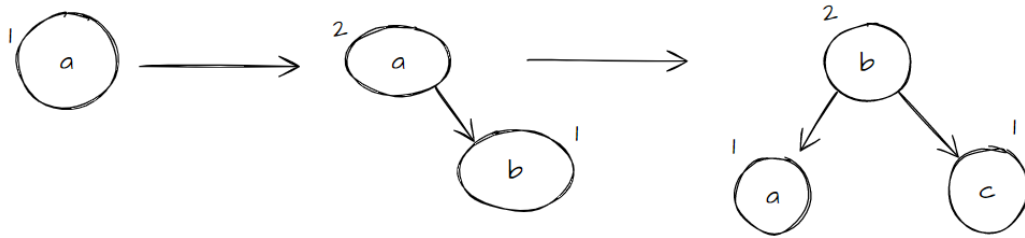
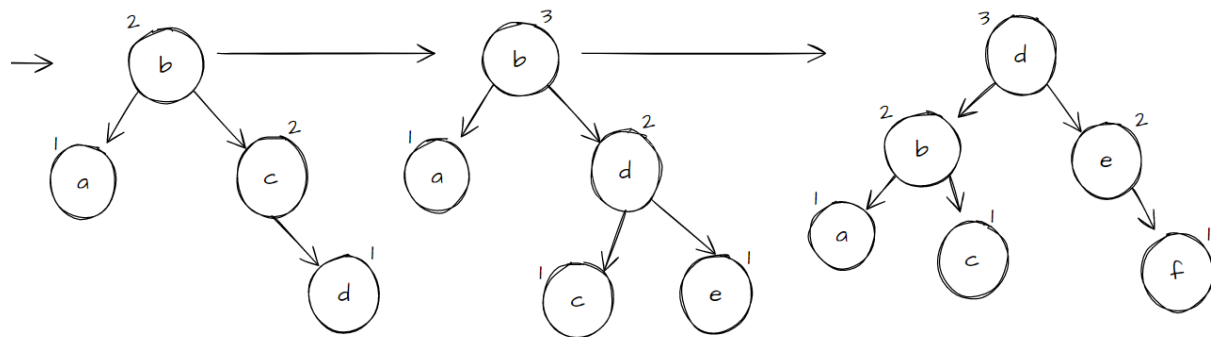


2383 Assignment

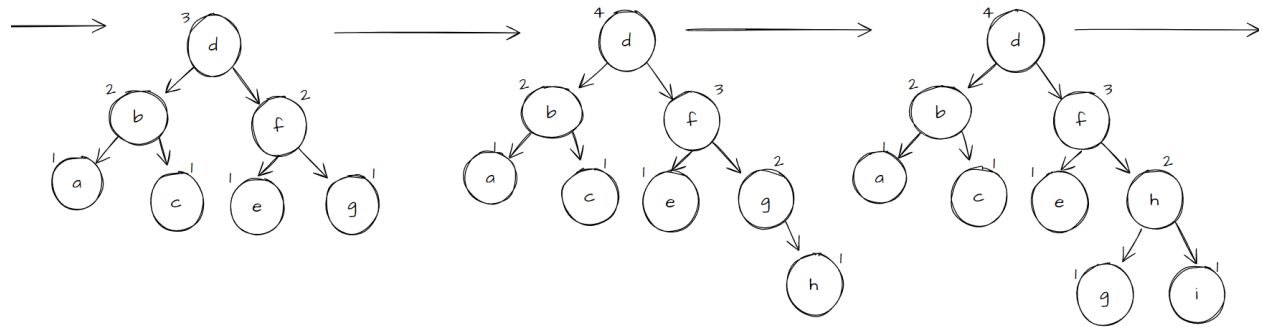
1- a,b,c,d,e,f,g,h,i,j,k,l



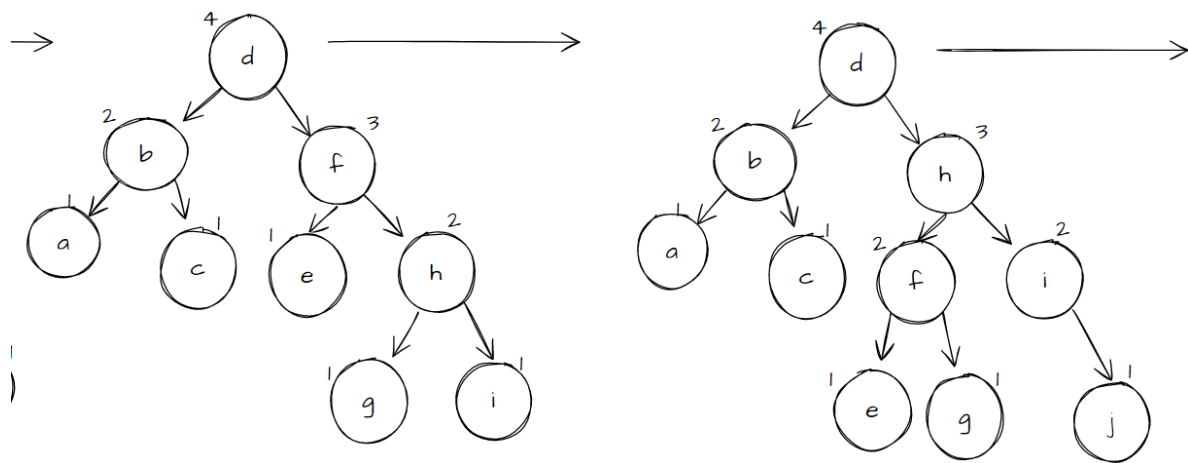
Then



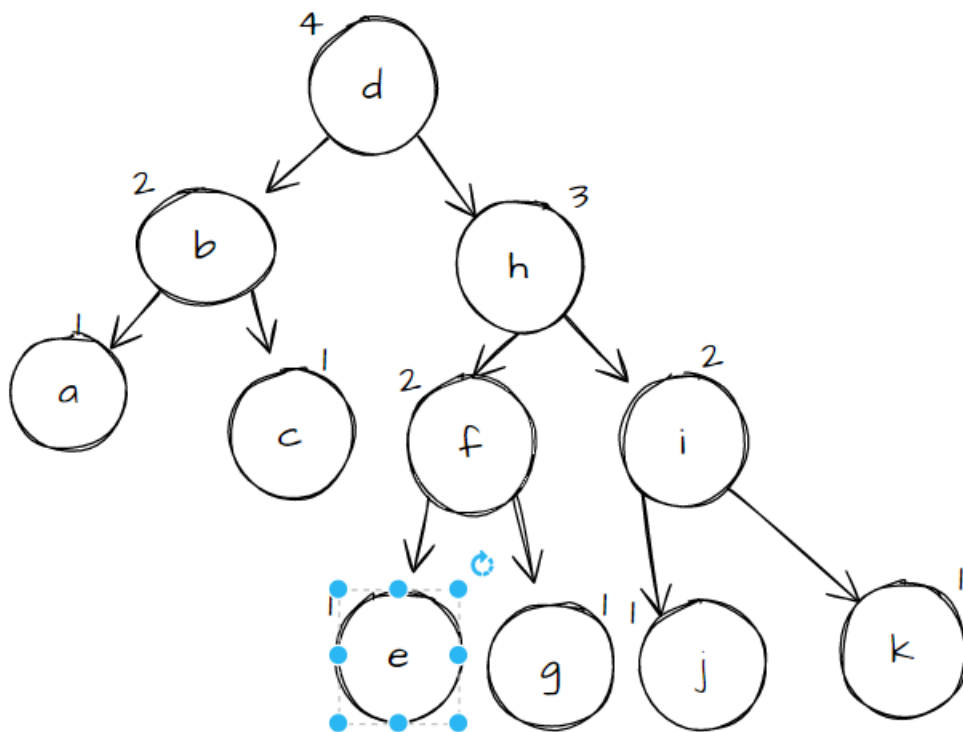
Then



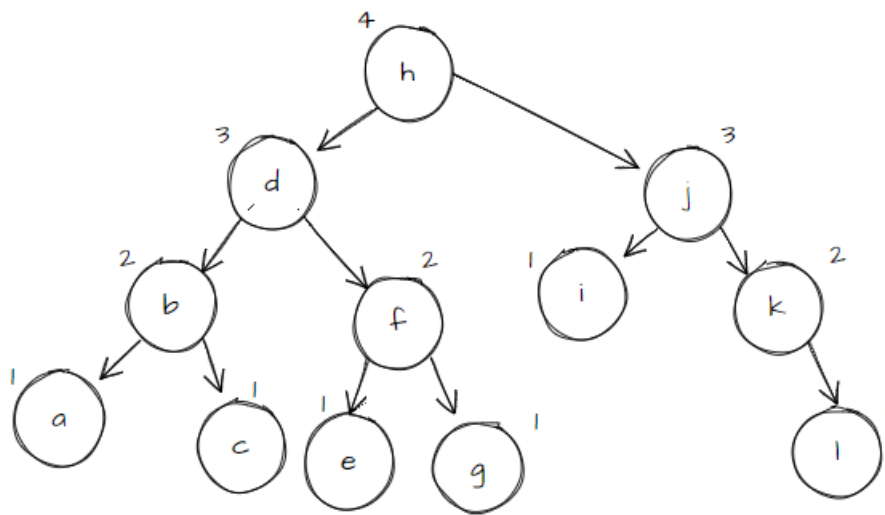
Then



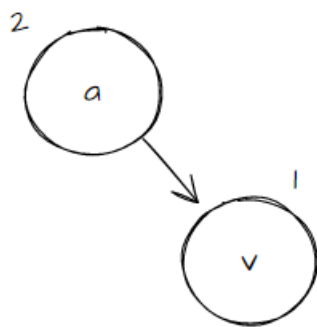
Then



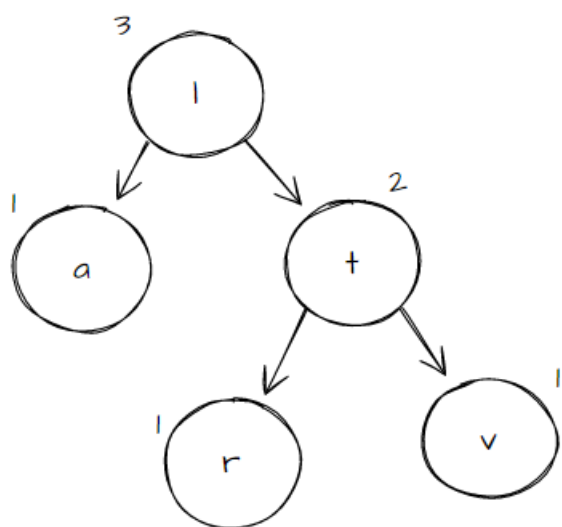
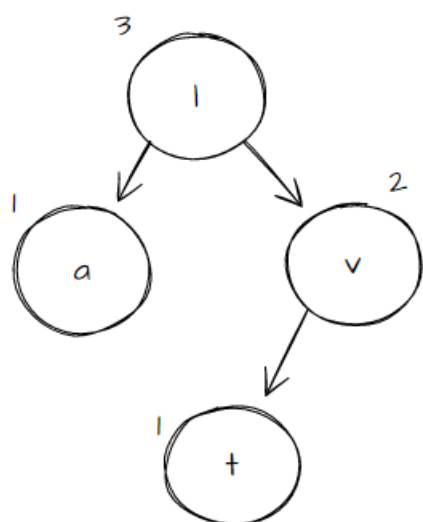
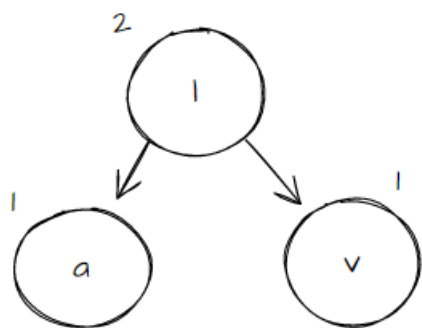
Finally

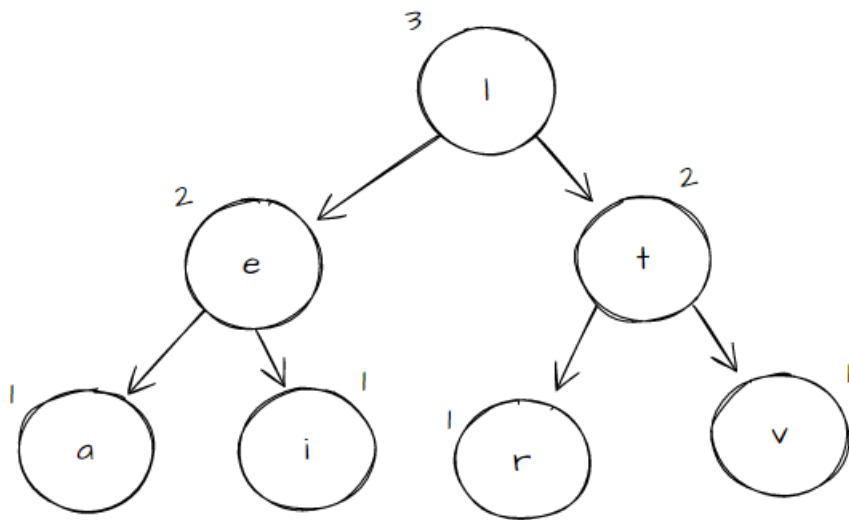
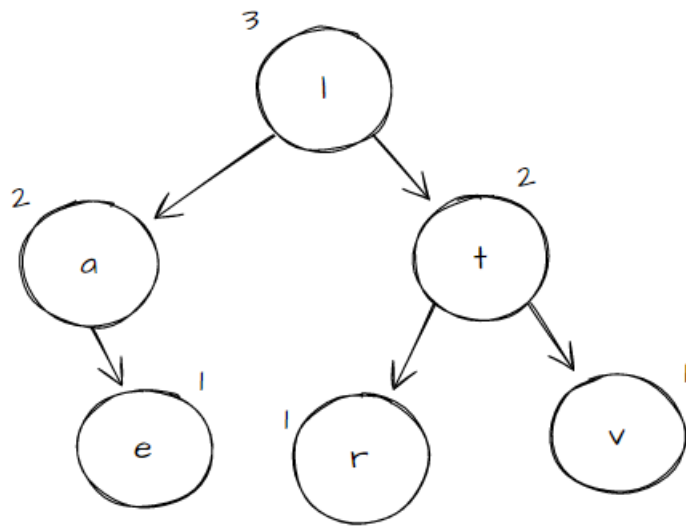


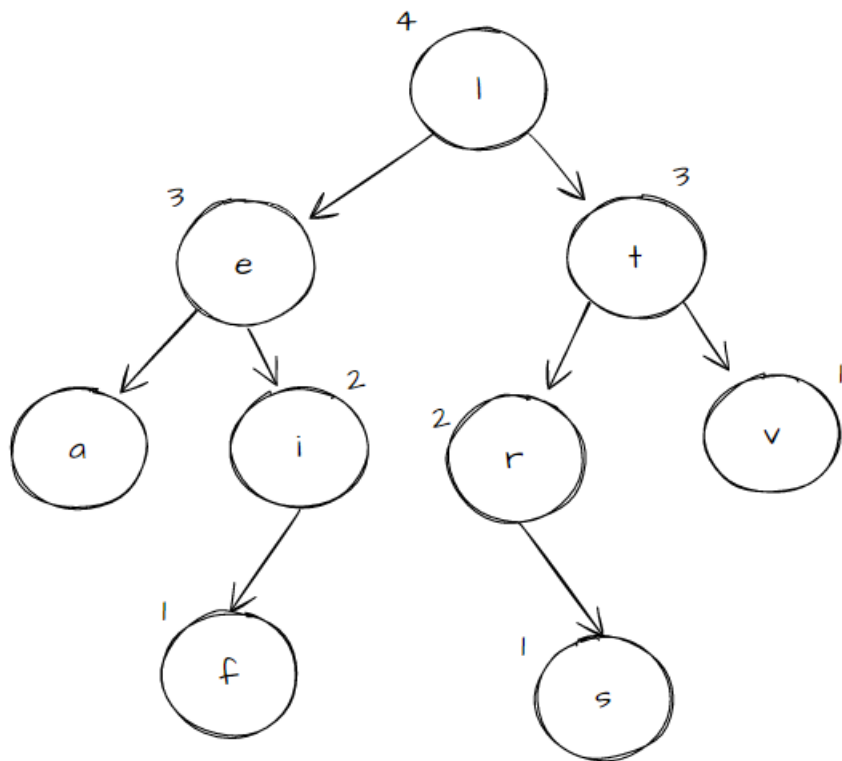
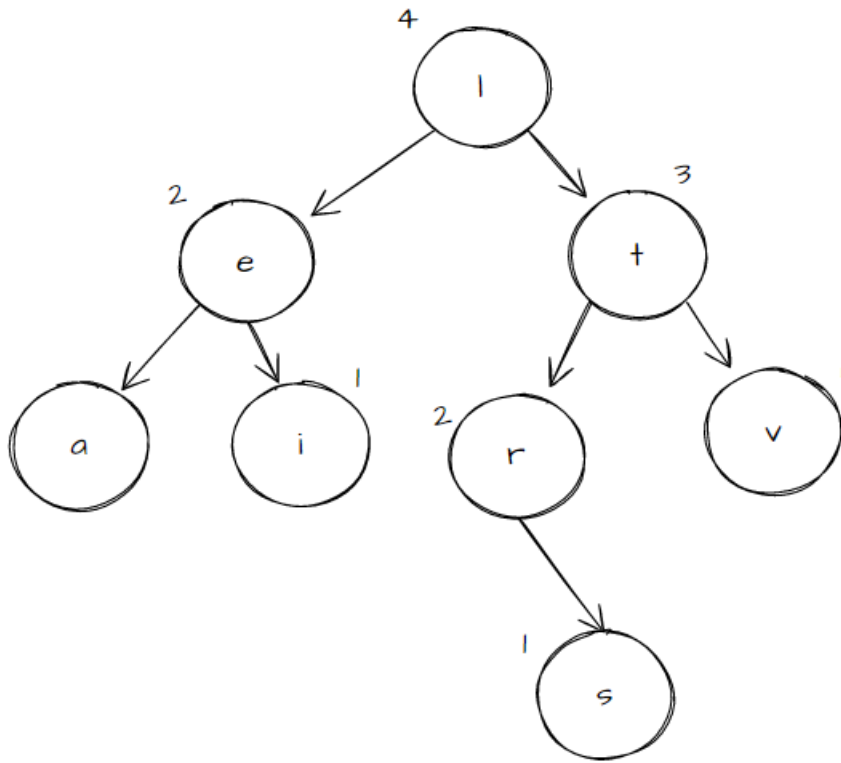
1- a,v,l,t,r,e,i,s,f,u,n

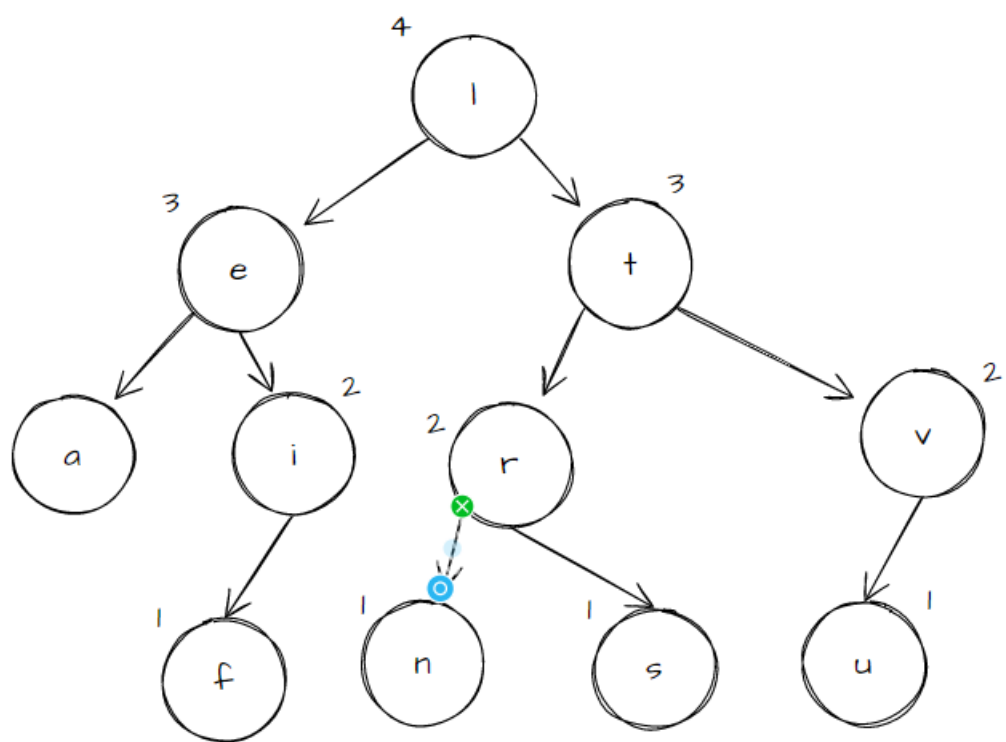


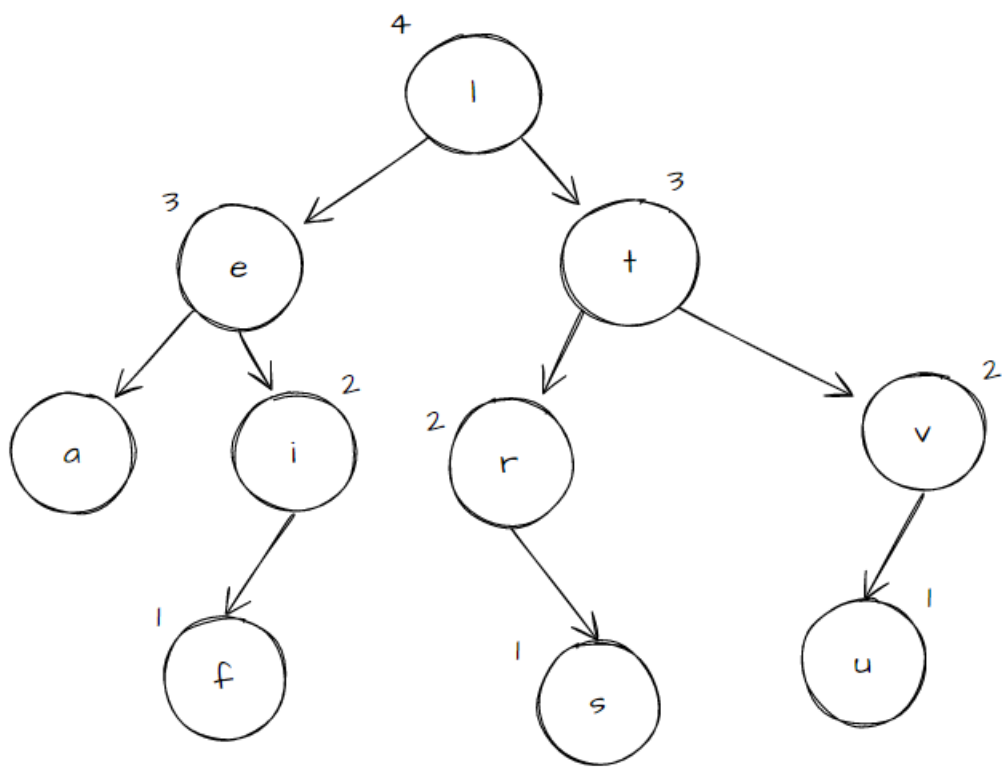
Then

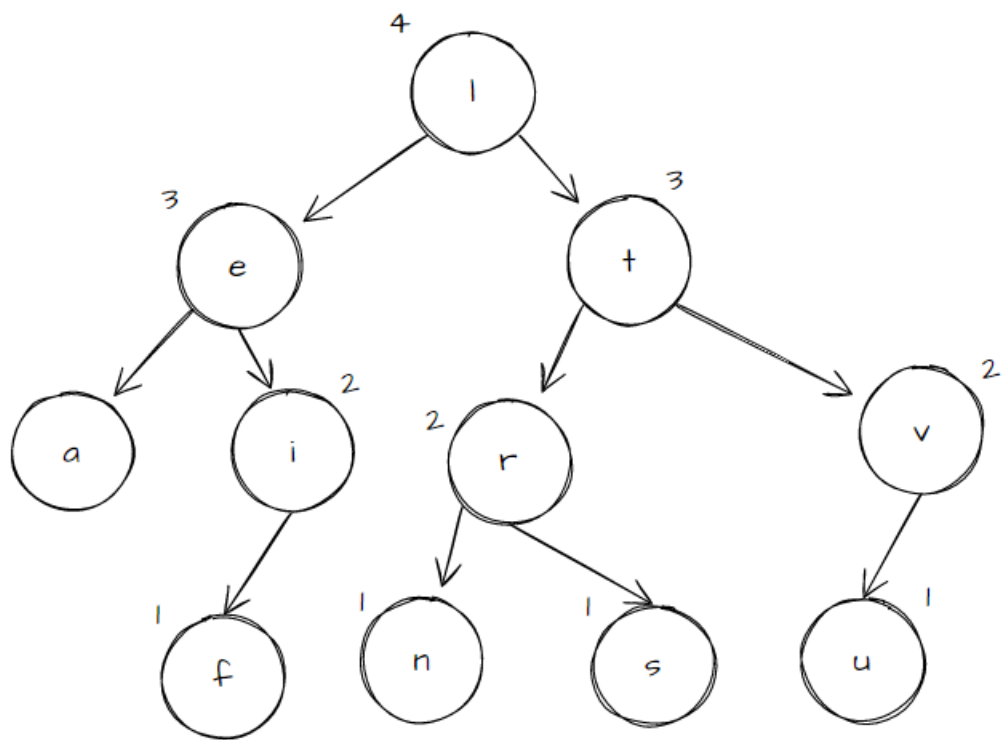












2-

Algorithm: findAllInRange (n, k1, k2)

Input: Node n, int k1, int k2

```
findAllInRange(n,k1,k2){
    count ← 0;
    if(n = null){
        return;
    }
    if (k1 < n.data)
    {
        findAllInRange(n.left, k1, k2);
    }
    if (k1 <= n.data AND k2 >= n.data) {
        print(n.data + " ");
        count++;
    }
    if (k2 > n.data) {
        findAllInRange(n.right, k1, k2);
    }
}
```

findAllInRange(int k1, int k2)

```
{
    findAllInRange(root, k1, k2);
}
```

Time complexity is O(n).

3-

k	$(2i+5)\text{mod}11$	$7 - (i \text{ mod } 7)$
12	7	
44	5	
13	9	
88	5	$3 \rightarrow (5+3) \text{ mod } 11 = 8$
23	7	$5 \rightarrow 7+5\text{mod}11 = 1$
94	6	
11	5	$3 \rightarrow 8$ Then $(5+2*3) \text{ mod } 11 = 0$
39	6	$3 \rightarrow 9 \rightarrow 1 \rightarrow 4$
20	1	$1 \rightarrow 2$
16	4	$5 \rightarrow 9 \rightarrow 3$
5	4	$2 \rightarrow 6 \rightarrow 8 \rightarrow 10$

Hash Table	
H[0]	11
H[1]	23
H[2]	20
H[3]	16
H[4]	39
H[5]	44
H[6]	94
H[7]	12
H[8]	88
H[9]	13
H[10]	5

4-

4) Algorithm: merge (curArray [], l, m1, m2, h, destArray [])
input: int curArray [], l, m1, m2, h, destArray [].

```
merge (curArray [ ], l, m1, m2, h, destArray [ ]) {  
    i ← l  
    j ← m1  
    k ← m2  
    lc ← l  
    while ((i < m1) AND (j < m2) AND (k < h)) {  
        if (curArray [i] < curArray [j]) {  
            if (curArray [i] >= curArray [k])  
                destArray [lc++] ← curArray [k]  
            else  
                destArray [lc++] ← curArray [i++]  
        }  
        else {  
            if (curArray [j] < curArray [k]) {  
                destArray [lc] ← curArray [j]  
                lc++  
                j++  
            }  
            else {  
                destArray [lc] ← curArray [k]  
                lc++  
                k++  
            }  
        }  
    }  
}
```

```

while ((i < m1) AND (j < m2)) {
    if (curArray[i] < curArray[j]) {
        destArray[lc] ← curArray[i]
        lc++
        i++
    }
    else {
        destArray[lc] ← curArray[j]
        lc++
        j++
    }
}

while ((j < m2) AND (k < h)) {
    if (curArray[j] < curArray[k]) {
        destArray[lc] ← curArray[j]
        lc++
        j++
    }
    else {
        destArray[lc] ← curArray[k]
        lc++
        k++
    }
}

while ((i < m1) AND (k < h)) {
    if (curArray[i] < curArray[k]) {
        destArray[lc] ← curArray[i]
        lc++
        i++
    }
    else {
        destArray[lc++] ← curArray[k++]
    }
}

```

```

    while (i < m1) {
        destArray[lc] ← curArray[i]
        lc++
        i++
    }
    while (j < m2) {
        destArray[lc] ← curArray[j]
        lc++
        j++
    }
    while (k < h) {
        destArray[lc] ← curArray[k]
        lc++
        k++
    }
}

Algorithm: MS3WR (curArray[], l, h, destArray[])
input: int curArray[], l, h, destArray[]

MS3WR (curArray[], l, h, destArray[]) {
    if (h - l < 2) THEN
        return
    m1 ← 1 + ((h - l) / 3)
    m2 ← 1 + 2 * ((h - l) / 3) + 1
    MS3WR (destArray, l, m1, curArray)
    MS3WR (destArray, m1, m2, curArray)
    MS3WR (destArray, m2, h, curArray)
    merge (destArray, l, m1, m2, h, curArray)
}

```

```

Algorithm: MS3Way (curArray[], n)
input: int curArray[], n

MS3Way (curArray[], n) {
    if (n = 0)
        return
    for (i ← 0; i < n; i++)
        fArray[i] ← curArray[i]
    MS3WR (fArray, 0, n, curArray)
    for (i ← 0; i < n; i++)
        curArray[i] ← fArray[i]
}

```

$$T(n) = 3T\left(\frac{n}{3}\right) + O(n)$$

$$= 3(3T(n/3) + n/3) + n$$

$$= 3^2 T(n/3^2) + 2n$$

$$= 3^2 (3T(n/3^2) + n/9) + 2n$$

⋮

$$3^k T(n/3^k) + kn$$

$$\frac{n}{3^k} = 1 \rightarrow n = 3^k \rightarrow \log n = k \log 3$$

$T(n)$ is $O(n \log n)$

5-

Algorithm: exchange(array, ind1, ind2)

Input: int[] array, int ind1, ind2

```
exchange(array, ind1, ind2){  
    temp ← array[ind1]  
    array[ind1] ← array[ind2]  
    array[ind2] ← temp;  
}
```

Algorithm: gRI(min, max)

Input: int min, int max

```
gRI(min, max){  
    r ← new Random()  
    lim ← (max-min)+1  
    rni ← r.nextInt(lim)+min  
    return rni  
}
```

Algorithm: fKL(array, k)

Input: int[] array, int k

```
fKL(array, k){  
    if array.length = 1 then  
        return array[0]  
    return sR(array, 0, array.length-1, k)  
}
```


Algorithm: sR(array, start, end, k)

Input: int[] array, int start, int end, int k

```
sR(array, start, end, k){
    ind ← rP(array, start, end)
    if (ind = (k-1))
        return array[ind]
    else if(ind >= k)
        return sR(array, start, ind-1, k)
    else
        return sR(array, ind+1, end, k)
}
```

Algorithm: rP(array, start, end)

Input: int[] array, int start, int end

```
rP(array, start, end){
    rI ← gRi (start, end)
    exchange(array, rI)
    piv ← array[end]
    p ← start-1
    for (i ← start to end){
        if (array[i]>=piv){
            p++
            exchange(array, i, p)
        }
    }
    exchange(array, p+1, end)
    return p++
}
```

Time complexity is $O(n)$