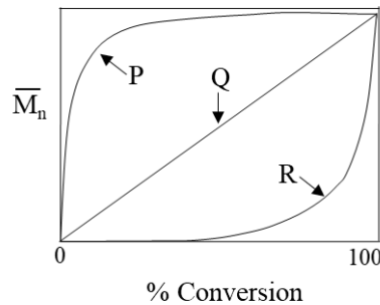


Fig. 9: Graphs to be matched with polymerization methods

- a) P – living polymerization; Q – chain growth; R – step growth
 b) P – chain growth; Q – living polymerization; R – step growth
 c) P – step growth; Q – living polymerization; R – chain growth
 d) P – living polymerization; Q – step growth; R – chain growth
- 10) From the options given, identify the correct match(es) between the polymer products with the most appropriate processing technique. (GATE 2023 XE)

TABLE 10: Matching polymer products with processing techniques

Polymer product	Processing technique
P. Fishing rods	1. Compression moulding
Q. Soft drink bottles	2. Thermoforming
R. Plastic sheets	3. Pultrusion
S. Plastic trays	4. Blow moulding

- a) P-3; Q-4; R-1; S-2
 b) P-3; Q-2; R-1; S-4
 c) P-1; Q-2; R-3; S-4
 d) P-3; Q-4; R-1; S-1
- 11) Among the options given, which agents are used to vulcanize or cure rubbers? (GATE 2023 XE)
- a) Dicumyl peroxide
 b) Zinc stearate
 c) Carbon black
 d) Dinitrobenzene
- 12) Lipase is a natural enzyme, which cleaves carboxylic ester bonds. Among the options given, identify the polymer(s) degraded by lipase. (GATE 2023 XE)
- a) Polypropylene (PP)
 b) Polycaprolactone (PCL)
 c) Polyvinylidene fluoride (PVDF)
 d) Polyethylene terephthalate (PET)

- 13) Among the options given, identify the correct pair(s) of catalyst and co-catalyst that form a Ziegler-Natta catalyst.

(GATE 2023 XE)

- a) TiCl_3 and $\text{Al}(\text{CH}_3\text{CH}_2)_2\text{Cl}$ c) TiO_2 and $\text{Al}(\text{CH}_3)_3$
 b) ZnCl_2 and $\text{Al}(\text{CH}_3)_3$ d) VCl_4 and $\text{Al}(\text{CH}_3\text{CH}_2)_2\text{Cl}$

- 14) Mechanical stress is applied on a polymer. Identify the correct match(es) between the statements (1, 2, 3, 4, 5) that describe the deformations and the regimes (P, Q, R). (GATE 2023 XE)

TABLE 14: Matching deformation statements with viscoelastic regimes

Regime	Statements
P. Rubbery regime	1. Stress-relaxation takes place and the excess free energy is dissipated
Q. Region around glass transition temperature (T_g)	2. The motions of the molecules are long-range
R. Sample under deformed state	3. Segmental motion of the molecules is important
	4. The maximum relaxation time is strongly dependent on the molecular weight
	5. The deformations are independent of the molecular weight and primarily depend on the local

- a) P-2; Q-5; R-1 c) P-2; Q-3; R-4
 b) P-1; Q-5; R-1 d) P-4; Q-3; R-1

- 15) Stress versus elongation profiles for different polymeric materials are shown in the figure. Choose the combination that best describes these profiles. (GATE 2023 XE)

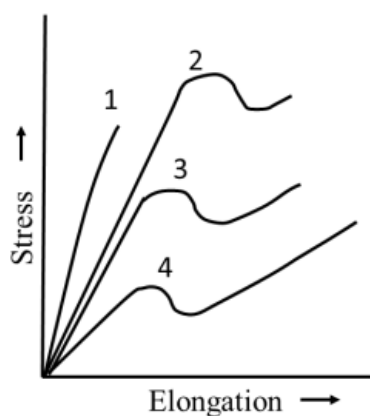


Fig. 15: Stress–elongation profiles for different polymeric materials

- a) 1-Nylon fibers; 2-Polyethylene; 3-Vulcanized rubber; 4-Polystyrene c) 1-Polystyrene; 2-Nylon fibers; 3-Polyethylene; 4-Vulcanized rubber
 b) 1-Polyethylene; 2-Vulcanized rubber; 3-Polystyrene; 4-Nylon fibers d) 1-Vulcanized rubber; 2-Polyethylene; 3-Nylon fibers; 4-Polystyrene

- 16) Among the options given, which method(s) is/are used for the synthesis of atactic polystyrene? (GATE 2023 XE)

- a) Free radical polymerization c) Polycondensation
 b) Ring opening polymerization d) Ionic polymerization

- 17) A nylon sample of 0.03 m² cross-sectional area is subjected to a creep load of 10 kN. The load is removed after a duration of 60 s. Young's modulus and the viscosity for nylon are 1 GPa and 300 Giga Poise. The compliance of the specimen is _____ $\times 10^{-9}$ m²/N. (Answer in integer)
(GATE 2023 XE)
- 18) Polyvinylidene fluoride (PVDF) was quenched from the melt in one case and in the other case, it was slowly cooled from the melt at 10 °C/min. The percentage crystallinity of the slowly cooled PVDF is 60%. The heat of fusion for the quenched PVDF is $0.5\Delta H_m$ (ΔH_m is the heat of fusion for the slowly cooled PVDF), and the heat of fusion for 100% crystalline PVDF is 100 J/g. The percentage crystallinity of the quenched PVDF is _____. (Answer in integer)
(GATE 2023 XE)
- 19) A polymeric material of density 0.9 g/cc and melt volume of 10 cc in an extruder has a residence time of 100 s. The output of the extruder is _____ kg/h. (Rounded off to two decimal places)
(GATE 2023 XE)
- 20) A polymer weighing 0.2 g is dissolved in 100 ml of benzene and has a relative viscosity of 1.5. The polymer obeys Mark-Houwink equation with constants $a = 0.5$ and $K = 0.001$. The molecular weight of the polymer is _____ $\times 10^{10}$ g/mol. (Rounded off to two decimal places)
(GATE 2023 XE)
- 21) A continuous and aligned glass-fiber reinforced composite consists of 40 vol% of glass-fiber having a modulus of elasticity of 69 GPa and 60 vol% of a polyester resin, which when hardened, displays a modulus of 3.4 GPa. The modulus of elasticity of this composite in the longitudinal direction is _____ GPa. (Rounded off to two decimal places)
(GATE 2023 XE)

TABLE 21: Table-5

No. of Molecules	Molar Mass g/mol
100	7500
50	5000

The resulting weight average molecular weight of the polymer is _____ g/mol. (Answer in integer)
(GATE 2023 XE)

END OF SECTION-E