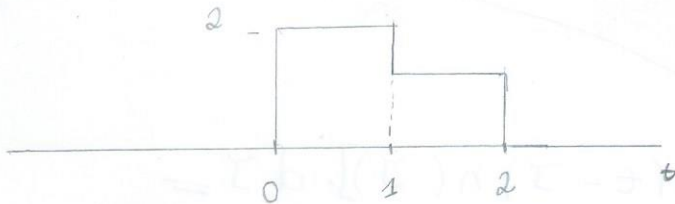


② d) Convolução

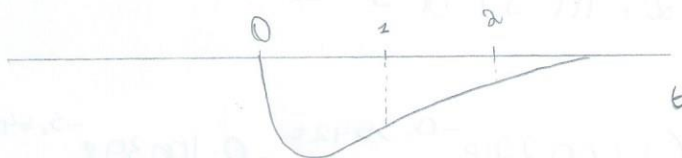
$$\int_{-\infty}^{\infty} [u(t-\tau) \cdot h(\tau)] \cdot d\tau \quad ; \text{ Onde}$$

Propriedade
comutativa

$u(t)$



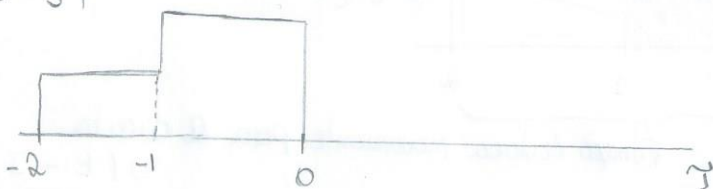
$h(t)$



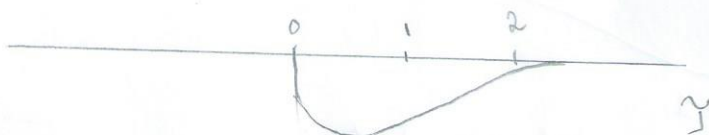
→ Podemos para o domínio τ

A REFLEXÃO DO GRÁFICO ACONTECE SUSTAMENTE PELO $(+ - \tau)$

$u(t-\tau)$

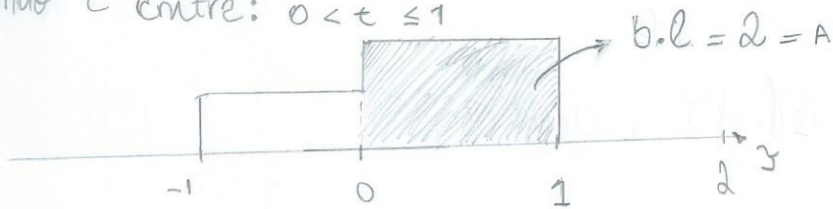


$h(\tau)$



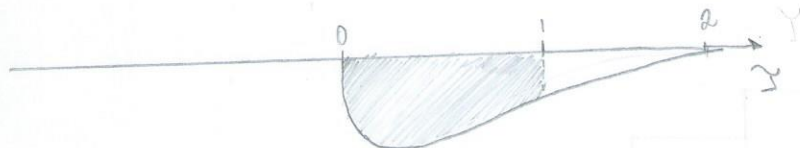
→ Vamos ver o caso $0 < t \leq 1$

→ Variando t entre: $0 < t \leq 1$



Função que desloca para a direita (justamente por $u(t-z)$)

VARIANDO



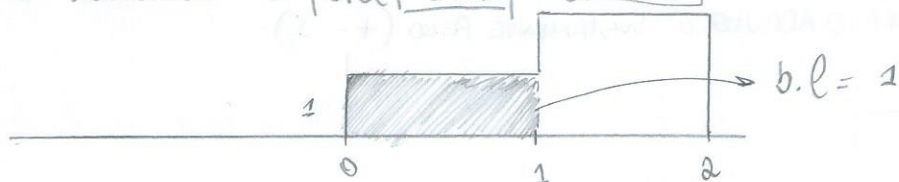
$$\int_0^t \underbrace{[u(t-z) h(z)]}_2 \cdot dz =$$

integral utilizada na
convolução →

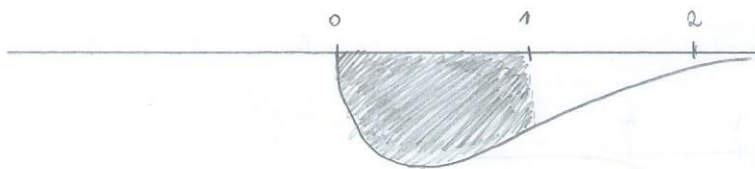
$$\int_0^t 2 \cdot h(z) \cdot dz =$$

$$y_1 = 2 \cdot (1.60022e^{-0.3542t} - 0.10039e^{-5.6457t} - 1.4998)$$

→ Variando t para $t > 1$ e $t \leq 2$



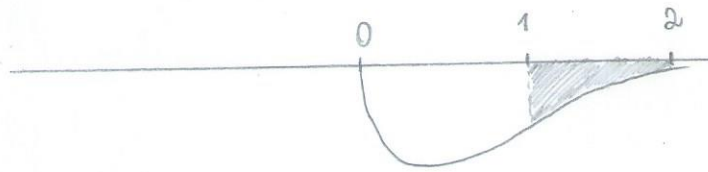
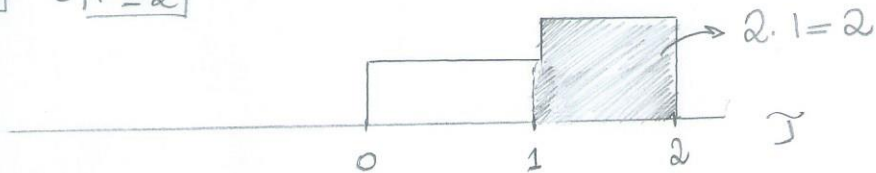
Função desloca novamente para a direita
 $u(t-z)$, onde
 $t > 1$



$$\int_0^{t-1} 1 \cdot h(z) \cdot dz =$$

$$y_2 = 1 \cdot (1.60022e^{-0.3542(t-1)} - 0.10039e^{-5.6457(t-1)} - 1.4998)$$

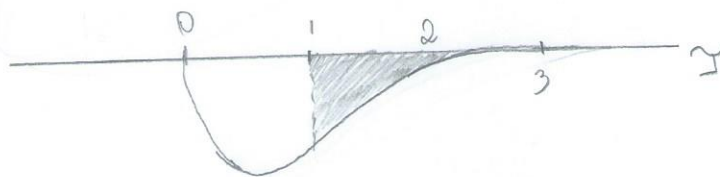
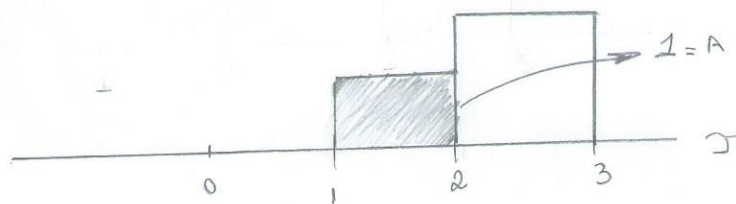
Ainda para $t > 1$ e $t \leq 2$



$$\int_{t-1}^t 2 \cdot h(\tau) \cdot d\tau =$$

$$y_3 = 2(1.60022(e^{-0.3542t} - e^{-0.3542(t-1)}) - 0.10039(e^{-5.6457t} - e^{-5.6457(t-1)}))$$

$$1 \leq t < \infty$$



$$\int_{t-2}^{t-1} 1 \cdot h(\tau) \cdot d\tau =$$

$$y_4 = 1.60022(e^{-0.3542 \cdot (t-1)} - e^{-0.3542 \cdot (t-2)}) - 0.10039(e^{-5.6457(t-1)} - e^{-5.6457 \cdot (t-2)})$$

ou seja:

$$y_{cdc} = y_1 * (u(t) - u(t-1)) + y_2 * (u(t-1) - u(t-2)) + y_3 * (u(t-1)) + y_4 * u(t-2)$$