

$$3)a) f(x) = x^3 + 4x^2 - 10$$

$$x_0 = 1.5 \quad (1, 2) \text{ interval}$$

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$$

$$f'(x) = 3x^2 + 8x$$

$$x_1 = 1.5 - \frac{(1.5)^3 + 4(1.5)^2 - 10}{3(1.5)^2 + 8(1.5)} = 1.37333$$

$$x_2 = 1.37333 - \frac{(1.37333)^3 + 4(1.37333)^2 - 10}{3(1.37333)^2 + 8(1.37333)} = 1.36526$$

$$x_3 = 1.36526 - \frac{(1.36526)^3 + 4(1.36526)^2 - 10}{3(1.36526)^2 + 8(1.36526)} = 1.36523$$

$$x_4 = 1.36523 - \frac{(1.36523)^3 + 4(1.36523)^2 - 10}{3(1.36523)^2 + 8(1.36523)} = 1.36523$$

convergence occurred at x_4

$$3) b) |x_n - r| / |x_{n-1} - r|^2$$

$$f''(x) = 6x + 8$$

$$\text{at } x_1 = 1.37333$$

$$|1.37333 - r| / |1.5 - r|^2 = 0.44596$$

$$|6(1.37333) + 8 / 2(3(1.37333)^2 + 8(1.37333))| \\ = 0.48784$$

$$\text{at } x_2 = 1.36526$$

$$|1.36526 - r| / |1.37333 - r|^2 = 0.45724$$

$$|6(1.36526) + 8 / 2(3(1.36526)^2 + 8(1.36526))| \\ = 0.49024$$

$$\text{at } x_3 = 1.36523$$

$$|1.36523 - r| / |1.36526 - r|^2 = 0.4875$$

$$|6(1.36523) + 8 / 2(3(1.36523)^2 + 8(1.36523))| \\ = 0.49024$$