

Distribution: the possible values a variable can take and how frequently they occur.

Y: the actual outcome of an event

y: one of the possible outcomes

$p(y)$: the probability function

mean = average value (μ)

variance = how spread out the data is or how the data is far away from the mean (σ^2)

standard deviation is the root square of the variance (σ for population data) and (s for sample data)

x	\sim	N	(μ, σ^2)
variable	tilde	type	characteristics

Binomial Distribution: $B(n, p)$ or $B(\text{number of trials and the probability of success in each one})$

Conditional Probability Law: $p(E|F) = p(E \cap F) / p(F)$

Or

Product rule: $p(E \cap F) = p(E|F) * p(F)$

Independent Events Law: $p(E|F) = p(E)$

If you want to know if two events are independent or not, we use the following law: if $p(E \cap F) = p(E) * p(F)$ then the two events are independent.

So, $p(E_1 \cap E_2 \cap \dots \cap E_n) = p(E_1) * p(E_2) * \dots * p(E_n)$

Bayes' theorem: $P(A|E) = [P(A) * P(E|A)] / P(E)$.

Sample space: every possible result that can happen.

Outcome: number of results \wedge number of repetitions.

Ex: $A = \{1,2,3\}$, $B = \{2,3,4\}$, $S = \{0,1,2,3,4\}$.

$$A \cap B = \{2,3\}$$

$$A \cup B = \{1,2,3,4\}$$

$$A^c = \{0,4\}$$

$$B^c = \{0,1\}$$

$$P(A \cap B) = 2/5$$

$$P(A \cup B) = 4/5$$

$$P(A) = 3/5$$

$$P(B^c) = 2/5$$

$$P(S) = 5/5 = 1$$

Counting techniques

1. Multiplication rule

2. Permutation rule:

- a. Ordering elements
- b. Of similar objects
- c. Of subsets

3. Combination

Multiplication rule:

Ex: a coffee shop has 4 types of sandwiches, 5 types of coffee and 2 cake types in how many ways can we choose one of each.

$$= 4 \times 5 \times 2 = 40.$$

Permutation rule:

1 – ordering elements:

Ex: 6 students are lining up outside the heads office what is the number of different orders that they could queue up in ?

$$= 6! = 720$$

2 – subsets

Ex: in an examination a student must choose 4 out of 10 questions. how many different ways can she select which 4 questions she attempts.

$$P_r^n = \frac{n!}{(n-r)!} = {}^{10}P_4 = 5040$$

3 – similar objects

Ex: how many different orders of that word [MINIMUM]

$$= n! / (n! * n!) = 7! / (3! * 2!) = 420.$$

