

Programming 4kids

1D Arrays

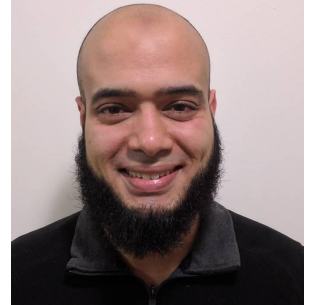
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Write a program that:

- That reads 1000 integers and print them reversed!
- That reads 1000 integers and find pairs of numbers with sum 12345?
- We can define 1000 variables! But this is a crazy idea!
- Programming languages introduce datatype **array** of **size K**
 - K variables defined in the memory (consecutively)
 - They all of **same data** type
- So now we create an array of size 1000
 - Then print them reversed!
 - That is all

Declare an array

```
10_01.cpp
1 #include<iostream>
2 using namespace std;
3
4 int main() {
5     const int size = 5;
6
7     // Declare 5 positions of type integer
8     int numbers[size] = {10, 2, 7, 5, 3};
9
10
11     numbers[0] = 9;
12     numbers[2] *= 3;
13     numbers[4]++;
14
15     cout<<numbers[4];
16
17     return 0;
18 }
19
20
```

Problems Console Tasks Properties

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- `Int number = 10;`
- `Int numbers[5];`
 - Create 5 numbers (variables)
 - Type integer
- `numbers[i]`
 - Access **ith** number
 - Completely like normal variable
 - We can read/output/change
- **Zero indexing**
 - `numbers[0]` first variable
 - `numbers[size-1]` last variable

Declare an array

```
10_01.cpp
1 #include<iostream>
2 using namespace std;
3
4 int main() {
5     const int size = 5;
6
7     // Declare 5 positions of type integer
8     int numbers[size] = {10, 2, 7, 5, 3};
9
10
11     numbers[0] = 9;
12     numbers[2] *= 3;
13     numbers[4]++;
14
15     cout<<numbers[4];
16
17     return 0;
18 }
19
20
```

Problems Console Tasks Properties

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- Line 8 declare the array

Index	0	1	2	3	4
numbers	10	2	7	5	3

- Line 11 changes first number to 9

Index	0	1	2	3	4
numbers	9	2	7	5	3

- Line 12 and 13 also do changes

Index	0	1	2	3	4
numbers	9	2	21	5	4

Printing array forward and backward

10_02.cpp

```
3 using namespace std;
4
5 int main() {
6     const int size = 5;
7
8     // Declare 5 positions of type integer
9     int numbers[size] = {1, 2, 3, 4, 5};
10
11     for (int i = 0; i < size; ++i)
12         cout<<numbers[i]<<" ";
13     cout<<"\n";
14
15     for (int i = 0; i < size; ++i)
16         cout<<numbers[size-i-1]<<" ";
17     cout<<"\n";
18
19     return 0;
20 }
21
```

- Remember last element position is size-1
- Trace the backward
 - Index 4
 - Index 3
 - Index 2
 - Index 1
 - Index 0

Problems Console Tasks Properties

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```
1 2 3 4 5
5 4 3 2 1
|
```

Read 5 numbers in array - find minimum

- Remember: Deal with each cell as a variable
 - read/write/assign

10_03.cpp

```
3
4 int main() {
5     const int size = 5;
6
7     // Declare 5 positions of type integer
8     int numbers[size];
9
10    for (int i = 0; i < size; ++i)
11        cin >> numbers[i];
12
13    int minimum = numbers[0];
14    for (int i = 1; i < size; ++i)
15        if (minimum > numbers[i])
16            minimum = numbers[i];
17
18    cout << minimum;
19
20    return 0;
21 }
```

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70 50 20 100 200

20|

Practice: Find first and 2nd Maximum values

- Read an Integer N (< 200), then read N (distinct) integers. Find the maximum and 2nd maximum values
- Input: 5 10 20 3 30 7 \Rightarrow Output 30 20
 - 30 is the maximum in the array
 - If we removed it, the next maximum is 20
- Stop the video and code it

Practice: Find first and 2nd Maximum values

```
10_04.cpp
1 using namespace std;
2
3
4 int main() {
5     int n, numbers[200];    // max expected size
6
7     cin >> n;
8     for (int i = 0; i < n; ++i)
9         cin >> numbers[i];
10
11     int maximum_idx = 0;
12     for (int i = 1; i < n; ++i)
13         if (numbers[maximum_idx] < numbers[i])
14             maximum_idx = i;
15
16     int max1 = numbers[maximum_idx];
17     numbers[maximum_idx] = -1000000;    // assume good value
18
19     maximum_idx = 0;    // same code again
20     for (int i = 1; i < n; ++i)
21         if (numbers[maximum_idx] < numbers[i])
22             maximum_idx = i;
23
24     int max2 = numbers[maximum_idx];
25     cout << max1 << " " << max2;
26     return 0;
27 }
```

- Easy idea
- Find first maximum (idx)
 - Mark with very small value
- Find again first maximum
 - This is now the 2nd maximum
- Disadvantages
 - Need to loop twice
 - Need good value for -ve
 - Workaround: ignore previous position

Problems Console Tasks Properties Call Graph Search

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```
5 10 20 3 30 7
30 20|
```


Practice: Find first and 2nd Maximum values

```
10_05.cpp
1 #include<iostream>
2 using namespace std;
3
4 int main() {
5     int n, numbers[200];    // max expected size
6
7     cin >> n;
8     for (int i = 0; i < n; ++i)
9         cin >> numbers[i];
10
11     int max1, max2;
12     if (numbers[0] >= numbers[1])
13         max1 = numbers[0], max2 = numbers[1];
14     else
15         max1 = numbers[1], max2 = numbers[0];
16
17     for (int i = 2; i < n; ++i)
18         if (max1 <= numbers[i])
19             max2 = max1, max1 = numbers[i];
20         else if (max2 < numbers[i])
21             max2 = numbers[i];
22
23     cout << max1 << " " << max2;
24     return 0;
25 }
26
```

- Maintain 2 variables for the 2 maximums
- Iterate on the array and update together
- Say we have so far 20 10
 - And we found value 30
 - Now we should be 30 20
- Say we have so far 20 10
 - And we found value 15
 - Now we should be 20 15

Practice: Find pair values of maximum sum

- Read an Integer N, then read $N \leq 200$ (distinct) integers. Find a pair of numbers (e.g. 2 different indices) whose sum is maximum
- Input: 5 2 10 3 50 15 \Rightarrow 65 (from 50 + 15)
- Stop the video and code it

Practice: Find pair of max sum - Buggy

10_06_bug.cpp

```
1 #include<iostream>
2 using namespace std;
3
4 int main() {
5     int n, numbers[200];
6
7     cin >> n;
8     for (int i = 0; i < n; ++i)
9         cin >> numbers[i];
10
11     int idx1 = -1, idx2 = -1;
12
13     for (int i = 0; i < n; ++i) {
14         for (int j = 0; j < n; ++j) {
15             if (idx1 == -1)
16                 idx1 = i, idx2 = j;
17             else if (numbers[idx1] + numbers[idx2] <
18                     numbers[i] + numbers[j])
19                 idx1 = i, idx2 = j;
20         }
21     }
22     cout<<numbers[idx1]<<" "<<numbers[idx2];
23
24     return 0;
25 }
26
```

- Let's just do 2 nested loops to find the pair
 - There is a bug
 - Also half of operations is useless!

Practice: Find pair of max sum - Fixed

```
10_07.cpp
1 #include<iostream>
2 using namespace std;
3
4 int main() {
5     int n, numbers[200];
6
7     cin >> n;
8     for (int i = 0; i < n; ++i)
9         cin >> numbers[i];
10
11     int idx1 = -1, idx2 = -1;
12
13     for (int i = 0; i < n; ++i) {
14         for (int j = i+1; j < n; ++j) {
15             if (idx1 == -1)
16                 idx1 = i, idx2 = j;
17             else if (numbers[idx1] + numbers[idx2] <
18                    numbers[i] + numbers[j])
19                 idx1 = i, idx2 = j;
20         }
21     }
22     cout<<numbers[idx1]<<" "<<numbers[idx2];
23
24     return 0;
25 }
```

Problems Console Tasks Properties 1010 0101 Call Graph

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5 2 10 3 50 15

50 15

- Trick: Start j from i+1
 - Avoid duplicate bug
 - Avoid duplicate processing
 - We test positions (2, 4) and then test (4, 2) which is same locations!
- This is very inefficient code!
 - Can you do it using a single loop!
 - Hint: Simple observation

Practice: Find pair of max sum - FASTER

- Simply, the pair of maximum sum must come from **the maximum value and the 2nd maximum value**
- Use the code we explained, get them and sum them
- Think more \Rightarrow Code efficient

Practice: Reverse in place

- Read an Integer N, then read $N \leq 200$ integers.
 - In-place: Change the current array, don't use 2 arrays
- Simple idea: Iterate from the begin and end in same time
 - Swap the 2 positions
 - Do this till the middle only
- Let say array is 1 2 3 4 5 6 7 8
 - Step 1: swap (1, 8) \Rightarrow 8 2 3 4 5 6 7 1
 - Step 2: swap (2, 7) \Rightarrow 8 7 3 4 5 6 2 1
 - Step 3: swap (3, 6) \Rightarrow 8 7 6 4 5 3 2 1
 - Step 4: swap (4, 5) \Rightarrow 8 7 6 5 4 3 2 1
 - Stop after $n/2$ steps

Practice: Reverse in place

10_08.cpp

```
1 #include<iostream>
2 using namespace std;
3
4 int main() {
5     int n, numbers[200];
6
7     cin >> n;
8     for (int i = 0; i < n; ++i)
9         cin >> numbers[i];
10
11     for (int i = 0; i < n/2; ++i) {
12         int last = n - i - 1;
13         // swap positions: i and last
14         int temp = numbers[i];
15         numbers[i] = numbers[last];
16         numbers[last] = temp;
17     }
18
19     for (int i = 0; i < n; ++i)
20         cout<<numbers[i]<<" ";
21     return 0;
22 }
```

Problems Console Tasks Properties

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6

1 2 3 4 5 6

6 5 4 3 2 1 |

Practice: Find most frequent number

- Read an Integer N , then read $N \leq 200$ integers. Find the value that repeated the most number of times.
 - Each integer is $0 \leq \text{integer} \leq 150$
- Example for array: 1 2 1 3 1 5 5
 - 1 repeated 3 times: the largest
 - 2 repeated 1 time
 - 5 repeated 2 times
- Stop video and think

Practice: Find most frequent number

10_09.cpp

```
4 int main() {
5     int n, numbers[200];
6
7     cin >> n;
8     for (int i = 0; i < n; ++i)
9         cin >> numbers[i];
10
11     int max_value = -1, max_repeat = -1;
12
13     for (int i = 0; i < n; ++i)
14     {
15         // count how many times numbers[i] exists
16         int repeat = 0;
17         for (int j = 0; j < n; ++j)
18             repeat += numbers[i] == numbers[j];
19
20         if (max_repeat == -1 || max_repeat < repeat)
21             max_repeat = repeat, max_value = numbers[i];
22     }
23     cout<<max_value<<" repeated "<<max_repeat<<" times";
24
25     return 0;
26 }
```

Problems Console Tasks Properties Call Graph Search

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```
5 1 1 1 2 1
1 repeated 4 times|
```

- One easy idea
- For each number, count how many times it in the array. Find maximum of them
- Disadvantage: nested loops (much processing)
- Can you do in 1 loop only?
 - Hint: use another array

Practice: Find most frequent number - FASTER

```
10_10.cpp
1 #include<iostream>
2 using namespace std;
3
4 int main() {
5     int n, numbers[200];
6
7     // Be careful: max value is 150.
8     // So we need to access the array at 150
9     int frequency[150+1] = {0}; // {0} set all to zeros
10
11     cin >> n;
12     for (int i = 0; i < n; ++i)
13     {
14         cin >> numbers[i];
15         frequency[numbers[i]]++;
16     }
17
18     // just find max position in the array
19     int max_pos = -1;
20
21     for (int i = 0; i < 151; ++i) // Iterate on ALL array
22     {
23         if (max_pos == -1 || frequency[max_pos] < frequency[i])
24             max_pos = i;
25     }
26     cout<<max_pos<<" repeated "<<frequency[max_pos]<<" times";
27
28     return 0;
29 }
```

- Let's use another array
- We will use a trick called frequency array
 - We think of the index as value
 - If we have M values, create array of M+1 values
- Iterate on the array and increment each time you meet a number
- Find max in the array

```
Problems Console Tasks Properties Call Graph Search
<terminated> ztemp [C/C++ Application] /home/moustafa/workspaces/eclipse_cpp/zt
3
100 100 2
100 repeated 2 times|
```

Run time error: Index out of boundary

- One of the most errors we do
- You access array with
 - Negative index
 - Index > its max value
- E.g. `int arr[100];`
- Don't
 - `arr[100]` ⇒ Only 0 to 99
 - `arr[-10]`
 - The program may **crash**

Other Data types

- We focused on integer, but we can define array of other values
- **double** salary[100];
 - Array of 100 salaries
- **char** letters[300];
 - Array of 300 letters
- **string** names[200];
 - Array of 200 names

Homework 1: Search for a number

- Read an Integer N, then read $N \leq 200$ integers $[0 \leq A[i] \leq 500]$.
 - We will search in this array for numbers
- Then read integer Q (for a number of queries), then read Q integers
 - For each integer, find the **last occurrence** in the array. Print its index
 - If doesn't exist, print -1
- Input 5 1 2 7 3 7 3 7 9 2
 - Means Array of 5 numbers (1 2 7 3 7) and 3 queries (7 9 2)
- Output
 - 4 [7 exists in 2 positions (2 and 4). The last is 4]
 - -1 [9 doesn't exist]
 - 1 [2 exists only in position 1]
- Easy with nested loops. Can you do with 1 loop?

Homework 2: Is increasing array?

- Read an Integer N, then read N \leq 200 integers. Print YES if the array is increasing. Array is increasing if every element is \geq the previous number
- Inputs
 - 4 1 2 2 5 \Rightarrow YES
 - 5 1 0 7 8 9 \Rightarrow NO [0 is $<$ 1, the previous number]
 - 2 -10 10 \Rightarrow YES

Homework 3: Replace MinMax

- Given a number N and an array A of N numbers. Assume all values [0, 2000]
- Print the array after doing the following operations:
 - Find minimum number in these numbers.
 - Find maximum number in these numbers.
 - Replace **each** minimum number with maximum number and Vice Versa.
- Input \Rightarrow Output
 - 7 4 1 3 10 8 10 10 \Rightarrow 4 10 3 1 8 1 1

Homework 4: Find the 3 minimum values

- Read integer N (≥ 3), then read N integers. Find the 3 lowest numbers.
 - Don't change the array content
 - Don't iterate on the array more than once
- Input \Rightarrow Output
 - 5 4 1 3 10 8 \Rightarrow 1 3 4
 - 3 7 9 -2 \Rightarrow -2 7 9

Homework 5: Smallest pair

- Given a number N (≤ 200) and an array A of N numbers.
- Print the smallest possible result of $A_i + A_j + j - i$, where $1 \leq i < j \leq N$.
- Input \Rightarrow Output
 - 4 20 1 9 4 \Rightarrow 7

Homework 6: Is Palindrome?

- Given a number N and an array A of N numbers. Determine if it's palindrome or not.
- *An array is called palindrome if it reads the same backward and forward*
 - *for example, arrays $\{ 1 \}$ and $\{ 1,2,3,2,1 \}$ are palindrome*
 - *while arrays $\{ 1,12 \}$ and $\{ 4,7,5,4 \}$ are not.*
- Inputs \Rightarrow Outputs
 - $5\ 1\ 3\ 2\ 3\ 1 \Rightarrow \text{YES}$
 - $4\ 1\ 2\ 3\ 4 \Rightarrow \text{NO}$

Homework 7: Find most frequent number

- Read an Integer N, then read $N \leq 200$ integers. Find the value that repeated the most number of times.
 - Each integer is $-500 \leq \text{integer} \leq 270$
- Example for array: 7 -1 2 -1 3 -1 5 5
 - -1 repeated 3 times: the largest
- Don't use nested loops

Homework 8: Digits frequency

- Read an Integer N, then read $N \leq 200$ integers. For all the digits from 0 to 9, we want to know how many times appeared
 - Input 2 78 307
 - Output:
 - 0 1
 - 1 0 [digit 1 never appeared]
 - 2 0
 - 3 1
 - 4 0
 - 5 0
 - 6 0
 - 7 2 [digit 7 appeared twice]
 - 8 1
 - 9 0

Homework 9: Recamán's sequence

- Sequence is a series of numbers. The first terms are 0, 1, 3, 6, 2, **7**, ...
 - So last term **value** is 7 and its **index** is 5 (zero based)
 - The next value is either:
 - **Last value-last index-1** if 2 conditions satisfied
 - It is > 0
 - It did not appear before
 - E.g. $7 \text{ (last value)} - 5 \text{ (last index)} - 1 = 7 - 5 - 1 = 1$ (> 0 but already exists)
 - Or last **value+last index+1** = $7 + 5 + 1 = 13$
- Read integer index ($[0, 200]$) and print the value of this index
 - E.g. $(6 \Rightarrow 13)$, $(9 \Rightarrow 21)$, $(17 \Rightarrow 25)$
- Don't use nested loops
- The series is: 0, 1, 3, 6, 2, 7, **13**, 20, 12, **21**, 11, 22, 10, 23, 9, 24, 8, **25**, 43

Homework 10: Fixed sliding window

- Read Integers K and N , (where $K \leq N$). then read $N \leq 200$ integers. Then find a sub-array of K elements that has maximum sum.
- Input 3 7 1 0 3 -4 2 -6 9
 - Let's list all sub-arrays of length 3
 - 1 0 3 \Rightarrow sum = 4
 - 0 3 -4 \Rightarrow sum = -1
 - 3 -4 2 \Rightarrow sum = 1
 - -4 2 -6 \Rightarrow sum = -8
 - 2 -6 9 \Rightarrow sum = 5
- Output: 4 6 5 (Sub-array from indices 4 to 6 has maximum sum of 5)
- Hard: Can you do without nested loops? There are 2 ways.

Homework 11: Count increasing subarrays

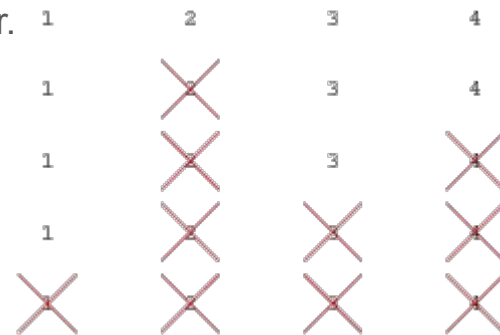
- Read an Integer N, then read $N \leq 200$ integers. Count how many sub-arrays are increasing in the array. A sub-array is set of consecutive numbers in array
- E.g. If array is 1 2 3 4
 - We can find all sub-arrays of length 1 \Rightarrow 1 / 2 / 3 / 4
 - All sub-arrays of length 2 \Rightarrow 1, 2 / 2, 3 / 3, 4
 - All sub-arrays of length 3 \Rightarrow 1, 2, 3 / 2, 3, 4
 - All sub-arrays of length 4 \Rightarrow 1, 2, 3, 4
- Inputs \Rightarrow Outputs
 - 4 1 2 3 4 \Rightarrow 10 [10 sub-arrays from previous example, all are increasing]
 - 4 4 3 2 1 \Rightarrow 4 [only sub-arrays of length 1 can be considered]
 - 4 10 20 1 5 \Rightarrow 6
- Easy using 3 nested loops. Medium using 2 loops. Can you do it with 1 loop?

Homework 12: Josephus problem

- Read integers N (≤ 200) and K (≤ 1000000). Find the game winner for following game:
- We have a group of N people in Circle. They are numbered 1, 2, ..., N
 - Someone is the master of the game.
 - He starts from Person #1. Count K . Then remove this person from the circle.
 - He keeps doing so till only 1 person remains. This is the winner.

- Input 4 2

- Means we have people: 1, 2, 3, 4. Master starts at 1
 - Count 2 persons (2 removed), start from 3
 - Count 2 persons (4 removed), start from 1
 - Count 2 persons (3 removed), 1 is winner



- Output

- People removed in order: 2 4 3 1 [same answer for 10 2 why?]

Homework 13: longest subarray

- Read integers N (≤ 1000) then N numbers each is either 0 or 1. Find longest **subarray** with number of zeros = numbers of ones
 - You can easily implement it using 3 loops
 - Or with little thinking using 2 loops (even with no extra arrays)
 - Hard: You can implement it without any nested loops
- Inputs \Rightarrow outputs
 - 7 1 0 0 0 1 1 1 \Rightarrow 6 (e.g. 100011 or 000111)
 - 19 1 0 0 0 0 0 1 0 1 1 0 1 0 0 0 0 0 0 1 \Rightarrow 8 (e.g. 00101101)
- Reduction
 - How may this problem be reduced to another problem: longest subarray of zero sum?

تم بحمد الله

علمكم الله ما ينفعكم

ونفعكم بما تعلمتم

وزادكم علماً