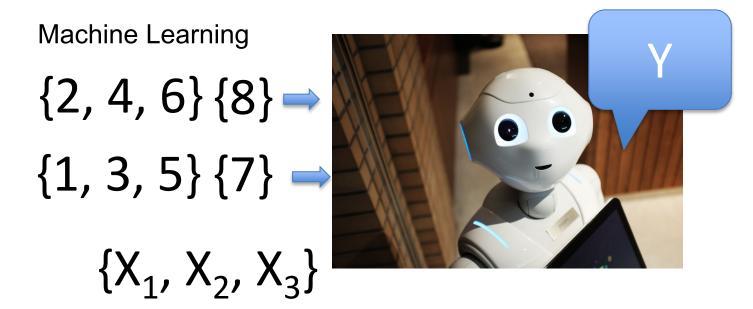






Branch of artificial intelligence using data to train a machine (model) to make predictions based on inputs (data)



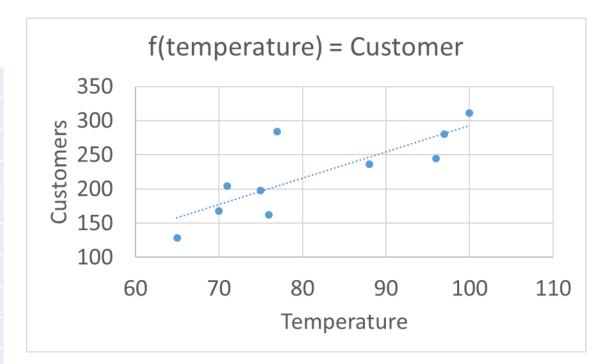
- Supervised Learning
  - Data for training machine learning model include known labels (outputs) and features (inputs)
- Unsupervised Learning
  - Data for training model include only features (inputs) but no known labels (outputs)
    - Machine learning model is trained by observing similarities in features (inputs)

- Supervised Learning
  - Popular supervised learning method
    - Regression model

$$f(x) = y$$
$$Y = a + bX$$

where X is the explanatory variable
Y is the dependent variable.
b is the slope of the line
a is the intercept value of y when x = 0)

Temperature	Customer
71	204
75	198
100	311
65	128
97	280
77	284
70	168
88	236
76	162
96	245





Temperature	Customer
71	204
75	198
100	311
65	128
97	280
77	284
70	168
88	236
76	162
96	245

#### SUMMARY OUTPUT

Regression Statistics						
Multiple R	0.813790773					
R Square	0.662255423					
Adjusted R Square	0.620037351					
Standard Error	36.81556566					
Observations	10					

#### ANOVA

	Coefficients	Standard Error	t Ctat	D value	Lower 05%	Unnar 05%	104
Total	9	32104.4					
Residual	8	10843.087	1355.385875				
Regression	1	21261.313	21261.313	15.68653871	0.004173386		
	df	SS	MS	F	Significance F		

	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	-91.29220104	79.85396655	-1.143239403	0.285994895	-275.4357781	92.85137604	-275.4357781	92.85137604
Temperature	3.839168111	0.969334269	3.960623525	0.004173386	1.603879278	6.074456944	1.603879278	6.074456944

# Multiple R

- Absolute value of correlation coefficient (Pearson r)
  - The large the number the more indication of possible relationship
  - Can't tell the direction because of the absolute value

# $R^2$

- coefficient of determination
  - How well the regression model (line) fits the data
  - Proportion of the variance in the dependent variable that is explainable (predictable) by he independent variable
  - R<sup>2</sup> = 1 means 100% of the dependent variable can be explained by the independent variable
  - R<sup>2</sup> = 0.80 means 80% of the dependent variable can be explained by the independent variable

# **Standard Error**

- A measure of the precision of the model
  - Average error of the regression model.
  - Tells how wrong the model is
  - The smaller the better (in relation to the coefficient)

# Significant F

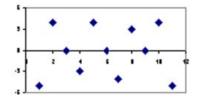
- Significant F is the P-value of F
  - a ratio computed by dividing the mean regression sum of squares by the mean error sum of squares
  - Ranges from 0 to very large number
  - Model is OK if less than 0.05
  - Look for another independent variable if greater than 0.05

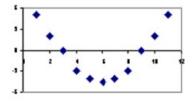
## P-values

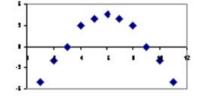
- Probability that the estimated coefficient is unreliable.
  - OK if less than 0.05
  - Otherwise, delete the independent variable > 0.05

## Residuals

• error =  $y - \hat{y}$  (y actual – y predicted)











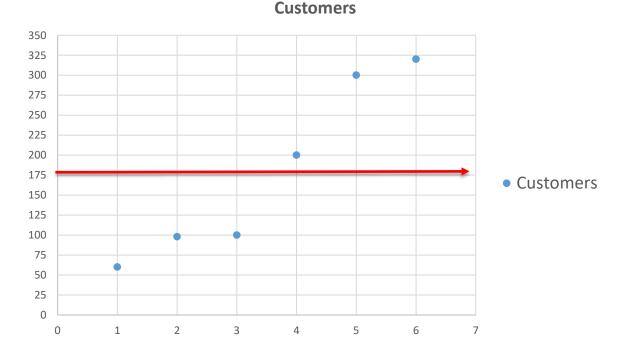
#### Data Science Fundamentals: Regression Results

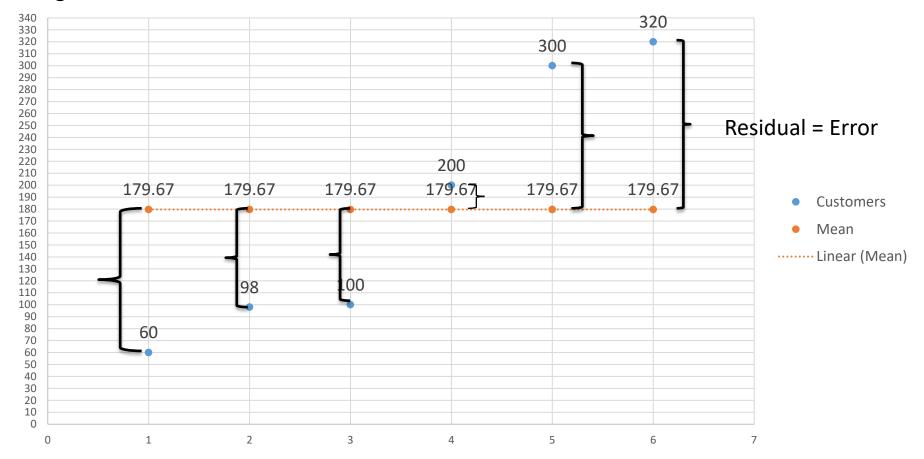
# • Temperature vs. Customers

Temperature	Customers
100	60
95	98
90	100
85	200
80	300
75	320

# Customers = Y = Dependent Variable

Υ	Ϋ́
Customers	Mean
60	180
98	180
100	180
200	180
300	180
320	180





# Regression Results ERROR

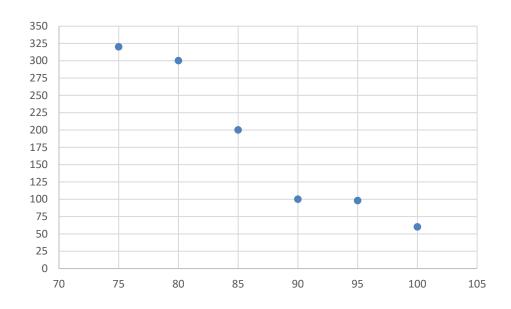
## Residual Residual <sup>2</sup>

Υ	Ÿ	Υ - Ϋ	(Y - Ÿ)^2
60	179.67	-119.67	14320.11
98	179.67	-81.67	6669.44
100	179.67	-79.67	6346.78
200	179.67	20.33	413.44
300	179.67	120.33	14480.11
320	179.67	140.33	19693.44

Total Sum of Square (SST) =  $\Sigma(Y - \overline{Y})^2 = 61923.33$ 

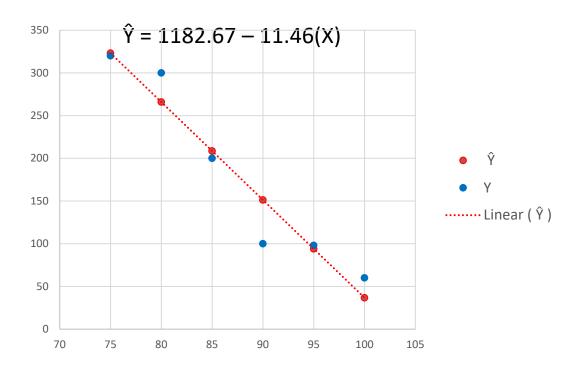
61923.33

X	Υ
Temperature	Customers
100	60
95	98
90	100
85	200
80	300
75	320



Regression S	tatistics							
Multiple R	0.963506714							
R Square	0.928345189							
Adjusted R Square	0.910431486							
Standard Error	33.30579815							
Observations	6							
ANOVA								
	df	SS	MS	F	Significance F			
Regression	1	57486.22857	57486.22857	51.82318801	0.00197334			
Residual	4	4437.104762	1109.27619					
Total	5	61923.33333						
	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	1182.666667	139.990045	8.448219777	0.001075413	793.9919915	1571.341342	793.9919915	1571.341342
Temerature	-11.46285714	1.592321712	-7.198832406	0.00197334	-15.88385097	-7.041863319	-15.88385097	-7.041863319

$$\hat{Y} = 1182.67 - 11.46(X)$$



Χ	Υ	Ŷ	Y-Ŷ	(Y-Ŷ)^2
100	60	36.67		
٥٢	00	93.97	1 55	K
	CT	51.27		
	) J	08.57	CC	
80	300	265.87	1 55	
75	320	323.17		
Sum of Squ	ares Error	(SSE)		4437.49
Total Sum	of Squares		61923.33	
Sum of Squ	iares Regre	ssion (SSR	)	57485.84

Regression S	tatistics						Χ	Υ	Ŷ	Υ-	Ŷ	(Y-Ŷ)^2
Regression 3	latistics					_	100	60	36.67	23.3	33	544.29
Multiple R	0.963506714	R Squa	re = SSR	/ SST		╄	95	98	93.97	4.0	)3	16.24
R Square	0.928345189		= 574	85.84/	51923.33		90	100	151.27	-51.	27	2628.61
Adjusted R Square	0.910431486		= 0.92	•		ı	85	200	208.57	-8.5	57	73.44
Standard Error	33.30579815					J	80	300	265.87	34.3	13	1164.86
Observations	6						75	320	323.17	-3.1	17	10.05
							Sum of S	Squares Error	(SSE)			4437.49
ANOVA							Total Su	m of Squares	(CCT)			61923.33
	df	SS	MS	F	Significance F		Total Su	iii oi squares	(331)			01923.33
Regression	1	57486.22857	57486.22857	51.82318801	0.00197334		Sum of S	SquaresRegre	ssion (SSI	R)		57485.84
Residual	4	4437.104762	1109.27619									
Total	5	61923.33333										
	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upp	er 95%	Lower 95.0%	Upper 9	5.0%		
Intercept	1182.666667	139.990045	8.448219777	0.001075413	793.9919915	157	1.341342	793.9919915	1571.3	41342		
Temerature	-11.46285714	1.592321712	-7.198832406	0.00197334	-15.88385097	-7.04	1863319	-15.88385097	-7.0418	63319		

$$\hat{Y} = 1182.67 - 11.46(X)$$

#### Machine Learning- Python -Regression Analysis



# • Temperature vs. Customers

Temperature	Customers
100	60
95	98
90	100
85	200
80	300
75	320

Regression S	tatistics							
Multiple R	0.963506714							
R Square	0.928345189							
Adjusted R Square	0.910431486							
Standard Error	33.30579815							
Observations	6							
ANOVA								
	df	SS	MS	F	Significance F			
Regression	1	57486.22857	57486.22857	51.82318801	0.00197334			
Residual	4	4437.104762	1109.27619					
Total	5	61923.33333						
	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	1182.666667	139.990045	8.448219777	0.001075413	793.9919915	1571.341342	793.9919915	1571.341342
Temerature	-11.46285714	1.592321712	-7.198832406	0.00197334	-15.88385097	-7.041863319	-15.88385097	-7.041863319

$$\hat{Y} = 1182.67 - 11.46(X)$$

```
import pandas as pd
```

```
# need for regression analysis
```

import statsmodels.api as sm from statsmodels.formula.api import ols

```
temperature = [100,95,90,85,80,75]
customer= [60,98,100,200,300,320]
```

```
df = pd.DataFrame(temperature, columns=["Temperature"])
df["Customer"] = customer
```

```
# Perform Regression Analysis
```

```
results = ols ("Customer ~ Temperature", data=df).fit() print (results.summary())
```

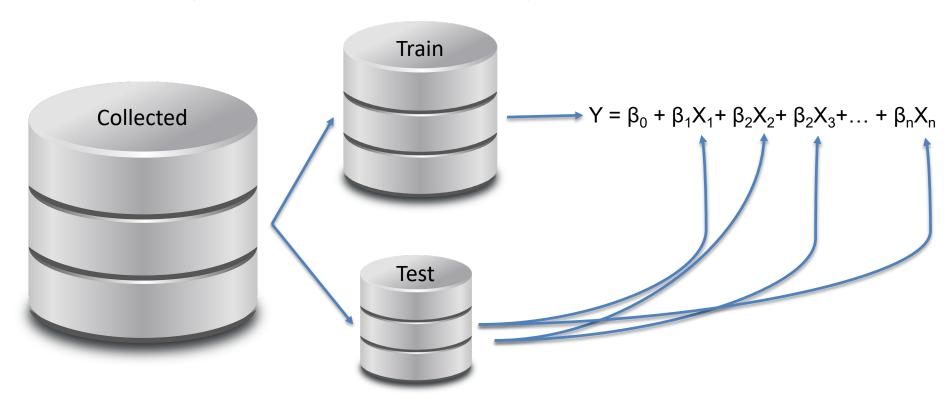
#### OLS Regression Results

Dep. Variable: Model: Method: Date: Time: No. Observations:	Customer OLS Least Squares Fri, 29 May 2020 21:50:05	AIC:	: (	0.928 0.910 51.82 0.00197 -28.332 60.66
Df Residuals:	4	BIC:		60.25
Df Model: Covariance Type:	1 nonrobust			
CO	ef std err	t P> t	[0.025	0.975]
Intercept 1182.66 Temperature / -11.46		8.448 0.001 -7.199 0.002	793.992 -15.884	1571.341 -7.042
Omnibus: Prob(Omnibus): Skew: Kurtosis:	nan nan -0.659 2.585	Durbin-Watson: Jarque-Bera (JB): Prob(JB): Cond. No.		1.909 0.477 0.788 905.
Ŷ = 1182.67 – 11	.46(X)			:======

#### Linear Regression in Machine Learning: Train and Test Model



#### Linear Regression in Machine Learning: Train and Test Model



import mysql.connector as sq import pandas as pd

# needed for machine learning regression model training and testing from sklearn.model\_selection import train\_test\_split from sklearn.linear\_model import LinearRegression

# Connecting to MySQL, query database, store results in dataframe variable mydb=sq.connect(host="localhost",user="root",passwd="ucla", buffered=True) query = "SELECT \* FROM covid19USA531.covid19USA531" df = pd.read\_sql(query,mydb)

	iso_code	location	date	total_cases	new_cases	total_deaths	new_deaths	total_tests	new_tests
0	USA	United States	3/14/2020	2174	511	47	7	31732	4575
1	USA	United States	3/15/2020	2951	777	57	10	39332	7600
2	USA	United States	3/16/2020	3774	823	69	12	57173	17841
3	USA	United States	3/17/2020	4661	887	85	16	72856	15683
4	USA	United States	3/18/2020	6427	1766	108	23	97590	24734

# prepare x by droping y = total\_deaths
x = df.drop(["iso\_code", "location", "date", "total\_deaths"], axis=1)

	total_cases	new_cases	new_deaths	total_tests	new_tests
0	2174	511	7	31732	4575
1	2951	777	10	39332	7600
2	3774	823	12	57173	17841
3	4661	887	16	72856	15683
4	6427	1766	23	97590	24734

```
# prepare y = total_deaths
y = df.total_deaths
0
          47
           57
           69
3
          85
4
         108
74
       98916
75
      100442
76
      101617
77
      102836
78
      103781
```

Name: total\_deaths, Length: 79, dtype: int64

```
#train_and_test_data
from sklearn.model_selection import train_test_split
x_train,x_test,y_train,y_test = train_test_split(x,y,test_size=0.2,random_state=40)
```

```
model = LinearRegression()
model.fit(x_train, y_train)
```

model.score(x\_test,y\_test)

 $model.coef\_$ 

model.intercept\_

## Machine Learning: Multicollinearity



Multiple Regression: Multicollinearity

- More may not be better
  - May create problems
    - Independent variable correlates with one or more independent variables
    - Independent is no longer independent!

## Machine Learning: Multicollinearity



Multiple Regression: Multicollinearity

# VIF for Multicollinearity Testing from statsmodels.stats.outliers\_influence import variance\_inflation\_factor