

# Solutions



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# Colligative Properties of Solutions

**Solution**- a homogenous mixture of two or more substances.

**Solubility**- the maximum amount of a solute that will dissolve in a given quantity of solvent at a specific temperature.

- When solute is introduced into the volume of solvent, the solvent properties change
- Colligative properties are properties of solutions that depend **solely on the number of particles dissolved in the solution**

Four types of colligative properties of solutions:

1. Vapor-Pressure Lowering
2. Boiling-Point Elevation
3. Freezing-Point Depression
4. Osmotic Pressure

# Vapor-Pressure Lowering

Occurs with **non-volatile**, **non-ionizing solutes** at low solute concentrations.

~0 vapor pressure

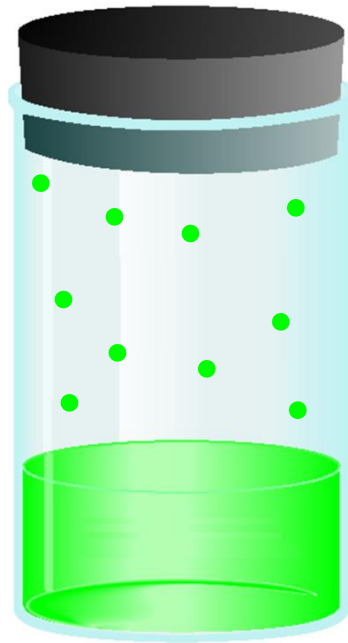
does not dissociate

Larger  
entropy  
increase

disordered

strong  
driving  
force

"Ordered"  
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Gas

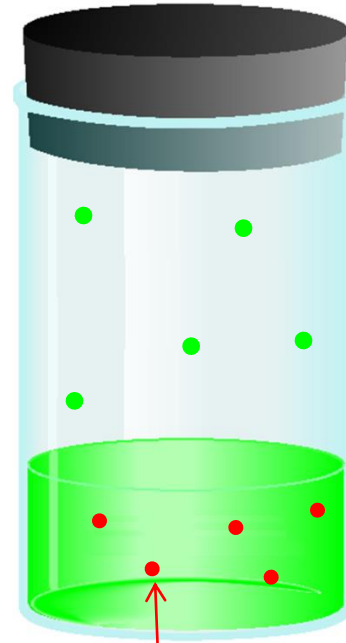
Liqui  
d

Smaller  
entropy  
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weaker  
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"Ordered"  
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Solute molecule

The vapor pressure of a pure solvent drops whenever non-volatile solute is added

# Raoult's Law (Vapor Pressure Lowering)

- The vapor pressure ( $P_s$ ) of a solvent is directly proportional to the mole fraction of the solvent in the solution

vapor pressure ( $P_s$ )  $\propto$  mole fraction of solvent

- **Raoult's Law:**

$$P_s = \frac{N}{N + n} \times P$$

( $P$  = vapor pressure of the pure solvent)

Where,  $N$  = moles of solvent  
 $n$  = moles of solute

For pure solvent  $P_s = P$

moles of solute  $\uparrow$        $X_1 \downarrow$        $P \downarrow$

As solute is added, the vapor pressure drops.

# Raoult's Law (Vapor Pressure Lowering)

- $P$  – the vapor pressure of the pure solvent

$P_s$  – the vapor pressure of the solution with solute

$$P_s = \frac{N}{N + n} \times P$$

$$\frac{P_s}{P} = \frac{N}{N + n}$$

$$1 - \frac{P_s}{P} = 1 - \frac{N}{N + n}$$

$$\frac{P - P_s}{P} = \frac{n}{n + N}$$

**The relative lowering of vapour pressure of a dilute solution is equals to the mole fraction of the solute present in the dilute solution.**

# Determination of molecular weight from Vapor Pressure Lowering

From Raoult's Law

$$(P - P_s)/P = n/(n+N)$$

Considering

**w** gms of solute; Moles of solute (n) = **w/m**

**W** gms of solvent; Moles of solvent (N) = **W/M**

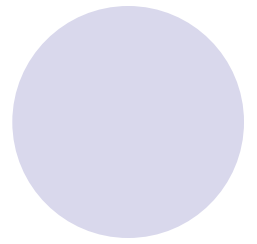
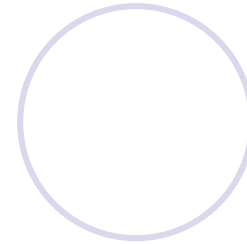
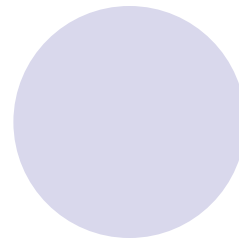
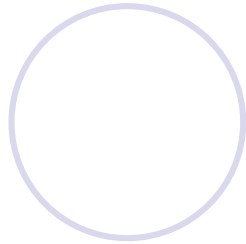
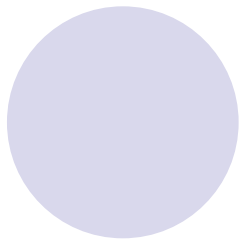
Where **m** = molecular weight of solute

And **M** = molecular weight of solvent

$$(P - P_s)/P = n/(n+N)$$

$$(P - P_s)/P = (w/m)/(w/m + W/M)$$

$$(P - P_s)/P = wM/mW$$



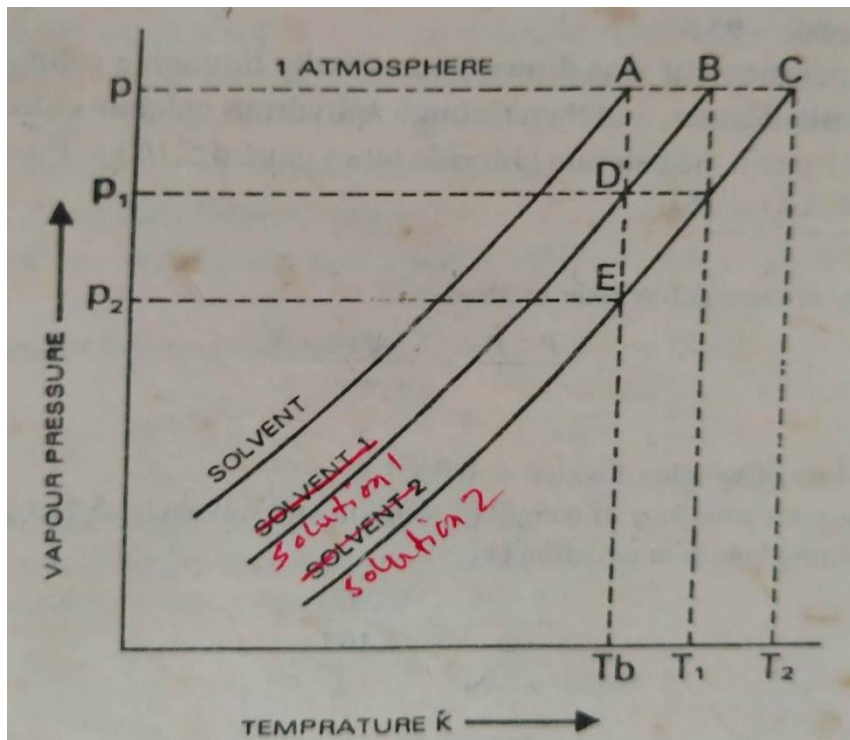
## Limitations of Raoult's Law

1. At higher conc.; solute gain intermolecular forces
2. It does not applies to volatile solutes.
3. Dissociate or associate

# Boiling Point Elevation

## (Relation between Boiling Point Elevation and Vapor Pressure Lowering)

When a liquid is heated, its vapour pressure rises and when it equals to atmospheric Pressure, the liquid boils.



If,  $T_b$  = Boiling point of solvent  
And  $T$  = Boiling point of solution

$$\text{EVP, } T - T_b = \Delta T$$

For dilute solution, the curves BD and CE are parallel and straight lines approximately. Therefore, ACE and ABD are similar triangles.

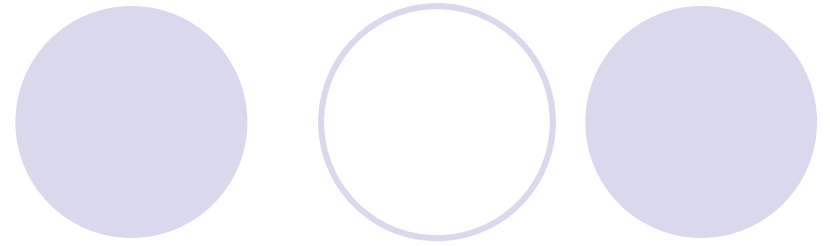
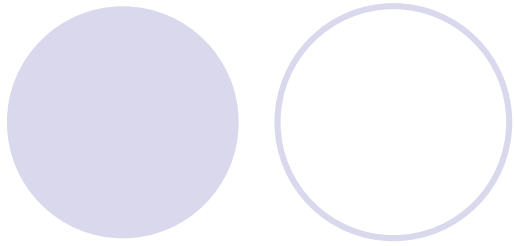
$$\frac{AB}{AC} = \frac{AD}{AE}$$

$$\frac{T_1 - T_b}{T_2 - T_b} = \frac{p - p_1}{p - p_2}$$

Where,  $p - p_1$  and  $p - p_2$  are lowering of vapour pressure for solution 1 and 2.  
Hence Elevation of boiling point is directly proportional to the lowering of vapour pressure.

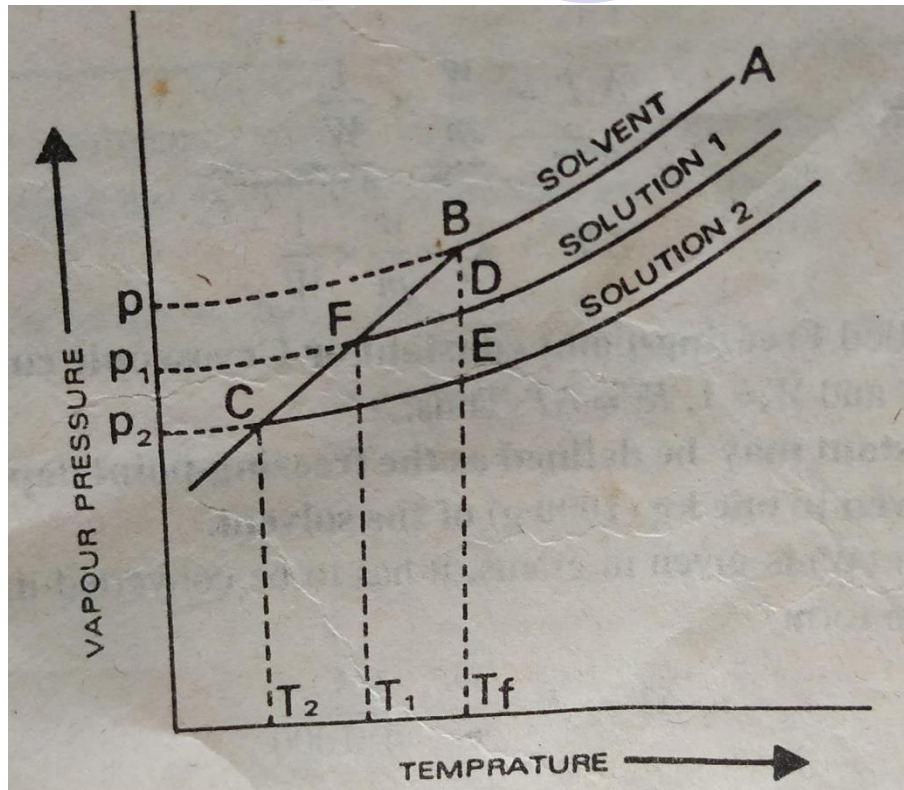
$$\Delta T = \frac{p - p_s}{p_s} \cdot T_b$$





Determination of molecular weight from Boiling Point Elevation

# Freezing-Point Depression



If,  $T_f$  = Freezing point of solvent  
 And  $T_1$  = Freezing point of solution 1

$$\text{DFP, } T_f - T_1 = \Delta T$$

For dilute solution, the curves FD and CE are parallel and straight lines approximately. Therefore, BDF and BEC are similar triangles

$$\frac{DF}{EC} = \frac{BD}{BE}$$

$$\frac{T_f - T_1}{T_f - T_2} = \frac{p - p_1}{p - p_2}$$

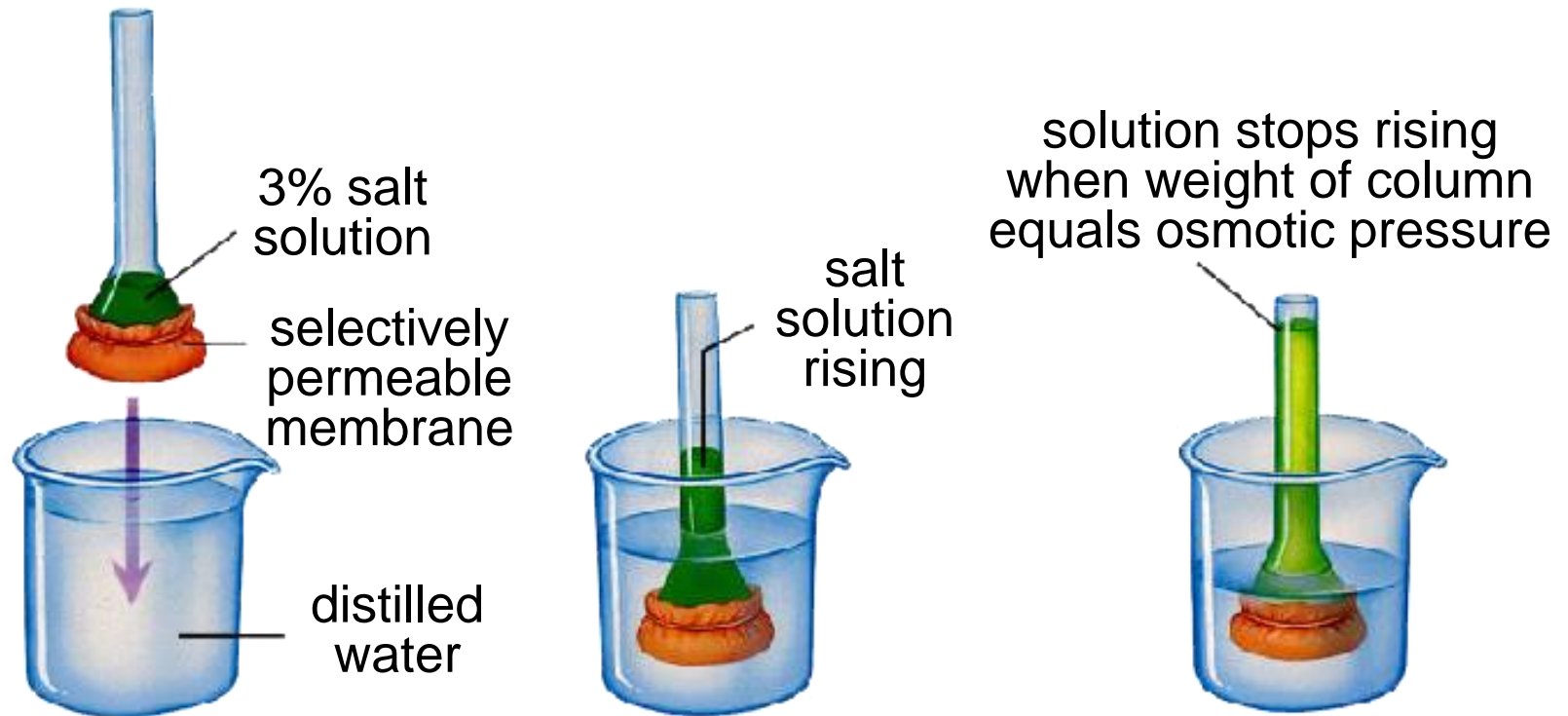
Where,  $p - p_1$  and  $p - p_2$  are lowering of vapour pressure for solution 1 and 2.  
 Hence depression of freezing point is directly proportional to the lowering of vapour pressure

$$\Delta T = p - p_s$$

# Osmosis

**Osmosis** is the selective passage of solvent molecules through a porous membrane from a dilute solution to a more concentrated one.

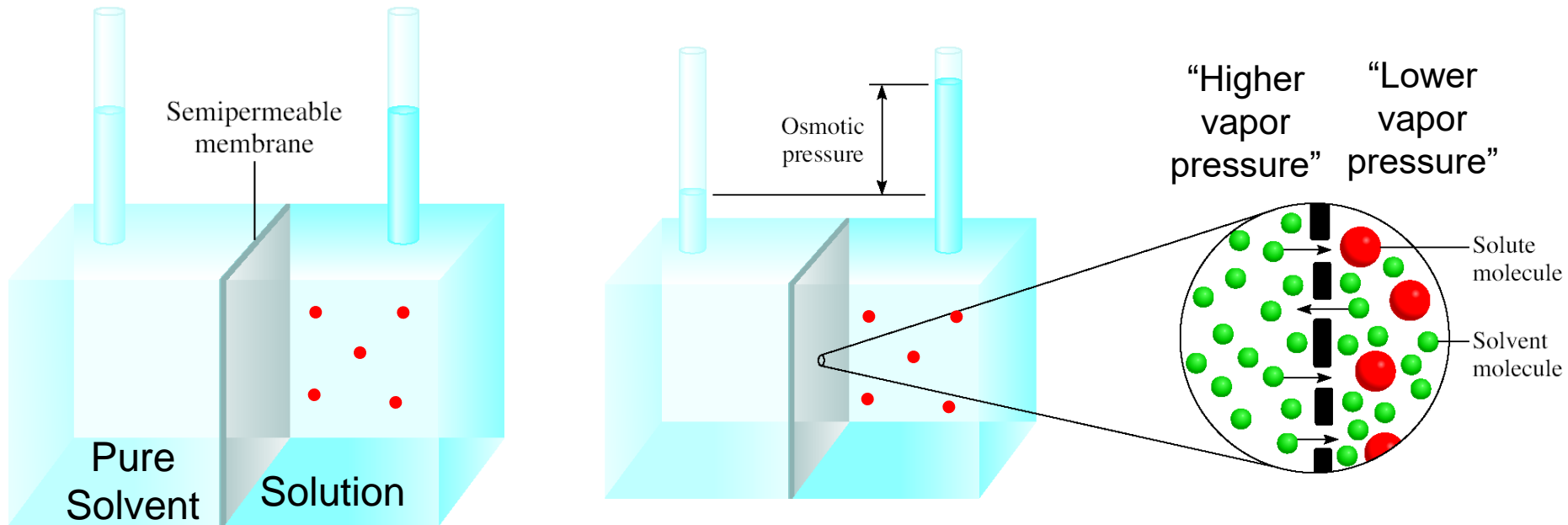
A **semipermeable membrane** allows the passage of solvent molecules but blocks the passage of solute molecules.



# Osmosis

**Osmosis** is the selective passage of solvent molecules through a porous membrane from a dilute solution to a more concentrated one.

A **semipermeable membrane** allows the passage of solvent molecules but blocks the passage of solute molecules.



**Osmotic pressure ( $\pi$ )** is the pressure required to stop osmosis.

# Osmotic Pressure

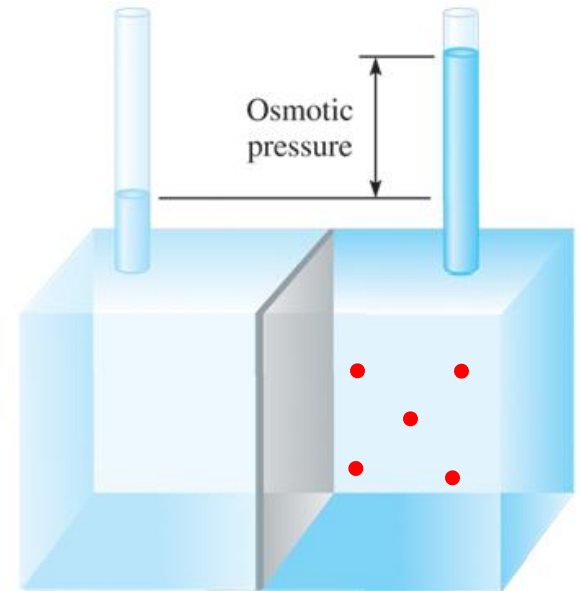
- Osmosis is a rate controlled phenomenon.
  - The solvent is passing from the dilute solution into the concentrated solution at a faster rate than in opposite direction, i.e. establishing an equilibrium.
- The osmotic pressure
$$\pi = MRT$$

$\pi$  = osmotic pressure (atm)

$M$  = molar concentration of solution (mol/L)

$$R = 0.0821 \frac{\text{L atm}}{\text{mol K}}$$

$T$  = absolute temperature (K)



# Abnormal Colligative Properties of Solutions



