

ST405 Mini Project

S/18/841

2024-04-05

Introduction

The National Health and Nutrition Examination Survey (NHANES) conducted by the Centers for Disease Control and Prevention (CDC) gathers extensive health and nutritional information from a diverse U.S. population. In this study, we narrow our focus to predicting respondents' age by extracting a subset of features from the NHANES dataset. These features include physiological measurements, lifestyle choices, and biochemical markers, hypothesized to correlate strongly with age.

Methodology

Dataset Description: The dataset used in this study is derived from NHANES 2013-2014, comprising various health and nutritional data from the U.S. population. Key variables include "SEQN" (Respondent Sequence Number), "age_group" (Respondent's Age Group), "RIDAGEYR" (Respondent's Age), "RIAGENDR" (Respondent's Gender), "PAQ605" (Engagement in Physical Activities), "BMXBMI" (Body Mass Index), "LBXGLU" (Blood Glucose after Fasting), "DIQ010" (Diabetes Status), "LBXGLT" (Oral Glucose Tolerance Test), and "LBXIN" (Blood Insulin Levels).

Statistical Methods Employed: This analysis employs Exploratory Factor Analysis (EFA) and Confirmatory Factor Analysis (CFA). EFA uncovers underlying patterns and correlations among variables, while CFA validates the factor structure and assesses model fit. Descriptive statistics such as means, standard deviations, and correlations are computed to summarize the dataset and examine relationships between variables.

#Libraries

```
library(tidyverse)
```

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
```

```
## v dplyr      1.1.3      v readr      2.1.4
```

```
## v forcats    1.0.0      v stringr   1.5.0
```

```
## v ggplot2    3.4.3      v tibble    3.2.1
```

```
## v lubridate  1.9.3      v tidyr     1.3.0
```

```
## v purrr      1.0.2
```

```
## -- Conflicts ----- tidyverse_conflicts() --
```

```
## x dplyr::filter() masks stats::filter()
```

```
## x dplyr::lag()     masks stats::lag()
```

```
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
```

```
library(ggplot2)
```

```
library(psych)
```

```
## Warning: package 'psych' was built under R version 4.3.3
```

```
##
## Attaching package: 'psych'
##
## The following objects are masked from 'package:ggplot2':
##
##      %+%, alpha
```

```
library(corrplot)
```

```
## Warning: package 'corrplot' was built under R version 4.3.3
```

```
## corrplot 0.92 loaded
```

```
library(ggcorrplot)
```

```
## Warning: package 'ggcorrplot' was built under R version 4.3.3
```

```
library(GPArotation)
```

```
## Warning: package 'GPArotation' was built under R version 4.3.3
```

```
##
## Attaching package: 'GPArotation'
##
## The following objects are masked from 'package:psych':
##
##      equamax, varimin
```

```
library(nFactors)
```

```
## Warning: package 'nFactors' was built under R version 4.3.3
```

```
## Loading required package: lattice
##
## Attaching package: 'nFactors'
##
## The following object is masked from 'package:lattice':
##
##      parallel
```

```
library(factoextra)
```

```
## Warning: package 'factoextra' was built under R version 4.3.3
```

```
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
```

```
library(psych)
library(lavaan)
```

```
## Warning: package 'lavaan' was built under R version 4.3.3
```

```
## This is lavaan 0.6-17
## lavaan is FREE software! Please report any bugs.
##
## Attaching package: 'lavaan'
##
## The following object is masked from 'package:psych':
##
##     cor2cov
```

###Data Loading and Inspection

```
nhanes_data <- read.csv("../Data/NHANES_age_prediction.csv")
```

```
# View the structure of the dataset
str(nhanes_data)
```

```
## 'data.frame':    2278 obs. of  10 variables:
## $ SEQN      : num  73564 73568 73576 73577 73580 ...
## $ age_group: chr   "Adult" "Adult" "Adult" "Adult" ...
## $ RIDAGEYR  : num   61 26 16 32 38 50 14 57 75 43 ...
## $ RIAGENDR  : num    2 2 1 1 2 1 1 2 1 1 ...
## $ PAQ605    : num    2 2 2 2 1 2 2 2 2 1 ...
## $ BMXBMI    : num   35.7 20.3 23.2 28.9 35.9 23.6 38.7 38.3 38.9 28.9 ...
## $ LBXGLU    : num   110 89 89 104 103 110 94 107 89 90 ...
## $ DIQ010    : num    2 2 2 2 2 2 2 2 2 2 ...
## $ LBXGLT    : num   150 80 68 84 81 100 202 164 113 95 ...
## $ LBXIN     : num   14.91 3.85 6.14 16.15 10.92 ...
```

View summary statistics of the dataset

```
summary(nhanes_data)
```

```
##      SEQN      age_group      RIDAGEYR      RIAGENDR
## Min.   :73564  Length:2278    Min.    :12.0    Min.    :1.000
## 1st Qu.:76172  Class :character  1st Qu.:24.0    1st Qu.:1.000
## Median :78749  Mode  :character  Median :41.0    Median :2.000
## Mean   :78692                      Mean   :41.8    Mean   :1.511
## 3rd Qu.:81214                      3rd Qu.:58.0    3rd Qu.:2.000
## Max.   :83727                      Max.    :80.0    Max.    :2.000
##      PAQ605      BMXBMI      LBXGLU      DIQ010      LBXGLT
## Min.   :1.000    Min.   :14.50    Min.   : 63.00    Min.   :1.000    Min.   : 40
## 1st Qu.:2.000    1st Qu.:22.80    1st Qu.: 91.00    1st Qu.:2.000    1st Qu.: 87
## Median :2.000    Median :26.80    Median : 97.00    Median :2.000    Median :105
## Mean   :1.823    Mean   :27.96    Mean   : 99.55    Mean   :2.016    Mean   :115
## 3rd Qu.:2.000    3rd Qu.:31.20    3rd Qu.:104.00    3rd Qu.:2.000    3rd Qu.:130
## Max.   :7.000    Max.   :70.10    Max.   :405.00    Max.   :3.000    Max.   :604
##      LBXIN
## Min.   : 0.14
## 1st Qu.: 5.86
## Median : 9.04
## Mean   :11.83
## 3rd Qu.:14.44
## Max.   :102.29
```

```
# View the first few rows of the dataset
head(nhanes_data)
```

```
##      SEQN age_group RIDAGEYR RIAGENDR PAQ605 BMXBMI LBXGLU DIQ010 LBXGLT LBXIN
## 1 73564   Adult      61        2      2  35.7   110     2    150 14.91
## 2 73568   Adult      26        2      2  20.3    89     2     80  3.85
## 3 73576   Adult      16        1      2  23.2    89     2     68  6.14
## 4 73577   Adult      32        1      2  28.9   104     2     84 16.15
## 5 73580   Adult      38        2      1  35.9   103     2     81 10.92
## 6 73581   Adult      50        1      2  23.6   110     2    100  6.08
```

```
#Dimensions of the dataset
dim(nhanes_data)
```

```
## [1] 2278  10
```

```
# Check for missing values
colSums(is.na(nhanes_data))
```

```
##      SEQN age_group RIDAGEYR RIAGENDR PAQ605 BMXBMI LBXGLU DIQ010
##      0      0      0      0      0      0      0      0
##      LBXGLT LBXIN
##      0      0
```

```
###Data Preprocessing
# Select only numeric variables from the NHANES dataset
numerical_nhanes_data <- nhanes_data[, apply(nhanes_data, is.numeric)]

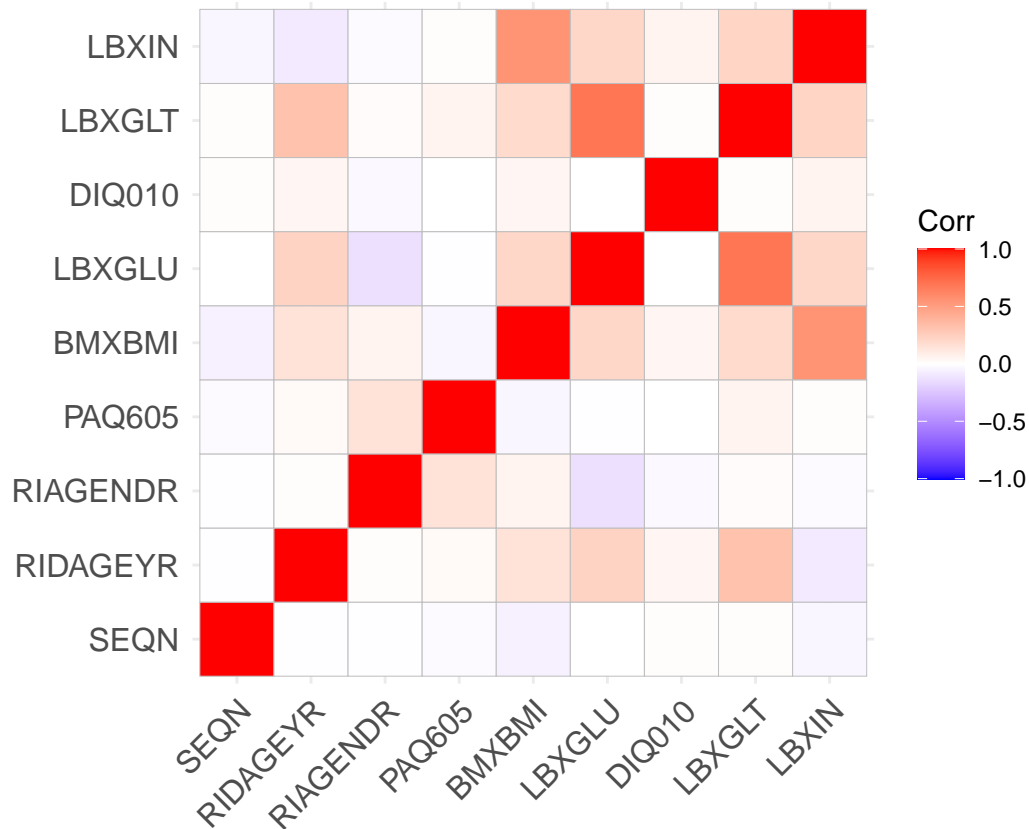
# Scale the numeric variables
normalized_data <- scale(numerical_nhanes_data)

# View the first few rows of the normalized data
head(normalized_data)
```

```
##      SEQN RIDAGEYR RIAGENDR PAQ605 BMXBMI LBXGLU
## [1,] -1.755294 0.9527694 0.9772131 0.4445743 1.0684040 0.5839564
## [2,] -1.753924 -0.7836767 0.9772131 0.4445743 -1.0560381 -0.5898946
## [3,] -1.751186 -1.2798041 -1.0228690 0.4445743 -0.6559808 -0.5898946
## [4,] -1.750844 -0.4860002 -1.0228690 0.4445743 0.1303387 0.2485704
## [5,] -1.749817 -0.1883237 0.9772131 -2.0622083 1.0959942 0.1926727
## [6,] -1.749474 0.4070292 -1.0228690 0.4445743 -0.6008005 0.5839564
##      DIQ010 LBXGLT LBXIN
## [1,] -0.08753347 0.7441596 0.31641794
## [2,] -0.08753347 -0.7432641 -0.82158128
## [3,] -0.08753347 -0.9982510 -0.58595576
## [4,] -0.08753347 -0.6582685 0.44400555
## [5,] -0.08753347 -0.7220152 -0.09412608
## [6,] -0.08753347 -0.3182859 -0.59212936
```

```
#Compute the correlation matrix
cor_matrix<-cor(normalized_data)
```

```
#Visualize the correlation matrix
ggcorrplot(cor_matrix)
```



```
# Compute eigenvalues
eigen_values<- eigen(cor_matrix)
eigen_values
```

```
## eigen() decomposition
## $values
## [1] 2.1418878 1.3348263 1.1767796 1.0160941 0.9879332 0.9034897 0.7669540
## [8] 0.3898257 0.2822095
##
## $vectors
##      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]
## [1,] 0.03646881 0.15073249 0.13750447 -0.38628977 0.881753293 -0.11384612
## [2,] -0.28593232 0.41656848 -0.13248116 -0.20694686 -0.264312936 -0.48300427
## [3,] 0.03376956 -0.12259966 -0.70518475 -0.06876054 0.115613452 -0.44014485
## [4,] -0.01553227 0.06523268 -0.65792079 -0.09663964 0.070342547 0.62229942
## [5,] -0.41684427 -0.50287947 -0.03407413 -0.04021793 0.001373012 -0.26987367
## [6,] -0.53783408 0.28434144 0.11179158 0.12922155 0.064669696 0.19742268
## [7,] -0.05282271 -0.08903474 0.11254312 -0.87865877 -0.325365980 0.18019687
```

```
## [8,] -0.54741455  0.31135426 -0.07198483  0.05664455  0.070340646  0.09564474
## [9,] -0.38736744 -0.58809690  0.04347161  0.01790093  0.139069676  0.13905225
##      [,7]      [,8]      [,9]
## [1,]  0.12997570  0.02008895 -0.00868437
## [2,]  0.52436617 -0.27986519 -0.16702184
## [3,] -0.50091859 -0.03013175 -0.15130786
## [4,]  0.39005911  0.09378322 -0.01258607
## [5,]  0.28949716  0.61239269  0.19724977
## [6,] -0.26706440  0.29822754 -0.63029195
## [7,] -0.25398540  0.04132088 -0.00504460
## [8,] -0.28540781 -0.16189105  0.68792686
## [9,]  0.06310858 -0.64783339 -0.19882551
```

```
# Principal Component Analysis (PCA)
```

```
PCA <- princomp(cor_matrix)
PCA
```

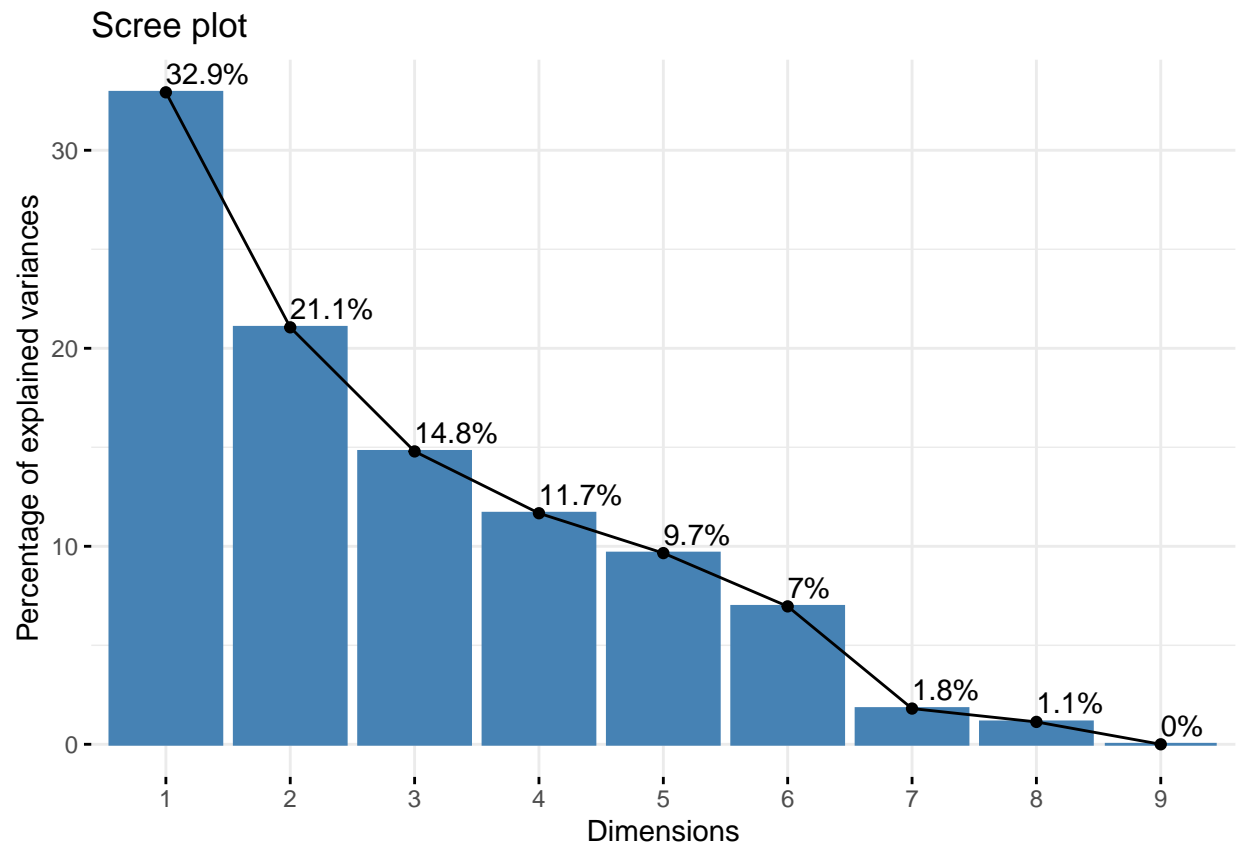
```
## Call:
## princomp(x = cor_matrix)
##
## Standard deviations:
##      Comp.1      Comp.2      Comp.3      Comp.4      Comp.5      Comp.6
## 5.562252e-01 4.448188e-01 3.728026e-01 3.311339e-01 3.012191e-01 2.558409e-01
##      Comp.7      Comp.8      Comp.9
## 1.302323e-01 1.030893e-01 3.155841e-09
##
## 9 variables and 9 observations.
```

```
summary(PCA)
```

```
## Importance of components:
##
##      Comp.1      Comp.2      Comp.3      Comp.4      Comp.5
## Standard deviation  0.5562252 0.4448188 0.3728026 0.3311339 0.30121906
## Proportion of Variance 0.3292547 0.2105702 0.1479069 0.1166911 0.09655962
## Cumulative Proportion 0.3292547 0.5398248 0.6877318 0.8044229 0.90098254
##
##      Comp.6      Comp.7      Comp.8      Comp.9
## Standard deviation  0.25584094 0.13023230 0.10308935 3.155841e-09
## Proportion of Variance 0.06965795 0.01804962 0.01130989 1.059890e-17
## Cumulative Proportion 0.97064049 0.98869011 1.00000000 1.000000e+00
```

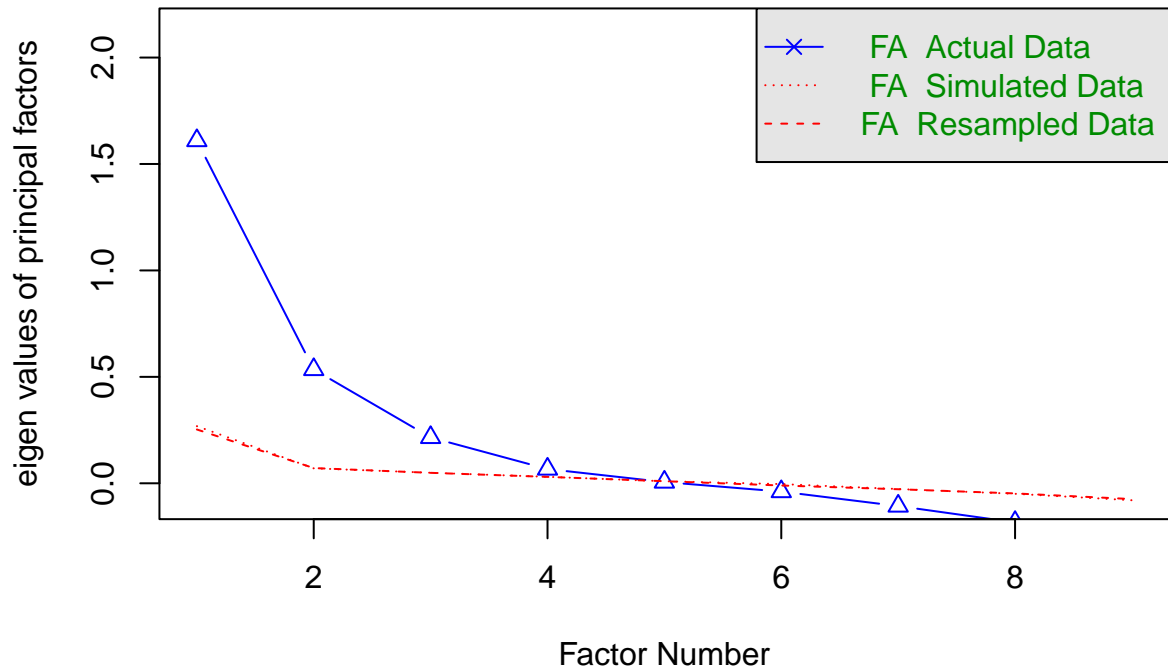
```
# Visualize the eigenvalues
```

```
fviz_eig(PCA,addlabels=TRUE)
```



```
# Perform parallel analysis for factor extraction  
fa.parallel(normalized_data, fm = "pa", fa = "fa")
```

Parallel Analysis Scree Plots



Parallel analysis suggests that the number of factors = 4 and the number of components = NA

Compute covariance matrix

```
covariance_matrix <- cov(normalized_data)
covariance_matrix
```

```
##          SEQN      RIDAGEYR      RIAGENDR      PAQ605      BMXBMI
## SEQN      1.000000000 -0.008805540 -0.012962358 -0.019700576 -0.06134269
## RIDAGEYR -0.008805540  1.000000000  0.006397727  0.025973321  0.14716313
## RIAGENDR -0.012962358  0.006397727  1.000000000  0.151076048  0.06387261
## PAQ605   -0.019700576  0.025973321  0.151076048  1.000000000 -0.04293533
## BMXBMI   -0.061342686  0.147163129  0.063872606 -0.042935333  1.00000000
## LBXGLU   -0.004146668  0.229623521 -0.132342297 -0.007848679  0.20833006
## DIQ010    0.014102187  0.049970042 -0.032768864 -0.002599301  0.04713345
## LBXGLT    0.006035900  0.318044363  0.017405743  0.060412732  0.19337459
## LBXIN     -0.040028480 -0.091879158 -0.016660137  0.010011012  0.55271719
##          LBXGLU      DIQ010      LBXGLT      LBXIN
## SEQN      -0.004146668  0.014102187  0.006035900 -0.04002848
## RIDAGEYR   0.229623521  0.049970042  0.318044363 -0.09187916
## RIAGENDR  -0.132342297 -0.032768864  0.017405743 -0.01666014
## PAQ605    -0.007848679 -0.002599301  0.060412732  0.01001101
## BMXBMI     0.208330061  0.047133447  0.193374586  0.55271719
## LBXGLU     1.000000000 -0.004427431  0.685579317  0.21191124
## DIQ010    -0.004427431  1.000000000  0.009795877  0.05898570
## LBXGLT     0.685579317  0.009795877  1.000000000  0.21727159
## LBXIN      0.211911242  0.058985703  0.217271586  1.00000000
```



```
# Kaiser-Meyer-Olkin (KMO) Test
KMO(r=nhanes_data[, -c(2)])
```

```
## Kaiser-Meyer-Olkin factor adequacy
## Call: KMO(r = nhanes_data[, -c(2)])
## Overall MSA = 0.53
## MSA for each item =
##      SEQN RIDAGEYR RIAGENDR  PAQ605  BMXBMI  LBXGLU  DIQ010  LBXGLT
##      0.63      0.50      0.32      0.45      0.52      0.57      0.52      0.55
##      LBXIN
##      0.50
```

```
cor_matrix <- cor_matrix[, KMO(cor_matrix)$MSAi > 0.5]
round(KMO(cor_matrix)$MSA, 2)
```

```
## [1] 0.54
```

```
# Perform Bartlett's test of sphericity
cortest.bartlett(normalized_data)
```

```
## R was not square, finding R from data
```

```
## $chisq
## [1] 3084.423
##
## $p.value
## [1] 0
##
## $df
## [1] 36
```

```
# Compute the determinant of the covariance matrix
det(covariance_matrix)
```

```
## [1] 0.2574618
```

```
# Compute proportion of variance explained by each principal component
Pop_var_exp <- eigen_values$values/sum(eigen_values$values)*100
round(Pop_var_exp, 3)
```

```
## [1] 23.799 14.831 13.075 11.290 10.977 10.039 8.522 4.331 3.136
```

```
# Total variance explained by all principal components
sum(eigen_values$values)
```

```
## [1] 9
```

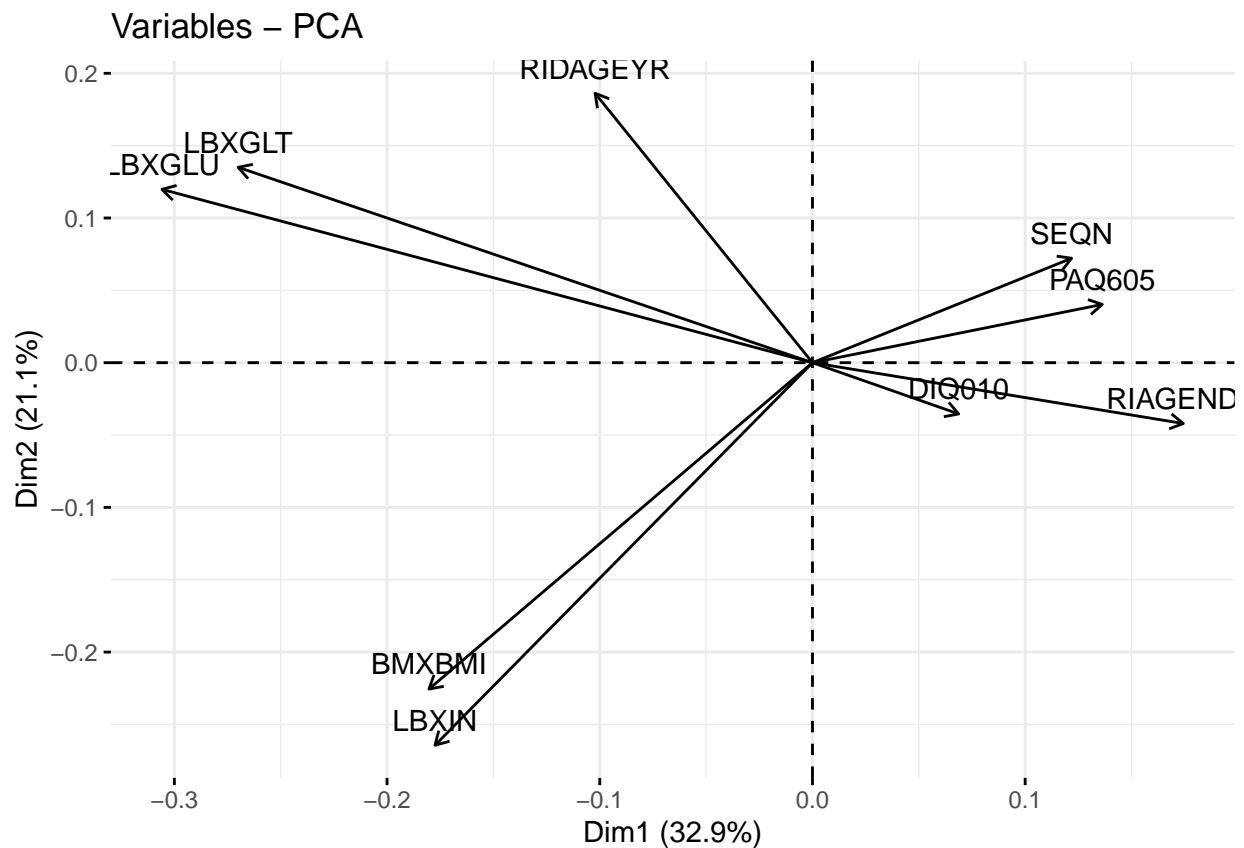
```
# Sum of proportion of variance explained
sum(Pop_var_exp)
```

```
## [1] 100
```

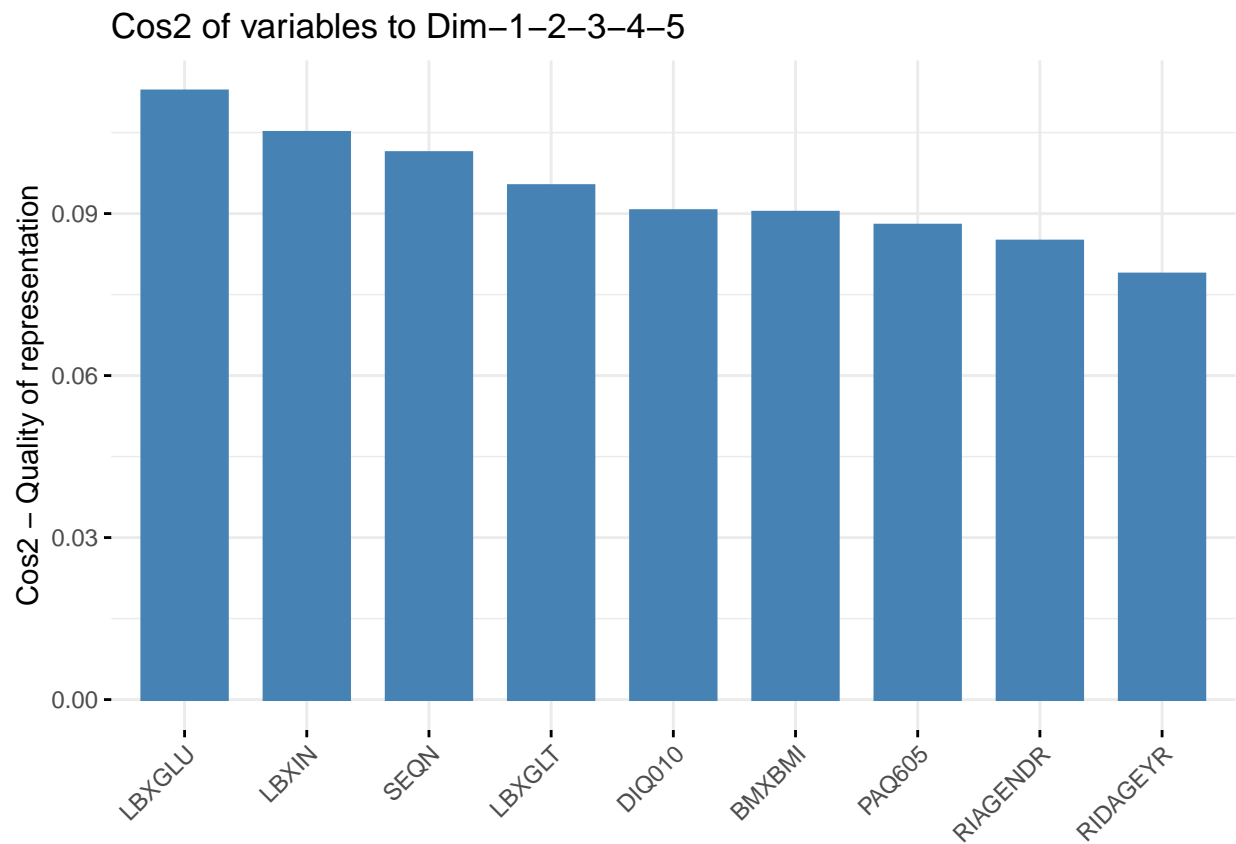
```
# Factor Loadings using PCA
PCA$loadings[,1:5]
```

	Comp.1	Comp.2	Comp.3	Comp.4	Comp.5
SEQN	0.2190399	0.16226286	0.510407355	0.63629338	0.08430368
RIDAGEYR	-0.1837077	0.41854584	-0.067064946	-0.33372524	0.47956831
RIAGENDR	0.3134556	-0.09449175	-0.509188553	0.04348126	0.42649093
PAQ605	0.2449615	0.09052242	-0.474162993	-0.01117905	-0.63348046
BMXBMI	-0.3241362	-0.50705491	-0.054899611	-0.02398356	0.26552462
LBXGLU	-0.5497668	0.26924425	-0.019558318	0.10951391	-0.19625453
DIQ010	0.1235834	-0.07958088	0.478670383	-0.66895238	-0.20065759
LBXGLT	-0.4854211	0.30354996	-0.135388369	0.07378786	-0.09980103
LBXIN	-0.3190583	-0.59438565	0.005590889	0.12740548	-0.14308124

```
# Visualize the variables in PCA
fviz_pca_var(PCA, col.var = "black")
```



```
# Visualize the squared cosines of variables in PCA
fviz_cos2(PCA, choice = "var", axes = 1:5)
```



```
# Factor Analysis using factanal
numerical_nhanes_data.fa<-factanal(numerical_nhanes_data,factors = 3)
numerical_nhanes_data.fa
```

```
##
## Call:
## factanal(x = numerical_nhanes_data, factors = 3)
##
## Uniquenesses:
##      SEQN RIDAGEYR RIAGENDR  PAQ605  BMXBMI  LBXGLU  DIQ010  LBXGLT
##      0.998   0.850   0.005   0.974   0.678   0.425   0.995   0.151
##      LBXIN
##      0.005
##
## Loadings:
##      Factor1 Factor2 Factor3
## SEQN
## RIDAGEYR  0.366  -0.117
## RIAGENDR                0.993
## PAQ605                0.156
## BMXBMI    0.134   0.547
## LBXGLU    0.739   0.158
```

```
## DIQ010
## LBXGLT    0.903    0.155    0.101
## LBXIN          0.995
##
##          Factor1 Factor2 Factor3
## SS loadings    1.528    1.357    1.033
## Proportion Var    0.170    0.151    0.115
## Cumulative Var    0.170    0.321    0.435
##
## Test of the hypothesis that 3 factors are sufficient.
## The chi square statistic is 160.19 on 12 degrees of freedom.
## The p-value is 4.79e-28
```

```
# Compute squared loadings
apply(numerical_nhanes_data.fa$loadings^2,1,sum)
```

```
##          SEQN    RIDAGEYR    RIAGENDR    PAQ605    BMXBMI    LBXGLU
## 0.001958084 0.149571781 0.995000045 0.025756857 0.322403421 0.574617189
##          DIQ010    LBXGLT    LBXIN
## 0.004520238 0.849247707 0.995001183
```

```
# Factor Analysis using fa function
nhanes_data_PC<- fa(covariance_matrix ,nfactors = 3,rotate = "varimax",n.obs
= 1000 ,covar = TRUE,fm = "pa")
```

```
## maximum iteration exceeded
```

```
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs = np.obs, :
## The estimated weights for the factor scores are probably incorrect. Try a
## different factor score estimation method.
```

```
nhanes_data_PC
```

```
## Factor Analysis using method = pa
## Call: fa(r = covariance_matrix, nfactors = 3, n.obs = 1000, rotate = "varimax",
## covar = TRUE, fm = "pa")
## Standardized loadings (pattern matrix) based upon correlation matrix
##          PA1    PA2    PA3    h2    u2 com
## SEQN      0.00 -0.05 -0.03 0.0038 0.996 1.5
## RIDAGEYR  0.36 -0.04 0.06 0.1366 0.863 1.1
## RIAGENDR -0.05 0.04 0.68 0.4637 0.536 1.0
## PAQ605    0.04 0.00 0.22 0.0488 0.951 1.1
## BMXBMI    0.16 0.54 0.05 0.3159 0.684 1.2
## LBXGLU    0.74 0.17 -0.15 0.6036 0.396 1.2
## DIQ010    0.01 0.06 -0.03 0.0043 0.996 1.7
## LBXGLT    0.89 0.17 0.07 0.8233 0.177 1.1
## LBXIN     0.04 1.02 -0.07 1.0381 -0.038 1.0
##
##          PA1    PA2    PA3
## SS loadings    1.50 1.39 0.55
## Proportion Var    0.17 0.15 0.06
## Cumulative Var    0.17 0.32 0.38
```

```
## Proportion Explained  0.44 0.40 0.16
## Cumulative Proportion 0.44 0.84 1.00
##
## Mean item complexity =  1.2
## Test of the hypothesis that 3 factors are sufficient.
##
## df null model =  36  with the objective function =  1.36 with Chi Square =  1350.33
## df of the model are 12  and the objective function was  0.08
##
## The root mean square of the residuals (RMSR) is  0.03
## The df corrected root mean square of the residuals is  0.05
##
## The harmonic n.obs is  1000 with the empirical chi square  57.25  with prob <  7.1e-08
## The total n.obs was  1000  with Likelihood Chi Square =  80.36  with prob <  3.5e-12
##
## Tucker Lewis Index of factoring reliability =  0.844
## RMSEA index =  0.075  and the 90 % confidence intervals are  0.06 0.092
## BIC =  -2.53
## Fit based upon off diagonal values = 0.98
```

```
# Rotate the factors
```

```
nhanes_data_PC_rotate <- fa(cor_matrix ,nfactors = 3,rotate =
"varimax",n.obs = 1000 ,cor = TRUE,fm = 'pa',max.iter = 1000)
```

```
## Warning in fa.stats(r = r, f = f, phi = phi, n.obs = n.obs, np.obs = np.obs, :
## The estimated weights for the factor scores are probably incorrect. Try a
## different factor score estimation method.
```

```
## Warning in fac(r = r, nfactors = nfactors, n.obs = n.obs, rotate = rotate, : An
## ultra-Heywood case was detected. Examine the results carefully
```

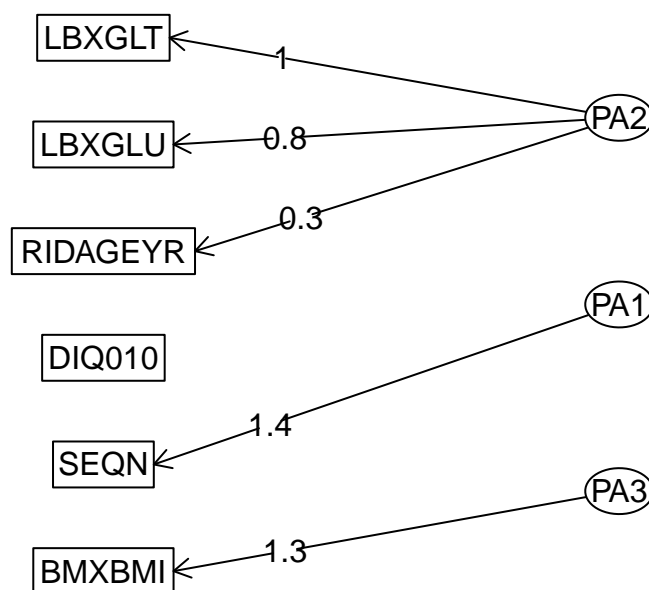
```
nhanes_data_PC_rotate
```

```
## Factor Analysis using method = pa
## Call: fa(r = cor_matrix, nfactors = 3, n.obs = 1000, rotate = "varimax",
##      max.iter = 1000, fm = "pa", cor = TRUE)
## Standardized loadings (pattern matrix) based upon correlation matrix
##          PA2  PA1  PA3  h2    u2 com
## SEQN      -0.14  1.40 -0.15 2.01 -1.011 1.0
## RIDAGEYR   0.35 -0.12 -0.06 0.14  0.863 1.3
## BMXBMI     0.07 -0.13  1.29 1.67 -0.673 1.0
## LBXGLU     0.85 -0.08  0.09 0.73  0.271 1.0
## DIQ010    -0.30 -0.11 -0.11 0.11  0.889 1.6
## LBXGLT     1.04 -0.09  0.02 1.09 -0.091 1.0
##
##
##          PA2  PA1  PA3
## SS loadings      2.03 2.03 1.70
## Proportion Var    0.34 0.34 0.28
## Cumulative Var    0.34 0.68 0.96
## Proportion Explained 0.35 0.35 0.29
## Cumulative Proportion 0.35 0.71 1.00
##
```

```
## Mean item complexity = 1.2
## Test of the hypothesis that 3 factors are sufficient.
##
## df null model = 15 with the objective function = 2.25 with Chi Square = 11.61
## df of the model are 0 and the objective function was 0.01
##
## The root mean square of the residuals (RMSR) is 0.01
## The df corrected root mean square of the residuals is NA
##
## The harmonic n.obs is 9 with the empirical chi square 0.04 with prob < NA
## The total n.obs was 9 with Likelihood Chi Square = 0.02 with prob < NA
##
## Tucker Lewis Index of factoring reliability = Inf
## Fit based upon off diagonal values = 1
```

```
# Plot the factor diagram
fa.diagram(nhanes_data_PC_rotate)
```

Factor Analysis



```
###Confirmatory Factor Analysis (CFA):
# Define the CFA model
variables <-
normalized_data[,c("RIDAGEYR", "RIAGENDR", "BMXBMI", "LBXGLU", "LBXGLT", "LBXIN")]
#define the CFA model
model <- '
Factor1 =~ BMXBMI+LBXIN
```

```
Factor2 =~ LBXGLT+ LBXGLU+ RIDAGEYR
Factor3 =~ RIAGENDR
'
```

```
# Fit the CFA model
```

```
fit <- cfa(model, data = variables)
```

```
# Assess model fit
```

```
summary(fit, fit.measures = TRUE)
```

```
## lavaan 0.6.17 ended normally after 27 iterations
```

```
##
```

```
## Estimator ML
```

```
## Optimization method NLMINB
```

```
## Number of model parameters 14
```

```
##
```

```
## Number of observations 2278
```

```
##
```

```
## Model Test User Model:
```

```
##
```

```
## Test statistic 318.591
```

```
## Degrees of freedom 7
```

```
## P-value (Chi-square) 0.000
```

```
##
```

```
## Model Test Baseline Model:
```

```
##
```

```
## Test statistic 2980.033
```

```
## Degrees of freedom 15
```

```
## P-value 0.000
```

```
##
```

```
## User Model versus Baseline Model:
```

```
##
```

```
## Comparative Fit Index (CFI) 0.895
```

```
## Tucker-Lewis Index (TLI) 0.775
```

```
##
```

```
## Loglikelihood and Information Criteria:
```

```
##
```

```
## Loglikelihood user model (H0) -18060.330
```

```
## Loglikelihood unrestricted model (H1) -17901.035
```

```
##
```

```
## Akaike (AIC) 36148.660
```

```
## Bayesian (BIC) 36228.894
```

```
## Sample-size adjusted Bayesian (SABIC) 36184.414
```

```
##
```

```
## Root Mean Square Error of Approximation:
```

```
##
```

```
## RMSEA 0.140
```

```
## 90 Percent confidence interval - lower 0.127
```

```
## 90 Percent confidence interval - upper 0.153
```

```
## P-value H_0: RMSEA <= 0.050 0.000
```

```
## P-value H_0: RMSEA >= 0.080 1.000
```

```
##
```

```
## Standardized Root Mean Square Residual:
```

```
##
```

```
## SRMR 0.051
```

```
##
## Parameter Estimates:
##
## Standard errors          Standard
## Information             Expected
## Information saturated (h1) model Structured
##
## Latent Variables:
##      Estimate Std.Err z-value P(>|z|)
## Factor1 =~
##   BMXBMI      1.000
##   LBXIN        0.968    0.087   11.102    0.000
## Factor2 =~
##   LBXGLT       1.000
##   LBXGLU       0.849    0.042   20.366    0.000
##   RIDAGEYR     0.376    0.027   13.755    0.000
## Factor3 =~
##   RIAGENDR     1.000
##
## Covariances:
##      Estimate Std.Err z-value P(>|z|)
## Factor1 ~~
##   Factor2      0.216    0.021   10.250    0.000
##   Factor3      0.026    0.019    1.397    0.162
## Factor2 ~~
##   Factor3     -0.025    0.020   -1.210    0.226
##
## Variances:
##      Estimate Std.Err z-value P(>|z|)
##   .BMXBMI      0.429    0.052    8.312    0.000
##   .LBXIN        0.465    0.049    9.503    0.000
##   .LBXGLT       0.191    0.037    5.156    0.000
##   .LBXGLU       0.417    0.029   14.271    0.000
##   .RIDAGEYR     0.885    0.027   32.849    0.000
##   .RIAGENDR     0.000
##   Factor1      0.571    0.057   10.057    0.000
##   Factor2      0.808    0.047   17.258    0.000
##   Factor3      1.000    0.030   33.749    0.000
```

```
# Standardized estimates (factor loadings)
parameterEstimates(fit, standardized = TRUE, ci = TRUE)
```

```
##      lhs op      rhs    est    se      z pvalue ci.lower ci.upper std.lv
## 1  Factor1 =~ BMXBMI  1.000 0.000    NA     NA    1.000    1.000  0.755
## 2  Factor1 =~ LBXIN   0.968 0.087  11.102  0.000    0.797    1.139  0.731
## 3  Factor2 =~ LBXGLT  1.000 0.000    NA     NA    1.000    1.000  0.899
## 4  Factor2 =~ LBXGLU  0.849 0.042  20.366  0.000    0.767    0.931  0.763
## 5  Factor2 =~ RIDAGEYR 0.376 0.027  13.755  0.000    0.322    0.429  0.338
## 6  Factor3 =~ RIAGENDR 1.000 0.000    NA     NA    1.000    1.000  1.000
## 7  BMXBMI ~~ BMXBMI  0.429 0.052    8.312  0.000    0.328    0.530  0.429
## 8  LBXIN   ~~ LBXIN   0.465 0.049    9.503  0.000    0.369    0.560  0.465
## 9  LBXGLT  ~~ LBXGLT  0.191 0.037    5.156  0.000    0.119    0.264  0.191
## 10 LBXGLU  ~~ LBXGLU  0.417 0.029   14.271  0.000    0.360    0.475  0.417
## 11 RIDAGEYR ~~ RIDAGEYR 0.885 0.027   32.849  0.000    0.833    0.938  0.885
```



```
## 12 RIAGENDR ~~ RIAGENDR 0.000 0.000 NA NA 0.000 0.000 0.000
## 13 Factor1 ~~ Factor1 0.571 0.057 10.057 0.000 0.459 0.682 1.000
## 14 Factor2 ~~ Factor2 0.808 0.047 17.258 0.000 0.716 0.900 1.000
## 15 Factor3 ~~ Factor3 1.000 0.030 33.749 0.000 0.942 1.058 1.000
## 16 Factor1 ~~ Factor2 0.216 0.021 10.250 0.000 0.174 0.257 0.318
## 17 Factor1 ~~ Factor3 0.026 0.019 1.397 0.162 -0.011 0.063 0.035
## 18 Factor2 ~~ Factor3 -0.025 0.020 -1.210 0.226 -0.065 0.015 -0.027
## std.all std.nox
## 1 0.756 0.756
## 2 0.732 0.732
## 3 0.899 0.899
## 4 0.763 0.763
## 5 0.338 0.338
## 6 1.000 1.000
## 7 0.429 0.429
## 8 0.465 0.465
## 9 0.192 0.192
## 10 0.417 0.417
## 11 0.886 0.886
## 12 0.000 0.000
## 13 1.000 1.000
## 14 1.000 1.000
## 15 1.000 1.000
## 16 0.318 0.318
## 17 0.035 0.035
## 18 -0.027 -0.027
```

```
#remotes::install_github("rstudio/htmltools")
#install.packages("html",dependencies = TRUE)
```