

Homework4

Database Design

A. $R(A, B, C, D, E)$

$F = \{BC \rightarrow D, D \rightarrow E, A \rightarrow C, B \rightarrow C\}$

i. $(AB)^+ : - B \rightarrow C, BC \rightarrow D, D \rightarrow E = \{A, B, C, D, E\}$

ii. Yes, since $BC \rightarrow D$ and $D \rightarrow E$, then $BC \rightarrow E$ in F^+ transitivity

iii.

Step1.

1. $(A)^+ : A \rightarrow C = \{A, C\}$

2. $(B)^+ : B \rightarrow C = \{B, C, D, E\}$

3. $(C)^+ : C = \{C\}$

4. $(D)^+ : D \rightarrow E = \{D, E\}$

5. $(E)^+ : E = \{E\}$

- There is no candidate key in a single closure because none of their closure contains all the attributes in R

Step2

Calculating the closures of 2 attributes at once we get: $AB^+, AC^+, AD^+, AE^+, BC^+, BD^+, BE^+, CD^+, CE^+, DE^+$

1. $(AB)^+ = A \rightarrow C, B \rightarrow C, BC \rightarrow D, D \rightarrow E = (ABCDE)$AB is a superkey and hence it is also a candidate key
2. $(AC)^+ = (AC)$
3. $(AD)^+ = (ACDE)$it is not a superkey
4. $(AE)^+ = (ACE)$...it is not a superkey
5. $(BC)^+ = (BCDE)$... it is not a superkey
6. $(BD)^+ = (BCDE)$... it is not a superkey
7. $(BE)^+ = (BCDE)$... it is not a superkey
8. $(CD)^+ = (CDE)$...it is not a superkey

9. $(CE)^+ = (CE)$...it is not a superkey
10. $(DE)^+ = (DE)$...it is not a superkey

Step3

Checking with the three attributes if they form a superkey, we need to remove any attribute that contain AB

1. $(ACD)^+ = (ACDE)$
2. $(ACE)^+ = (ACE)$
3. $(ADE)^+ = (ACDE)$
4. $(BCD)^+ = (BCDE)$
5. $(BCE)^+ = (BCDE)$
6. $(BDE)^+ = (BCDE)$
7. $(CDE)^+ = (CDE)$
 - All of them doesn't form a super key

Step4

Checking with the four attributes if they form a superkey, we need to remove any attribute that contain AB

1. $(ACDE)^+ = (ACDE)$
 2. $(BCDE)^+ = (BCDE)$
 - All of them doesn't form a super key
- We do not need to check with five attributes because AB is subset of ABCDE and AB is the candidate key.

B. $R(A, B, C, D, E)$
 $F = \{AB \rightarrow D, E \rightarrow C\}$

1. R is **not** in BCNF because the condition to be in BCNF is $\alpha \rightarrow \beta$, α should be the superkey in all the dependencies. In our function $D \rightarrow C$, D is neither a superkey of R or trivial this is D should be a subset of AB and C should be a subset of D. Therefore, R is not in BCNF.
2. R is **not** in 3NF, as D is also not contained in any candidate key of R as the only candidate key is AB.

C. $R(A, B, C, D)$

$F = \{A \rightarrow B, BC \rightarrow D\}$

1. The only candidate key is AC.
2. R is **not** in 3NF because of $A \rightarrow B$ where B is not part of any key neither A is primary key which violates the principle of 3NF because in 3NF for $X \rightarrow F$ is valid when either X is super key or attribute F is part of any key but none of them is happening in $A \rightarrow B$, neither A is superkey nor B is part of any key.

D. Player (ID, Name, Birthday, Address, Email, PhoneNumber, PlayPos)

1. $ID \rightarrow (Name, Birthday, Address, Email, PhoneNumber, PlayPos)$

$Name \rightarrow (ID, Birthday, Address, Email, PhoneNumber, PlayPos)$

2. The candidate keys are

$\{ID\}$

$\{Name\}$