

### Program 58.find the Kth Smallest Sum of a Matrix With Sorted Rows

You are given an  $m \times n$  matrix `mat` that has its rows sorted in non-decreasing order and an integer `k`.

You are allowed to choose exactly one element from each row to form an array.

Return the `k`th smallest array sum among all possible arrays.

Example 1:

Input: `mat = [[1,3,11],[2,4,6]]`, `k = 5`

Output: 7

Explanation: Choosing one element from each row, the first `k` smallest sum are: `[1,2]`, `[1,4]`, `[3,2]`, `[3,4]`, `[1,6]`. Where the 5th sum is 7.

#### Program:

```
import heapq
def kthSmallest(mat, k):
    # Start with the smallest possible sum using the first element of each row
    m, n = len(mat), len(mat[0])
    min_heap = [(sum(row[0] for row in mat), [0] * m)] # (sum, indices)
    visited = set(tuple([0] * m)) # To keep track of visited indices

    while k > 0:
        current_sum, indices = heapq.heappop(min_heap)
        k -= 1
        if k == 0:
            return current_sum

        # Try to increment each index in the indices array
        for i in range(m):
            if indices[i] + 1 < n:
                new_indices = list(indices)
                new_indices[i] += 1
                new_sum = current_sum - mat[i][indices[i]] + mat[i][new_indices[i]]
                new_tuple = tuple(new_indices)

                if new_tuple not in visited:
                    visited.add(new_tuple)
                    heapq.heappush(min_heap, (new_sum, new_indices))

# Example usage
mat = [[1, 3, 11], [2, 4, 6]]
k = 5
print(kthSmallest(mat, k)) # Output: 7
```

#### Output:

```
"C:\Program Files\Python312\python.exe" "C:\Work Space\DAA COADS.PYTHON\program 58.py"
7

Process finished with exit code 0
```

#### Time complexity:

$O(m * (k \log k))$

