Table of Contents

- ▼ 1 Customer Segmentation for a Credit Card Company
 - 1.1 Problem statement
 - 1.2 Summary of results
- ▼ 2 Exploring the data
 - 2.1 Import modules
 - 2.2 Helper functions
 - 2.3 Import data
 - 2.4 EDA
 - 3 PCA
- ▼ 4 Kmeans
 - 4.1 Selecting K
 - 4.2 Comparing Clusters
- ▼ 5 Hierarchical Clustering
 - 5.1 Building a agglomerative clustering model
 - 5.2 Selecting the number of clusters and comparison

1 Customer Segmentation for a Credit Card Company

mahshidxyz (http://www.github.com/mahshidxyz)

November 2020

1.1 Problem statement

This project is about customer segmentation for a credit card company. One way to reduce the costs associated with credit card signup incentives and offering successful marketing campaigns is to offer credit cards with carefully targeted benefits that will attract new cardholders. The goal of customer segmentation here is to get an idea of popular benefits to associate with each new card offering. To study the various kinds of users who use the company's products we are looking at the user data over a 6 month period. The data consists of 8950 rows (one for each cardholder) organized in columns with descriptive headers. The data has been provided by J. Patrick Weller. Currently this data is not publicly available.

Column label information:

- . CUST ID: Credit card holder ID
- BALANCE : Monthly average balance (based on daily balance averages)
- BALANCE_FREQUENCY: Ratio of last 12 months with balance
- PURCHASES: Total purchase amount spent during last 12 months
- · ONEOFF PURCHASES: Total amount of one-off purchases
- · INSTALLMENTS_PURCHASES: Total amount of installment purchases
- · CASH ADVANCE: Total cash-advance amount
- PURCHASES_FREQUENCY: Frequency of purchases (percentage of months with at least one purchase)
- ONEOFF_PURCHASES_FREQUENCY: Frequency of one-off-purchases
- PURCHASES_INSTALLMENTS_FREQUENCY: Frequency of installment purchases
- CASH_ADVANCE_FREQUENCY : Cash-Advance frequency
- AVERAGE PURCHASE TRX: Average amount per purchase transaction
- CASH ADVANCE TRX: Average amount per cash-advance transaction
- PURCHASES TRX: Average amount per purchase transaction

- CREDIT LIMIT : Credit limit
- PAYMENTS: Total payments (due amount paid by the customer to decrease their statement balance) in the period

1.2 Summary of results

I used Kmeans and Hierarchical Clustering to segment customers. Both methods resulted in comparable outcomes. I identified 4 clusters with the following descriptions:

- Cluster 1: Low balance, infrequent users. Mostly use the card for one off purchases and cash advances. Rarely pay the balance in full. Low credit limit.
- Cluster 2: Low balance, frequent users. Don't spend too much money with this card but use it frequently for small purchases. Rarely do cash advance. Low credit limit.
- Cluster 3: High balance driven by frequent cash advance not purchases. Prefer to pay for everything in cash! Rarely pay the balance in full. High credit limit.
- Cluster 4: High balance driven by frequent purchases (both one-off purchases and installments), not so much by cash advances. Use credit to pay for everything!. High credit limit.

Reommendation:

Here I came up with some simple offer components that can be attractive to different customer segments. Tailoring these offers requires a lot of knowledge about the costs associated with each type of offer.

- Offer low APR for customers who rarely pay their balance in full (cluster # 1 and # 3)
- Offer low cash advance fee for customers who frequently take cash advances (cluster # 3)
- Offer sign up bonuses (e.g. \$200 bonus if you spend \$500 in the first 3 months) for customers with low balance, customers who use their cards frequently but for small purchases or do not use it often (cluster # 1 and # 2)
- Offer higher cash back for high spenders and frequent users (stay competitive in the credit card space) to retain customers (cluster # 1 and # 4)

2 Exploring the data

2.1 Import modules

```
In [1]: ▶ import datetime as dt
            import numpy as np
            import pandas as pd
            import seaborn as sns
            import warnings
            import matplotlib.dates as mdates
            import matplotlib.pyplot as plt
            from sklearn.decomposition import PCA
            from sklearn.cluster import KMeans, AgglomerativeClustering
            from scipy.cluster.hierarchy import dendrogram
            from sklearn.preprocessing import StandardScaler
            from scipy.spatial.distance import cdist
            from sklearn.metrics import davies bouldin score, silhouette score
            from patsy import dmatrices
            from statsmodels.stats.outliers_influence import variance_inflation_factor
            pd.set_option("display.max_columns", None)
            sns.set_context("poster", font_scale=1.2)
            # warnings.filterwarnings('ignore')
```

2.2 Helper functions

```
In [2]: ▶ def print full(x):
                  pd.set_option("display.max_rows", len(x))
                  pd.set_option("display.max_columns", None)
                  pd.set option("display.width", 2000)
                  pd.set option("display.float format", "{:20,.2f}".format)
                  pd.set_option("display.max_colwidth", None)
                  print(x)
                  pd.reset_option("display.max_rows")
                  pd.reset_option("display.max_columns")
                 pd.reset option("display.width")
                  pd.reset_option("display.float_format")
                  pd.reset_option("display.max_colwidth")
             def col_name_cleaner(df):
                 df.columns = [column.replace("(", "") for column in df.columns]
                 df.columns = [column.replace(")", "") for column in df.columns]
                 df.columns = [column.replace(" ", "_") for column in df.columns]
df.columns = [column.replace("/", "_") for column in df.columns]
                  df.columns = [column.lower() for column in df.columns]
```

2.3 Import data

```
In [3]: M df = pd.read_csv("cc_info.csv")
df.head()
```

Out[3]:

	CUST_ID	BALANCE	BALANCE_FREQUENCY	PURCHASES	ONEOFF_PURCHASES	INSTALLMENTS_PU
0	C10001	40.900749	0.818182	95.40	0.00	_
1	C10002	3202.467416	0.909091	0.00	0.00	
2	C10003	2495.148862	1.000000	773.17	773.17	
3	C10004	1666.670542	0.636364	1499.00	1499.00	
4	C10005	817.714335	1.000000	16.00	16.00	

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 8950 entries, 0 to 8949
Data columns (total 18 columns):

	6.1		11 6 1	Б.
#	Column	Non-Nu	ull Count	Dtype
0	cust_id	8950 r	non-null	object
1	balance	8950 r	non-null	float64
2	balance_frequency	8950 r	non-null	float64
3	purchases	8950 r	non-null	float64
4	oneoff_purchases	8950 r	non-null	float64
5	installments_purchases	8950 r	non-null	float64
6	cash_advance	8950 r	non-null	float64
7	purchases_frequency	8950 r	non-null	float64
8	oneoff_purchases_frequency	8950 r	non-null	float64
9	<pre>purchases_installments_frequency</pre>	8950 r	non-null	float64
10	cash_advance_frequency	8950 r	non-null	float64
11	cash_advance_trx	8950 r	non-null	int64
12	purchases_trx	8950 r	non-null	int64
13	credit_limit	8949 r	non-null	float64
14	payments	8950 r	non-null	float64
15	minimum_payments	8637 r	non-null	float64
16	prc_full_payment	8950 r	non-null	float64
17	tenure	8950 r	non-null	int64
d+,,n	$ac \cdot f(a) + f(a) + f(a) + f(a) + f(a) + f(a)$	1\		

dtypes: float64(14), int64(3), object(1)

memory usage: 1.2+ MB

```
In [5]:

    df.isnull().sum()

   Out[5]: cust_id
                                                 0
            balance
                                                 0
           balance_frequency
                                                 0
            purchases
                                                 0
                                                 0
           oneoff purchases
            installments purchases
                                                 0
            cash_advance
                                                 0
            purchases frequency
                                                 0
           oneoff purchases frequency
                                                 0
            purchases_installments_frequency
                                                 0
                                                 0
            cash advance frequency
            cash advance trx
                                                 0
                                                 0
            purchases_trx
            credit limit
                                                 1
            payments
                                                 0
                                               313
           minimum_payments
           prc full payment
                                                 0
           tenure
                                                 0
            dtype: int64
In [6]:

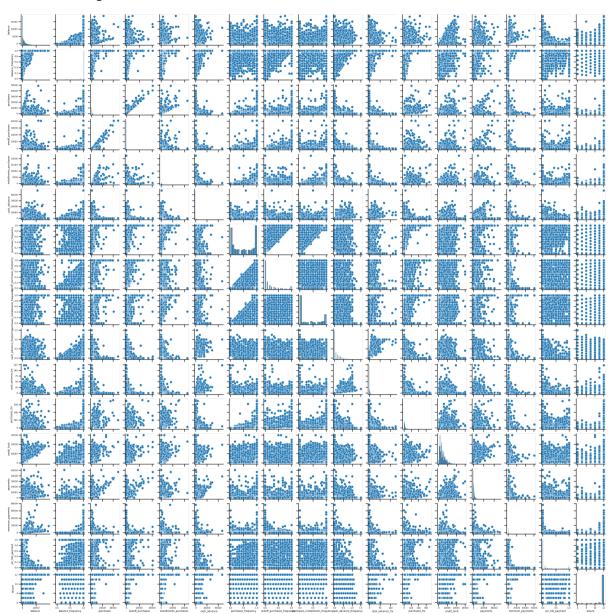
    df = df.dropna()

           df.info()
            <class 'pandas.core.frame.DataFrame'>
            Int64Index: 8636 entries, 0 to 8949
           Data columns (total 18 columns):
                Column
                                                  Non-Null Count Dtype
                -----
                                                  _____
            ---
            0
                cust id
                                                                 object
                                                  8636 non-null
                                                  8636 non-null float64
             1
                balance
             2
                                                  8636 non-null float64
                balance_frequency
                                                                 float64
             3
                purchases
                                                  8636 non-null
                oneoff_purchases
             4
                                                                 float64
                                                  8636 non-null
             5
                                                                 float64
                installments_purchases
                                                  8636 non-null
                cash advance
                                                  8636 non-null
                                                                 float64
             7
                purchases_frequency
                                                  8636 non-null
                                                                 float64
             8
                oneoff_purchases_frequency
                                                  8636 non-null
                                                                 float64
             9
                purchases installments frequency 8636 non-null
                                                                 float64
             10
                cash_advance_frequency
                                                  8636 non-null
                                                                 float64
             11 cash_advance_trx
                                                                 int64
                                                  8636 non-null
             12 purchases trx
                                                  8636 non-null
                                                                 int64
             13 credit_limit
                                                  8636 non-null
                                                                 float64
             14 payments
                                                                 float64
                                                  8636 non-null
             15
                minimum payments
                                                  8636 non-null
                                                                 float64
             16 prc full payment
                                                  8636 non-null
                                                                 float64
             17 tenure
                                                  8636 non-null
                                                                 int64
            dtypes: float64(14), int64(3), object(1)
            memory usage: 1.3+ MB
In [7]:
         df.cust_id.nunique()
   Out[7]: 8636
```

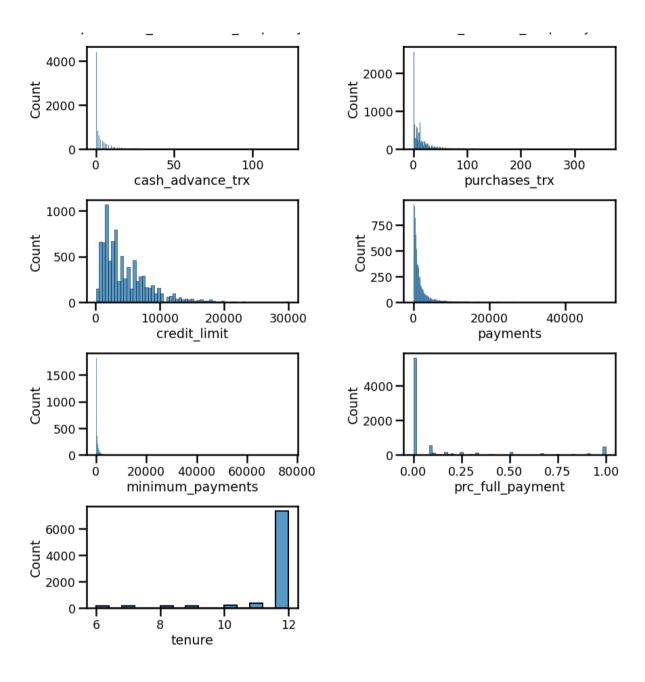
2.4 EDA

In [8]: ## Pair plots, no obvious clusters stand out
sns.set_context("poster", font_scale=0.5)
sns.pairplot(df.iloc[:, 1:])

Out[8]: <seaborn.axisgrid.PairGrid at 0x1f62b83fa60>



```
▶ ## Plot histograms
In [9]:
             sns.set_context("poster", font_scale=0.8)
             n_cols = len(df.columns)
             fig, ax = plt.subplots((n_{cols}) // 2, 2, figsize=(14, 2 * (n_{cols})))
             for i in range(1, n_cols):
                 sns.histplot(df.iloc[:, i], ax=ax[(i - 1) // 2][(i - 1) % 2])
                 ax[(i - 1) // 2][(i - 1) % 2].set_xlabel(df.columns[i])
             fig.subplots_adjust(hspace=0.5, wspace=0.5)
             fig.delaxes(ax[8][1])
                                                                 6000
                2000
                                                              Count 2000
             Oont
1000
                    0
                                                                    0
                             5000
                                     10000
                                            15000
                                                                       0.00
                                                                              0.25
                                                                                      0.50
                                                                                             0.75
                                                                                                    1.00
                                   balance
                                                                              balance_frequency
                                                                 4000
                2000
             000 1000
                                                              2000
2000
                    0
                                                                    0
                                 20000
                                             40000
                                                                             10000 20000 30000 40000
                                                                        0
                                  purchases
                                                                               oneoff_purchases
                4000
                                                                 4000
                                                              Count
2000
             2000
                    0
                                                                    0
                       Ó
                            5000 10000 15000 20000
                                                                        Ō
                                                                                  20000
                                                                                               40000
                           installments_purchases
                                                                                cash_advance
                                                                 4000
                2000
             000 th
                                                              Count
                                                                 2000
                   0
                                                                    0
                             0.25
                                     0.50
                                            0.75
                                                                       0.00
                                                                              0.25
                                                                                     0.50
                                                                                             0.75
                      0.00
                                                   1.00
                                                                                                     1.00
                            purchases_frequency
                                                                         oneoff_purchases_frequency
                                                                 4000
                3000
                                                              Count
2000
             2000
2000
                1000
                    0
                                                                    0
                             0.25
                                                                                 0.5
                                     0.50
                                            0.75
                                                                       0.0
                                                                                           1.0
                                                                                                     1.5
                     purchases installments frequency
                                                                           cash advance frequency
```



```
In [34]:
          M
             ## Correlation matrix
             plt.figure(figsize=(20, 20))
             sns.set(font_scale=2.5, style="whitegrid")
             correlation matrix = df.corr()
             # sns.heatmap(df.corr())
             matrix = np.triu(df.corr())
             sns.heatmap(
                  correlation matrix,
                 mask=matrix,
                  vmax=1,
                  vmin=-1,
                  square=True,
                  cmap="Oranges",
                  annot=True,
                 fmt=".1f",
                  linewidth=3,
                 linecolor="white",
                 cbar=False,
             plt.xticks(rotation=90);
```

```
balance
                    balance_frequency
                                purchases
                                                     0.1 0.9
                      oneoff purchases
                                                           0.7
              installments_purchases
                                                           -0.1 -0.0 -0.1
                          cash_advance
                 purchases_frequency -0.1 0.2
                                                           0.4
                                                                        0.4 -0.2
                                                                  0.5
                                                      0.2
                                                           0.5
                                                                        0.2
                                                                              -0.1 0.5
       oneoff_purchases_frequency
purchases_installments_frequency -0.1 0.2
                                                           0.3
                                                                 0.1 0.5 -0.2 0.9
                                                           -0.1
                                                                 -0.1 -0.1 0.6 -0.3 -0.1 -0.3
           cash_advance_frequency
                     cash_advance_trx 0.4
                                                      0.1
                                                           -0.1
                                                                 -0.0
                                                                        -0.1
                                                                              0.7
                                                                                    -0.2 -0.1 -0.2 0.8
                                                      0.2
                                                           0.7
                                                                  0.5
                                                                        0.6
                                                                              -0.1 0.6
                                                                                          0.5
                           purchases trx
                               credit_limit
                                                                        0.3
                                                                              0.3
                                                           0.6
                                                                 0.6
                                                                        0.4
                                               0.3
                                 payments
                                                                                          -0.0
                   minimum_payments
                      prc_full_payment -0.3 -0.2
                                                            0.2
                                                                  0.1
                                                                              -0.2
                                                                                    0.3
                                                                                                      -0.3 -0.2
                                                                              -0.1
                                                                                                       -0.1 -0.0
                                                                                                                                      0.1 -0.0
                                                           0.1
                                                                                    0.1
                                     tenure
                                                                  0.4
                                                                        0.4
                                                                              0.3
                                                                                          0.4
                                                                                                                               0.4
                                                      0.3
                                    cluster
                                 h_cluster 0.5
                                                                                                             cash advance trx
                                                                                                                   purchases_trx
                                                                                                                                payments
                                                                                                                                      minimum_payments
                                                balance
                                                      balance_frequency
                                                            purchases
                                                                  oneoff_purchases
                                                                        installments_purchases
                                                                              cash_advance
                                                                                    purchases_frequency
                                                                                          oneoff_purchases_frequency
                                                                                                 purchases_installments_frequency
                                                                                                       cash_advance_frequency
                                                                                                                          credit_limit
                                                                                                                                            prc_full_payment
                                                                                                                                                         cluster
                                                                                                                                                               h_cluster
```

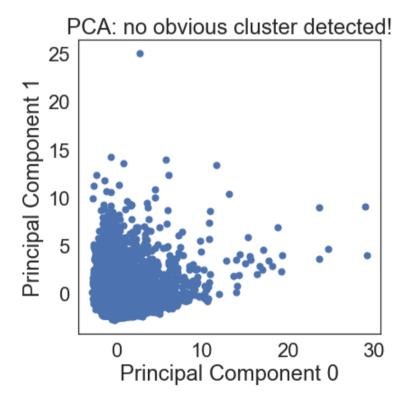
3 PCA

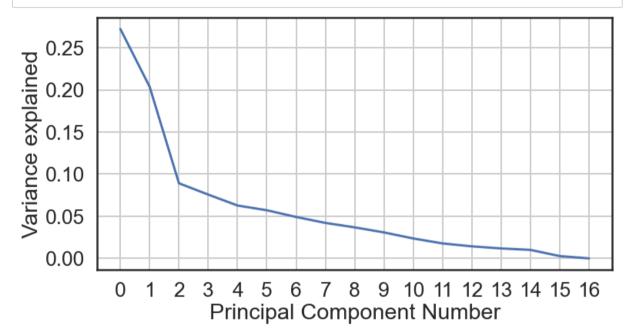
The purpose of the PCA study here is to understand if there are a limited number of features which can explain most of the variations in the feature space. If we could determine only 2 or 3 features are important we can use those features for 2D/3D plotting and visualizing the clusters. It is important to do standardization before PCA to avoid having outliers determine the structure of PCA. Here 80% of the variance can be explained by the first 7 components. Therefore, PCA cannot help us much with making 2D/3D plots after clustering. Therefore I won't use it.

Explained variation per principal component: [0.27231177 0.20374308]

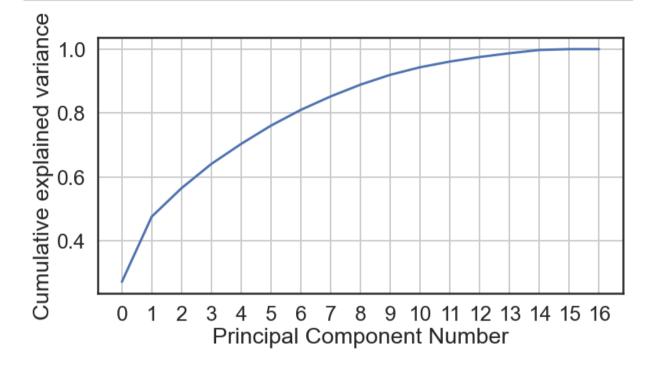
```
In [13]:
         | ## Structure of these two components based on the original features
            print("pca components:\n", pca.components )
            pca components:
             0.32366483 0.2947613
                                     0.27722627 -0.09914536 -0.05696032 0.39106662
               0.2100521
                         0.26372558 0.05932642 0.13056491 0.07791863]
             [ 0.40597942  0.12773854  0.04953037  0.06992969  -0.01148122  0.43724697
              -0.18658162 -0.01474647 -0.17357694 0.42999685 0.41641174 -0.01194676
              0.24382257   0.26418161   0.17041556   -0.19570867   -0.00456549]]
         ## Visualizing the data on the first and second PCs: no obvious clusters using the first
In [14]:
            sns.set(font scale=2, style="white")
            plt.figure(figsize=(6, 6))
            plt.xlabel("Principal Component 0")
            plt.ylabel("Principal Component 1")
            plt.title("PCA: no obvious cluster detected!")
            plt.scatter(
                principalDf.loc[:, "principal component 0"],
                principalDf.loc[:, "principal component 1"],
                s=50,
```

Out[14]: <matplotlib.collections.PathCollection at 0x1f644843880>





```
In [16]: ## Cumulative variance explained by components
## 80% of variance was explained by first 7 PCs
fig, ax = plt.subplots(figsize=(12, 6))
plt.plot(np.cumsum(pca.explained_variance_ratio_))
ax.set_xlabel("Principal Component Number")
ax.set_ylabel("Cumulative explained variance")
ax.set_xticks([x for x in range(len(pca.explained_variance_ratio_))])
ax.grid()
```



4 Kmeans

K-Means is one of the most popular "clustering" algorithms. K-means stores k centroids that it uses to define clusters. A point is considered to be in a particular cluster if it is closer to that cluster's centroid than any other centroid.

K-Means finds the best centroids by alternating between (1) assigning data points to clusters based on the current centroids (2) choosing centroids (points which are the center of a cluster) based on the current assignment of data points to clusters.

4.1 Selecting K

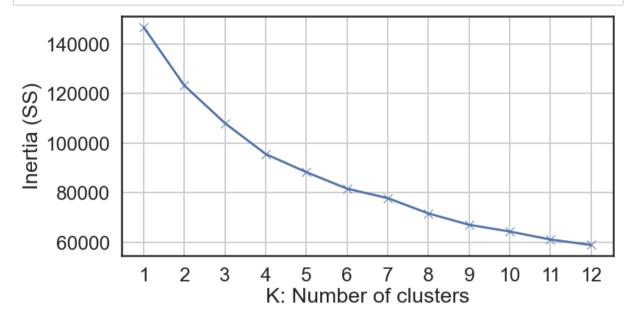
The Elbow Method is one of the most popular methods to determine this optimal value of k. The idea behind the elbow method is to identify the value of k where the score begins to decrease most rapidly before the Inertia curve reaches a plateau. Inertia is the sum of squared distances of samples to their closest cluster center.

Another method is using the Silhouette score. The silhouette value for every data point is a measure of how similar an object is to its own cluster compared to other clusters. The silhouette ranges from -1 to +1, where a high value indicates that the object is well matched to its own cluster and poorly matched to neighboring clusters. The cluster number with the maximum average Silhouette score would be the optimum one. In this problem, Silhouette scores for clusters between 2 to 13 are all close and vary between 0.2 to 0.24, so there is no real winner.

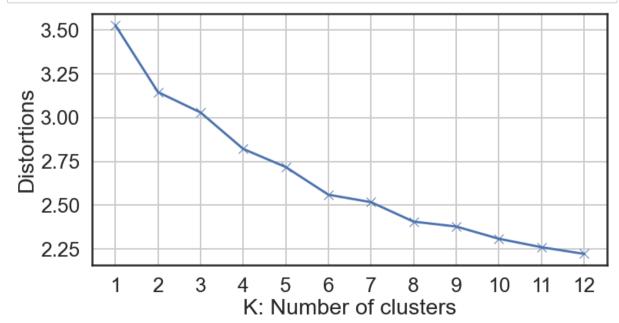
I selected k=4 based on the elbow method and observing a decrease in the Inertia slope after 4 clusters. However, the elbow does not have a sharp bend that we would like to see in the inertia plots. Therefore, I plan to use another clustering algorithm later that could work better for this data.

```
In [17]:
          🔰 ## Calculating Inertia (sum of squared distances from the cluster centers) as a function
             SS = []
             D = []
             DB = []
             SIL = []
             for k in range(1, 13):
                 model = KMeans(n_clusters=k, init="random", random_state=0)
                 model.fit(X std)
                 clusters = model.labels_
                 SS.append(model.inertia )
                 D.append(
                     sum(np.min(cdist(X_std, model.cluster_centers_, "euclidean"), axis=1))
                     / X std.shape[0]
                 if k >= 2:
                     SIL.append(silhouette score(X std, clusters))
```

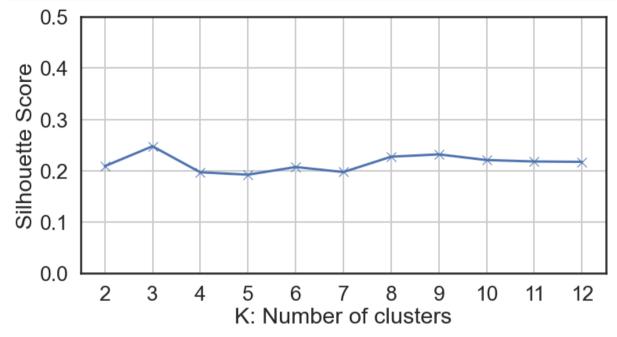
In [18]: ## Plotting Inertia vs number of clusters
fig, ax = plt.subplots(figsize=(12, 6))
plt.plot(range(1, 13), SS, "bx-")
plt.xlabel("K: Number of clusters")
plt.xticks(range(1, 13))
plt.ylabel("Inertia (SS)")
plt.grid()



In [19]: ## Plotting Distortion vs number of clusters
Distortion: It is calculated as the average of the squared distances from the cluster
fig, ax = plt.subplots(figsize=(12, 6))
plt.plot(range(1, 13), D, "bx-")
plt.xlabel("K: Number of clusters")
plt.xticks(range(1, 13))
plt.ylabel("Distortions")
plt.grid()



```
In [20]: ## Plotting Silhouette Score vs number of clusters
fig, ax = plt.subplots(figsize=(12, 6))
plt.plot(range(2, 13), SIL, "bx-")
plt.xlabel("K: Number of clusters")
plt.xticks(range(2, 13))
plt.ylabel("Silhouette Score")
plt.ylim((0, 0.5))
plt.grid()
```



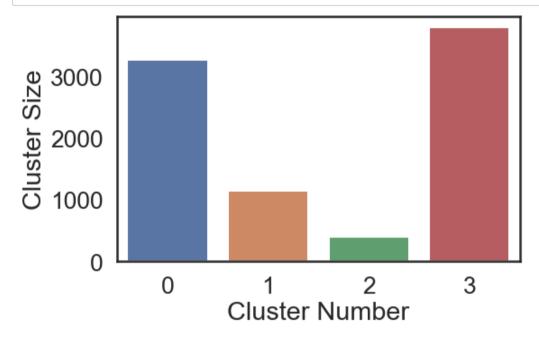
```
In [21]:
          ## I have selected k=4 based on the elbow method
             ## Cluster sizes
             k = 4
             model = KMeans(n_clusters=k, random_state=1)
             model.fit(X_std)
             ## Counting the number of units in each cluster
             # labels = model.predict(X_std)
             # counter = {}
             # for label in labels: # or use scipy.stats.itemfreq
                   if label not in counter:
             #
                       counter[label] = 1
             #
                   else:
             #
                       counter[label] += 1
             # fig, ax = plt.subplots(figsize=(8, 5))
             # plt.bar(counter.keys(), counter.values())
             # plt.xlabel("Cluster Number")
             # plt.ylabel("Cluster Size")
             # plt.xticks(range(0, k));
```

Out[21]: KMeans(n_clusters=4, random_state=1)

4.2 Comparing Clusters

```
In [22]: ## Labeling the rows with cluster numbers
kmeans = KMeans(n_clusters=4, init="random", random_state=0).fit(X_std)
df["cluster"] = kmeans.labels_
```

```
In [23]: | ## Counting the number of units in each cluster
fig, ax = plt.subplots(figsize=(8, 5))
sns.countplot(x='cluster', data=df)
plt.xlabel("Cluster Number")
plt.ylabel("Cluster Size");
```



```
In [24]: ## Rename the clusters to make comparison easier, start the numbering from one not zero
def cluster_name_changer(x):
    dic = {0: 2, 3: 1, 1: 3, 2: 4}
    return dic[x]

df["cluster"] = df["cluster"].apply(lambda x: cluster_name_changer(x))
```

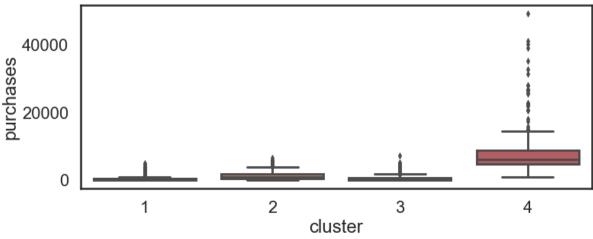
In [25]:

Compare the mean of the clusters
df.groupby("cluster").mean().transpose()

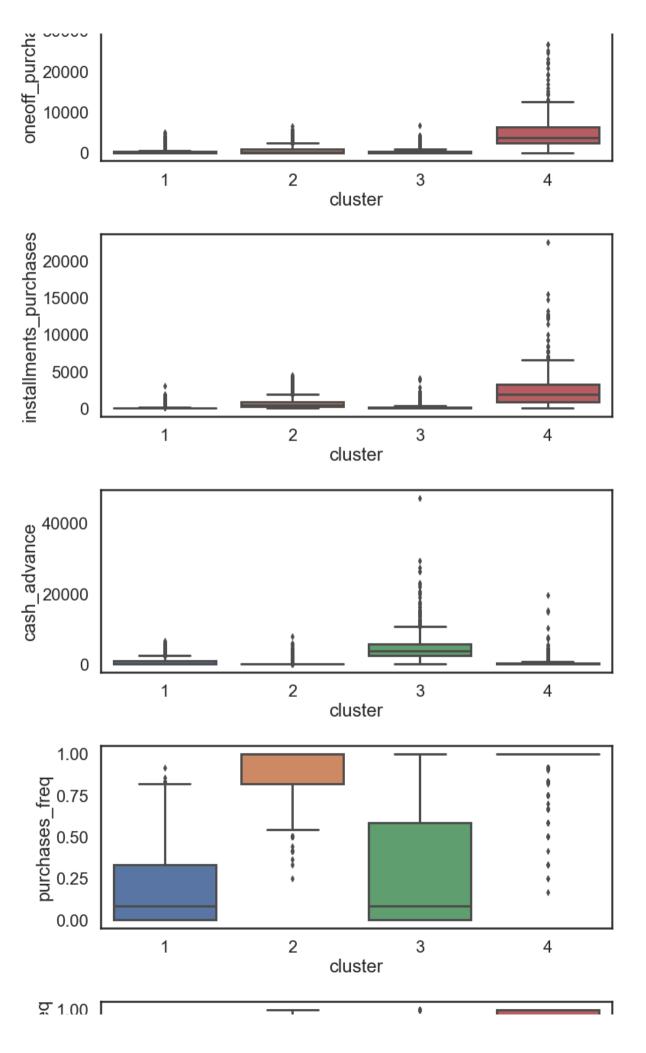
Out[25]:

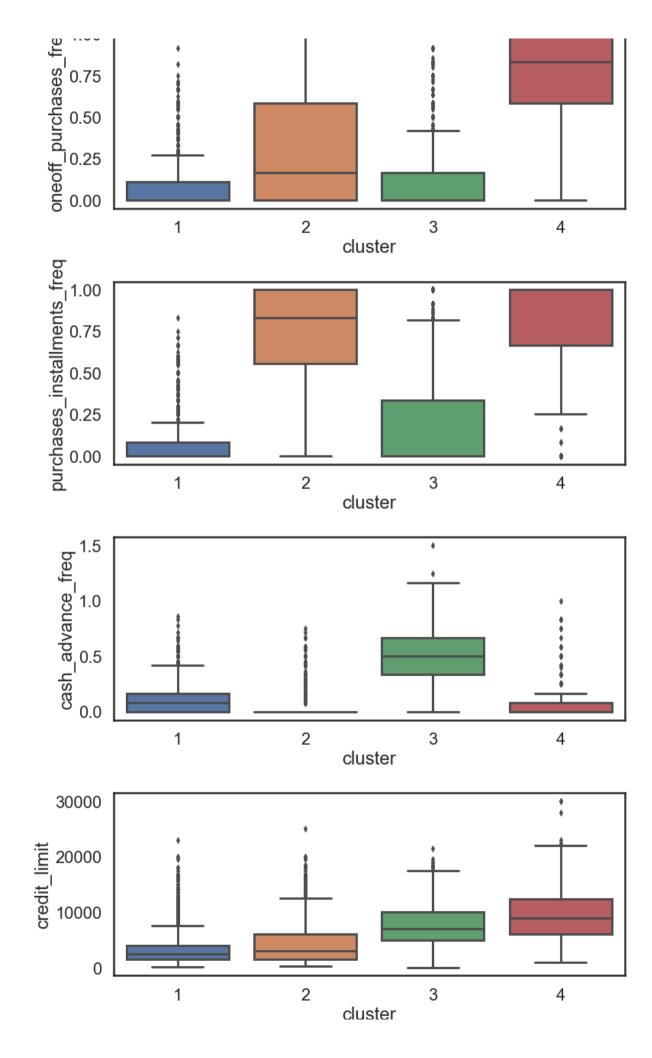
cluster	1	2	3	4
balance	1061.245064	914.398598	4654.668634	3586.147809
balance_frequency	0.818901	0.946186	0.969185	0.986840
purchases	273.943703	1264.766249	504.585671	7816.070736
oneoff_purchases	210.942878	611.185037	319.242797	5194.559518
installments_purchases	63.279848	653.862529	185.430900	2623.034061
cash_advance	606.661232	218.782441	4588.716197	658.230083
purchases_frequency	0.174488	0.887337	0.290148	0.944589
oneoff_purchases_frequency	0.087724	0.302426	0.139707	0.737344
purchases_installments_frequency	0.083122	0.713626	0.187588	0.786971
cash_advance_frequency	0.119162	0.043855	0.487532	0.070831
cash_advance_trx	2.211038	0.816880	14.457143	2.098985
purchases_trx	2.997898	22.507313	7.752381	90.347716
credit_limit	3259.159877	4255.521101	7648.099174	9775.380711
payments	1013.575184	1373.920198	3556.710634	7454.041676
minimum_payments	573.842255	649.503571	2038.647135	2016.140976
prc_full_payment	0.084056	0.274251	0.035357	0.291842
tenure	11.479106	11.601158	11.385281	11.949239

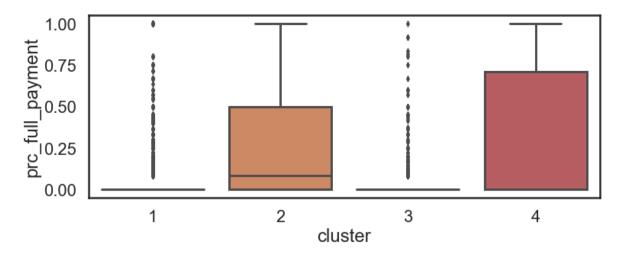
```
In [26]:
          ⋈ ## boxplots
             sns.set_context("poster", font_scale=1)
             cols_to_plot = [
                 "balance",
                 "purchases",
                 "oneoff_purchases",
                 "installments purchases",
                 "cash advance",
                 "purchases_frequency",
                 "oneoff_purchases_frequency",
                 "purchases_installments_frequency",
                 "cash_advance_frequency",
                 "credit_limit",
                 "prc_full_payment",
             n = len(cols_to_plot)
             fig, ax = plt.subplots(n, 1, figsize=(12, 6 * n))
             for i in range(n):
                 sns.boxplot(x="cluster", y=cols_to_plot[i], data=df, ax=ax[i])
                 ## shorten the ylabels
                 if cols_to_plot[i][-9:] == "frequency":
                     y_label = cols_to_plot[i][:-9] + "freq"
                     ax[i].set_ylabel(y_label)
             fig.subplots_adjust(hspace=0.4)
                 15000
              balance
                 10000
                   5000
                       0
                                                     2
                                   1
                                                                         3
                                                                                            4
                                                            cluster
```



40000 % 30000







5 Hierarchical Clustering

There are two types of Hierarchical clustering techniques:

- 1. Agglomerative clustering which is a bottom-up approach. Each data point is assumed to be a separate cluster at first. Then the similar clusters are iteratively combined.
- 2. Divisive clustering which is a top down approach. We start with one giant cluster including all data points. Then the data points are separated into different clusters. This method is less popular.

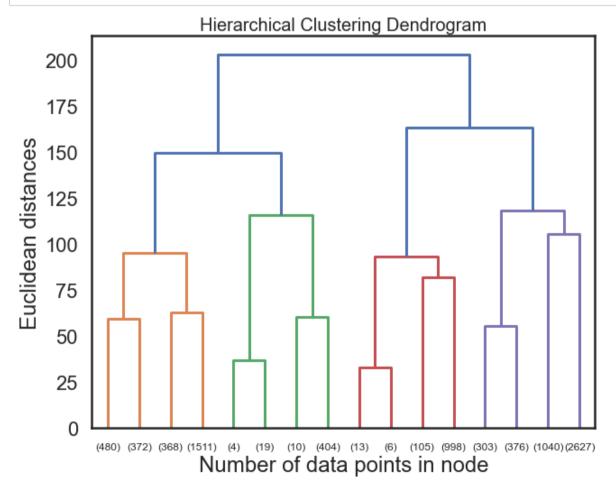
How do the algorithms identify closest clusters? There are a few methods to measure the similarity. Ward's linkage is one of the popular ones. In general "linkage" specifies how the distance between two clusters is calculated. Ward's linkage minimizes the within variance of the clusters being merged. Least increase in total variance around cluster centroids is aimed. In K-means we were trying to minimize the sum of squared distances from the cluster centers (inertia) to plot our elbow method chart, here it's almost the same; however, instead of minimizing inertia we are minimizing the within-cluster variance.

Here I will use Agglomerative clustering with Ward's linkage.

5.1 Building a agglomerative clustering model

Out[27]: AgglomerativeClustering(distance_threshold=0, n_clusters=None)

```
In [28]:
          🔰 ## A Dendrogram is a tree-like diagram that records the sequences of merges or splits.
             ## Create linkage matrix and then plot the dendrogram
             def plot dendrogram(model, **kwargs):
                 # create the counts of samples under each node
                 counts = np.zeros(model.children_.shape[0])
                 n samples = len(model.labels )
                 for i, merge in enumerate(model.children ):
                     current count = 0
                     for child idx in merge:
                         if child idx < n samples:</pre>
                             current_count += 1 # leaf node
                         else:
                             current count += counts[child idx - n samples]
                     counts[i] = current_count
                 linkage_matrix = np.column_stack([model.children_, model.distances_,
                                                    counts]).astype(float)
                 # Plot the corresponding dendrogram
                 dendrogram(linkage matrix, **kwargs)
             ## Plot the top 3 levels of the dendrogram
             plt.figure(figsize = (10,8))
             plot_dendrogram(hc, truncate_mode='level', p=3)
             plt.title('Hierarchical Clustering Dendrogram', size = 20)
             plt.xlabel("Number of data points in node") # (or index of point if no parenthesis)
             plt.ylabel('Euclidean distances');
```



5.2 Selecting the number of clusters and comparison

Dendrograms helps in showing progressions as clusters are merged. It also demonestrates how each cluster is composed of its child nodes. From the dendrogram we can realize that a good candidate for the number of clusters is four and that two of the clusters (red and orange) have better seperation from the rest compared to the other two. In general the separation between the four clusters is not as much as we would like since the amount of the jump in the Euclidean distances by merging the lower level clusters is not very large.

```
In [29]:
          ## Selecting 4 clusters
             hc4 = AgglomerativeClustering(n_clusters=4,
                                               affinity='euclidean',
                                               linkage='ward')
             hc4.fit_predict(X_std)
             df['h_cluster'] = hc4.labels_
          ## Rename the clusters to make comparison easier, start the numbering from one not zero
In [30]:
             def cluster_name_changer(x):
                 dic = \{0: 1, 3: 2, 1: 4, 2: 3\}
                 return dic[x]
             df['h_cluster'] = df['h_cluster'].apply(lambda x: cluster_name_changer(x))
In [31]:
          ## Size of the clusters
             fig, ax = plt.subplots(figsize=(8, 5))
             sns.countplot(x='h_cluster', data=df)
             plt.xlabel("Cluster Number")
             plt.ylabel("Cluster Size");
                 4000
                 3000
                 2000
                  1000
                      0
                                1
                                                                            4
```

Cluster Number

In [32]: ► ## Compare the mean of the clusters ## One quick dirty way to compare these results with Kmeans labels is to look at the las ## which is the avg of previously assigned Kmeans labels for the points inside these new df.groupby('h_cluster').mean().transpose()

Out[32]:

h_cluster	1	2	3	4
balance	979.609234	954.735370	4695.246244	3879.514557
balance_frequency	0.813965	0.975482	0.976833	0.988517
purchases	338.900152	1385.719044	516.485713	6908.217849
oneoff_purchases	209.611742	709.145632	333.451417	4581.572037
installments_purchases	129.627200	676.753047	183.144519	2328.018810
cash_advance	651.253000	286.676850	4167.246654	679.151156
purchases_frequency	0.261787	0.893277	0.259272	0.950319
oneoff_purchases_frequency	0.090834	0.333145	0.141404	0.720803
purchases_installments_frequency	0.169404	0.700948	0.161969	0.807517
cash_advance_frequency	0.119777	0.050301	0.442056	0.078805
cash_advance_trx	2.293833	1.007689	13.413547	1.940503
purchases_trx	4.463185	23.716221	7.625668	84.908467
credit_limit	3234.823232	4430.276955	7805.748663	9467.048055
payments	946.141268	1577.517889	3759.561600	6344.149755
minimum_payments	625.426832	539.832131	2217.096414	1794.436496
prc_full_payment	0.112638	0.283814	0.037234	0.158697
tenure	11.169351	11.939216	11.795009	11.965675
cluster	1.230557	2.036250	2.667558	3.450801

