## Math Routing Agent Final Proposal

### Overview

built a math tutoring agent that behaves like a patient instructor: it solves problems step by step, checks an internal knowledge base first, and falls back to a focused web search when needed. It improves over time using student feedback.

## Results at a glance

- Accuracy on challenging JEE-level problems: 80%
- Average response time: 4.6 seconds
- Non-math queries blocked: 100%
- Runtime stability during testing: no observed errors

# 1) Privacy & Safety Guardrails

To keep the system strictly educational and protect students, I used NeMo Guardrails to allow only math-related content.

### How it behaves

- Allows questions like "What is the derivative of  $x^2$ ?" or "Solve: 2x + 5 = 11."
- Redirects anything outside mathematics with a polite message.
- Avoids collecting or processing personal information.

## Why this matters

- Keeps students on task
- Preserves privacy
- Reduces wasted compute on irrelevant prompts
- Minimizes misuse

During testing, the guardrails filtered out all non-math inputs.

# 2) Knowledge Base

Dataset: GSM8K (selected 100 word problems with step-by-step solutions)

# Implementation details

- Stored in **Qdrant** for fast similarity search
- Uses Google embeddings for semantic matching
- Automatically updates when improved answers are created from feedback

# **Examples to try**

- "Janet's ducks lay 16 eggs per day... how much does she make daily?"
- "A recipe needs 3 cups flour and 2 cups sugar. For 9 cups flour, how much sugar?"
- "A jacket is \$80, price increases 25%, then a 20% discount. What's the final price?"

# 3) Web Search via MCP

When the knowledge base doesn't suffice, the agent queries the web through a custom **Model Context Protocol (MCP)** server tuned for math topics.

### **Process**

- 1. Augments queries with math-specific context
- 2. Uses **Tavily** to prioritize high-quality educational sources
- 3. Filters for precise mathematical explanations
- 4. Handles failures gracefully with clear error messages

### Stress tests

- "What is the Riemann Hypothesis and why is it important?"
- "Latest quantum computing algorithms for factorization?"
- "How is differential geometry used in general relativity?"

Observed success rate: ~95% with total response times of 6–8 seconds when a web search is required.

# 4) Human-in-the-Loop Learning

The agent incorporates student feedback to refine future answers.

## Feedback loop

- 1. Student asks a question → agent provides a step-by-step solution
- 2. Student responds (e.g., "step 3 isn't clear")
- 3. Agent regenerates or clarifies the explanation
- 4. The improved answer is saved back to the knowledge base

### What's tracked

Positive and negative feedback

- Which explanations students prefer
- · Coverage of topics over time

#### **Outcome**

Each interaction helps the system explain concepts more clearly to the next student.

## 5) JEE Benchmark Results

Setup: 10 hard problems across calculus, algebra, trigonometry, and linear algebra.

# Metric Result Interpretation

Accuracy 80% 8/10 correct

Avg. response time **4.6 s** Responsive for live tutoring

Error rate 0% No crashes or failures observed

Total runtime 51 s Efficient batch execution

## By subject

Calculus: 2/2 correct

Trigonometry: 2/2 correct

General Math: 3/4 correct

Algebra: 1/2 correct (priority area for further tuning)

## **Technical Architecture**

- FastAPI for the API layer
- Qdrant for vector search
- Google Gemini for mathematical reasoning
- LangGraph to orchestrate routing and tool use

• Custom MCP server for targeted math web search

These choices emphasize reliability, speed, and maintainability for classroom use.

# **Key Capabilities**

- Intelligent routing between knowledge base and web search
- Continuous improvement from student feedback
- Stable performance under test
- Low latency suitable for interactive sessions
- Strict topic guardrails for safety and focus
- Scales to multiple learners

## Conclusion

This agent delivers clear, step-by-step math help with strong accuracy and fast responses. It learns from feedback, stays within safe and relevant boundaries, and uses a robust architecture designed for real classrooms. It is ready for deployment and for continued improvement with real student interactions.