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AI1110 Assignment 1

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1 ICSE 2018 GRADE 10 QUESTION 11(A)

The 4^{th} term of an A.P. is 22 and 15^{th} term is 66. Find the first term and the common difference.Hence find the sum of series upto 8^{th} term.

2 SOLUTION

Symbol	Value
m	4
n	15
a_m	22
a_n	66

Let \mathbf{m}^{th} and \mathbf{n}^{th} term of an A.P be a_m and a_n respectively

Let first term of A.P. be a

Let common difference of A.P. be d

The \mathbf{x}^{th} (a_x) term of any Arithmetic progression is given by

$$a_x = a + (x - 1)d$$

So,

$$a_m = a + (m-1)d (2.0.1)$$

$$a_n = a + (n-1)d (2.0.2)$$

Subtracting (2.0.1) and (2.0.2) we get,

$$(m-n)d = a_m - a_n$$
 (2.0.3)

$$d = \frac{a_m - a_n}{m - n} \tag{2.0.4}$$

Putting the value of d in (2.0.1) equation

$$a + (m-1)\left(\frac{a_m - a_n}{m-n}\right) = a_m$$
 (2.0.5)

$$a = a_m - (m-1)\left(\frac{a_m - a_n}{m-n}\right)$$
 (2.0.6)

Given the 4^{th} term of the A.P is 22

 15^{th} term of A.P. is 66

Putting the values of m, n, a_m and a_n from the table in (2.0.4) and (2.0.6)

We get 1st term of the A.P. is 10 and common difference is 4.

Sum of an A.P till x terms is given by

$$S_x = \left(\frac{x}{2}\right)(2a + (x - 1)d) \tag{2.0.7}$$

Putting the values of a and d from (2.0.4) and (2.0.6), we get

$$S_{x} = \left(\frac{x}{2}\right) \left(2\left(a_{m} - (m-1)\left(\frac{a_{m} - a_{n}}{m-n}\right)\right)\right)$$

$$+ \left(\frac{x}{2}\right) \left((x-1)\left(\frac{a_{m} - a_{n}}{m-n}\right)\right)$$

$$S_{x} = \left(\frac{x(a_{m}(m-n) - (m-1)(a_{m} - a_{n}))}{m-n}\right)$$

$$+ \left(\frac{x(x-1)(a_{m} - a_{n})}{2(m-n)}\right)$$
(2.0.9)

So, putting the values of

m ,n , a_m and a_n from the table and x=8 in (2.0.9) we get sum of A.P till 8^{th} term is

$$S_8 = \left(\frac{(8)(22(-11) - (3)(-44))}{-11}\right) + \left(\frac{8(7)(-44)}{2(-11)}\right)$$
(2.0.10)

$$S_8 = 80 + 112 \tag{2.0.11}$$

$$S_8 = 192 (2.0.12)$$