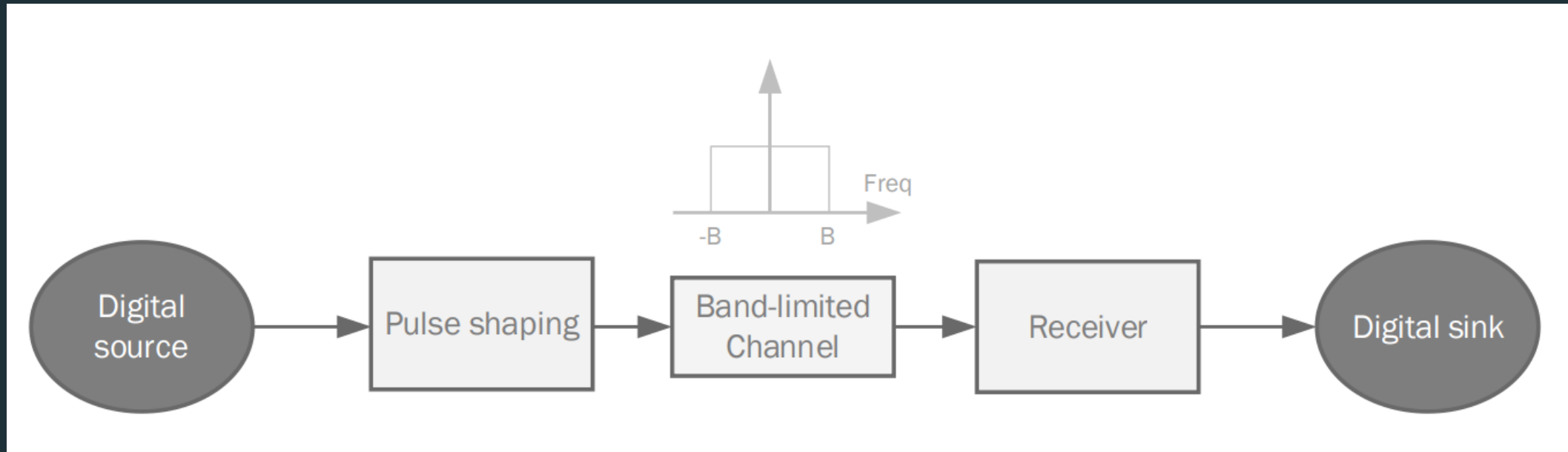


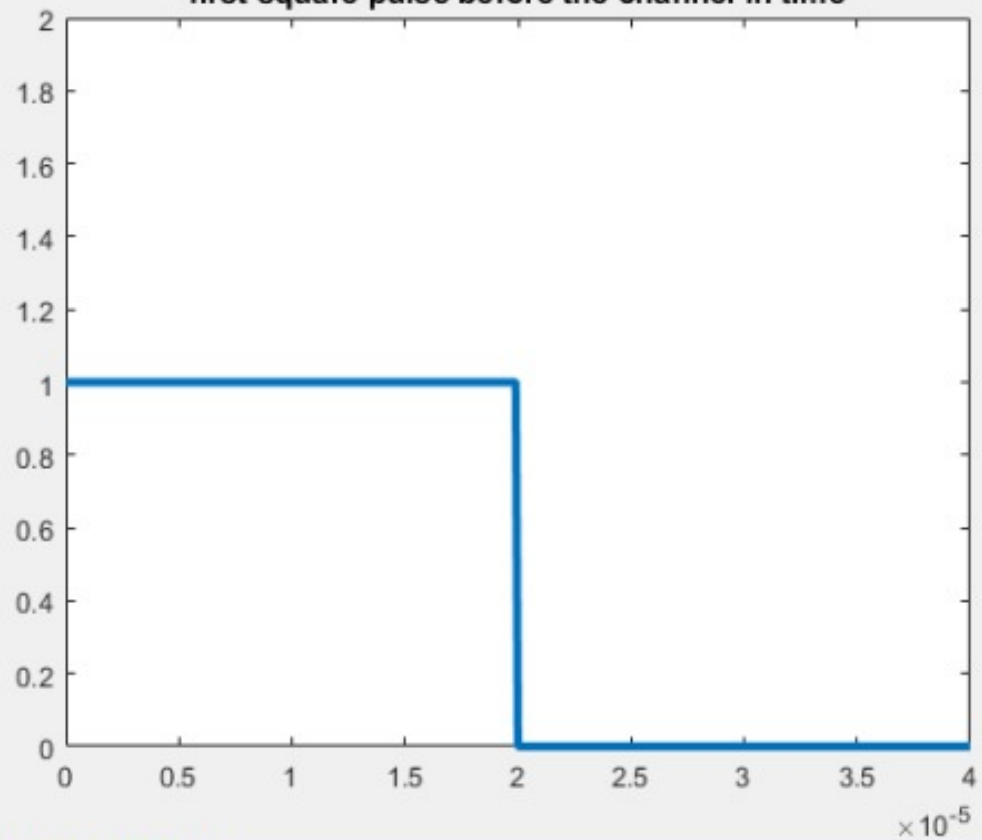


INTER-SYMBOL
INTERFERENCE DUE
TO BAND-LIMITED
CHANNELS

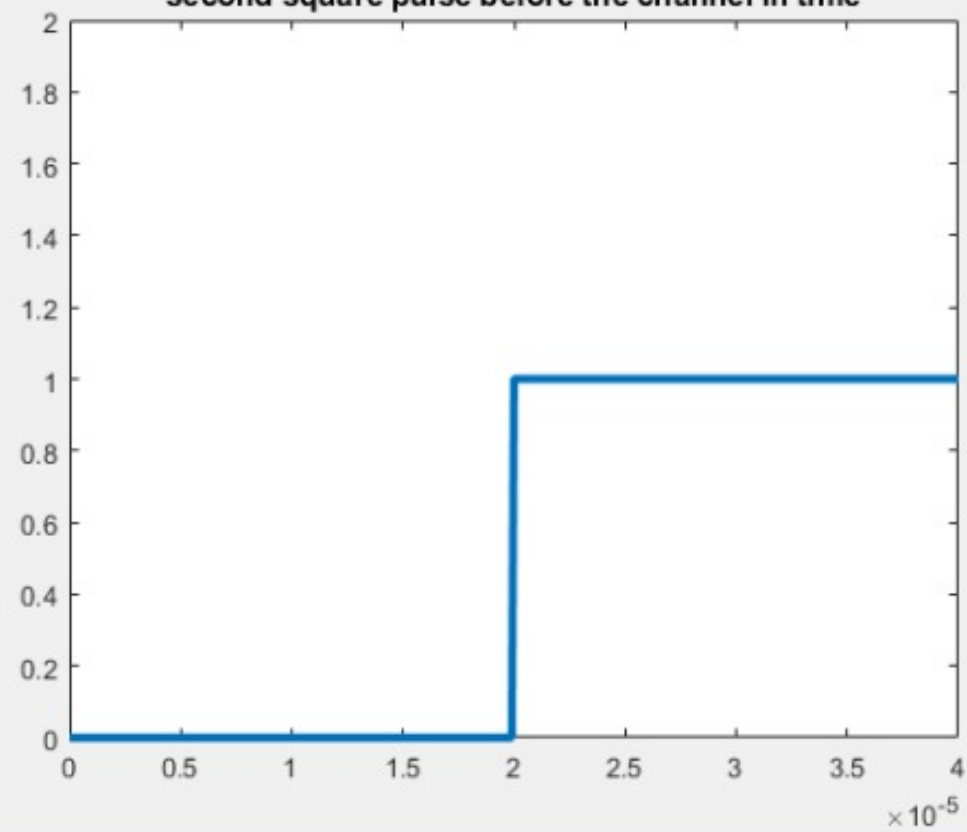
GENERATING FIRST AND SECOND PULSE WITH PERIOD = $2/B$ IN TIME DOMAIN



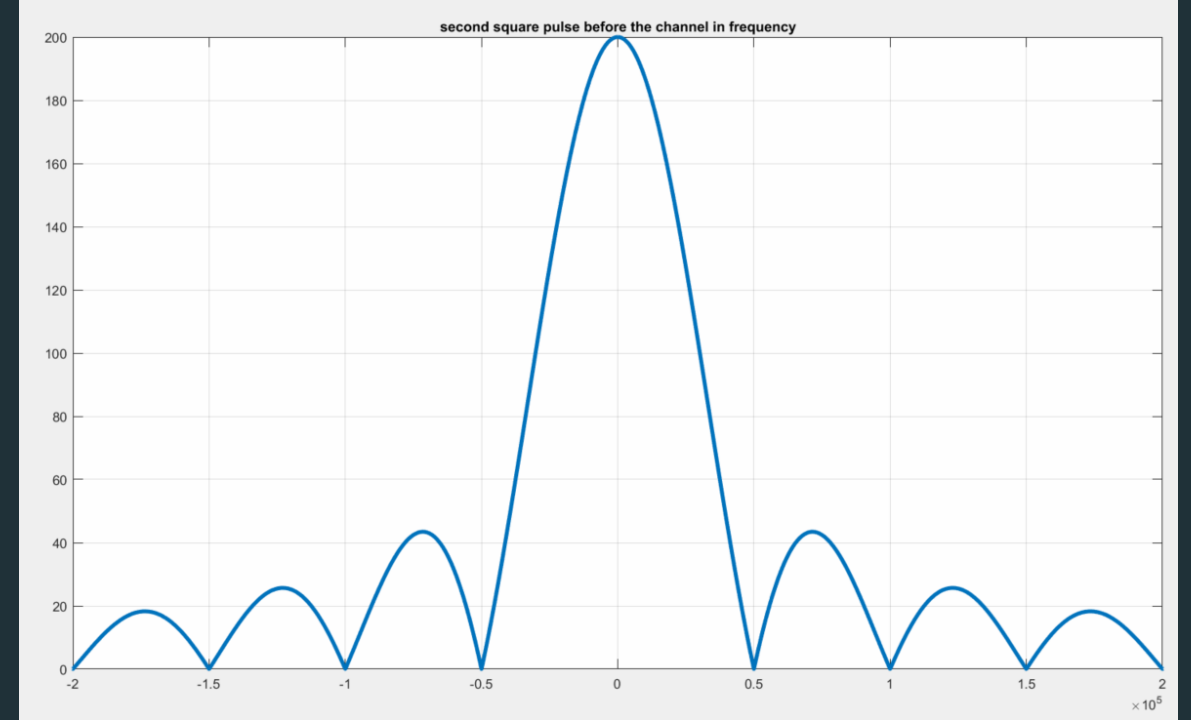
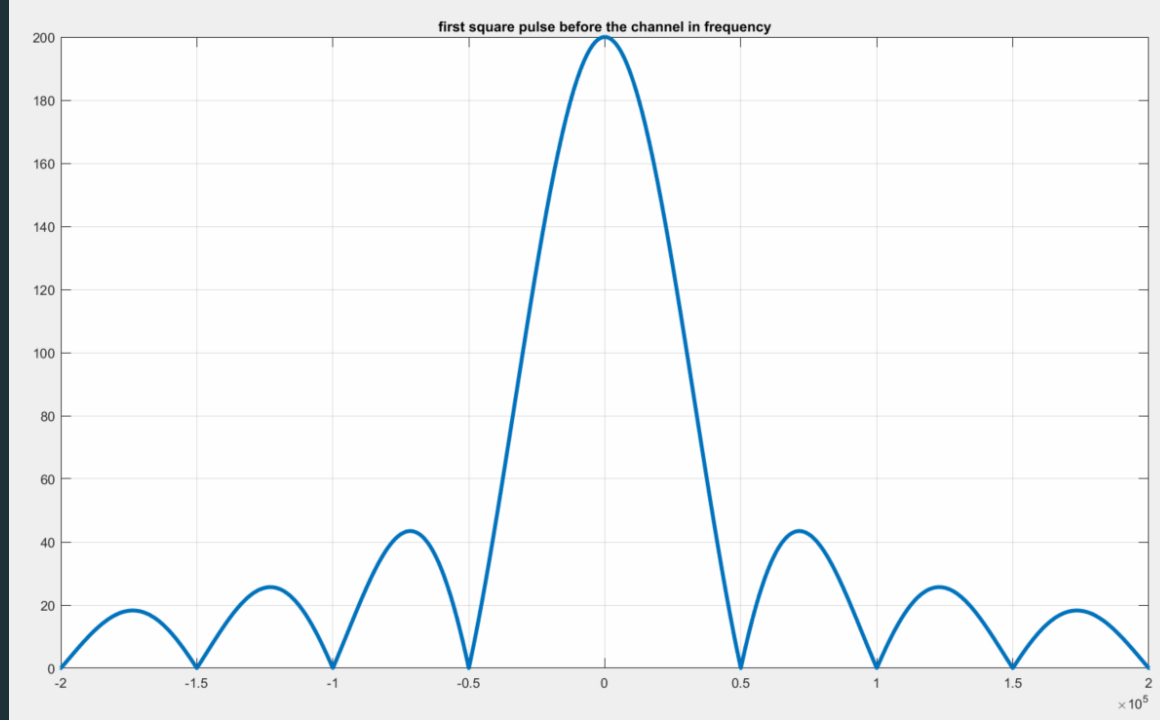
first square pulse before the channel in time



second square pulse before the channel in time

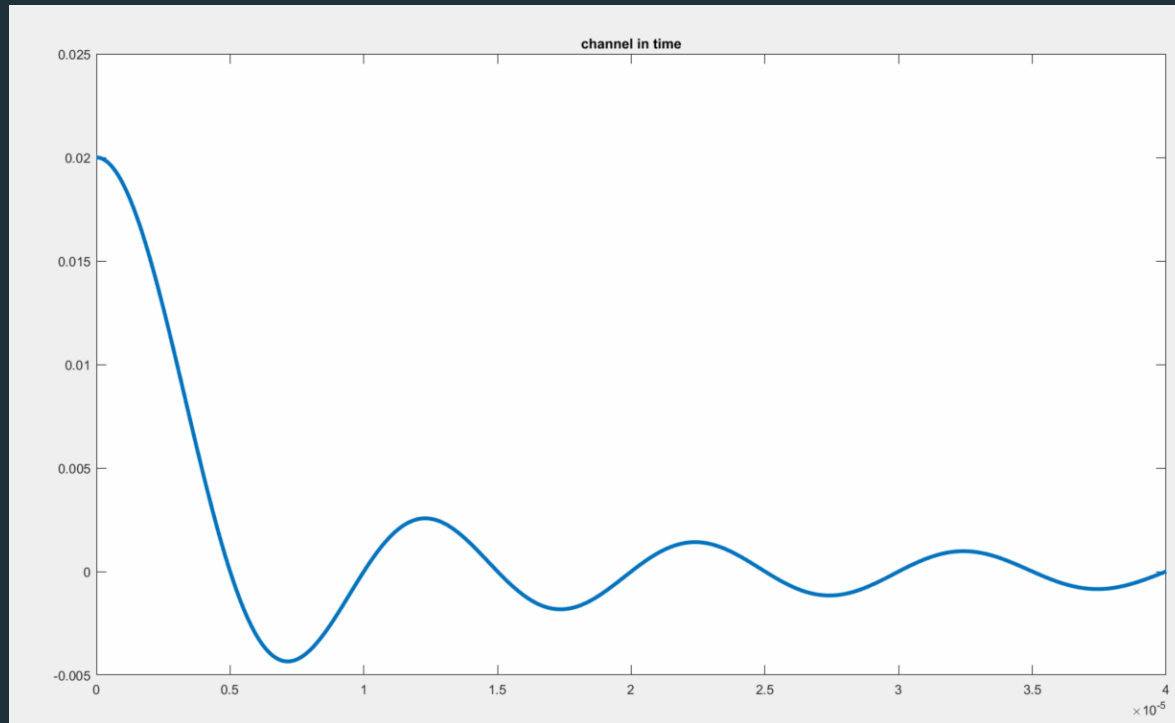


GENERATING FIRST AND SECOND PULSE WITH PERIOD = $2/B$ IN FREQUENCY DOMAIN

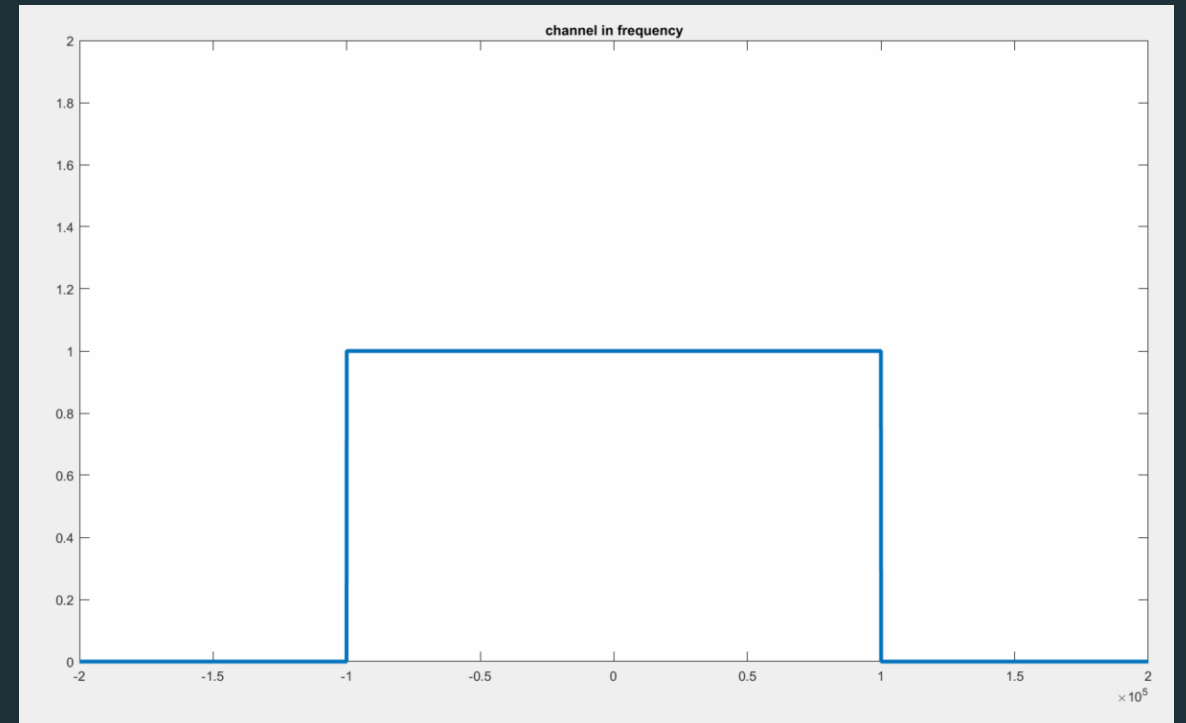


NRZ INPUT NULL TO NULL BANDWIDTH IS $1/T_b = 50\text{KHZ}$

BAND-LIMITED CHANNEL WITH BANDWIDTH $B = 100$ KHZ.

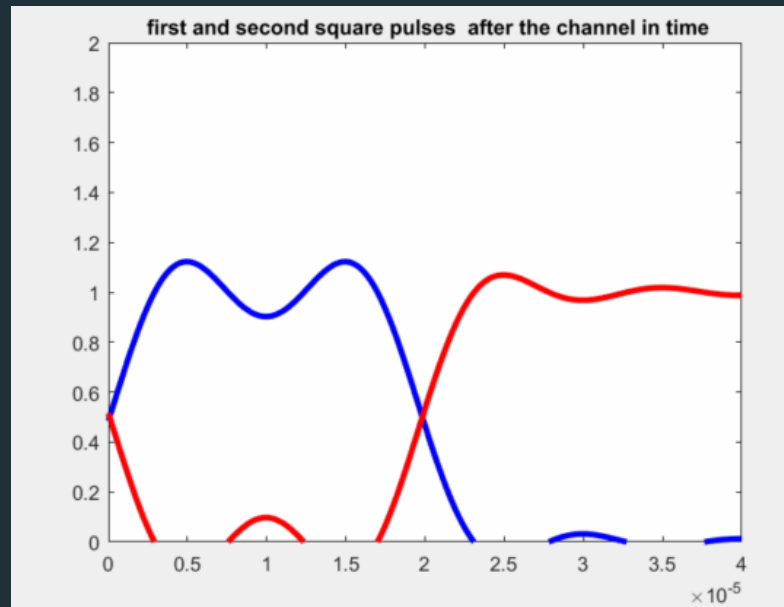


In time domain

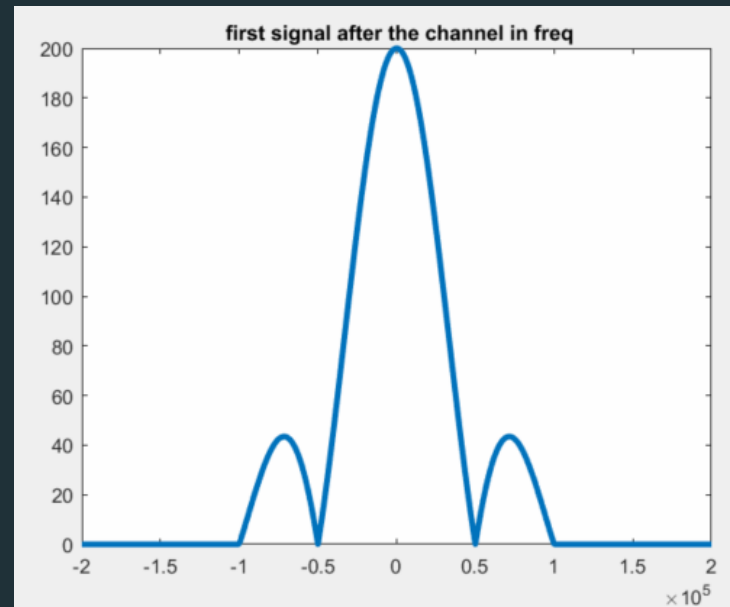


In frequency domain

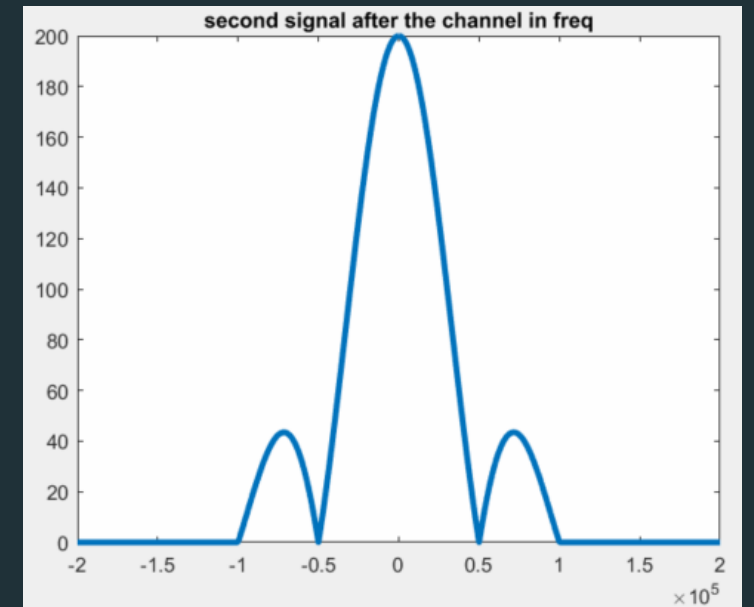
FIRST AND SECOND SQUARE AFTER THE CHANNEL IN TIME AND FREQUENCY DOMAIN



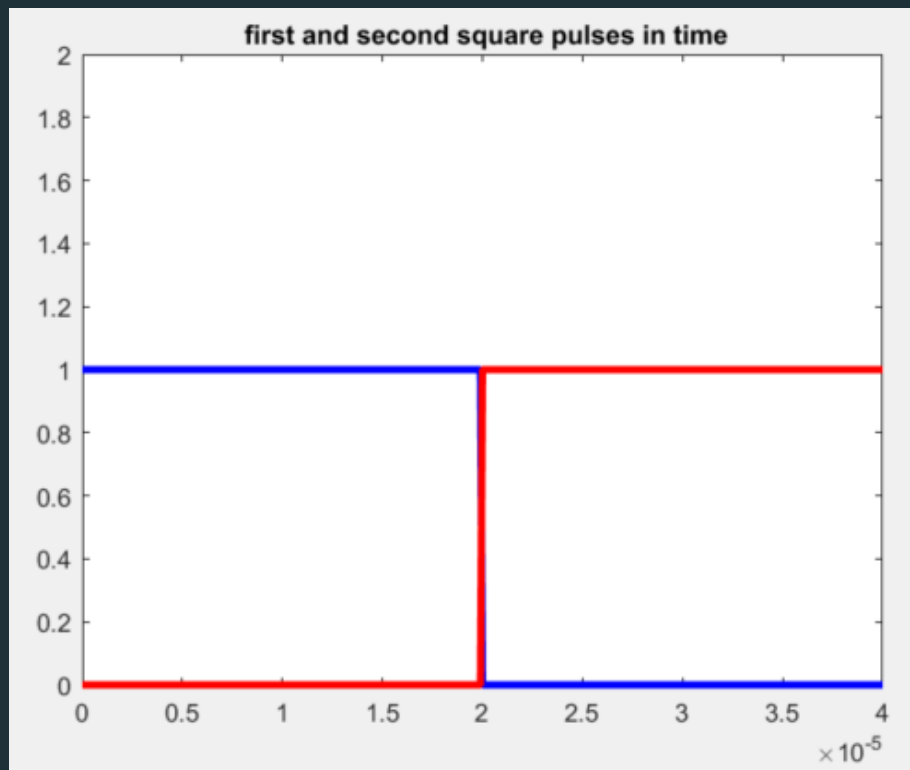
In time domain



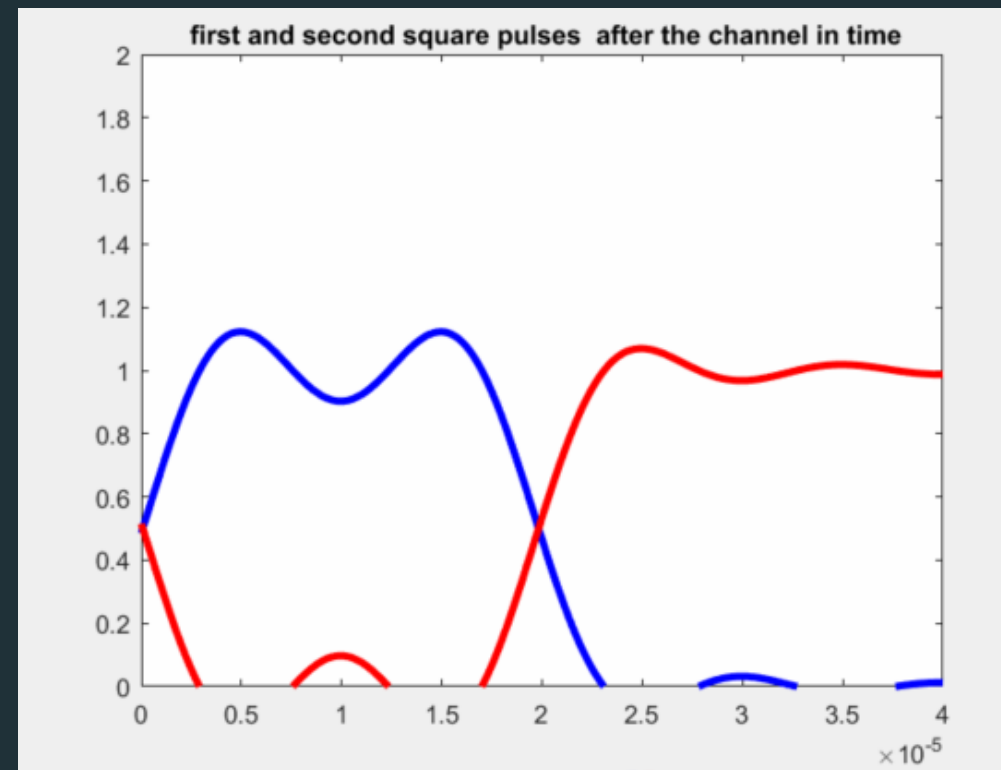
In frequency domain



SHOWING THE TWO PLOTS THE FIRST SQUARE PULSE BEFORE IT PASSES THROUGH THE CHANNEL, AND ONE AFTER IN TIME DOMAIN.

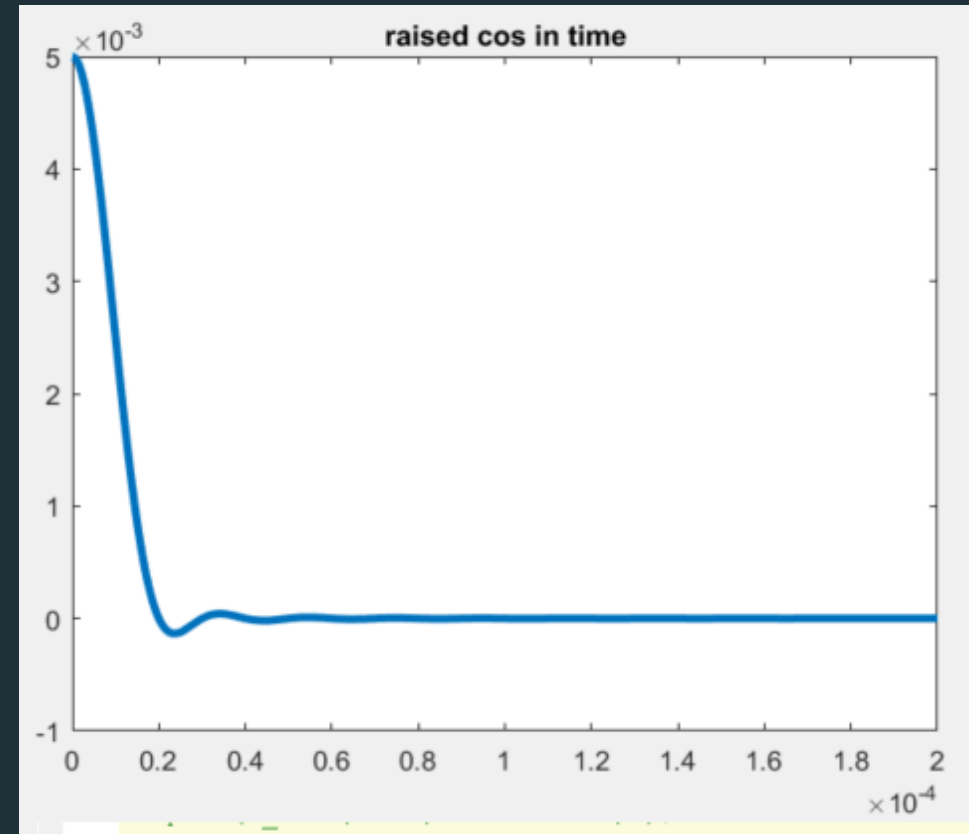
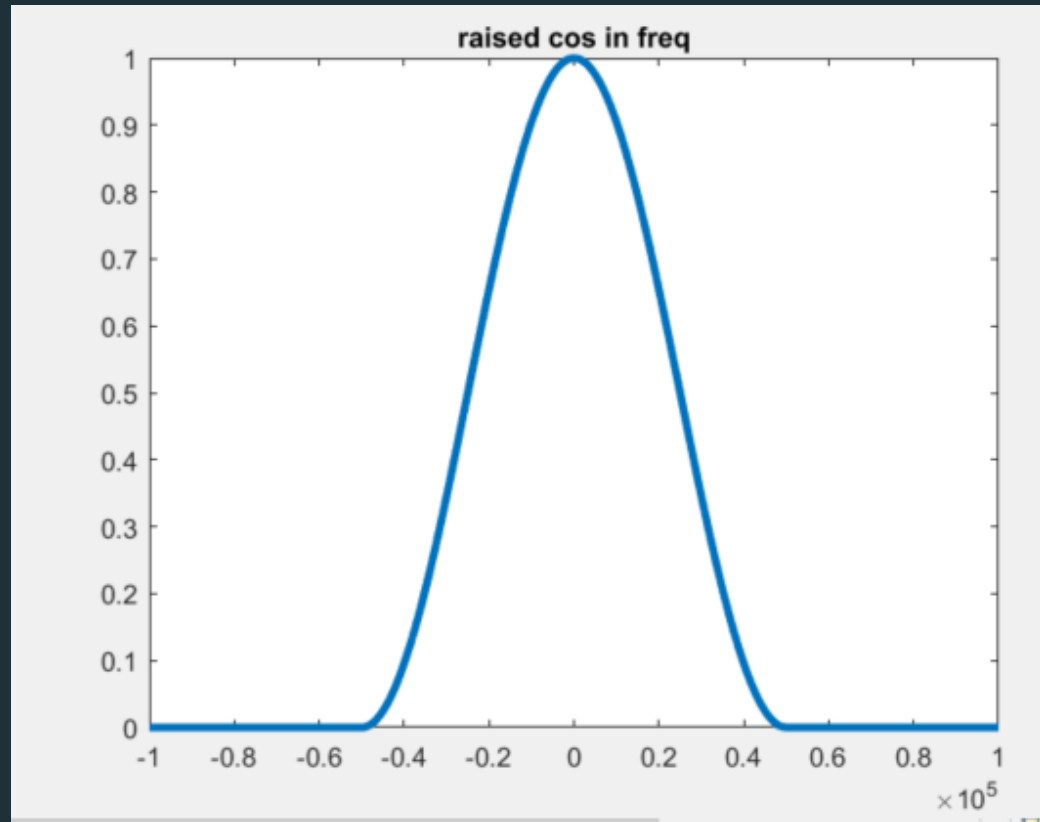


Before the channel

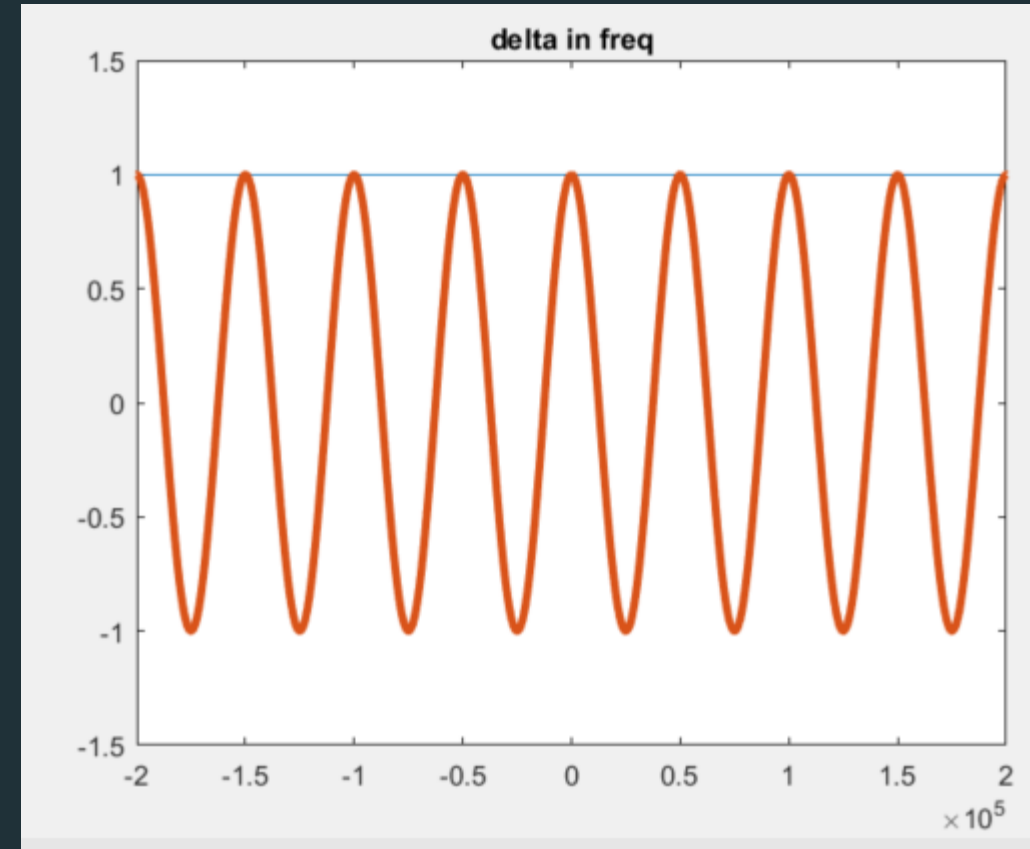
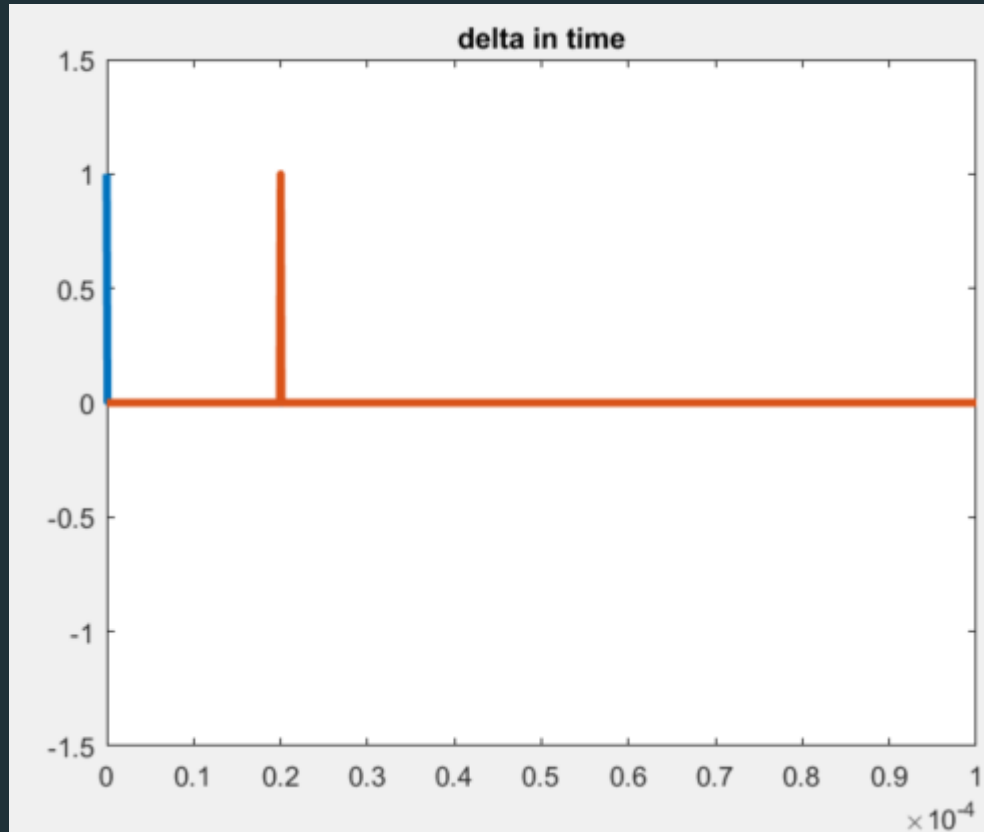


After the channel

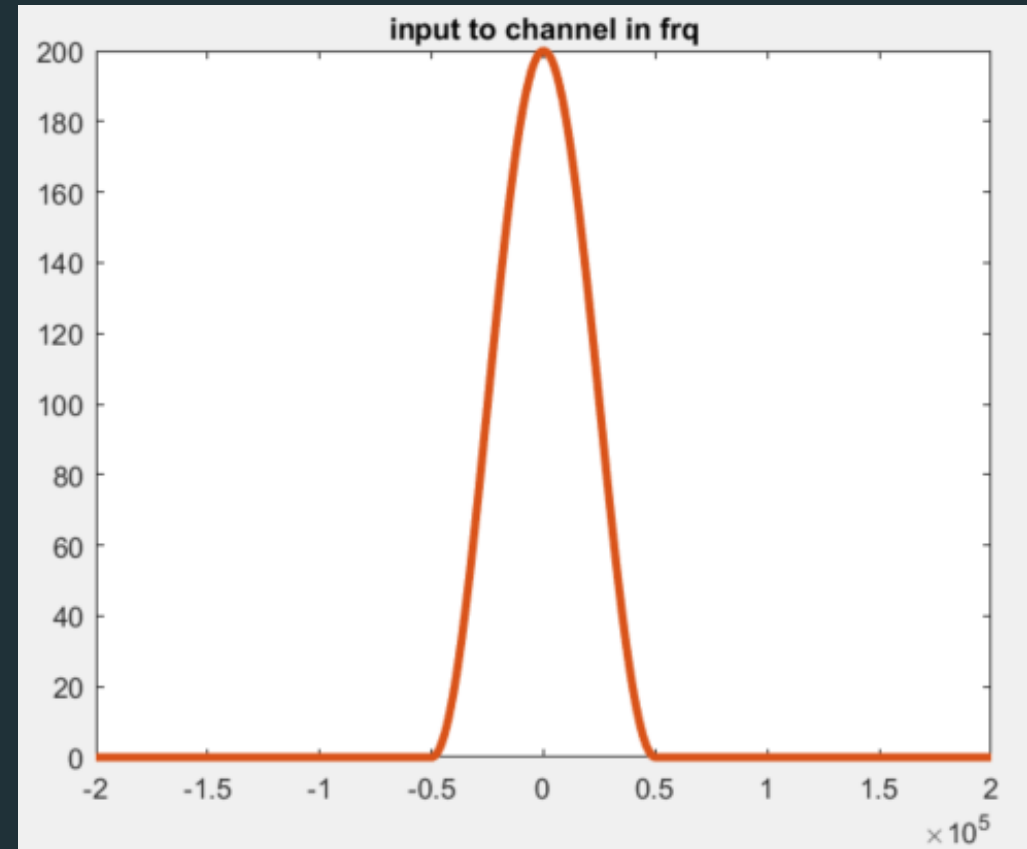
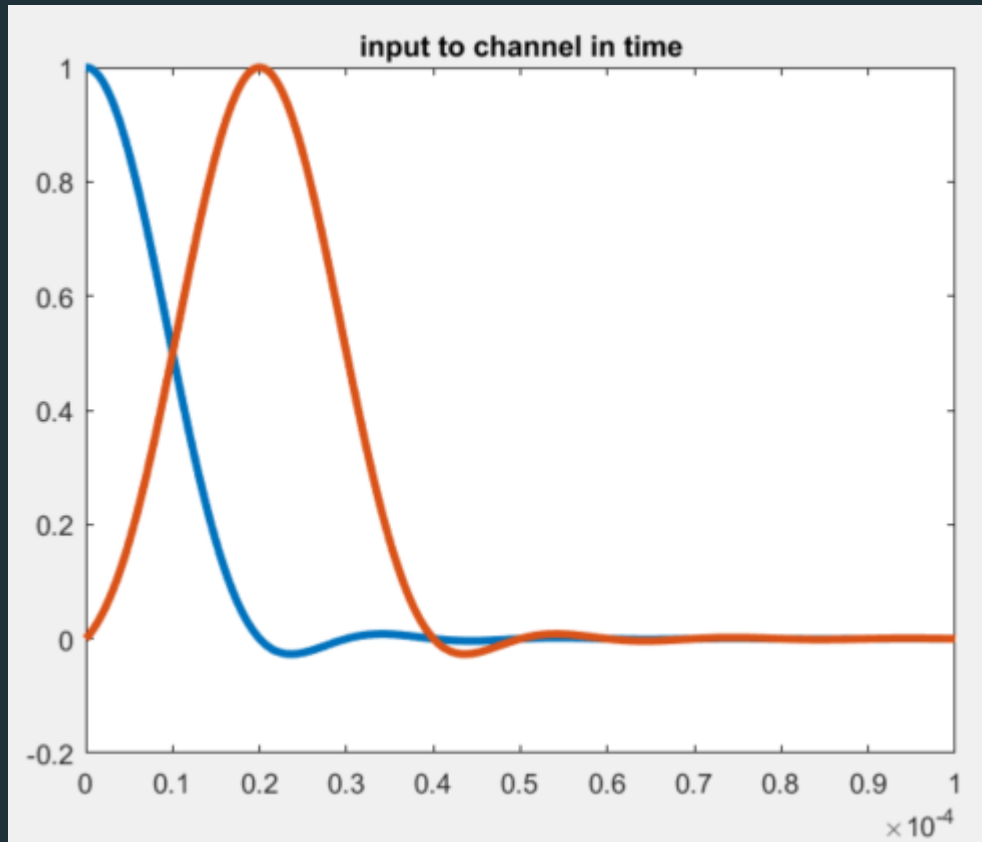
RAISED COSINE: LIMITED IN FREQUENCY AND UNLIMITED IN TIME ($\beta = 1$).



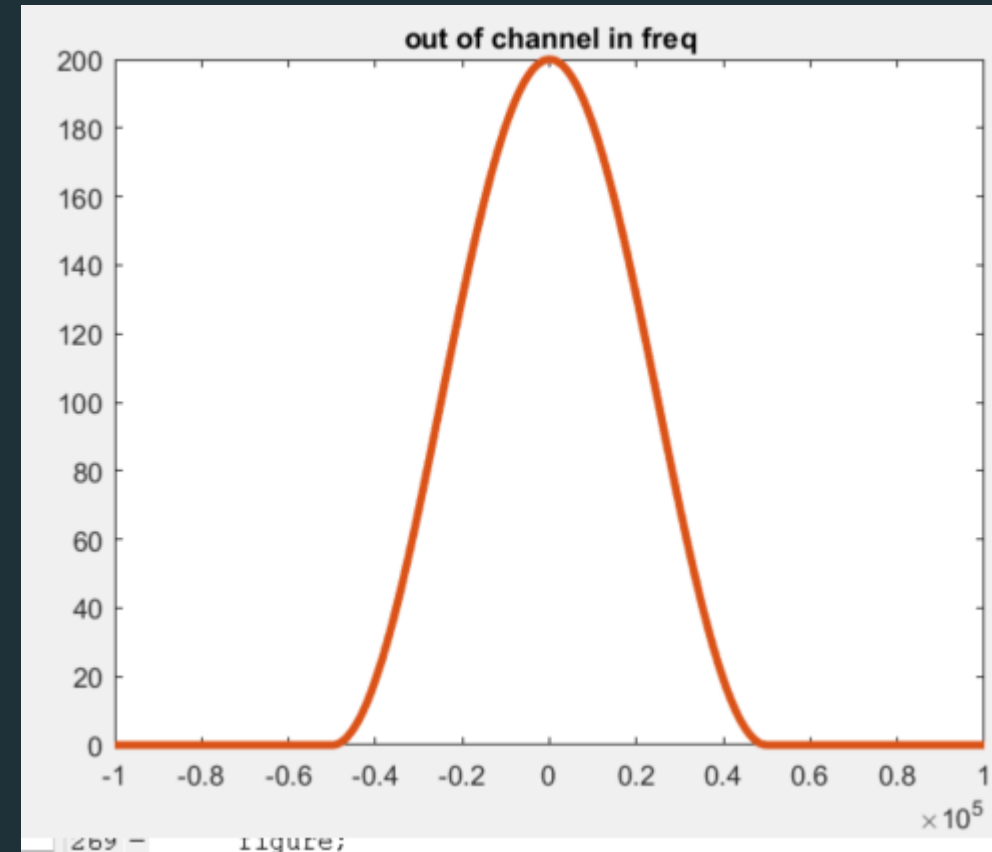
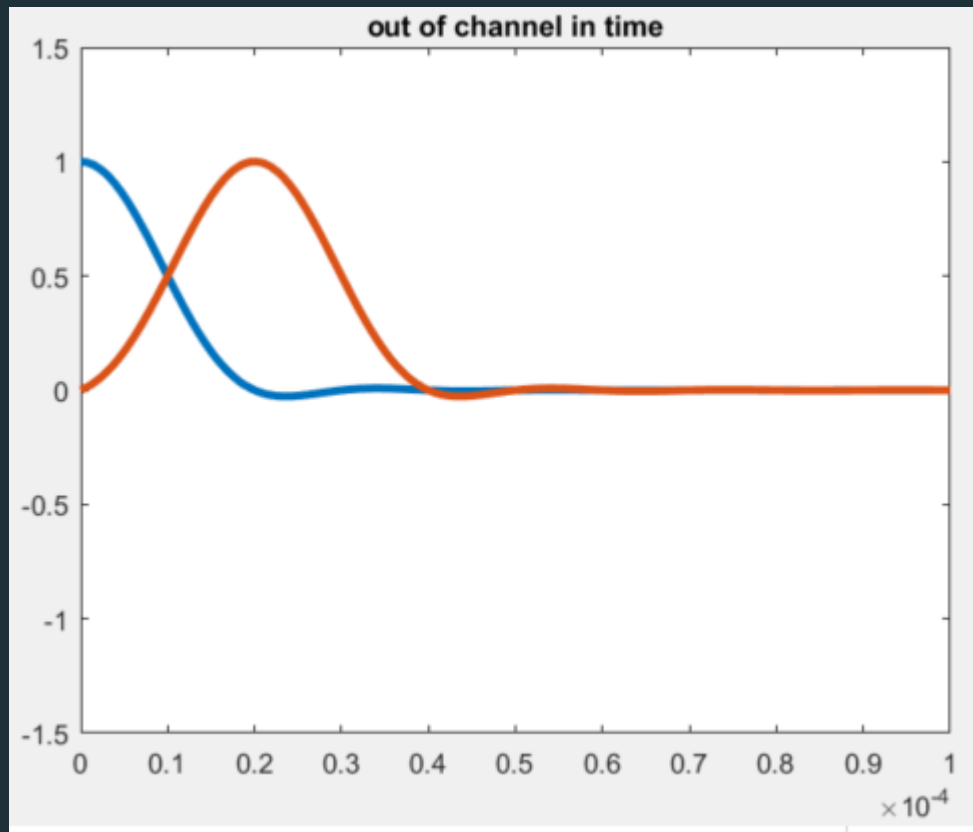
GENERATING DELTA FOR SHIFTING THE SIGNAL



SHIFTING

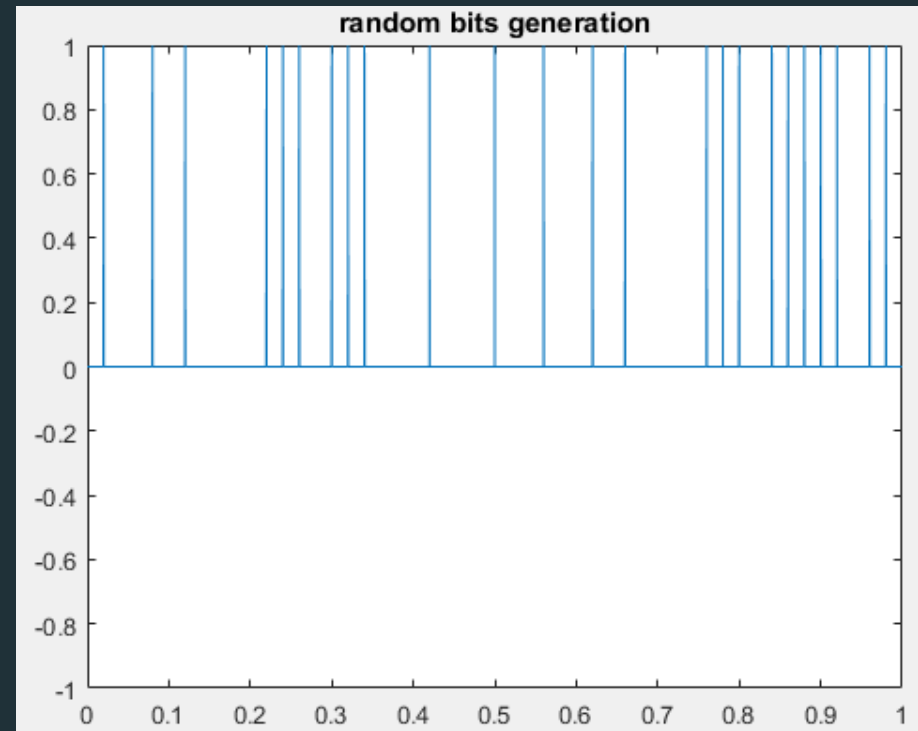


OUTPUT FROM THE CHANNEL

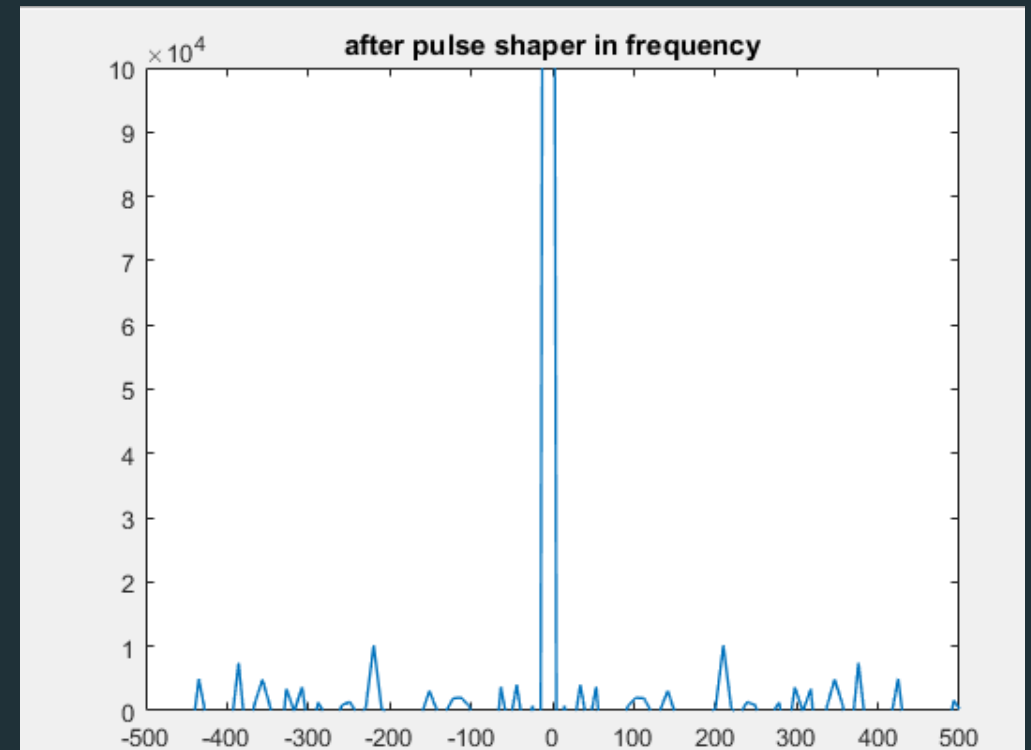
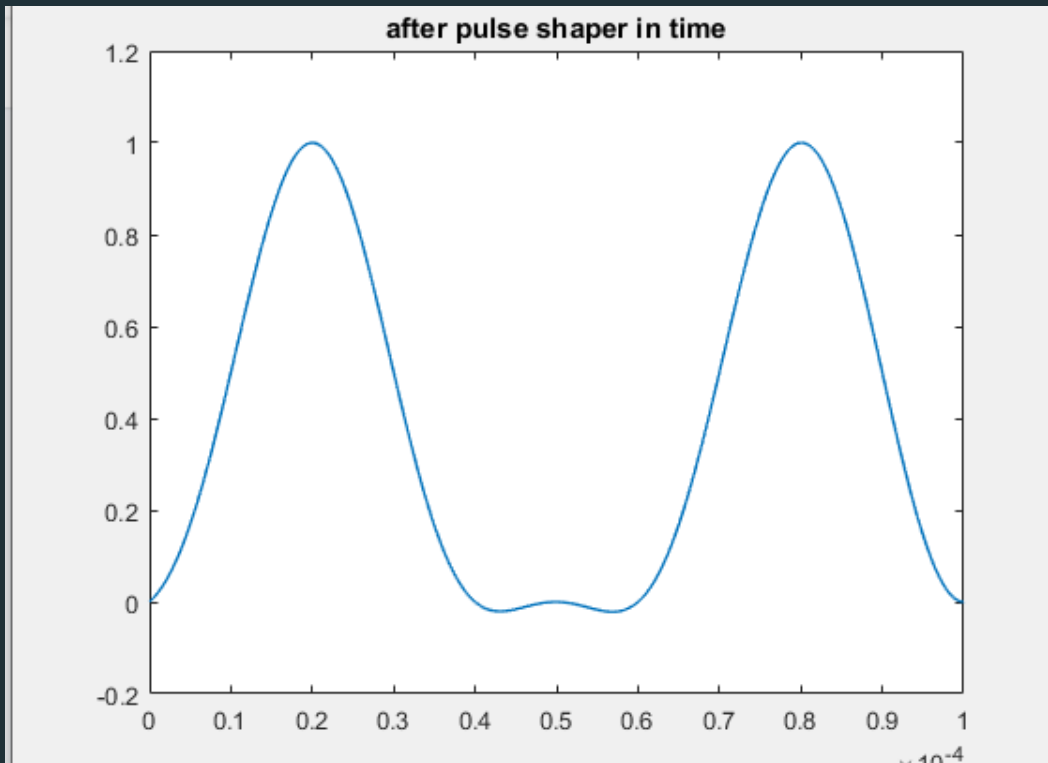


Channel has no effect

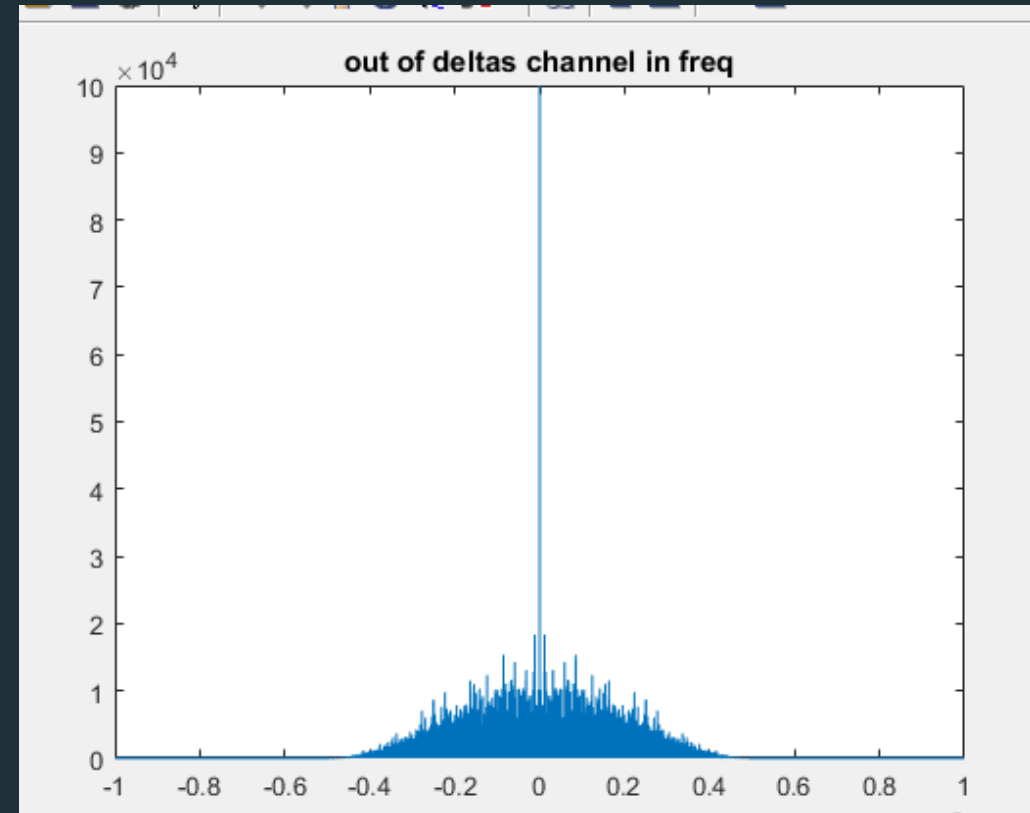
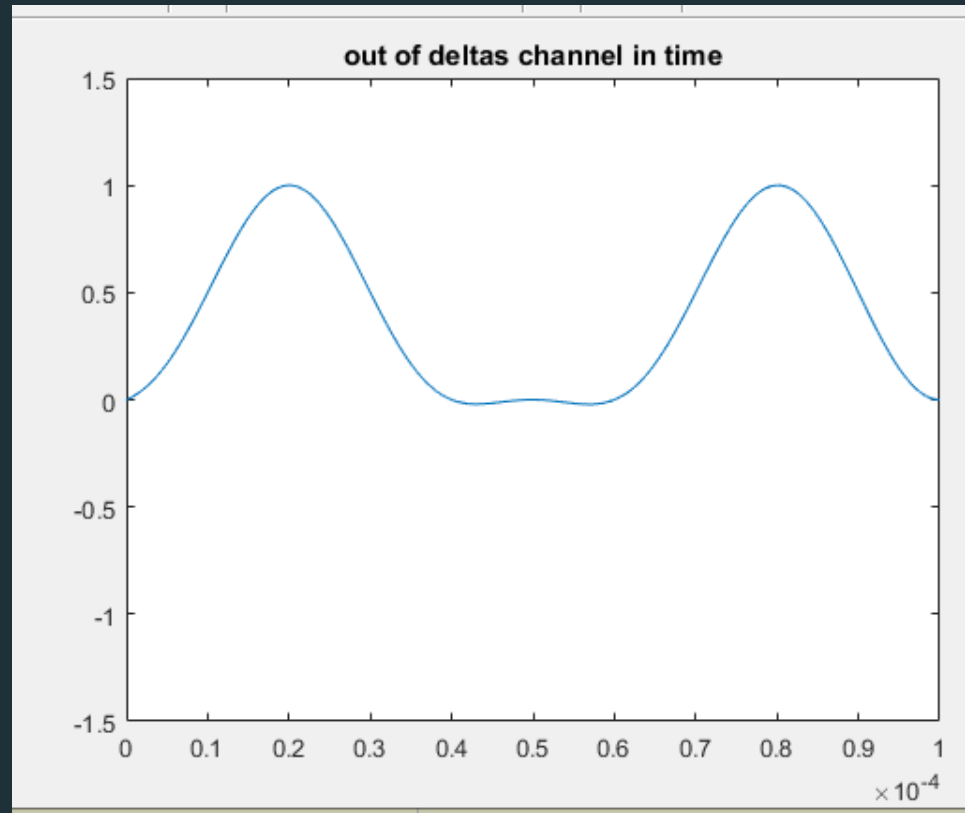
GENERATING RANDOM BITS



AFTER PULSE SHAPER IN TIME AND FREQUENCY DOMAIN



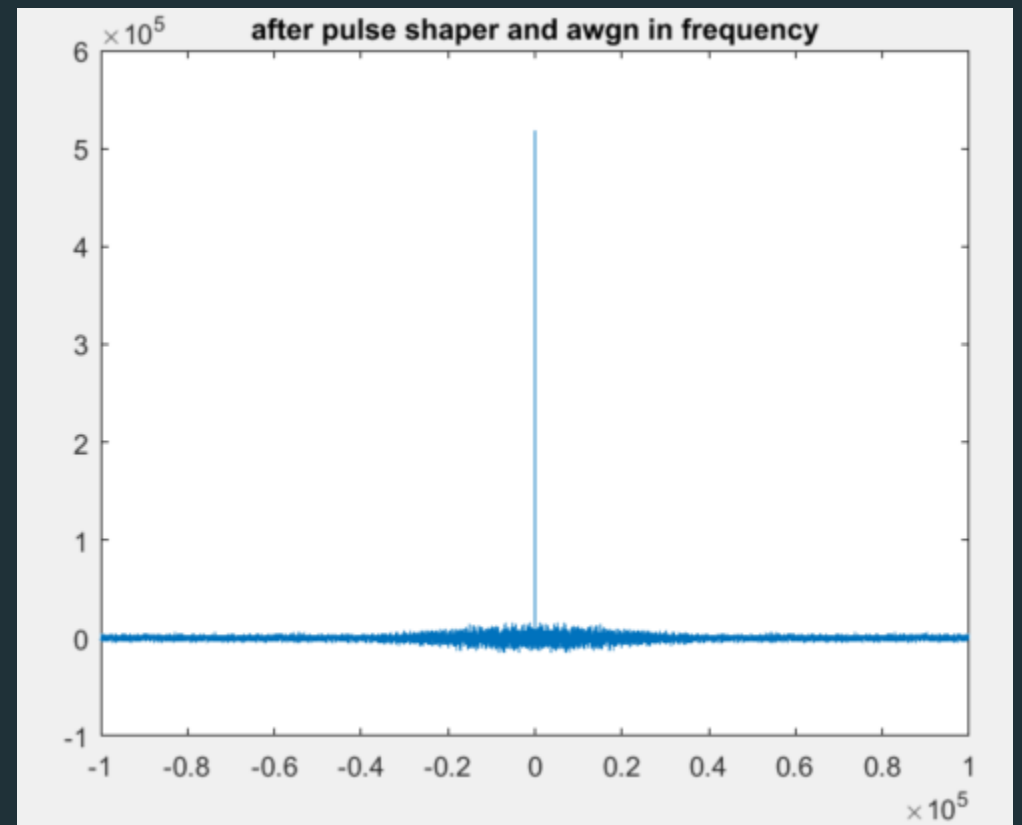
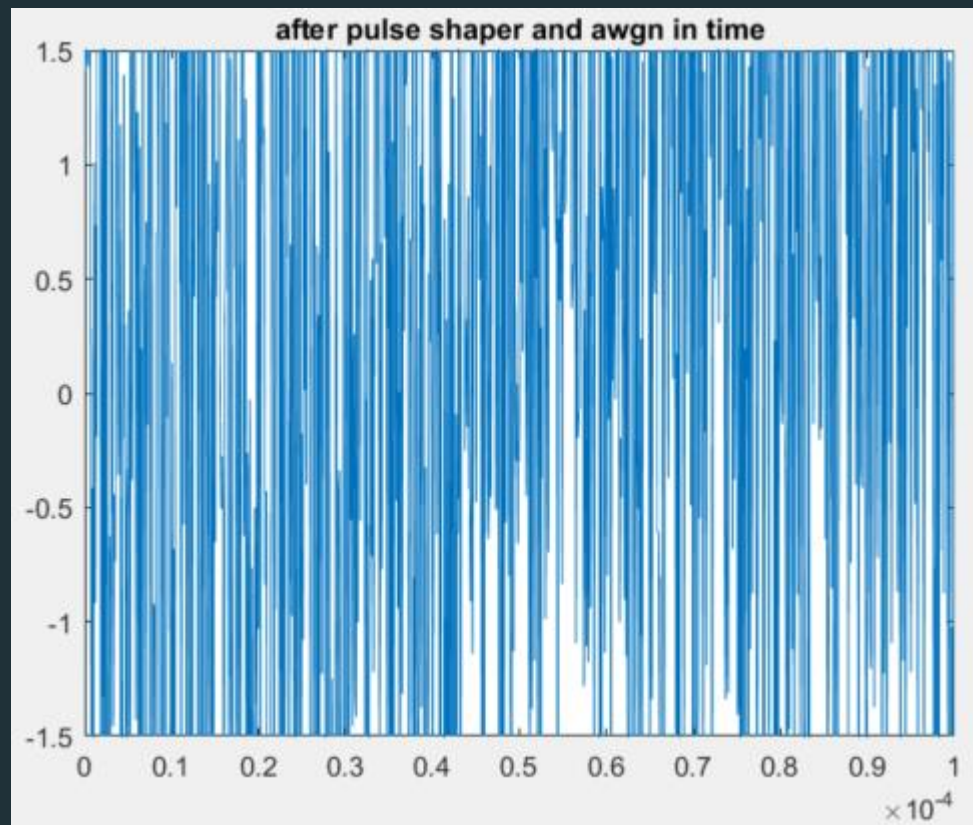
OUTPUT FROM CHANNEL



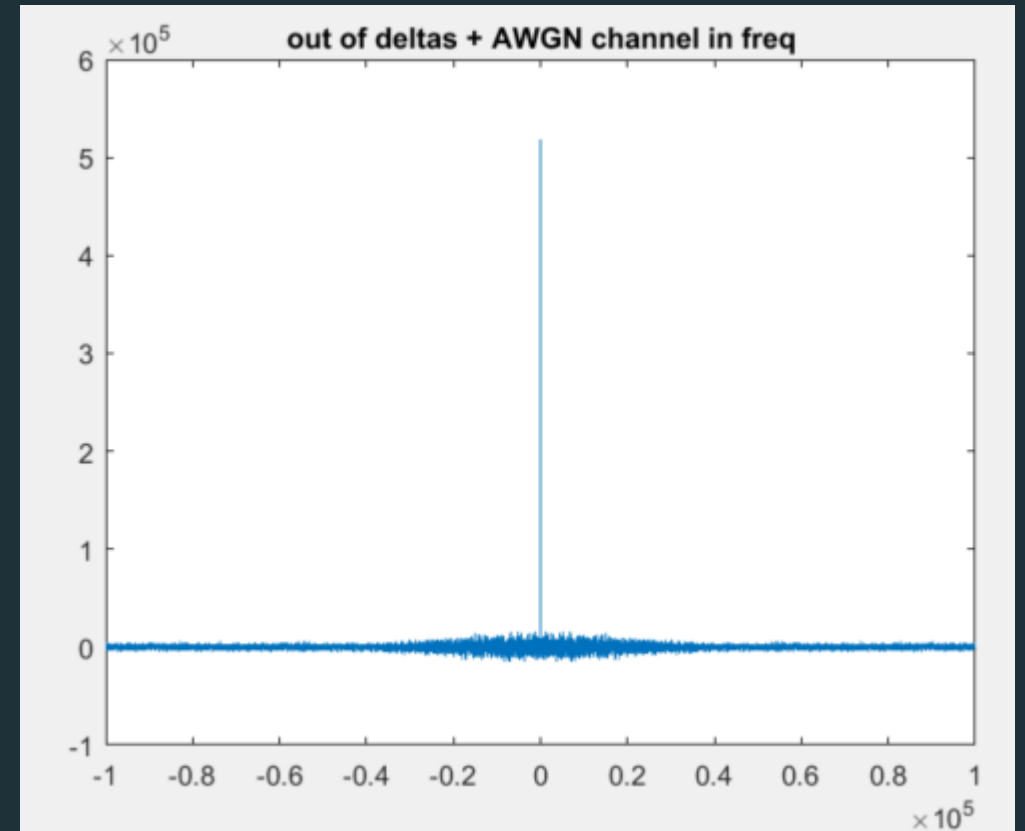
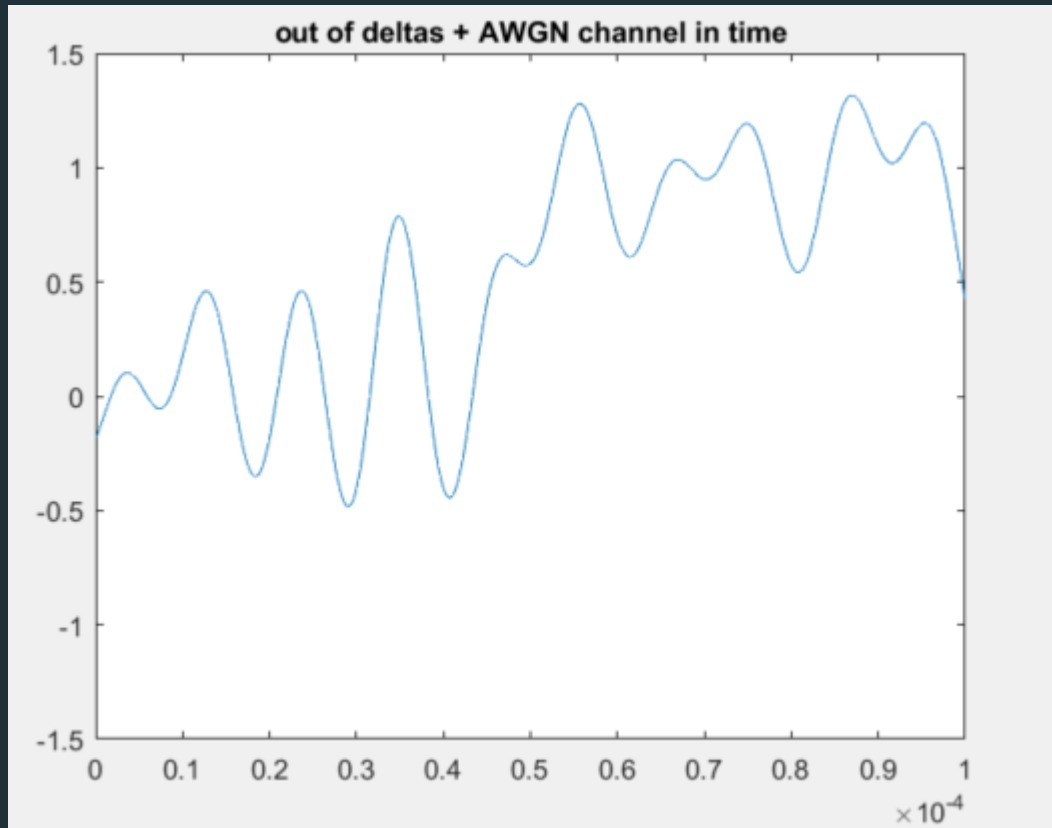
COMPUTE BER

```
BER = 0.000000
```

ADDING AWGN ($N_o = 10$)



OUT OF DELTAS + AWGN CHANNEL



COMPUTE BER WITH AWGN

```
BER = 0.060168
```

AT $N_0 = 10$

```
BER = 0.438172
```

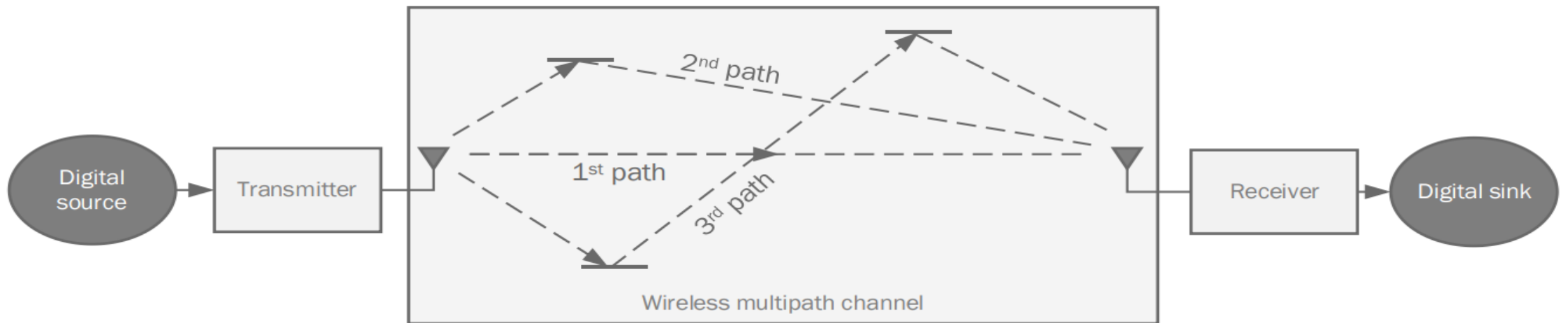
AT $N_0 = 1000$



INTER-SYMBOL
INTERFERENCE DUE
TO MULTI-PATH
CHANNELS

STEPS OF PROCESS

- I. Generate transmitted symbols(X).
- II. Generate channel coefficients (H).
- III. Add effect of AWGN channel (N).
- IV. Get Received signal $Y=HX+N$.
- V. Estimate transmitted signal.
- VI. Calculate BER vs E_b/N_0



GENERATE TRANSMITTED SYMBOLS

- Generate random signal of 1's and -1's with length L.

GENERATE CHANNEL COEFFICIENTS

- Arrange H matrix as shown:

$$\underbrace{\begin{bmatrix} h_0 & & & & & \\ h_1 & h_0 & & & & \\ h_2 & h_1 & h_0 & & & \\ \vdots & & & \ddots & h_1 & h_0 \\ h_{L-1} & h_{L-2} & h_{L-3} & \cdots & h_2 & h_1 & h_0 \end{bmatrix}}_H$$

- The next slide shows a part of result in MATLAB

Result in MATLAB:
For L=4000 :

	1
1	1
2	1
3	1
4	1
5	1
6	-1
7	1
8	-1
9	-1
10	1
11	1
12	1
13	-1
14	-1
15	-1
16	1
17	1
18	1
19	-1
20	1
21	-1
22	-1
23	-1
24	1
⋮	
4000	1

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	
1	1.5288	0	0	0	0	0	0	0	0	0	0	0	0	0	
2	0.8038	1.5288	0	0	0	0	0	0	0	0	0	0	0	0	
3	0.7523	0.8038	1.5288	0	0	0	0	0	0	0	0	0	0	0	
4	0.2557	0.7523	0.8038	1.5288	0	0	0	0	0	0	0	0	0	0	
5	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	0	0	0	0	0	0	0	
6	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	0	0	0	0	0	0	
7	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	0	0	0	0	0	
8	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	0	0	0	0	
9	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	0	0	0	
10	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	0	0	
11	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	0	
12	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	0	
13	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	0	
14	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	1.5288	
15	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	0.8038	
16	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	0.7523	
17	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	0.2557	
18	3.5935e-...	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	0.1994	
19	7.8799e-...	3.5935e-...	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	0.2707	
20	1.5967e-...	7.8799e-...	3.5935e-...	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	0.1044	
21	7.5317e-...	1.5967e-...	7.8799e-...	3.5935e-...	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	0.0426	
22	5.0013e-...	7.5317e-...	1.5967e-...	7.8799e-...	3.5935e-...	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	0.0261	
23	1.6571e-...	5.0013e-...	7.5317e-...	1.5967e-...	7.8799e-...	3.5935e-...	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	0.0132	
24	1.3804e-...	1.6571e-...	5.0013e-...	7.5317e-...	1.5967e-...	7.8799e-...	3.5935e-...	6.7266e-...	0.0011	0.0014	0.0024	0.0027	0.0037	0.0034	

ADD EFFECT OF AWGN CHANNEL

- Generate random noise with zero mean and one variance.

Result in MATLAB:

	1
1	0.4117
2	-0.4186
3	0.6624
4	-0.4599
5	-0.5680
6	-0.1180
7	-0.4343
8	-1.3030
9	-0.1754
10	0.9302
11	-1.7471
12	0.1420
13	0.7690
14	-0.6486
15	-0.0481
16	-0.4305
17	-0.3492
18	1.1565
19	1.1871
20	1.2258
⋮	
4000	0.4786

GET RECEIVED SIGNAL

- Calculate received signal by this equation $Y=HX+N$.

Result in MATLAB:

	1
1	1.9405
2	1.9140
3	3.7473
4	2.8807
5	2.9720
6	0.6350
7	1.8730
8	-1.9076
9	-1.3683
10	1.4161
11	-0.3039
12	3.0271
13	0.6929
14	-2.1071
15	-2.5277
16	-0.1869
17	1.1623
18	3.6791
19	0.9743
20	2.7804
⋮	
4000	3.9351

ESTIMATE TRANSMITTED SIGNAL

- Equalize channel effect by multiply the received signal by inverse of channel matrix.
- Make decision for each bit using threshold voltage equals (0) to get estimated (transmitted) signal

CALCULATE BER VS Eb/NO

- Change value of Eb/No from -15 to 0 .
- Calculate BER for each change .

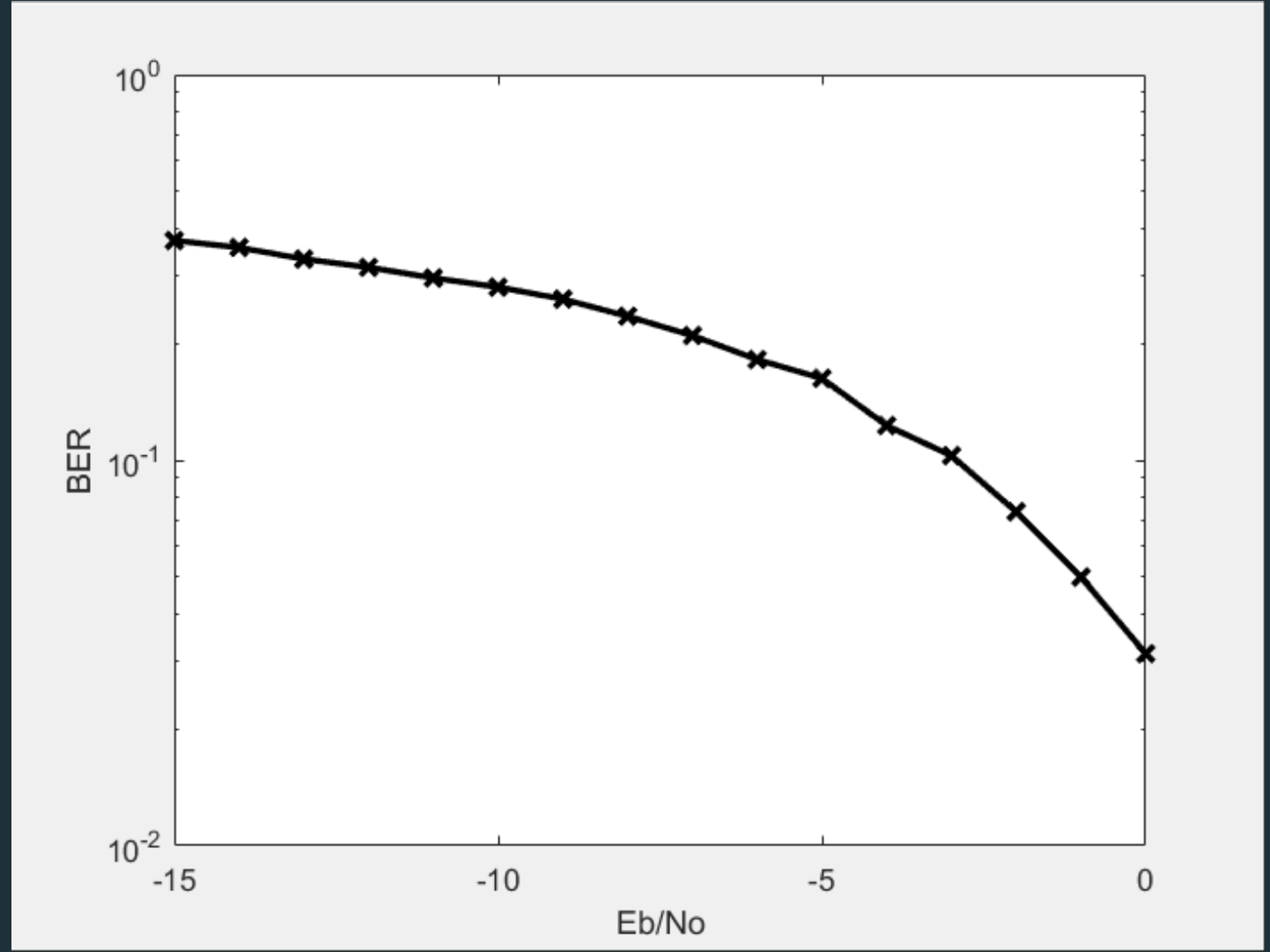
Values of BER

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	0.3715	0.3563	0.3325	0.3165	0.2970	0.2813	0.2618	0.2363	0.2105	0.1825	0.1630	0.1230	0.1028	0.0735	0.0498	0.0315

Result in MATLAB:

	1
1	1
2	1
3	1
4	1
5	1
6	-1
7	1
8	-1
9	-1
10	1
11	-1
12	1
13	-1
14	-1
15	-1
16	1
17	1
18	1
19	-1
20	1
21	-1
22	-1
23	-1
24	1
⋮	
4000	1

- Draw relation between BER and E_b/N_o .
- The value of BER decrease as E_b/N_o increase.

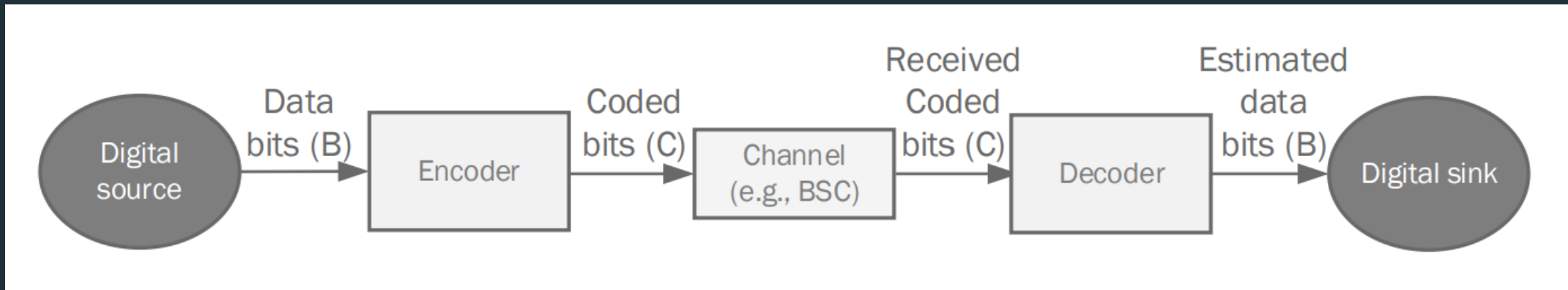




REPETITION CODE

STEPS OF PROCESS

- I. Generate information (transmitted) bits with length N .
- II. Repeat information bits L times.
- III. See effect of BSC channel.
- IV. Make decision for each bit to get received bits.
- V. Compute BER.
- VI. See effect of bit flipping probability on BER.



$b \rightarrow$ block length

$c \rightarrow$ coded length

GENERATE INFORMATION (TRANSMITTED) BITS

- Generate a sequence of bits which consists of 0's and 1's.

Result in MATLAB:

For N=1000

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	...	1000
1	1	1	0	1	1	0	0	1	1	1	0	1	1	0	1	0	0	...	1

REPEAT INFORMATION BITS L TIMES

- Calculate coding rate of repetition code ($r = \frac{N}{C}$).
- Repeat each bit L times ($L = \frac{1}{r}$) to get sequence of samples.

Result in MATLAB:

For C=5000

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	...	4996	4997	4998	4999	5000
1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	...	1	1	1	1	1

SEE EFFECT OF BSC CHANNEL

- Pass Sequence of sample through BSC channel .
- generates the output sample sequence based on the Independent channel and parameter.

Result in MATLAB:

Channel effect:

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	...	4999	5000
1	1	1	0	0	1	0	1	1	0	0	0	1	0	0	1	...	0	0

Output sample sequence:

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	...	4999	5000
1	0	0	1	1	0	1	0	0	1	1	0	1	0	0	1	...	1	1

MAKE DECISION FOR EACH BIT TO GET RECEIVED BITS

- Make decision for each L bits using threshold voltage equals $(L/2)$ to get received bits .

Result in MATLAB:

Received bits

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	...	1000
1	0	1	0	1	0	0	0	0	1	0	0	1	1	0	1	0	0	...	1

Compute BER for $p=0.5$

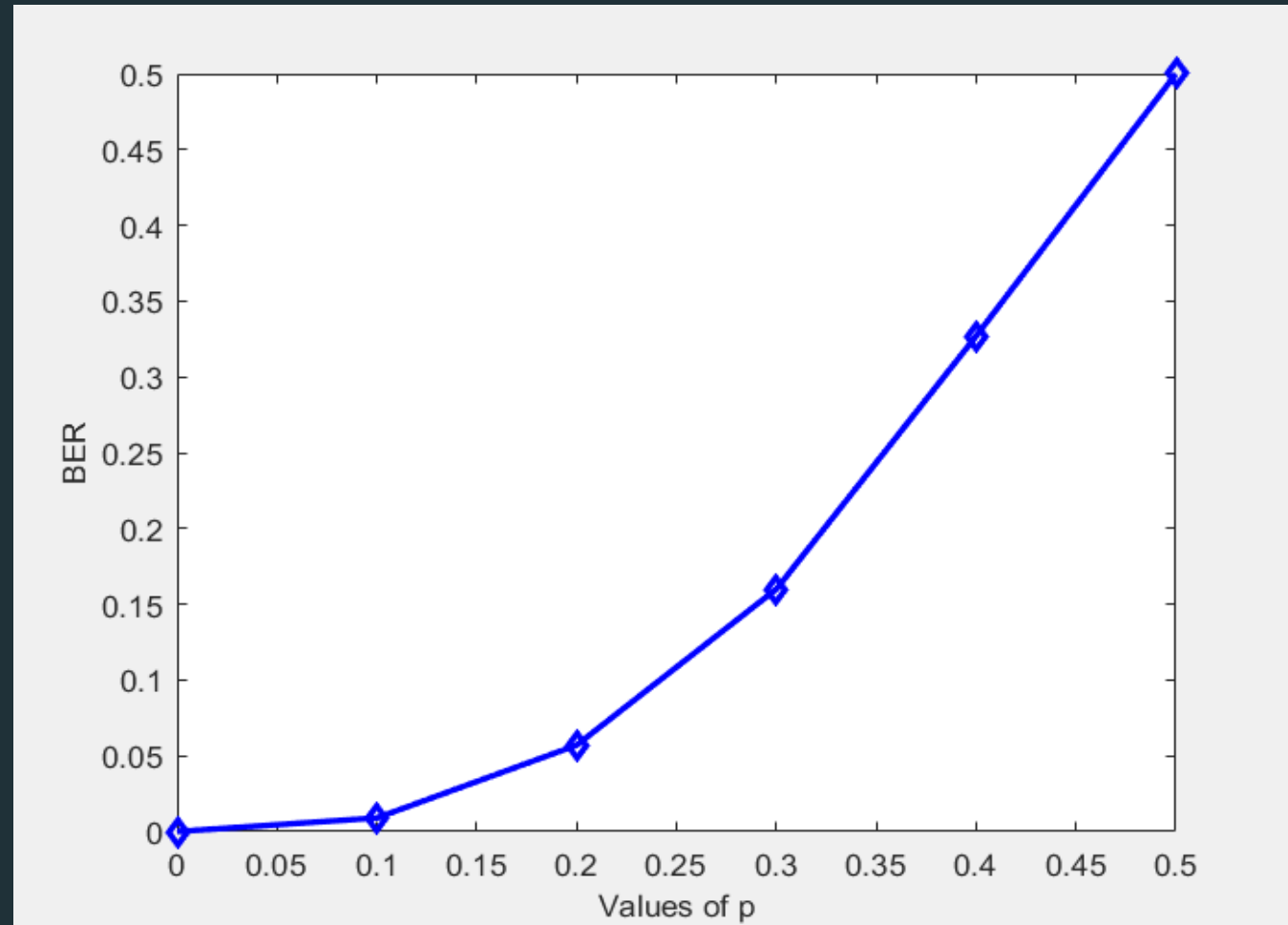
BER 0.4730

SEE EFFECT OF BIT FLIPPING PROBABILITY ON BER

- Change the channel parameter from 0 to 0.5 .
- Calculate BER for each change .

Result in MATLAB:

- Draw relation between BER and P.
- BER increases as channel parameter increases because when p is large value , random numbers which equal or smaller than p are large so there are large number of ones XOR with signal so there is high effect of flipping on signal.

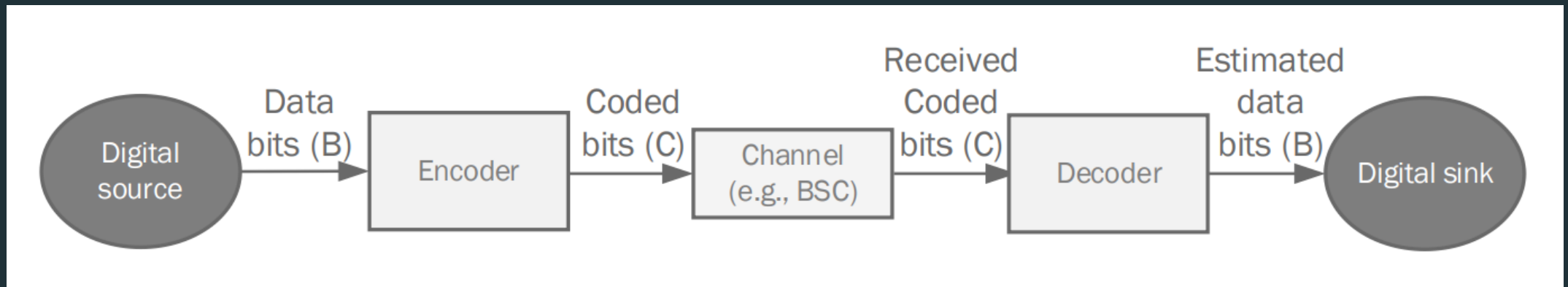




CONVOLUTIONAL
CODE

STEPS OF PROCESS

- I. Generate input bits .
- II. Encode information bits based on a given Generator polynomial.
- III. See effect of BSC channel .
- IV. Decode received coded bits into estimated data bits by Viterbi algorithm.
- V. Compute BER.
- VI. See effect of bit flipping probability on BER.



GENERATE INPUT BITS

- Generate a sequence of bits which consists of 0's and 1's.

Result in MATLAB:

	1	2	3	4	5	6	7	8	9	10	11	...	4000
1	0	1	0	1	1	1	1	1	1	0	1		1

ENCODE INFORMATION BITS

- Pass input bits through m shift registers.
- Number of encoded bits = $m \times \text{length of msg}$.

Result in MATLAB:

	1	2	3	4	5	6	7	8	9	10	11	...	11996	11997	11998	11999	12000
1	1	1	1	1	1	0	0	1	0	1	0		0	0	1	1	1

SEE EFFECT OF BSC CHANNEL

- Pass Sequence of sample through BSC channel .
- generates the output sample sequence based on the Independent channel and parameter.

Result in MATLAB:

	1	2	3	4	5	6	7	8	9	10	11	12	...	11999	12000
1	0	1	1	1	0	0	1	0	1	1	1	1		1	1

DECODE RECEIVED CODED BITS INTO ESTIMATED DATA BITS

- Decode received bits using vitdec function .

Result in MATLAB:

	1	2	3	4	5	6	7	8	9	10	11	12	...	3999	4000
1	0	1	1	0	1	0	1	0	0	1	1	0		1	1

COMPUTE BER

Compute BER for $p=0.5$

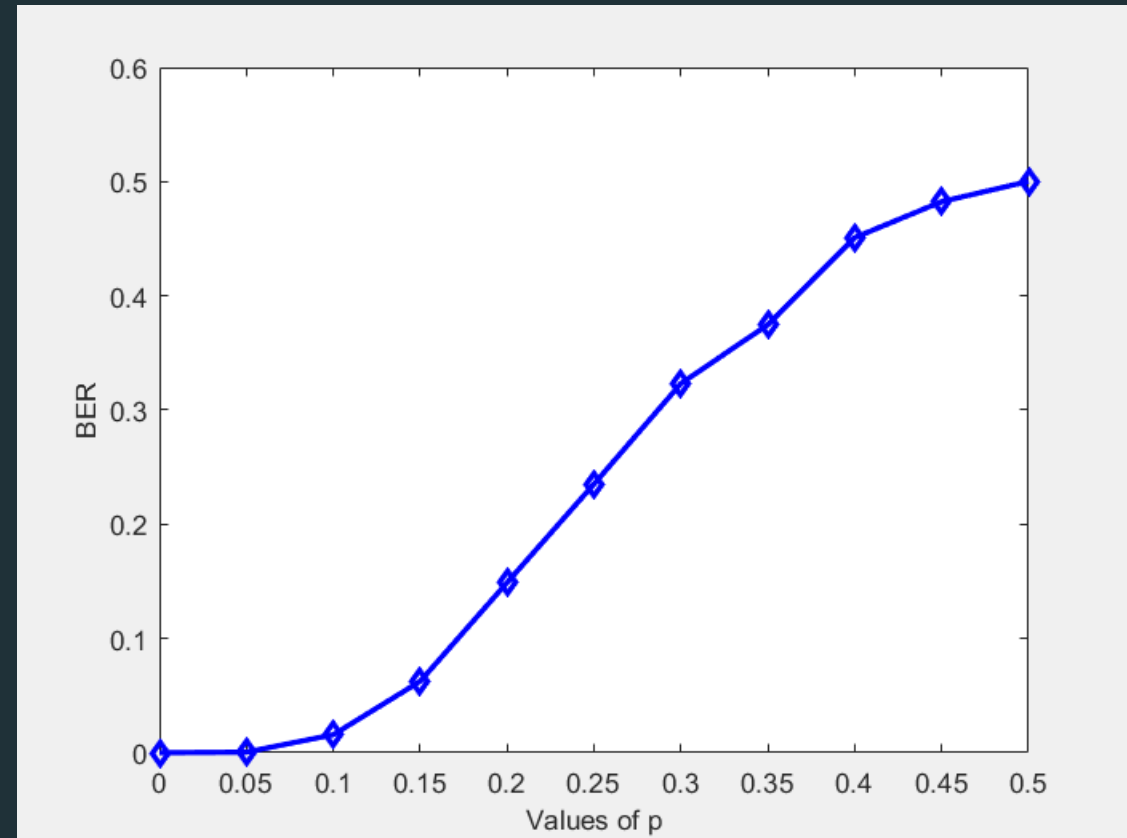
BER	0.5053
-----	--------

SEE EFFECT OF BIT FLIPPING PROBABILITY ON BER

- Change the channel parameter from 0 to 0.5 .
- Calculate BER for each change .

Result in MATLAB:

- BER increases as channel parameter increases because when p is large value , random numbers which equal or smaller than p are large so there are large number of ones XOR with signal so there is high effect of flipping on signal.

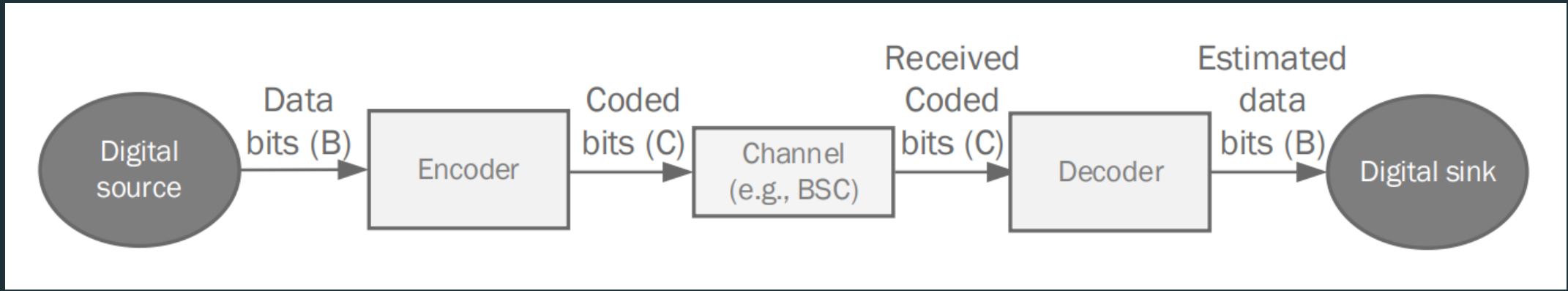




POLAR CODE

STEPS OF PROCESS

- I. Generate input bits .
- II. Encode information bits by polarization transformation.
- III. See effect of BSC channel .
- IV. Decode received coded bits into estimated data bits by Successive Cancellation.



GENERATE INPUT BITS

- $N=2^n$
- Message : m of length K bits
- Form a vector U of length N bits as follows:
 - Find N-K least reliable (worst) channels from reliability sequence
 - Set U_i for those N-K channels to zero (called frozen positions)
 - m:remaining K bits of U (called message positions)

Example on reliability sequence for N=16

(16,10)

• 1 2 3 5 9 4 6 10 7 11 13 8 12 14 15 16

• Frozen: 1 2 3 5 9 4

• Message: 6 10 7 11 13 8 12 14 15 16

Result in MATLAB:

1	2	3	4	5	6	7	8	9	10						
0	1	1	1	1	0	1	1	1	1	Message bits					

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16		
0	0	0	0	0	0	1	0	0	1	1	1	1	1	1	1	Input bits	

ENCODER

- Binary tree representation

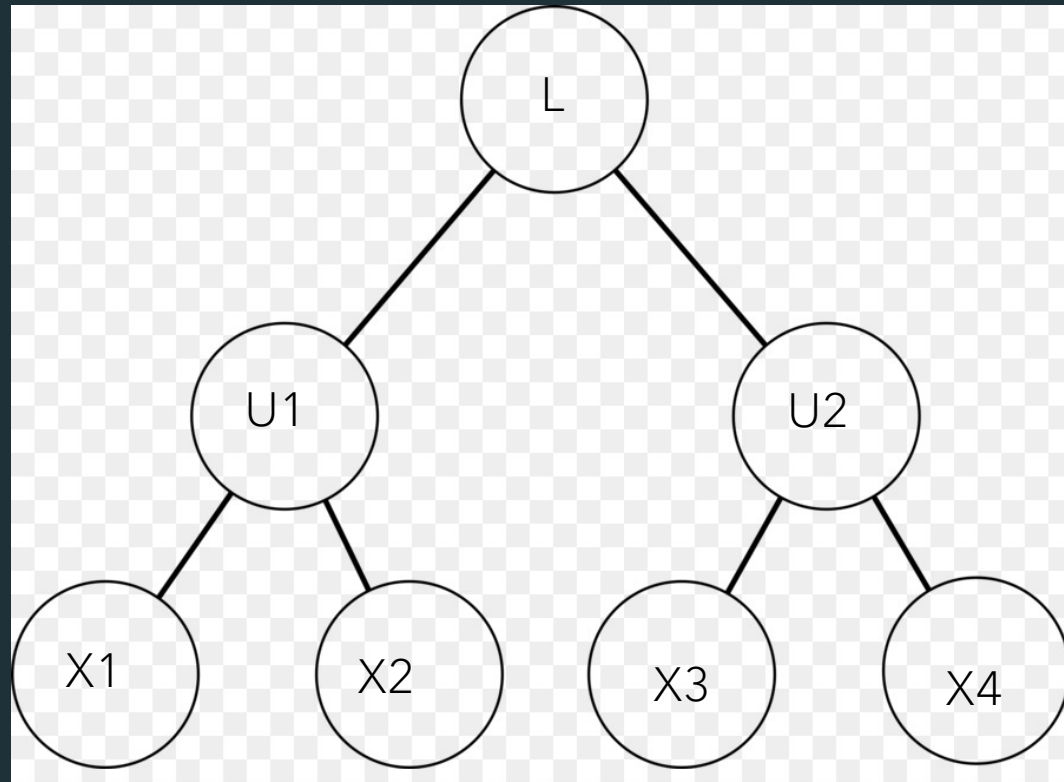
Depth n

- $U1 = [X1+X2 \quad X2]$

- $U2 = [X3+X4 \quad X4]$

- $L = [U1 \quad U2]$

- $L = [X1+X2+X3+X4 \quad X2+X4 \quad X3+X4 \quad X4]$



ENCODER

- G_N : N*N matrix , Kronecker product of 2*2 kernel.

- Binary tree representation

- Depth n

- $U^{(N)} = U * G_N$: evaluated on tree with u at bottom and $U^{(N)}$ at top

$$G_{2^n} = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}^{\otimes n}$$

Result in MATLAB:

Generator Matrix

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0
4	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0
5	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0
6	1	1	0	0	1	1	0	0	0	0	0	0	0	0	0	0
7	1	0	1	0	1	0	1	0	0	0	0	0	0	0	0	0
8	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0
9	1	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0
10	1	1	0	0	0	0	0	0	1	1	0	0	0	0	0	0
11	1	0	1	0	0	0	0	0	1	0	1	0	0	0	0	0
12	1	1	1	1	0	0	0	0	1	1	1	1	0	0	0	0
13	1	0	0	0	1	0	0	0	1	0	0	0	1	0	0	0
14	1	1	0	0	1	1	0	0	1	1	0	0	1	1	0	0
15	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0
16	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

Encoded bits

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
0	0	1	0	1	0	1	1	1	0	0	0	0	0	0	1

BSC CHANNEL

- take the sample sequence passing through the channel.
- generates the output sample sequence based on the Independent channel and parameter.

Result in MATLAB :

for $p=0.5$:

Channel Effect

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	0	0	0	1	0	1	1	1	1	1	1	0	0	0	1

Received bits

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	0	1	0	0	0	0	0	0	1	1	1	0	0	0	0