## 1

## AI1110 Assignment 2

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## 1 ICSE 2018 GRADE 12 QUESTION 8(B)

Water is dripping out of a conical funnel of semi verticle angle  $\frac{\pi}{4}$  at the uniform rate of  $2~cm^2/sec$  in the surface ,through a tiny hole at the vertex of the bottom. When slant height of the water level is 4 cm ,find the rate of decrease of slant height of water .

## 2 SOLUTION

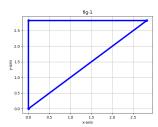


Fig. 0.

Let r be the radius , h be the height and V be the Volume of the funnel at any time t.

$$V = \frac{1}{3}\pi r^2 h {(2.0.1)}$$

Let l be the slant height of the funnel. Semi-Verical angle =  $\theta^{\circ}$  So

$$h = l\sin\theta \tag{2.0.2}$$

$$r = l\cos\theta \tag{2.0.3}$$

So, equation (2.0.1) becomes

$$V = \frac{1}{3}\pi l^3 \cos^2 \theta \sin \theta \qquad (2.0.4)$$

Differentiating it w.r.t t will give us rate of change of volume

$$\frac{dV}{dt} = \left(\frac{1}{3}\pi\cos^2\theta\sin\theta\right)3l^2\frac{dl}{dt} \tag{2.0.5}$$

$$\frac{dl}{dt} = \frac{dV}{\pi l^2 \cos^2 \theta \sin \theta dt}$$
 (2.0.6)

As it is given that rate of change of water w.r.t to t is

$$\frac{dV}{dt} = -2\left(\frac{cm^3}{sec}\right) \tag{2.0.7}$$

Slant length = 4cm

Semi Vertical angle = 45°

Therefore, putting these values in equation (2.0.6), we get

$$\frac{dl}{dt} = \frac{4\sqrt{2}}{\pi l^2} \tag{2.0.8}$$

$$\frac{dl}{dt} = \frac{\sqrt{2}cm}{4\pi sec} \tag{2.0.9}$$

So, rate of decrease of slant height is

$$\frac{\sqrt{2}cm}{4\pi sec}$$