

## **Problem Statement**

- ❖ Poor waste management is a crucial problem in Bangladesh
- More than half of these wastes are dumped in open spaces illegally without proper treatment, which is threatening for both environment and public health
- So the authority wants to develop a system that can determine quantities of different types of wastes that are to be processed, when the management capacities and unit costs for each types of wastes are provided
- ❖ With the help of this system, any municipality can determine the daily quantity of wastes it wants to process and the minimum cost to manage these wastes effectively considering the resource constraints.

## **Objective**

To develop a C program for any municipality of Bangladesh to determine the total amount of processed wastes based on their type, and the minimum cost to manage these wastes effectively considering the resource constraints.

## **Data Used**

Percentage contribution of waste to different distribution centers:

Туре	Waste Type	Recycling Rate (R)	Disposal Rate after Treatment (L)
1	Construction& Demolition	99%	1%
2	Metal	99%	1%
3	Paper/Cardboard	44%	56%
4	Plastics	4%	96%
5	Food	18%	82%
6	Wood	66%	34%
7	Horticultural	73%	27%
8	Ash & Sludge	10%	90%
9	Textile/Leather	4%	96%
10	Used Slag	98%	2%
11	Glass	14%	86%
12	Scrap Tyres	94%	6%
13	Others (stones, ceramic, rubber, etc.)	7%	93%

#### Collected from:

Waste Statistics and Overall Recycling. (2020). Retrieved from https://www.nea.gov.sg/ourservices/waste-management/waste-statistics-and-overall-recycling

## **Process Used : Duality Theory**

For our problem, we have to

## **Objective function:**

Minimize waste treatment cost (BDT/day),

$$Z = C_1 X_1 + C_2 X_2 + C_3 X_3 + \dots + C_N X_N$$

### **Constraints:**

For landfill disposal, the constraint is:

$$L_1X_1 + L_2X_2 + L_3X_3 + \dots + L_NX_N \le Landfill Capacity$$

For recycling, the constraint is:

$$R_1X_1 + R_2X_2 + R_3X_3 + \dots + R_NX_N \le Recycling Capacity$$

## **Basic Algorithm of Dual Problems**

Step 1: Start.

**Step 2:** Primary matrix formation

**Step 3:** Transverse matrix

**Step 4:** Preparation of the matrix for iteration

**Step 5:** Iteration

**Step 6:** Checking if iteration is needed again

Step 7: If yes, go to step 4

**Step 8:** If no, print the answers

Step 9: End.

## Step 1

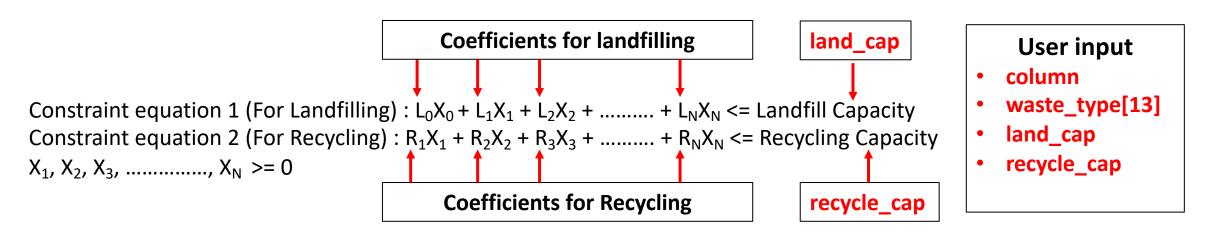
Start

#### **Primary matrix formation**

**N= Total number of types of wastes = 13**, Index starts from 0, ends at 12;

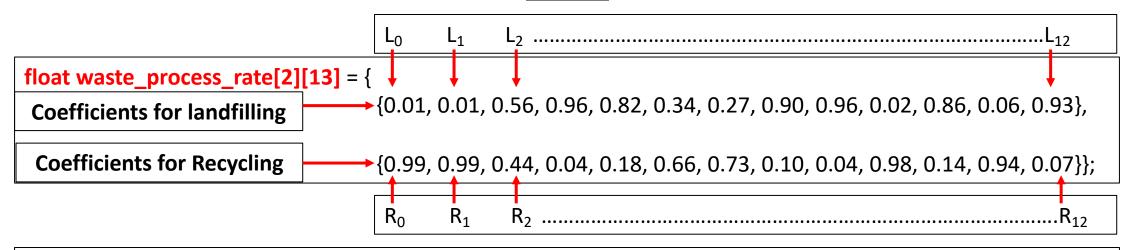
Number of type of wastes = Number of variables = Number of columns in the matrix = stored at 'column' variable Storing the index or type number at: int waste\_type[13];

Variables:  $X_0$ ,  $X_1$ ,  $X_2$ , .....,  $X_N$  = Total quantity of type wise waste to be processed (unit/day): a[i]



L = Percentage of each type of waste to be processed by landfilling disposal which is constant and is fixed in the equation.

R = Percentage of each type of waste to be processed by recycling which is constant and is fixed in the equation.

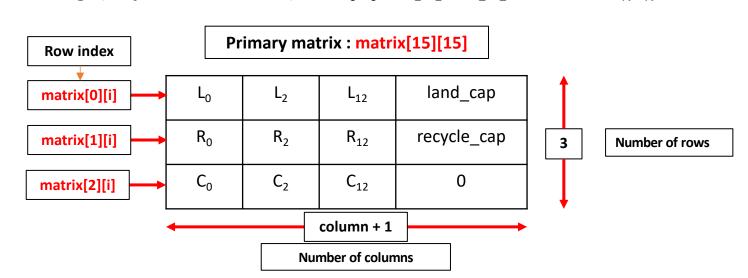


**User input**: Cost of unit waste processing by waste type (BDT/unit):  $C_0$ ,  $C_1$ ,  $C_2$  ......,  $C_N$ : stored at matrix[2][i]

The total cost of waste processing, (Objective Function)  $Z = C_0 X_0 + C_1 X_1 + C_2 X_2 + \dots + C_N X_N$ 

#### **User input**

- Column = 3
- waste\_type[0] = 0
- waste type[1] = 2
- waste type[2] = 12
- land\_cap = 120
- recycle cap= 130
- matrix[2][0] = 23 (cost for type 0,  $C_0$ )
- matrix[2][1] = 34 (cost for type 2, C<sub>2</sub>)
- matrix[2][2] = 45 (cost for type 12, C<sub>12</sub>)



#### **Transverse matrix**

### trans\_matrix[15][15]

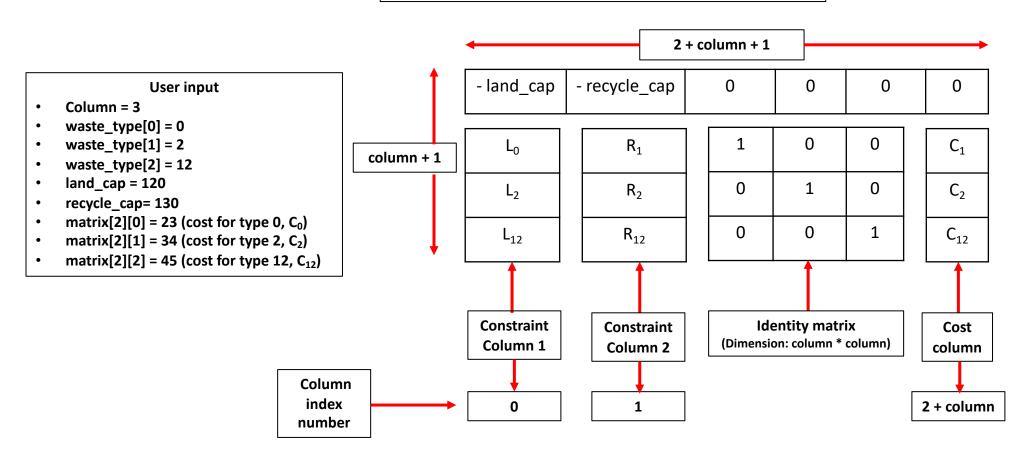
L <sub>o</sub>	R <sub>1</sub>	C <sub>1</sub>	1
L <sub>2</sub>	R <sub>2</sub>	C <sub>2</sub>	
L <sub>12</sub>	R <sub>12</sub>	C <sub>12</sub>	column + 1
land_cap	recycle_cap	0	
4	3		I <b>▼</b>

#### **User input**

- Column = 3
- waste\_type[0] = 0
- waste\_type[1] = 2
- waste\_type[2] = 12
- land\_cap = 120
- recycle\_cap= 130
- matrix[2][0] = 23 (cost for type 0, C<sub>0</sub>)
- matrix[2][1] = 34 (cost for type 2, C<sub>2</sub>)
- matrix[2][2] = 45 (cost for type 12, C<sub>12</sub>)

Step 4

#### **Preparation of the matrix for iteration**



#### Iteration Matrix\_new[15][15] **User input** - 120 -130 0 0 0 0 Column = 3 $waste_type[0] = 0$ 0.01 0.99 0 0 23 1 waste\_type[1] = 2 waste\_type[2] = 12 land\_cap = 120 0.56 0.44 0 0 34 1 recycle\_cap= 130 matrix[2][0] = 23 (cost for type 0, $C_0$ ) 0.93 0.07 0 45 0 1 matrix[2][1] = 34 (cost for type 2, $C_2$ ) matrix[2][2] = 45 (cost for type 12, $C_{12}$ ) Constraint Constraint **Identity matrix** Cost (Dimension: 3 \* 3) Column 1 Column 2 column Column index 2 + column 0 1 number

## Iteration

### Pivot column:

- 120	-130	0	0	0	0		- 120	-130	0	0	0	0
0.01	0.99	1	0	0	23	<b></b>	0.01	0.99	1	0	0	23
0.56	0.44	0	1	0	34		0.56	0.44	0	1	0	34
0.93	0.07	0	0	1	45		0.93	0.07	0	0	1	45

### **Pivot row:**

- 120	-130	0	0	0	0	float division[15]	- 120	-130	0	0	0	0
0.01	0.99	1	0	0	23	23/ 0.99 = 23.23 min_div	0.01	0.99	1	0	0	23
0.56	0.44	0	1	0	34	34/ 0.44 = 77.27 Lowest : 23.23	0.56	0.44	0	1	0	34
0.93	0.07	0	0	1	45	45/ 0.07 = 642.8	0.93	0.07	0	0	1	45

#### **Iteration**

#### New pivot row: iteration1[15][15] Matrix\_new[15][15] - 120 -130 0 0 0 0 0.01 0.99 0.01/0.99 0.99/0.99 1/0.99 0/0.99 0/0.99 23/0.99 0 23 1 0 0.56 0.44 0 34 1 0 0.93 0.07 0 0 45 1

Pivot value = matrix\_new[piv\_row][piv\_col]

New Pivot row = Old pivot row / pivot value

### Iteration

### New other rows:

## Matrix\_new[15][15]

iterat	ion1	[15]	[15]
--------	------	------	------

0 0 -118	0.00 131.31 0.00 0.00 3020.20	New row 0
0 23 0.0	1.00 1.01 0.00 0.00 23.23	New Pivot row
0 34 0.5	0.00 -0.44 1.00 0.00 23.78	New row 2
1 45 0.9	0.00 -0.07 0.00 1.00 43.37	New row 3

New row = (Current row) – (Its pivot column coefficient) \* (New pivot row)

Step 6

### **Checking if iteration is needed again**

Matrix after first iteration: iteration1[15][15]

Row 0 contains minus value, So iteration is needed again

-118.69	0.00	131.31	0.00	0.00	3020.20
0.01	1.00	1.01	0.00	0.00	23.23
0.56	0.00	-0.44	1.00	0.00	23.78
0.93	0.00	-0.07	0.00	1.00	43.37

Iteration will be continued until row 0 has no minus value

## Step 7

If yes, go to step 4

Execution: from step  $7 \longrightarrow \text{step } 4 \longrightarrow \text{step } 5 \longrightarrow \text{step } 6$ 

### Checking if iteration is needed again

### Matrix after second iteration: iteration1[15][15]

Row 0 contains no
minus value,
So further iteration is
not needed again

0.00	0.00	36.36	213.64	0.00	8100.00
0.00	1.00	1.02	-0.02	0.00	22.80
1.00	0.00	-0.80	1.80	0.00	43.80
0.00	0.00	0.67	-1.67	1.00	3.60

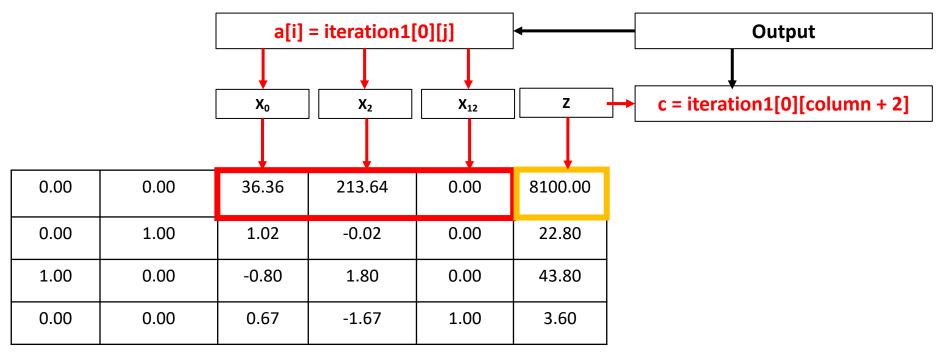
## Step 8

If no, print the answers

Step 8

### If no, print the answers

Matrix after second iteration: iteration1[15][15]



Step 9

End

```
Header files:
          <stdio.h>
Library Function Used:
          main(); printf(); scanf(); fflush(stdin);
Data types used:
          int, float
Operator used:
          ❖ Arithmetic Operator: Addition (+), Subtraction (-), Multiplication,
             (*), Division (\), Increment(++)
          ❖ Relational Operator: >, <, ==
          Assignment Operator: =
Escape Sequence: \n, \t
```

#### Variable:

- Local variables of main function: i, j, row, column, land\_cap, recycle\_cap, matrix[15][15], tranx\_matrix[15][15], waste\_process\_rate[2][13]
- ❖ Local variables of 'iteration' function: i, j, min, piv\_col, piv\_row, matrix\_new[15][15], column, waste\_type[13], division[15], min\_div, iteration1[15][15], a[13], c[2]

### **Array:**

- ❖ One dimensional array: waste\_type[13], a[13], division[15], c[2]
- Two dimensional array: waste\_process\_rate[2][13], matrix[15][15], trans\_matrix[15][15], matrix\_new[15][15], iteration1[15][15]

#### **Control statement:**

- **Decision making/ Selection statement:** if.....else statement
- **! Iterative statement:** The for loop, nested for loop
- ❖ Jumping statement: continue

### **User defined function:**

- **Return type:** void
- **Function name:** iteration
- Parameters: matrix\_new[15][15], column, waste\_type[13])
- **\*** Function call by value
- **Recursion:** Direct recursion

```
* Recursion: Direct recursion
void iteration(float matrix_new[15][15], int column, int waste_type[13]);
int main()
   Function_body;
   iteration(matrix_new, column, waste_type);
void iteration(float matrix_new[15][15], int column, int waste_type[13])
   Function_body;
   if (test == 1)
             iteration(iteration1, column, waste_type);
   else
              //print results
```

