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# Summarized Report on GloVe

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## 1 SUMMARY

### 1.1 INTRODUCTORY EXPLANATION

This report contains a write-up for the word embeddings of GloVe (Global Vectors for Word Representation) [1].

GloVe is an **unsupervised** learning algorithm which is used to obtain **vector representations** of words. This model captures the **global statistics** of the corpus by using a **co-occurrence matrix** of all the word pairs. Hence, the global corpus statistics are captured by this model.

The table 1.1 shows the relevant notations required to understand the working of this model.

$X_{ij}$	Number of times word $j$ occurs in the context of word $i$
$P_{ij} = Pr(j i) = X_{ij}/X_i$	Probability that word $j$ would appear in the context of word $i$

Table 1.1: Relevant Definitions

Now suppose  $i$  = ice and  $j$  = steam, words  $k$  related to ice but not steam eg.  $k$  = solid or cold, we can expect  $P_{ik}/P_{jk}$  to be large since  $P_{ik}$  will be large due to  $k$  being related to  $i$ .

Similarly for  $k$  related to steam eg. gas or hot, we can expect  $P_{ik}/P_{jk}$  to be small in magnitude since  $P_{jk}$  will be large due to  $k$  being related to  $j$ .

For words  $k$  related to both words  $i$  and  $j$  eg. water, the ratio  $P_{ik}/P_{jk}$  will be close to 1 as both  $P_{ik}$  and  $P_{jk}$  will end up being similar in magnitudes.

Since the ratio  $P_{ik}/P_{jk}$  depends on three words  $i, j, k$ , the most general form of a model would be  $F(w_i, w_j, \bar{w}_k) = P_{ik}/P_{jk}$  where  $w$  are word vectors and  $\bar{w}$  are separate context vectors.

$$F(w_i, w_j, \bar{w}_k) = \frac{P_{ik}}{P_{jk}} \quad (1.1)$$

The right hand side of the equation 1.1 i.e.  $P_{ik}/P_{jk}$  is obtained from the corpus.

After some mathematical manipulations (details in [1]), a least squares regression problem is formulated. Let  $V$  be the size of the vocabulary.

$$J = \sum_{i,j=1}^V (w_i^T \bar{w}_j + b_i + \bar{b}_j - \log X_{ij})^2 \quad (1.2)$$

However, this weighs all pairs with equal weights, irrespective of how frequently or rarely they occur in the corpus. Hence, a weighted function  $f(X_{ij})$  is introduced in the cost function to address these issues. The complexity of the model depends on the number of non-zero entries in  $X$  due to the weighting function  $f(x)$ .

$$J = \sum_{i,j=1}^V f(X_{ij})(w_i^T \bar{w}_j + b_i + \bar{b}_j - \log X_{ij})^2 \quad (1.3)$$

The weighting functions must satisfy the following properties:

- $f(0) = 0$
- $f(x)$  should be **non-decreasing** so that **rare** co-occurrences are not over-weighted.
- $f(x)$  should be relatively **small for large values** of  $X$ , so that **frequent** co-occurrences are not over-weighted.

With these properties in mind, the authors proposed the following weighting function.

$$f(x) = \begin{cases} (x/x_{max})^\alpha & \text{if } x < x_{max} \\ 1 & \text{otherwise} \end{cases}$$

The authors empirically found  $\alpha$  as  $3/4$  to be a suitable value.

## 1.2 TRAINING

The authors trained their model on five corpora of different sizes as shown in 1.2:

Corpus	# tokens (in billions)
2010 Wikipedia dump	1
2014 Wikipedia dump	1.6
Gigaword5	4.3
Gigaword5 + Wikipedia2014	6
Common Crawl	42

Table 1.2: Training Corpora Details

They then tokenized and lowercases each corpus with the Stanford tokenizer, to build a vocabulary of the 400,000 most frequent words, and then construct a matrix of co-occurrence counts  $X$ . While forming  $X$ , the size of the context window should be determined and it should be decided if a distinction is needed between left context and right context. In all of the cases, they used a **decreasing weighting function**, so that word pairs that are  $d$  words apart contribute  $1/d$  to the total count.

For all the experiments, they had used  $x_{max} = 100$ ,  $\alpha = 3/4$ , and trained the model using **AdaGrad** optimizer [2], stochastically sampling nonzero elements from  $X$ , with initial learning rate of 0.05. They ran **50** iterations for vectors smaller than **300** dimensions, and **100** iterations in other cases. They used a context of ten words to the left and ten words to the right.

The model generates two sets of word vectors,  $W$  and  $\tilde{W}$ . And they used the sum  $W + \tilde{W}$  as their word vectors.

## REFERENCES

- [1] Jeffrey Pennington, Richard Socher, and Christopher D. Manning. Glove: Global vectors for word representation. In *Empirical Methods in Natural Language Processing (EMNLP)*, pages 1532–1543, 2014.
- [2] John Duchi, Elad Hazan, and Yoram Singer. Adaptive subgradient methods for online learning and stochastic optimization. *J. Mach. Learn. Res.*, 12(null):2121–2159, July 2011.