Anticorrelated Emission of High Harmonics and Fast Electron Beams From Plasma Mirrors

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We report for the first time on the anticorrelated emission of high-order harmonics and energetic electron beams from a solid-density plasma with a sharp vacuum interface—plasma mirror—driven by an intense ultrashort laser pulse. We highlight the key role played by the nanoscale structure of the plasma surface during the interaction by measuring the spatial and spectral properties of harmonics and electron beams emitted by a plasma mirror. We show that the nanoscale behavior of the plasma mirror can be controlled by tuning the scale length of the electron density gradient, which is measured *in situ* using spatial-domain interferometry.

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Over the past 30 years, solid-density plasmas driven by intense femtosecond pulses, so-called plasma mirrors, have been successfully tested as a source of high-order harmonics and attosecond extreme ultraviolet (XUV) pulses in a number of experiments [1–10], where the laser intensity typically exceeds a few 10¹⁴ W/cm². Other experiments have shown it is also possible to accelerate energetic electrons from plasma mirrors for intensities above 10¹⁶ W/cm² [11–13]. Attempting to understand each of these experimental observations invariably points to the key role played by the plasma-vacuum interface during the interaction both on the nanoscale spatially and on the sublaser-cycle scale temporally [14,15].

It is commonly assumed that the electron density at the plasma mirror surface decreases exponentially from solid to vacuum over a distance L_q , also called the density gradient. When the laser pulse reflects on this plasma mirror, for every oscillation of the laser field, some electrons are driven towards vacuum and sent back to the plasma [16,17]. These bunches of so-called Brunel electrons [18] impulsively excite collective high-frequency plasma oscillations in the density gradient that lead to the emission of XUV radiation through linear mode conversion [19]. As illustrated in Fig. 1(a), each position x of the plasma behaves as a nanoscale oscillator of frequency $\omega_p(x) = \omega_0 \sqrt{n_e(x)/n_c}$, where ω_0 is the driving laser angular frequency, n_e is the local electron density at position x, and n_c is the critical density. This periodic mechanism, called coherent wake emission (CWE), leads to efficient high-harmonics generation for very short plasma scale lengths, typically $L_q \sim \lambda/100$ [19], even for subrelativistic intensities $a_0 < 1$, where $a_0 = eA_0/mc$ is the normalized vector potential, e and m are the electron charge and mass, and c is the speed of light. However, the efficiency significantly drops for $L_q \gg \lambda/20$ [4,5,19,20]. At higher intensities $a_0 \gg 1$, the relativistic oscillating mirror (ROM) becomes the dominant mechanism for harmonic generation [16,21].

A fraction of electrons do not follow Brunel-like trajectories: they are accelerated in the density gradient towards vacuum and escape the plasma, as illustrated in Fig. 1(b). Depending on the interaction conditions, the final energy and angular spread of these electrons can be influenced by plasma waves below the critical surface [11], interference fields created by the incident and reflected laser beams [13,22,23], betatronlike motion at the plasma surface [24], or even direct laser acceleration in vacuum [25]. Here again, the plasma scale length plays a critical role: enhanced electron generation is observed typically for $0.1 < L_g/\lambda < 1$ [11,13,26] or sometimes even for $L_g/\lambda > 1$ [27–29]. To our knowledge, the anticorrelated

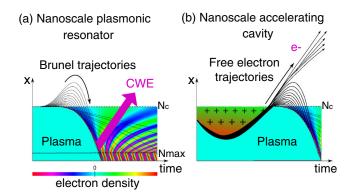


FIG. 1. Diagrams of nanoscale plasma mirror surface structures leading to (a) CWE, where electrons are pulled toward the vacuum and are sent back to the plasma where they excite high-frequency plasma waves, which radiate high-order harmonics (b) electron acceleration on the sub-laser-cycle time scale, where electrons are accelerated in the density gradient and escape from the plasma.

emission of harmonics and fast electrons from plasma mirrors has never been investigated experimentally. In this Letter, through a controlled pump-probe experiment using subrelativistic femtosecond laser pulses, we directly observe the transition from a confined plasma that can efficiently emit laser harmonics to an extended plasma structure that accelerates fast electrons into vacuum up to a few hundred keV energies, where the laser interference field only plays a second role.

The experiment was carried out using the "Salle Noire" laser system at the Laboratoire d'Optique Appliquée (LOA) delivering up to 3 mJ energy, 30 fs pulses at 1 kHz repetition rate with high temporal contrast (>10 10) [30]. The ppolarized pulses are focused down to 1.7 µm FWHM spot size onto an optically flat fused silica target ($\sim 250n_c$), leading to peak intensities on target $\approx 10^{18} \text{ W/cm}^2$ $(a_0 \approx 0.7)$ for an incidence angle $\theta_L = 49.3^{\circ}$, with high repeatability at 1 kHz [31]. Five percent of the main beam is picked off and focused down to 5 times the main beam spot size on target in order to induce homogeneous plasma expansion at the surface (see also Supplemental Material [32]). The plasma scale length L_g can then be varied by changing the relative delay between this prepulse and the main high-intensity pulse. We use spatial domain interferometry [33] to estimate the plasma expansion velocity c_s and find $c_s = dL_q/dt = 10.8 \pm 1.1$ nm/ps for a prepulse intensity of $\approx 3.5 \times 10^{14} \text{ W/cm}^2$ ($a_0 \approx 0.013$).

Harmonics emitted in the specular direction are sent into a homemade XUV spectrometer where the harmonic spectrum is resolved in the horizontal plane and the harmonic beam divergence in the vertical direction using a coupled micro-channel plate and phosphor screen detector. At the same time, a 6×17 cm Lanex screen was positioned 10 cm away, parallel to the target surface without blocking the specular direction. The angular electron emission profile in this geometry was recorded as a function of $\theta \in [-20^{\circ}30^{\circ}]$, the angle with respect to target normal in the plane of incidence, and $\phi \in [-20^{\circ} 20^{\circ}]$, the angle with respect to target normal in the tangential plane. Note that the Lanex screen only detects electrons with energies larger than 150 keV [34]. The Lanex screen could also be replaced by an electron spectrometer for characterizing the electron energy distribution.

Figure 2(a) shows the harmonic spectrum and the electron signal as a function of pump-probe delay, hence the gradient length. The harmonic signal was integrated along the divergence angle. The plasma scale length calculated from the plasma expansion velocity is indicated on the bottom axis. The first striking result is that harmonics are generated efficiently for pump-probe delays below 4 ps, corresponding to $L_g \leq 0.05\lambda$. The spectrum extends up to the plasma frequency cutoff $\omega_c/\omega_0=16$ and its divergence is about 1/10 that of the driving laser beam, which is the typical signature of CWE [20]. The plasma frequency cutoff confirms that Brunel electrons can

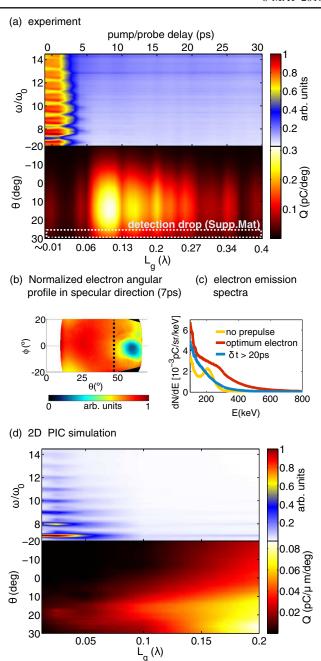


FIG. 2. (a) Experimental harmonic spectra and electron angular emission profiles as a function of pump-probe delay (top axis) between the prepulse and the main pulse. The electron signal was integrated along the tangential coordinate ϕ . The corresponding plasma scale length L_g (bottom axis) was extracted from the plasma expansion velocity $c_s=10.8$ nm/ps measured by spatial domain interferometry [33]. (b) Electron angular distribution when the Lanex is placed perpendicular to the specular direction and after deconvolution (see Supplemental Material [32]). (c) Electron energy spectra for three typical delays. (d) Same as (a) for 2D PIC simulations with $a_0=0.4$ and gradient length $L_g \in [0.01\lambda\,0.2\lambda]$.

efficiently excite collective plasma oscillations and therefore that the initial plasma scale length should be on the order of $L_g \sim 0.01\lambda$ [19] rather then rigorously 0λ . This also indicates that the temporal contrast close to the pulse peak

does not allow us to explore arbitrarily small plasma scale lengths. The drop in CWE efficiency with increasing density gradient has already been observed experimentally and is theoretically predicted to be in the range 0.02 < $L_q/\lambda < 0.1$ [20,36], depending on laser intensity [19]. This can be explained with 1D considerations: the minimum time required to excite plasma waves from the critical surface $x = x_c$ to the location of maximum density x = x_{max} is $\Delta t = (L_q/c) \log(n_{\text{max}}/n_c)$, which should be less than the laser period in order to prevent cycle-to-cycle destructive interferences. For traveling electrons, this limit reads $L_q \leq 0.17\lambda$. In our case, the drop in efficiency occurs at much lower values around $L_q \sim 0.05\lambda$ because the electron perturbation propagates at less than c and the initial perturbation strength (i.e., amplitude of plasma waves) decreases with L_q [19]. The second striking result is that a maximum electron signal is reached for a delay of 8 ps $(L_q \sim 0.1\lambda)$, where harmonic emission is negligible. The ejected electrons form a large spot between 10° and 20° and drop at the edge of the Lanex at $\sim 30^{\circ}$. This drop in signal is a geometrical artifact due to the anisotropic emission of the Lanex screen [34] (see Supplemental Material for details [32]). Figure 2(b) shows the full electron angular distribution for a delay of \sim 7 ps, obtained by moving the Lanex screen perpendicular to the specular direction. The distribution displays a hole close to the specular direction, presumably formed by the ponderomotive force of the reflected laser pulse [13,22,25,37]. Using the Lanex calibration [34], we estimate that the ejected charge reaches a maximum of \sim 11 pC compared to \sim 2 pC at zero delay. Figure 2(c) shows electron spectra respectively without prepulse, for the optimal delay for electron emission, and after 20 ps. Hence, electrons can be effectively accelerated up to ~600 keV at the optimal density gradient.

To summarize, we observe that the emission of harmonics and electrons is anticorrelated when changing the gradient scale length. These experimental results were confronted to 2D particle-in-cell (PIC) simulations, in which a $\lambda = 800$ nm, 30 fs pulse is focused onto an overdense plasma $(n_{\text{max}} = 250n_c)$ with immobile ions. The plasma density decreases exponentially with various scale lengths, from $L_q = 0.01\lambda$ to 0.2λ . The plasma density is cut at $n_b = n_c/5$, so that the plasma boundary is defined by $x_b = -\log 5L_q$. The laser amplitude is $a_0 = 0.4$ and the incidence angle is 45°. A good spatial resolution is required for simulating CWE harmonics, so we use $\delta x = \lambda/420$. In the simulations, electrons are detected at 9λ away from the critical surface and only electrons with energies > 150 keV are detected (as in the experiment). As illustrated in Fig. 2(d), the PIC simulations qualitatively reproduce our experimental observations: the CWE emission efficiency decreases for $L_g > 0.05\lambda$ and the effective ejected electron charge increases up to $\sim 3 \text{ pC} \cdot \mu\text{m}^{-1}$ for $L_a = 0.2\lambda$ compared to 0.12 pC $\cdot \mu \text{m}^{-1}$ when $L_q = 0.01\lambda$ (i.e., ≈ 10 and 0.7 pC, respectively, for a 3.4 μ m spot size FWHM). The electron angular distribution was plotted over the range $\theta \in [-20^{\circ} 30^{\circ}]$ for a direct comparison with experiment. Here again, there is a very good agreement with the experiment, with a large divergence 10 pC beam ejected at ~30° when $L_a \sim 0.2\lambda$. Note that PIC simulations were first performed with the experimental vacuum laser amplitude $a_0 = 0.8$, but a strong harmonic emission attributed to the ROM emission mechanism [20] persisted for longer gradients. These simulations at high intensities suggested a correlation between ROM harmonics and electron ejection, as opposed to the anticorrelation that we observed. In our experiment, ROM emission does not occur and the harmonics are due to CWE. This indicates that the laser intensity at focus is not high enough to support ROM emission [14]. Therefore, in the simulations, the beam spot size was doubled without changing the pulse energy; i.e., a_0 was decreased to 0.4, to reproduce the anticorrelated behavior. Note that our overestimation of the experimental intensity on target may be due to a slight defocusing of the laser on target or debris reducing the overall transmission of the focusing optic, a standard problem with high repetition rate laser-plasma interaction experiments using tight focusing.

Figure 3 shows a comparison of 2D PIC simulations with a gradient length optimized for harmonic emission $(L_q = \lambda/40)$ and electron emission $(L_q = \lambda/5)$, respectively. In Figs. 3(a) and 3(b), one can clearly see oscillations of the electron surface at the laser period. Strong harmonic generation can be seen in Fig. 3(a). The corresponding electron trajectories are shown in Fig. 3(c), where the xcoordinate (normal to the target) of electrons is plotted along time. For clarity, a single bunch of electrons is represented here, which interacts with the laser around its temporal maximum (t = 22T, where T is the optical period) in the center of the interference pattern. One can clearly see Brunel-like trajectories: electrons make a short excursion in vacuum before being driven back to the plasma where they trigger plasma waves. In Fig. 3(b), the amplitude of these oscillations is greater and layers of electrons are ejected from the plasma surface. The corresponding electron trajectories are plotted in Fig. 3(d). Once again, a bunch of electrons was selected for clarity. A fraction of these electrons (in red) escape from the plasma and propagate into vacuum in the interference pattern with a velocity $\simeq c/2$.

For each laser cycle, the ejection mechanism can be described as follows: (i) the laser electric field pushes electrons inside the plasma, while the heavy ions stay in place, creating a charge separation electrostatic field, i.e., a plasma capacitor which can give potential energy to electrons; (ii) half a cycle later, the laser field changes sign and both the capacitor and the laser electric force pull and accelerate electrons towards vacuum. Assuming that all the electrons originating from x < 0 (where $n = n_c$)

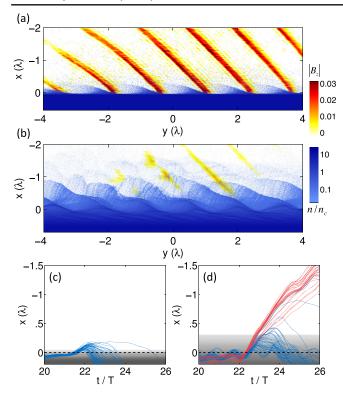


FIG. 3. (a) Snapshot from the 2D PIC simulation for $L_g = \lambda/40$. Blue, electron density (log scale). Yellow-red, reflected harmonic field (a Fourier filter was applied to keep only harmonic orders $\geq 5\omega_0$). The harmonic field comes out as a train of attosecond pulses. (b) Same as (a) for $L_g = \lambda/5$ (same instant, same color scale). (c),(d) Typical electron trajectories for $L_g = \lambda/40$ and $L_g = \lambda/5$, respectively. x is the coordinate normal to the plasma. The gray scale stands for the plasma initial density and the black dotted line (x = 0) shows the position of the critical density. The electrons represented here interact with the laser around its maximum (t = 22T). Red trajectories stand for ejected electrons.

are pushed towards $x \ge 0$, the electrostatic potential of the remaining ions can be calculated using Poisson's equation $\Delta V_P = -n_c/\epsilon_0 e^{x/L_g}$, and reads $V_P = -n_c L_q^2/\epsilon_0$. Therefore, electrons are expected to gain more energy from the plasma for longer gradients. Figure 4(a) shows the spectrum of ejected electrons when they cross the plasma boundary at x_b . The average energy is much higher for longer gradients, thus confirming our predictions. Hence, the plasma serves as an injector of electrons into the reflecting laser [25]. In order to determine whether the electrons are mainly accelerated in the plasma or in the interference pattern, we plot the simulated electron spectra at the plasma border, at 3.3λ and 9λ away from the plasma in Fig. 4(b). Within this range, no net energy gain can be observed from the electromagnetic wave in vacuum; we conclude that the energy gain is mostly due to acceleration inside the plasma gradient. However, farther away from the plasma at 9λ , the electron spectrum broadens and the tail of the distribution reaches 400 keV, which could be the signature of ponderomotive [13,23] and/or stochastic

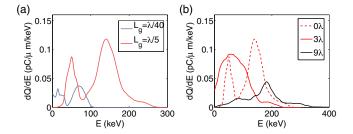


FIG. 4. Simulated ejected electron spectra at the plasma boundary x_b for $L_g = \lambda/40$ (gray line) and $L_g = \lambda/5$ (red line) as they cross the plasma critical surface. (b) Ejected electron spectra for $L_g = \lambda/5$ as they cross the plasma critical surface (dotted line), 3λ and 9λ away from the plasma surface (red and black solid line, respectively).

heating in the interference pattern [38]. The formation of a hole in the experimental electron angular emission profile [see Fig. 2(b)] and the absence of a beaming as seen in Ref. [25] are more evidence that the interaction between the accelerated electrons and the laser is purely ponderomotive. Finally, from simulations and experiments, we also conclude that for $a_0 < 1$ and $L_g \sim 0.1\lambda$ electrons cannot be accelerated by plasma waves related to the CWE mechanism, as suggested in Ref. [11], otherwise, electron and harmonic emission would be optimal simultaneously.

To conclude, we observe for the first time the transition from high-harmonic emission to fast electron ejection as the electron density gradient increases at the surface of a plasma mirror driven at subrelativistic laser intensity. Our measurements reveal that both processes cannot occur simultaneously for the same density gradient. For sharp gradients ($L_a < 0.05\lambda$), electrons drive oscillations in a confined plasma, leading to efficient coherent harmonic emission in their wake. For softer gradients, electrons can be efficiently accelerated out of the plasma by the spacecharge field created for $L_q \sim 0.1\lambda$. Although the interaction with the reflected laser field thermalizes the electron population and reshapes the spatial emission profile via ponderomotive interactions, most of the acceleration occurs inside the plasma density gradient. As the gradient length increases by ~40 nm, the plasma mirror behavior switches from a collection of efficient XUV resonators to a nanoscale electron accelerator.

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