

# Problem Set #4

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## 1 MSE

### 1.1 Interpretation

In this problem set, after reading, cleaning, and preparing the data, I define two indicator function as follows:

$$\hat{\beta} = \arg \max Q(\beta) = \sum_{y=1}^Y \sum_{b=1}^{M_y-1} \sum_{b'=b+1}^{M_y} \mathbb{1} [f(b, t|\beta) + f(b', t'|\beta) \geq f(b', t|\beta) + f(b, t'|\beta)] \quad (1)$$

$$\begin{aligned} \hat{\beta} &= \arg \max Q(\beta) \\ &= \sum_{y=1}^Y \sum_{b=1}^{M_y-1} \sum_{b'=b+1}^{M_y} \mathbb{1} [f(b, t|\beta) - f(b, t'|\beta) \geq p_{bt} - p_{b't'} \wedge f(b', t'|\beta) - f(b', t|\beta) \geq p_{b't'} - p_{bt}] \end{aligned} \quad (2)$$

where the first one is used for the case of GS algorithm and not considering transfers and the second one is used when we apply the transfers and use BSS algorithm. Also two different payoff functions provided in the prompt are defined as follows:

$$f_m(b, t) = x_{1bm}y_{1tm} + \alpha x_{2bm}y_{1tm} + \beta distance_{btm} + \varepsilon_{btm} \quad (3)$$

$$f_m(b, t) = \delta x_{1bm}y_{1tm} + \alpha x_{2bm}y_{1tm} + \gamma HHI_{tm} + \beta distance_{btm} + \varepsilon_{btm} \quad (4)$$

Estimation results for these four models and algorithms are provided in the results section. We can see that the sign of the coefficients in different models and algorithms are consistent with each other. Specifically, the coefficient for distance is positive in all models meaning that the further away is the target, the more is the payoff. Companies are more interested in expanding their ownership in farther locations.

### 1.2 Results

```
'''
Model 1, without transfers:
[-2.87660604  6.82904737]
Model 2, without transfers:
5 [ 0.6424948 -5.88855166  0.94272259  4.3610747 ]
EModel 1, with transfers:
[-1.81009295  9.45846765]
Model 2, with transfers:
10 [ 2.46167079 -4.62838499 -1.85642906  9.72866347]
'''
```

## 1.3 Executable Script

```
# Mahyar Ebrahimitorki
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import numpy as np
5 import pandas as pd
from pandas import DataFrame as df
import itertools
import scipy.optimize as opt
from scipy.optimize import minimize
10 from scipy.optimize import differential_evolution
import geopy
from geopy import distance

# Read and Clean data
15 df = pd.read_excel("radio_merger_data.xlsx")

df.price = df.price/1000
df.population_target = df.population_target/1000

20 # Defining counterfactual dataset for each year:
df2007 = df[df['year']==2007]
df2008 = df[df['year']==2008]

#The number of all possible combinations:
25 num_comb = len(list(itertools.product(df2007.buyer_id.tolist(), df2007.target_id.
    tolist())) + len(list(itertools.product(df2008.buyer_id.tolist(), df2008.
    target_id.tolist()))))
# Any possible combination (match) between the buyer and target (including real/
    factual and counterfactual data):
B2007 = df2007.loc[:, ['year', 'buyer_id', 'buyer_lat', 'buyer_long', '
    num_stations_buyer', 'corp_owner_buyer']]
B2008 = df2008.loc[:, ['year', 'buyer_id', 'buyer_lat', 'buyer_long', '
    num_stations_buyer', 'corp_owner_buyer']]
T2007 = df2007.loc[:, ['target_id', 'target_lat', 'target_long', 'price', '
    hhi_target', 'population_target']]
30 T2008 = df2008.loc[:, ['target_id', 'target_lat', 'target_long', 'price', '
    hhi_target', 'population_target']]
def cartesian_prod7(B2007, T2007):
    return(B2007.assign(key=1).merge(T2007.assign(key=1), on='key').drop('key', 1))
combinations_2007 = cartesian_prod7(B2007, T2007)
def cartesian_prod8(B2008, T2008):
35     return(B2008.assign(key=1).merge(T2008.assign(key=1), on='key').drop('key', 1))
combinations_2008 = cartesian_prod8(B2008, T2008)

# To drop common observations between "any possible combination of buyer and target"
    (combination_2007 and Combination_2008) and "the factual data in df2007 and
    df2008"
on = ['year', 'buyer_id', 'buyer_lat', 'buyer_long', 'num_stations_buyer', '
    corp_owner_buyer', 'target_id', 'target_lat', 'target_long', 'price', '
    hhi_target', 'population_target']
40 cf2007 = (combinations_2007.merge(df2007[on], on=on, how='left', indicator=True).
    query('_merge == "left_only"').drop('_merge', 1))

on = ['year', 'buyer_id', 'buyer_lat', 'buyer_long', 'num_stations_buyer', '
    corp_owner_buyer', 'target_id', 'target_lat', 'target_long', 'price', '
    hhi_target', 'population_target']
cf2008 = (combinations_2008.merge(df2008[on], on=on, how='left', indicator=True).
    query('_merge == "left_only"').drop('_merge', 1))

45 # Counterfactual dataset is counterfact and factual dataset is df
counterfact = pd.concat([cf2007, cf2008])

# define distance
def dist(d):
50     """
    This function calculates distance between two points in miles
    b_loc = The coordinates for buyer's location
    t_loc = The coordinates for target's location
    """
    b_loc = (d['buyer_lat'], d['buyer_long'])
```

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        t_loc = (d['target_lat'], d['target_long'])
        return distance.distance(b_loc, t_loc).miles

df['distance'] = df.apply(dist, axis=1)
60 counterfact['distance'] = counterfact.apply(dist, axis=1)

#Score function definition for model 1 without transfers
def score1_GS(params, m, n):
    """
65     Payoff function for mergers to be used in the indicator function
    Indicator == 1 if  $f(b,t) + f(b',t') > f(b',t) + f(b,t')$ 
    Indicator == 0 otherwise
    """
    f_b_t = m['num_stations_buyer'] * m['population_target'] + params[0] * m['
        corp_owner_buyer'] * m['population_target'] + params[1] * m['distance']
70 f_cb_ct = n['num_stations_buyer'] * n['population_target'] + params[0] * n['
        corp_owner_buyer'] * n['population_target'] + params[1] * n['distance']
    f_cb_t = n['num_stations_buyer'] * m['population_target'] + params[0] * n['
        corp_owner_buyer'] * m['population_target'] + params[1] * m['distance']
    f_b_ct = m['num_stations_buyer'] * n['population_target'] + params[0] * m['
        corp_owner_buyer'] * n['population_target'] + params[1] * m['distance']
    L = f_b_t + f_cb_ct
    R = f_cb_t + f_b_ct
75 indicator=(L>R)
    total_payoff = indicator.sum()
    return -total_payoff

bounds = [(-10,10), (-10,10)]
80 GS1_dif = differential_evolution(score1_GS, bounds, args=(df, counterfact), strategy
    ='best1bin', maxiter=10000)

def score2_GS(params, m, n):
    """
85     Payoff function for mergers to be used in the indicator function
    Indicator == 1 if  $f(b,t) + f(b',t') > f(b',t) + f(b,t')$ 
    Indicator == 0 otherwise
    """
    f_b_t = params[0] * m['num_stations_buyer'] * m['population_target'] + params[1]
        * m['corp_owner_buyer'] * m['population_target'] + params[2] * m['
        hhi_target'] + params[3] * m['distance']
90 f_cb_ct = params[0] * n['num_stations_buyer'] * n['population_target'] + params
        [1] * n['corp_owner_buyer'] * n['population_target'] + params[2]*n['
        hhi_target'] + params[3] * n['distance']
    f_cb_t = params[0] * n['num_stations_buyer'] * m['population_target'] + params
        [1] * n['corp_owner_buyer'] * m['population_target'] + params[2] * m['
        hhi_target'] + params[3] * m['distance']
    f_b_ct = params[0] * m['num_stations_buyer'] * n['population_target'] + params
        [1] * n['corp_owner_buyer'] * n['population_target'] + params[2] * m['
        hhi_target'] + params[3] * m['distance']

    L = f_b_t + f_cb_ct
95 R = f_cb_t + f_b_ct
    indicator=(L>R)
    total_payoff = indicator.sum()
    return -total_payoff

100 bounds = [(-5,5), (-10,10), (-10, 10), (-10,10)]
    GS2_dif = differential_evolution(score2_GS, bounds, args=(df, counterfact), strategy
        ='best1bin', maxiter=10000)

def score1_BSS(params, m, n):
    """
105     Payoff function for mergers to be used in the indicator function
    Indicator == 1 if  $f(b,t) + f(b',t') > f(b',t) + f(b,t')$ 
    Indicator == 0 otherwise
    """
    f_b_t = m['num_stations_buyer'] * m['population_target'] + params[0] * m['
        corp_owner_buyer'] * m['population_target'] + params[1] * m['distance']
110 f_cb_ct = n['num_stations_buyer'] * n['population_target'] + params[0] * n['
        corp_owner_buyer'] * n['population_target'] + params[1] * n['distance']

```

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f_cb_t = n['num_stations_buyer'] * m['population_target'] + params[0] * n['
corp_owner_buyer'] * m['population_target'] + params[1] * m['distance']
f_b_ct = m['num_stations_buyer'] * n['population_target'] + params[0] * m['
corp_owner_buyer'] * n['population_target'] + params[1] * m['distance']
L1 = f_b_t - f_b_ct
R1 = m['price'] - n['price']
115 L2 = f_cb_ct - f_cb_t
R2 = n['price'] - m['price']
indicator= ((L1 >= R1) & (L2 >= R2))
total_payoff = indicator.sum()
120 return -total_payoff

bounds = [(-5,5), (-10,10)]
BSS1_dif = differential_evolution(score1_BSS, bounds, args=(df, counterfact),
strategy='best1bin', maxiter=10000)

def score2_BSS(params, m, n):
125 """
Payoff function for mergers to be used in the indicator function.
Indicator == 1 if f(b,t) + f(b',t') > f(b',t) + f(b,t')
Indicator == 0 otherwise.
"""
130 f_b_t = params[0] * m['num_stations_buyer'] * m['population_target'] + params[1]
* m['corp_owner_buyer'] * m['population_target'] + params[2] * m['
hhi_target'] + params[3] * m['distance']
f_cb_ct = params[0] * n['num_stations_buyer'] * n['population_target'] + params
[1] * n['corp_owner_buyer'] * n['population_target'] + params[2]*n['
hhi_target'] + params[3] * n['distance']
f_cb_t = params[0] * n['num_stations_buyer'] * m['population_target'] + params
[1] * n['corp_owner_buyer'] * m['population_target'] + params[2] * m['
hhi_target'] + params[3] * m['distance']
f_b_ct = params[0] * m['num_stations_buyer'] * n['population_target'] + params
[1] * n['corp_owner_buyer'] * n['population_target'] + params[2] * m['
hhi_target'] + params[3] * m['distance']

135 L1 = f_b_t - f_b_ct
R1 = m['price'] - n['price']
L2 = f_cb_ct - f_cb_t
R2 = n['price'] - m['price']
indicator= ((L1 >= R1) & (L2 >= R2))
140 total_payoff = indicator.sum()
return -total_payoff

bounds = [(-5,5), (-10,10), (-10, 10), (-10,10)]
BSS2_dif = differential_evolution(score2_BSS, bounds, args=(df, counterfact),
strategy='best1bin', maxiter=10000)
145
print('Model 1, without transfers: \n', GS1_dif.x)
print('Model 2, without transfers: \n', GS2_dif.x)
print('EModel 1, with transfers: \n', BSS1_dif.x)
print('Model 2, with transfers: \n', BSS2_dif.x)

```