

# Random variables:

---

Ex: of a random variable:

$$X = \begin{cases} \text{value} & \text{condition} \\ \text{another value} & \text{another condition} \end{cases}$$

$$** \lim(1 + a/n)^n = e^a$$

## Types of random variables:

**1: discrete:** takes a finite number of discrete distinct separate values.

**2: continuous:** takes infinite number of values

Ex: Y = exact mass of a random animal selected at the zoo.

---

$$P(X=k) = \lim_{n \rightarrow \infty} \binom{n}{k} \left( \frac{\lambda}{n} \right)^k \left( 1 - \frac{\lambda}{n} \right)^{n-k} = \frac{\lambda^k}{k!} * e^{-\lambda}$$

Where:

X: is a random variable

K: is a particular number

## The law of large numbers:

**Ex:**

1- if I have a random variable  $X$  = # of heads after 100 tosses of a fair coin

2- then the expected value =  $E(X) = 100 * 0.5 = 50$

3- Now we calculate the mean of  $X = (X_1 + X_2 + X_3 + \dots + X_n)/n$

The law of large numbers tells us that the mean of all observations is going to be 50 if  $n$  approaches  $\infty$

---

$F$  = probability of making a free throw

$$P(\text{exactly } K \text{ scores in } N \text{ attempts}) = \binom{n}{k} F^k * (1 - F)^{n-k}$$