

Test Exercise 3

April 10, 2018

This is a IPython notebook that contains both the answers and the corresponding code for the problems in Test Exercise 3. All code is written in Python 3 and the text is generated using Markdown.

```
In [1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import statsmodels.api as sm
sns.set_style('whitegrid')
%matplotlib inline
```

```
/anaconda/envs/research/lib/python3.5/site-packages/statsmodels/compat/pandas.py:56: FutureWarning
from pandas.core import datetools
```

```
In [2]: df = pd.read_excel('_a367fe65dc319a76cea3558922a4174d_TestExer-3-TaylorRule-round1.xls')
```

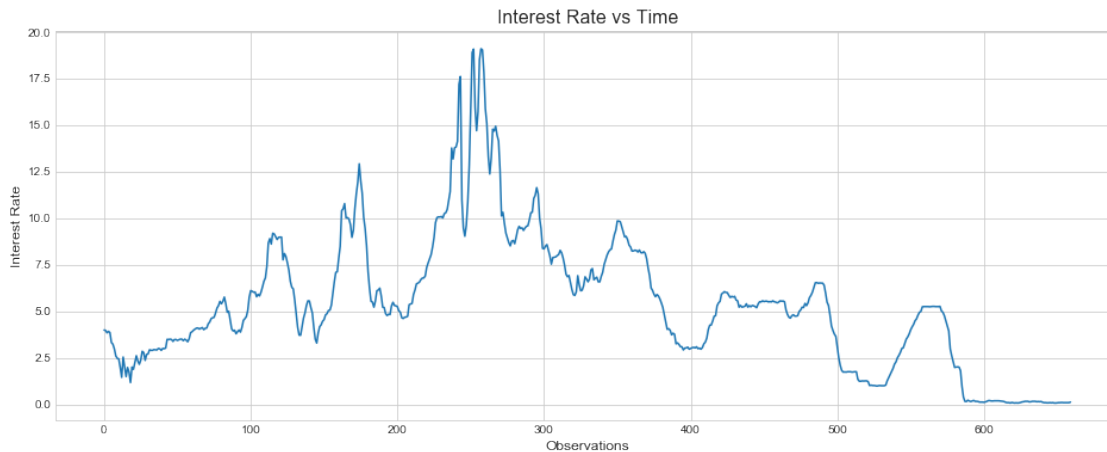
```
In [3]: df.head()
```

```
Out[3]:
```

	OBS	INTRATE	INFL	PROD	UNEMPL	COMPRI	PCE	PERSINC	\
0	1960:1	3.99	1.24095	10.03653	3.41845	7.95262	5.70962	1.68419	
1	1960:2	3.97	1.41379	6.96248	3.46575	-8.55856	5.06452	1.33094	
2	1960:3	3.84	1.51881	4.49681	2.71993	-16.83599	5.55733	0.89195	
3	1960:4	3.92	1.93237	1.50624	2.79820	-5.03145	7.77351	0.67636	
4	1960:5	3.85	1.82507	-0.11398	1.72552	-12.44240	4.39179	0.33667	

	HOUST
0	-11.88896
1	-9.83803
2	-31.54321
3	-18.93082
4	-15.15354

```
In [4]: plt.figure(figsize=(16,6))
plt.plot(df['INTRATE'])
plt.title('Interest Rate vs Time', fontsize=16)
plt.xlabel('Observations', fontsize=12)
plt.ylabel('Interest Rate', fontsize=12);
```



```
In [5]: df['INTRATE_diff'] = df['INTRATE'].diff()
```

```
In [6]: df.head()
```

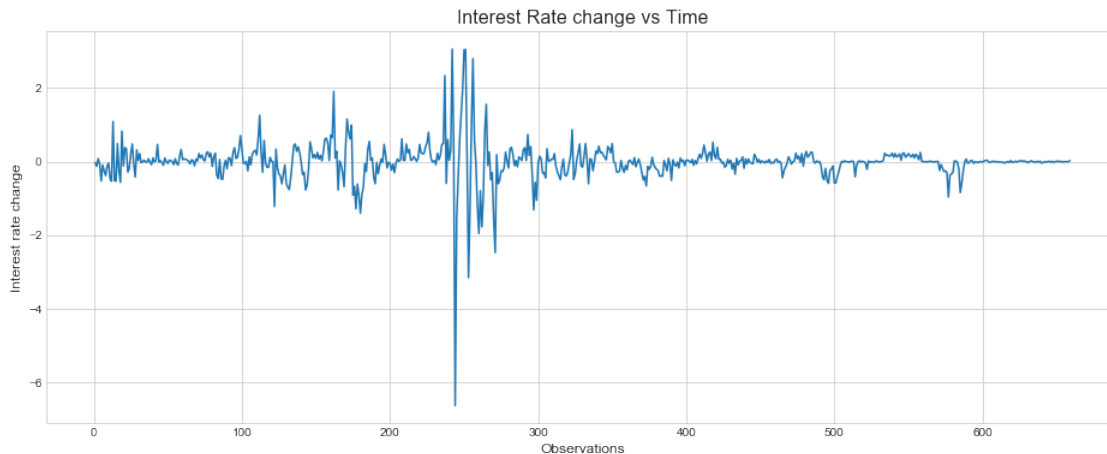
```
Out[6]:
```

	OBS	INTRATE	INFL	PROD	UNEMPL	COMPRI	PCE	PERSINC	\
0	1960:1	3.99	1.24095	10.03653	3.41845	7.95262	5.70962	1.68419	
1	1960:2	3.97	1.41379	6.96248	3.46575	-8.55856	5.06452	1.33094	
2	1960:3	3.84	1.51881	4.49681	2.71993	-16.83599	5.55733	0.89195	
3	1960:4	3.92	1.93237	1.50624	2.79820	-5.03145	7.77351	0.67636	
4	1960:5	3.85	1.82507	-0.11398	1.72552	-12.44240	4.39179	0.33667	

	HOUST	INTRATE_diff
0	-11.88896	NaN
1	-9.83803	-0.02
2	-31.54321	-0.13
3	-18.93082	0.08
4	-15.15354	-0.07

0.0.1 Check for stationarity

```
In [7]: plt.figure(figsize=(16,6))
plt.plot(df['INTRATE_diff'])
plt.title('Interest Rate change vs Time', fontsize=16)
plt.xlabel('Observations', fontsize=12)
plt.ylabel('Interest rate change', fontsize=12);
```



The data distribution appears to be stationary with a few deviations around observations 225 - 275.

1 Part (a)

The AIC and BIC scores increase on dropping COMMPRI. So, we keep COMMPRI in the model and the final model contains 5 explanatory variables.

INFL, COMMPRI, PCE, PERSINC, HOUST

```
In [8]: X = pd.concat([df['INFL'], df['PROD'], df['UNEMPL'], df['COMMPRI'], df['PCE'], df['PERSINC'], df['HOUST']])
        y = df['INTRATE']
        X = sm.add_constant(X)
        model = sm.OLS(y, X).fit()
        print(model.summary())
```

OLS Regression Results

=====						
Dep. Variable:	INTRATE		R-squared:	0.639		
Model:	OLS		Adj. R-squared:	0.635		
Method:	Least Squares		F-statistic:	164.5		
Date:	Tue, 10 Apr 2018		Prob (F-statistic):	1.64e-139		
Time:	00:08:18		Log-Likelihood:	-1449.2		
No. Observations:	660		AIC:	2914.		
Df Residuals:	652		BIC:	2950.		
Df Model:	7					
Covariance Type:	nonrobust					
=====						
	coef	std err	t	P> t	[0.025	0.975]

const	-0.2212	0.245	-0.903	0.367	-0.702	0.260
INFL	0.6961	0.062	11.185	0.000	0.574	0.818
PROD	-0.0577	0.040	-1.447	0.148	-0.136	0.021

UNEMPL	0.1025	0.097	1.059	0.290	-0.088	0.292
COMPRI	-0.0055	0.003	-1.857	0.064	-0.011	0.000
PCE	0.3444	0.069	4.958	0.000	0.208	0.481
PERSINC	0.2470	0.061	4.077	0.000	0.128	0.366
HOUST	-0.0194	0.005	-4.155	0.000	-0.029	-0.010

```
=====
Omnibus:                28.142    Durbin-Watson:                0.101
Prob(Omnibus):           0.000    Jarque-Bera (JB):         41.034
Skew:                    0.365    Prob(JB):                 1.23e-09
Kurtosis:                3.980    Cond. No.                 102.
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

1.0.1 Drop UNEMPL.

```
In [9]: X = pd.concat([df['INFL'], df['PROD'], df['COMPRI'], df['PCE'], df['PERSINC'], df['HOUST']])
        y = df['INTRATE']
        X = sm.add_constant(X)
        model = sm.OLS(y, X).fit()
        print(model.summary())
```

OLS Regression Results

```
=====
Dep. Variable:            INTRATE    R-squared:                0.638
Model:                    OLS        Adj. R-squared:           0.635
Method:                   Least Squares    F-statistic:            191.7
Date:                     Tue, 10 Apr 2018    Prob (F-statistic):      1.99e-140
Time:                     00:08:18          Log-Likelihood:         -1449.7
No. Observations:         660            AIC:                   2913.
Df Residuals:             653            BIC:                   2945.
Df Model:                  6
Covariance Type:          nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.2909	0.236	-1.232	0.218	-0.754	0.173
INFL	0.6933	0.062	11.150	0.000	0.571	0.815
PROD	-0.0255	0.026	-0.989	0.323	-0.076	0.025
COMPRI	-0.0065	0.003	-2.308	0.021	-0.012	-0.001
PCE	0.3686	0.066	5.618	0.000	0.240	0.497
PERSINC	0.2516	0.060	4.162	0.000	0.133	0.370
HOUST	-0.0210	0.004	-4.760	0.000	-0.030	-0.012

```
=====
Omnibus:                21.820    Durbin-Watson:                0.104
Prob(Omnibus):           0.000    Jarque-Bera (JB):         30.851
```

Skew:	0.303	Prob(JB):	2.00e-07
Kurtosis:	3.868	Cond. No.	97.1

=====

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

1.0.2 Drop PROD.

```
In [10]: X = pd.concat([df['INFL'], df['COMMPRI'], df['PCE'], df['PERSINC'], df['HOUST']], axis=1)
y = df['INTRATE']
X = sm.add_constant(X)
model = sm.OLS(y, X).fit()
print(model.summary())
```

```

                                OLS Regression Results
=====
Dep. Variable:                  INTRATE      R-squared:                0.637
Model:                            OLS      Adj. R-squared:            0.635
Method:                 Least Squares      F-statistic:                229.9
Date:                Tue, 10 Apr 2018      Prob (F-statistic):        2.03e-141
Time:                  00:08:18      Log-Likelihood:            -1450.2
No. Observations:                660      AIC:                        2912.
Df Residuals:                    654      BIC:                        2939.
Df Model:                          5
Covariance Type:                nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.2401	0.230	-1.042	0.298	-0.692	0.212
INFL	0.7175	0.057	12.555	0.000	0.605	0.830
COMMPRI	-0.0075	0.003	-2.841	0.005	-0.013	-0.002
PCE	0.3405	0.059	5.756	0.000	0.224	0.457
PERSINC	0.2402	0.059	4.048	0.000	0.124	0.357
HOUST	-0.0205	0.004	-4.678	0.000	-0.029	-0.012

```

=====
Omnibus:                    23.848      Durbin-Watson:                0.100
Prob(Omnibus):              0.000      Jarque-Bera (JB):             31.255
Skew:                      0.354      Prob(JB):                     1.63e-07
Kurtosis:                   3.797      Cond. No.:                    94.1
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

1.0.3 Drop COMMPRI.

```
In [11]: X = pd.concat([df['INFL'], df['PCE'], df['PERSINC'], df['HOUST']], axis=1)
        y = df['INTRATE']
        X = sm.add_constant(X)
        model = sm.OLS(y, X).fit()
        print(model.summary())
```

```

                        OLS Regression Results
=====
Dep. Variable:          INTRATE      R-squared:                0.633
Model:                  OLS          Adj. R-squared:            0.631
Method:                 Least Squares  F-statistic:              282.3
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):       6.18e-141
Time:                  00:08:18        Log-Likelihood:           -1454.3
No. Observations:      660            AIC:                     2919.
Df Residuals:          655            BIC:                     2941.
Df Model:               4
Covariance Type:       nonrobust
=====
               coef      std err          t      P>|t|      [0.025      0.975]
-----
const         -0.2136      0.231      -0.923      0.356      -0.668      0.241
INFL           0.7448      0.057     13.149      0.000       0.634      0.856
PCE            0.3110      0.059      5.311      0.000       0.196      0.426
PERSINC        0.2569      0.059      4.327      0.000       0.140      0.373
HOUST         -0.0215      0.004     -4.893      0.000      -0.030     -0.013
=====
Omnibus:            27.399   Durbin-Watson:           0.100
Prob(Omnibus):      0.000   Jarque-Bera (JB):        33.853
Skew:               0.416   Prob(JB):                4.46e-08
Kurtosis:           3.733   Cond. No.                 62.7
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

2 Part (b)

The AIC and BIC scores increase on adding PROD and UNEMPL. So, we do not include PROD and UNEMPL in the model and the final model contains 5 explanatory variables.

INFL, COMMPRI, PCE, PERSINC, HOUST

The model is same as the one obtained in Part (a).

```
In [12]: def regression(feature_list):
        X = feature_list
        y = df['INTRATE']
```

```

X = sm.add_constant(X)
model = sm.OLS(y, X).fit()
return model

```

```

In [13]: features = [df['INFL'], df['PROD'], df['UNEMPL'], df['COMPRI'], df['PCE'], df['PERSI']

for f in features:
    pd.concat([f], axis=1)
    model = regression(f)
    print("\n#####")
    print("#####")
    print(model.summary())

```

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.560
Model:                  OLS        Adj. R-squared:           0.559
Method:                 Least Squares    F-statistic:            836.6
Date:                   Tue, 10 Apr 2018    Prob (F-statistic):      2.47e-119
Time:                   00:08:18          Log-Likelihood:          -1514.2
No. Observations:       660             AIC:                   3032.
Df Residuals:           658             BIC:                   3041.
Df Model:                1
Covariance Type:        nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	1.6421	0.159	10.352	0.000	1.331	1.954
INFL	0.9453	0.033	28.925	0.000	0.881	1.010

```

=====
Omnibus:                 5.019    Durbin-Watson:           0.063
Prob(Omnibus):            0.081    Jarque-Bera (JB):         4.841
Skew:                     0.193    Prob(JB):                 0.0889
Kurtosis:                 3.166    Cond. No.                  8.46
=====

```

Warnings:

```
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
```

```

#####
#####

```

OLS Regression Results

```

Dep. Variable:          INTRATE    R-squared:          0.000
Model:                  OLS        Adj. R-squared:     -0.001
Method:                 Least Squares    F-statistic:       0.2880
Date:                  Tue, 10 Apr 2018    Prob (F-statistic): 0.592
Time:                  00:08:18    Log-Likelihood:    -1784.8
No. Observations:      660    AIC:               3574.
Df Residuals:          658    BIC:               3583.
Df Model:               1
Covariance Type:       nonrobust

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----
const          5.3942      0.166     32.592      0.000       5.069       5.719
PROD          -0.0159      0.030     -0.537      0.592      -0.074       0.042
=====

Omnibus:                 87.694    Durbin-Watson:           0.022
Prob(Omnibus):            0.000    Jarque-Bera (JB):        136.318
Skew:                     0.880    Prob(JB):                 2.51e-30
Kurtosis:                 4.364    Cond. No.                  6.61
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:          0.059
Model:                  OLS        Adj. R-squared:     0.058
Method:                 Least Squares    F-statistic:       41.57
Date:                  Tue, 10 Apr 2018    Prob (F-statistic): 2.21e-10
Time:                  00:08:18    Log-Likelihood:    -1764.7
No. Observations:      660    AIC:               3533.
Df Residuals:          658    BIC:               3542.
Df Model:               1
Covariance Type:       nonrobust

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----
const          4.5446      0.185     24.571      0.000       4.181       4.908
UNEMPL         0.4525      0.070      6.447      0.000       0.315       0.590
=====

Omnibus:                 152.160    Durbin-Watson:           0.022
Prob(Omnibus):            0.000    Jarque-Bera (JB):        326.769
Skew:                     1.251    Prob(JB):                 1.10e-71
Kurtosis:                 5.372    Cond. No.                  3.82

```


=====

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

=====

Dep. Variable:	INTRATE	R-squared:	0.011
Model:	OLS	Adj. R-squared:	0.010
Method:	Least Squares	F-statistic:	7.562
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	0.00613
Time:	00:08:18	Log-Likelihood:	-1781.2
No. Observations:	660	AIC:	3566.
Df Residuals:	658	BIC:	3575.
Df Model:	1		
Covariance Type:	nonrobust		

=====

	coef	std err	t	P> t	[0.025	0.975]
const	5.4017	0.142	38.159	0.000	5.124	5.680
COMPRI	-0.0115	0.004	-2.750	0.006	-0.020	-0.003

=====

Omnibus:	84.661	Durbin-Watson:	0.025
Prob(Omnibus):	0.000	Jarque-Bera (JB):	129.692
Skew:	0.861	Prob(JB):	6.88e-29
Kurtosis:	4.323	Cond. No.	34.1

=====

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

=====

Dep. Variable:	INTRATE	R-squared:	0.420
Model:	OLS	Adj. R-squared:	0.419
Method:	Least Squares	F-statistic:	476.6
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	6.74e-80
Time:	00:08:18	Log-Likelihood:	-1605.1
No. Observations:	660	AIC:	3214.
Df Residuals:	658	BIC:	3223.
Df Model:	1		
Covariance Type:	nonrobust		

=====

	coef	std err	t	P> t	[0.025	0.975]
const	-0.3361	0.282	-1.194	0.233	-0.889	0.217
PCE	0.8294	0.038	21.832	0.000	0.755	0.904
Omnibus:		102.688	Durbin-Watson:			0.089
Prob(Omnibus):		0.000	Jarque-Bera (JB):			175.000
Skew:		0.961	Prob(JB):			9.98e-39
Kurtosis:		4.635	Cond. No.			19.7

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

Dep. Variable:	INTRATE	R-squared:	0.003
Model:	OLS	Adj. R-squared:	0.002
Method:	Least Squares	F-statistic:	2.106
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	0.147
Time:	00:08:18	Log-Likelihood:	-1783.9
No. Observations:	660	AIC:	3572.
Df Residuals:	658	BIC:	3581.
Df Model:	1		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	5.1245	0.208	24.586	0.000	4.715	5.534
PERSINC	0.1043	0.072	1.451	0.147	-0.037	0.245
Omnibus:		102.087	Durbin-Watson:			0.023
Prob(Omnibus):		0.000	Jarque-Bera (JB):			167.927
Skew:		0.974	Prob(JB):			3.43e-37
Kurtosis:		4.520	Cond. No.			4.59

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:          0.038
Model:                  OLS        Adj. R-squared:       0.037
Method:                 Least Squares  F-statistic:         26.07
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):    4.32e-07
Time:                  00:08:18    Log-Likelihood:      -1772.1
No. Observations:      660        AIC:                 3548.
Df Residuals:          658        BIC:                 3557.
Df Model:               1
Covariance Type:       nonrobust
=====

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----
const          5.4036      0.139      38.956      0.000       5.131       5.676
HOUST         -0.0310      0.006     -5.106      0.000      -0.043      -0.019
=====

```

```

=====
Omnibus:          77.332    Durbin-Watson:          0.034
Prob(Omnibus):    0.000    Jarque-Bera (JB):        117.624
Skew:             0.800    Prob(JB):                2.87e-26
Kurtosis:         4.310    Cond. No.                 23.0
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

2.0.1 Select INFL.

```
In [14]: features = [df['PROD'], df['UNEMPL'], df['COMMPRI'], df['PCE'], df['PERSINC'], df['HOUST']]
```

```

for f in features:
    f1 = pd.concat([df['INFL'], f], axis=1)
    model = regression(f1)
    print("\n#####")
    print("#####")
    print(model.summary())

```

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:          0.575
Model:                  OLS        Adj. R-squared:       0.573
Method:                 Least Squares  F-statistic:         443.9
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):    1.06e-122
Time:                  00:08:18    Log-Likelihood:      -1502.8
=====

```

```

No. Observations:      660    AIC:      3012.
Df Residuals:          657    BIC:      3025.
Df Model:              2
Covariance Type:      nonrobust

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----+-----
const          1.2489      0.176       7.088      0.000       0.903      1.595
INFL           0.9750      0.033      29.785      0.000       0.911      1.039
PROD           0.0947      0.020       4.805      0.000       0.056      0.133
=====

Omnibus:             12.297    Durbin-Watson:           0.065
Prob(Omnibus):       0.002    Jarque-Bera (JB):       12.444
Skew:                0.326    Prob(JB):               0.00199
Kurtosis:            3.168    Cond. No.               11.9
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:      INTRATE    R-squared:           0.592
Model:              OLS       Adj. R-squared:      0.591
Method:             Least Squares    F-statistic:        477.1
Date:               Tue, 10 Apr 2018    Prob (F-statistic): 1.04e-128
Time:               00:08:18    Log-Likelihood:     -1488.9
No. Observations:   660    AIC:                2984.
Df Residuals:       657    BIC:                2997.
Df Model:           2
Covariance Type:    nonrobust

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----+-----
const          1.1230      0.169       6.653      0.000       0.792      1.454
INFL           0.9257      0.032      29.300      0.000       0.864      0.988
UNEMPL         0.3358      0.046       7.235      0.000       0.245      0.427
=====

Omnibus:             37.124    Durbin-Watson:           0.066
Prob(Omnibus):       0.000    Jarque-Bera (JB):       45.150
Skew:                0.529    Prob(JB):               1.57e-10
Kurtosis:            3.722    Cond. No.               9.90
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

```
=====
Dep. Variable:          INTRATE    R-squared:                0.562
Model:                  OLS        Adj. R-squared:             0.560
Method:                 Least Squares    F-statistic:           420.8
Date:                  Tue, 10 Apr 2018    Prob (F-statistic):      2.29e-118
Time:                  00:08:18    Log-Likelihood:         -1512.8
No. Observations:      660    AIC:                    3032.
Df Residuals:          657    BIC:                    3045.
Df Model:               2
Covariance Type:       nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	1.6820	0.160	10.496	0.000	1.367	1.997
INFL	0.9407	0.033	28.715	0.000	0.876	1.005
COMMPRI	-0.0046	0.003	-1.654	0.099	-0.010	0.001

```
=====
Omnibus:                4.941    Durbin-Watson:           0.063
Prob(Omnibus):          0.085    Jarque-Bera (JB):        4.806
Skew:                   0.178    Prob(JB):                0.0904
Kurtosis:               3.219    Cond. No.                 58.7
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

```
=====
Dep. Variable:          INTRATE    R-squared:                0.604
Model:                  OLS        Adj. R-squared:             0.603
Method:                 Least Squares    F-statistic:           501.5
Date:                  Tue, 10 Apr 2018    Prob (F-statistic):      5.86e-133
Time:                  00:08:18    Log-Likelihood:         -1479.1
No. Observations:      660    AIC:                    2964.
Df Residuals:          657    BIC:                    2978.
Df Model:               2
Covariance Type:       nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
--	------	---------	---	------	--------	--------

```

-----
const          0.1012      0.234      0.432      0.666      -0.359      0.561
INFL           0.7158      0.041     17.483      0.000      0.635      0.796
PCE            0.3562      0.041      8.590      0.000      0.275      0.438
=====
Omnibus:                12.948   Durbin-Watson:                0.076
Prob(Omnibus):          0.002   Jarque-Bera (JB):            13.530
Skew:                   0.302   Prob(JB):                    0.00115
Kurtosis:               3.357   Cond. No.                     23.2
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE   R-squared:                0.613
Model:                  OLS       Adj. R-squared:           0.612
Method:                 Least Squares   F-statistic:             519.7
Date:                  Tue, 10 Apr 2018   Prob (F-statistic):      4.67e-136
Time:                  00:08:18   Log-Likelihood:         -1471.9
No. Observations:      660   AIC:                     2950.
Df Residuals:          657   BIC:                     2963.
Df Model:               2
Covariance Type:       nonrobust
=====

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----
const          0.4472      0.195      2.292      0.022      0.064      0.830
INFL           1.0122      0.031     32.156      0.000      0.950      1.074
PERSINC        0.4360      0.046      9.478      0.000      0.346      0.526
=====

```

```

=====
Omnibus:                7.956   Durbin-Watson:                0.102
Prob(Omnibus):          0.019   Jarque-Bera (JB):            8.138
Skew:                   0.221   Prob(JB):                    0.0171
Kurtosis:               3.316   Cond. No.                     11.8
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.560
Model:                  OLS        Adj. R-squared:           0.559
Method:                 Least Squares    F-statistic:              418.6
Date:                  Tue, 10 Apr 2018    Prob (F-statistic):       5.93e-118
Time:                  00:08:18    Log-Likelihood:          -1513.8
No. Observations:      660    AIC:                    3034.
Df Residuals:          657    BIC:                    3047.
Df Model:               2
Covariance Type:       nonrobust
=====

```

```

=====
              coef      std err          t      P>|t|      [0.025      0.975]
-----
const         1.6767        0.163     10.278      0.000         1.356         1.997
INFL           0.9383        0.034     27.934      0.000         0.872         1.004
HOUST        -0.0038        0.004     -0.911      0.362        -0.012         0.004
=====

```

```

=====
Omnibus:                 6.328    Durbin-Watson:           0.063
Prob(Omnibus):           0.042    Jarque-Bera (JB):         6.229
Skew:                    0.208    Prob(JB):                 0.0444
Kurtosis:                 3.229    Cond. No.                  40.5
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

2.0.2 Select PERSINC.

```
In [15]: features = [df['PROD'], df['UNEMPL'], df['COMMPRI'], df['PCE'], df['HOUST']]
```

```

for f in features:
    f1 = pd.concat([df['INFL'], df['PERSINC'], f], axis=1)
    model = regression(f1)
    print("\n#####")
    print("#####")
    print(model.summary())

```

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.613
Model:                  OLS        Adj. R-squared:           0.611
Method:                 Least Squares    F-statistic:              346.0
Date:                  Tue, 10 Apr 2018    Prob (F-statistic):       1.15e-134

```

Time: 00:08:18 Log-Likelihood: -1471.9
 No. Observations: 660 AIC: 2952.
 Df Residuals: 656 BIC: 2970.
 Df Model: 3
 Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]
const	0.4422	0.196	2.257	0.024	0.057	0.827
INFL	1.0130	0.032	32.042	0.000	0.951	1.075
PERSINC	0.4280	0.053	8.030	0.000	0.323	0.533
PROD	0.0064	0.022	0.296	0.768	-0.036	0.049
Omnibus:	8.502		Durbin-Watson:	0.101		
Prob(Omnibus):	0.014		Jarque-Bera (JB):	8.655		
Skew:	0.236		Prob(JB):	0.0132		
Kurtosis:	3.305		Cond. No.	14.8		

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

 #####

OLS Regression Results

Dep. Variable: INTRATE R-squared: 0.617
 Model: OLS Adj. R-squared: 0.615
 Method: Least Squares F-statistic: 351.9
 Date: Tue, 10 Apr 2018 Prob (F-statistic): 3.79e-136
 Time: 00:08:19 Log-Likelihood: -1468.4
 No. Observations: 660 AIC: 2945.
 Df Residuals: 656 BIC: 2963.
 Df Model: 3
 Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]
const	0.4462	0.194	2.298	0.022	0.065	0.828
INFL	0.9916	0.032	30.705	0.000	0.928	1.055
PERSINC	0.3560	0.055	6.480	0.000	0.248	0.464
UNEMPL	0.1425	0.054	2.638	0.009	0.036	0.249
Omnibus:	21.055		Durbin-Watson:	0.091		
Prob(Omnibus):	0.000		Jarque-Bera (JB):	23.143		
Skew:	0.393		Prob(JB):	9.43e-06		
Kurtosis:	3.473		Cond. No.	12.6		

=====

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

=====

Dep. Variable:	INTRATE	R-squared:	0.616
Model:	OLS	Adj. R-squared:	0.614
Method:	Least Squares	F-statistic:	350.3
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	9.54e-136
Time:	00:08:19	Log-Likelihood:	-1469.4
No. Observations:	660	AIC:	2947.
Df Residuals:	656	BIC:	2965.
Df Model:	3		
Covariance Type:	nonrobust		

=====

	coef	std err	t	P> t	[0.025	0.975]
-----	-----	-----	-----	-----	-----	-----
const	0.4837	0.195	2.479	0.013	0.101	0.867
INFL	1.0071	0.031	32.009	0.000	0.945	1.069
PERSINC	0.4413	0.046	9.611	0.000	0.351	0.531
COMMPRI	-0.0059	0.003	-2.257	0.024	-0.011	-0.001

=====

Omnibus:	7.774	Durbin-Watson:	0.101
Prob(Omnibus):	0.021	Jarque-Bera (JB):	8.534
Skew:	0.186	Prob(JB):	0.0140
Kurtosis:	3.415	Cond. No.	76.7

=====

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

=====

Dep. Variable:	INTRATE	R-squared:	0.619
Model:	OLS	Adj. R-squared:	0.618
Method:	Least Squares	F-statistic:	356.0
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	3.77e-137
Time:	00:08:19	Log-Likelihood:	-1466.1
No. Observations:	660	AIC:	2940.
Df Residuals:	656	BIC:	2958.

=====

Df Model: 3
Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]
const	0.0212	0.230	0.092	0.927	-0.431	0.473
INFL	0.8754	0.051	17.224	0.000	0.776	0.975
PERSINC	0.3054	0.060	5.129	0.000	0.188	0.422
PCE	0.1812	0.053	3.412	0.001	0.077	0.285
Omnibus:		9.545	Durbin-Watson:			0.088
Prob(Omnibus):		0.008	Jarque-Bera (JB):			9.664
Skew:		0.260	Prob(JB):			0.00797
Kurtosis:		3.283	Cond. No.			23.9

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

Dep. Variable:	INTRATE	R-squared:	0.617			
Model:	OLS	Adj. R-squared:	0.615			
Method:	Least Squares	F-statistic:	352.4			
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	2.94e-136			
Time:	00:08:19	Log-Likelihood:	-1468.2			
No. Observations:	660	AIC:	2944.			
Df Residuals:	656	BIC:	2962.			
Df Model:	3					
Covariance Type:	nonrobust					
=====						
	coef	std err	t	P> t	[0.025	0.975]

const	0.4830	0.195	2.482	0.013	0.101	0.865
INFL	0.9957	0.032	31.207	0.000	0.933	1.058
PERSINC	0.4588	0.047	9.861	0.000	0.367	0.550
HOUST	-0.0109	0.004	-2.733	0.006	-0.019	-0.003
=====						
Omnibus:	17.329	Durbin-Watson:	0.107			
Prob(Omnibus):	0.000	Jarque-Bera (JB):	20.923			
Skew:	0.303	Prob(JB):	2.86e-05			
Kurtosis:	3.628	Cond. No.	51.9			

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

2.0.3 Select PCE.

```
In [16]: features = [df['PROD'], df['UNEMPL'], df['COMMPRI'], df['HOUST']]
```

```
for f in features:
    f1 = pd.concat([df['INFL'], df['PERSINC'], df['PCE'], f], axis=1)
    model = regression(f1)
    print("\n#####")
    print("#####")
    print(model.summary())
```

```
#####
#####
```

OLS Regression Results

```
=====
Dep. Variable:          INTRATE      R-squared:                0.621
Model:                  OLS          Adj. R-squared:            0.618
Method:                 Least Squares  F-statistic:              268.1
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):       2.50e-136
Time:                  00:08:19        Log-Likelihood:          -1465.0
No. Observations:      660            AIC:                     2940.
Df Residuals:          655            BIC:                     2962.
Df Model:               4
Covariance Type:       nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.0517	0.235	-0.220	0.826	-0.513	0.410
INFL	0.8383	0.056	14.849	0.000	0.727	0.949
PERSINC	0.3199	0.060	5.308	0.000	0.202	0.438
PCE	0.2243	0.060	3.720	0.000	0.106	0.343
PROD	-0.0369	0.025	-1.506	0.133	-0.085	0.011

```
=====
Omnibus:                7.399      Durbin-Watson:           0.093
Prob(Omnibus):           0.025      Jarque-Bera (JB):         7.845
Skew:                   0.193      Prob(JB):                 0.0198
Kurtosis:               3.370      Cond. No.                 26.4
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
#####
```

#####

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.620
Model:                  OLS        Adj. R-squared:           0.618
Method:                 Least Squares    F-statistic:             267.5
Date:                   Tue, 10 Apr 2018    Prob (F-statistic):      3.84e-136
Time:                   00:08:19    Log-Likelihood:         -1465.4
No. Observations:      660    AIC:                    2941.
Df Residuals:          655    BIC:                    2963.
Df Model:               4
Covariance Type:        nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	0.0993	0.239	0.415	0.678	-0.371	0.570
INFL	0.8902	0.052	17.013	0.000	0.787	0.993
PERSINC	0.2890	0.061	4.727	0.000	0.169	0.409
PCE	0.1478	0.060	2.458	0.014	0.030	0.266
UNEMPL	0.0722	0.061	1.184	0.237	-0.047	0.192

```

=====
Omnibus:                15.357    Durbin-Watson:           0.085
Prob(Omnibus):          0.000    Jarque-Bera (JB):        16.112
Skew:                   0.339    Prob(JB):                0.000317
Kurtosis:               3.356    Cond. No.:               25.6
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.625
Model:                  OLS        Adj. R-squared:           0.623
Method:                 Least Squares    F-statistic:             273.2
Date:                   Tue, 10 Apr 2018    Prob (F-statistic):      5.28e-138
Time:                   00:08:19    Log-Likelihood:         -1461.1
No. Observations:      660    AIC:                    2932.
Df Residuals:          655    BIC:                    2955.
Df Model:               4
Covariance Type:        nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
--	------	---------	---	------	--------	--------

const	-0.0211	0.229	-0.092	0.927	-0.471	0.429
INFL	0.8378	0.052	16.156	0.000	0.736	0.940
PERSINC	0.2841	0.060	4.772	0.000	0.167	0.401
PCE	0.2214	0.054	4.082	0.000	0.115	0.328
COMPRI	-0.0085	0.003	-3.173	0.002	-0.014	-0.003

Omnibus:	7.556	Durbin-Watson:	0.087
Prob(Omnibus):	0.023	Jarque-Bera (JB):	7.920
Skew:	0.201	Prob(JB):	0.0191
Kurtosis:	3.356	Cond. No.	90.3

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

#####

OLS Regression Results

Dep. Variable:	INTRATE	R-squared:	0.633
Model:	OLS	Adj. R-squared:	0.631
Method:	Least Squares	F-statistic:	282.3
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	6.18e-141
Time:	00:08:19	Log-Likelihood:	-1454.3
No. Observations:	660	AIC:	2919.
Df Residuals:	655	BIC:	2941.
Df Model:	4		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	-0.2136	0.231	-0.923	0.356	-0.668	0.241
INFL	0.7448	0.057	13.149	0.000	0.634	0.856
PERSINC	0.2569	0.059	4.327	0.000	0.140	0.373
PCE	0.3110	0.059	5.311	0.000	0.196	0.426
HOUST	-0.0215	0.004	-4.893	0.000	-0.030	-0.013

Omnibus:	27.399	Durbin-Watson:	0.100
Prob(Omnibus):	0.000	Jarque-Bera (JB):	33.853
Skew:	0.416	Prob(JB):	4.46e-08
Kurtosis:	3.733	Cond. No.	62.7

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

2.0.4 Select HOUST.

```
In [17]: features = [df['PROD'], df['UNEMPL'], df['COMMPRI']]
```

```
for f in features:
    f1 = pd.concat([df['INFL'], df['PERSINC'], df['PCE'], df['HOUST'], f], axis=1)
    model = regression(f1)
    print("\n#####")
    print("#####")
    print(model.summary())
```

```
#####
#####
```

OLS Regression Results

```
=====
Dep. Variable:          INTRATE      R-squared:                0.635
Model:                  OLS          Adj. R-squared:            0.632
Method:                 Least Squares  F-statistic:              227.5
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):       1.76e-140
Time:                  00:08:19        Log-Likelihood:          -1452.4
No. Observations:      660            AIC:                     2917.
Df Residuals:          654            BIC:                     2944.
Df Model:               5
Covariance Type:       nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.3126	0.237	-1.321	0.187	-0.777	0.152
INFL	0.6940	0.062	11.125	0.000	0.572	0.817
PERSINC	0.2736	0.060	4.569	0.000	0.156	0.391
PCE	0.3692	0.066	5.610	0.000	0.240	0.498
HOUST	-0.0222	0.004	-5.039	0.000	-0.031	-0.014
PROD	-0.0465	0.024	-1.923	0.055	-0.094	0.001

```
=====
Omnibus:                22.145      Durbin-Watson:           0.109
Prob(Omnibus):           0.000      Jarque-Bera (JB):        31.102
Skew:                    0.310      Prob(JB):                1.76e-07
Kurtosis:                 3.865      Cond. No.                 64.7
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
#####
#####
```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.633
Model:                  OLS        Adj. R-squared:           0.630
Method:                 Least Squares  F-statistic:             225.5
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):       1.08e-139
Time:                  00:08:19    Log-Likelihood:          -1454.2
No. Observations:      660        AIC:                     2920.
Df Residuals:          654        BIC:                     2947.
Df Model:               5
Covariance Type:       nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.2333	0.246	-0.949	0.343	-0.716	0.249
INFL	0.7398	0.060	12.235	0.000	0.621	0.859
PERSINC	0.2596	0.060	4.293	0.000	0.141	0.378
PCE	0.3199	0.069	4.610	0.000	0.184	0.456
HOUST	-0.0218	0.005	-4.745	0.000	-0.031	-0.013
UNEMPL	-0.0150	0.063	-0.239	0.811	-0.138	0.108

```

=====
Omnibus:                25.793    Durbin-Watson:           0.102
Prob(Omnibus):          0.000    Jarque-Bera (JB):        31.852
Skew:                   0.398    Prob(JB):                1.21e-07
Kurtosis:               3.724    Cond. No.:               67.3
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.637
Model:                  OLS        Adj. R-squared:           0.635
Method:                 Least Squares  F-statistic:             229.9
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):       2.03e-141
Time:                  00:08:19    Log-Likelihood:          -1450.2
No. Observations:      660        AIC:                     2912.
Df Residuals:          654        BIC:                     2939.
Df Model:               5
Covariance Type:       nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.2401	0.230	-1.042	0.298	-0.692	0.212
INFL	0.7175	0.057	12.555	0.000	0.605	0.830

PERSINC	0.2402	0.059	4.048	0.000	0.124	0.357
PCE	0.3405	0.059	5.756	0.000	0.224	0.457
HOUST	-0.0205	0.004	-4.678	0.000	-0.029	-0.012
COMPRI	-0.0075	0.003	-2.841	0.005	-0.013	-0.002

```
=====
Omnibus:                23.848    Durbin-Watson:                0.100
Prob(Omnibus):          0.000    Jarque-Bera (JB):          31.255
Skew:                   0.354    Prob(JB):                  1.63e-07
Kurtosis:               3.797    Cond. No.                  94.1
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

2.0.5 Select COMPRI.

```
In [18]: features = [df['PROD'], df['UNEMPL']]
```

```
for f in features:
    f1 = pd.concat([df['INFL'], df['PERSINC'], df['PCE'], df['HOUST'], df['COMPRI']],
                    model = regression(f1)
    print("\n#####")
    print("#####")
    print(model.summary())
```

```
#####
#####
```

OLS Regression Results

```
=====
Dep. Variable:          INTRATE    R-squared:                0.638
Model:                  OLS        Adj. R-squared:          0.635
Method:                 Least Squares    F-statistic:            191.7
Date:                   Tue, 10 Apr 2018    Prob (F-statistic):      1.99e-140
Time:                   00:08:19    Log-Likelihood:         -1449.7
No. Observations:       660    AIC:                    2913.
Df Residuals:           653    BIC:                    2945.
Df Model:                6
Covariance Type:        nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.2909	0.236	-1.232	0.218	-0.754	0.173
INFL	0.6933	0.062	11.150	0.000	0.571	0.815
PERSINC	0.2516	0.060	4.162	0.000	0.133	0.370
PCE	0.3686	0.066	5.618	0.000	0.240	0.497

HOUST	-0.0210	0.004	-4.760	0.000	-0.030	-0.012
COMMPRI	-0.0065	0.003	-2.308	0.021	-0.012	-0.001
PROD	-0.0255	0.026	-0.989	0.323	-0.076	0.025

```

=====
Omnibus:                21.820    Durbin-Watson:                0.104
Prob(Omnibus):          0.000    Jarque-Bera (JB):        30.851
Skew:                   0.303    Prob(JB):                2.00e-07
Kurtosis:               3.868    Cond. No.                97.1
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```

#####
#####

```

OLS Regression Results

```

=====
Dep. Variable:          INTRATE    R-squared:                0.637
Model:                  OLS        Adj. R-squared:          0.634
Method:                 Least Squares    F-statistic:            191.3
Date:                   Tue, 10 Apr 2018    Prob (F-statistic):      3.22e-140
Time:                   00:08:19    Log-Likelihood:          -1450.2
No. Observations:       660    AIC:                    2914.
Df Residuals:           653    BIC:                    2946.
Df Model:                6
Covariance Type:        nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.2460	0.245	-1.006	0.315	-0.726	0.234
INFL	0.7161	0.061	11.792	0.000	0.597	0.835
PERSINC	0.2411	0.061	3.985	0.000	0.122	0.360
PCE	0.3431	0.070	4.937	0.000	0.207	0.480
HOUST	-0.0206	0.005	-4.485	0.000	-0.030	-0.012
COMMPRI	-0.0075	0.003	-2.830	0.005	-0.013	-0.002
UNEMPL	-0.0045	0.062	-0.072	0.943	-0.127	0.118

```

=====
Omnibus:                23.442    Durbin-Watson:                0.100
Prob(Omnibus):          0.000    Jarque-Bera (JB):        30.775
Skew:                   0.348    Prob(JB):                2.08e-07
Kurtosis:               3.796    Cond. No.                101.
=====

```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

3 Part (c)

Model using the *Taylor rule of equation*.

Parameters	Model (a)	Taylor rule
R-squared	0.633	0.575
AIC	2919	3012
BIC	2941	3025

Since, the AIC, and the BIC scores of the model in Part (a) are lower than that of Taylor rule, so the model obtained in Part (a) is better. Also, the R-squared of the model in Part (a) is higher.

```
In [19]: X = pd.concat([df['INFL'], df['PROD']], axis=1)
        y = df['INTRATE']
        X = sm.add_constant(X)
        model = sm.OLS(y, X).fit()
        print(model.summary())
```

```

                        OLS Regression Results
=====
Dep. Variable:          INTRATE      R-squared:          0.575
Model:                  OLS          Adj. R-squared:      0.573
Method:                 Least Squares  F-statistic:        443.9
Date:                  Tue, 10 Apr 2018  Prob (F-statistic):  1.06e-122
Time:                  00:08:19        Log-Likelihood:     -1502.8
No. Observations:      660            AIC:                3012.
Df Residuals:          657            BIC:                3025.
Df Model:              2
Covariance Type:       nonrobust
=====
                        coef      std err          t      P>|t|      [0.025      0.975]
-----
const                1.2489        0.176        7.088      0.000        0.903        1.595
INFL                 0.9750         0.033       29.785      0.000        0.911        1.039
PROD                 0.0947         0.020        4.805      0.000        0.056        0.133
=====
Omnibus:              12.297    Durbin-Watson:        0.065
Prob(Omnibus):        0.002    Jarque-Bera (JB):      12.444
Skew:                 0.326    Prob(JB):              0.00199
Kurtosis:             3.168    Cond. No.              11.9
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

4 Part (d)

RESET test

Taking $p = 1$.

The p value of the γ coefficient is 0.112 and hence it is not significant. So we can conclude that H_0 (null hypothesis) is correct. In other words we can consider $\gamma = 0$.

```
In [20]: y_pred = model.predict(X)
         df['y_pred_2'] = y_pred**2

In [21]: X = pd.concat([df['INFL'], df['PROD'], df['y_pred_2']], axis=1)
         y = df['INTRATE']
         X = sm.add_constant(X)
         model = sm.OLS(y, X).fit()
         print(model.summary())
```

```

                        OLS Regression Results
=====
Dep. Variable:          INTRATE      R-squared:                0.576
Model:                  OLS          Adj. R-squared:            0.574
Method:                 Least Squares   F-statistic:              297.5
Date:                  Tue, 10 Apr 2018   Prob (F-statistic):       7.14e-122
Time:                  00:08:19          Log-Likelihood:           -1501.5
No. Observations:      660              AIC:                    3011.
Df Residuals:          656              BIC:                    3029.
Df Model:               3
Covariance Type:       nonrobust
=====

```

	coef	std err	t	P> t	[0.025	0.975]
const	0.9841	0.242	4.065	0.000	0.509	1.459
INFL	1.1650	0.124	9.418	0.000	0.922	1.408
PROD	0.0999	0.020	5.005	0.000	0.061	0.139
y_pred_2	-0.0137	0.009	-1.593	0.112	-0.031	0.003

```
=====
Omnibus:                 10.719   Durbin-Watson:                0.068
Prob(Omnibus):            0.005   Jarque-Bera (JB):           10.755
Skew:                     0.301   Prob(JB):                   0.00462
Kurtosis:                 3.170   Cond. No.                    157.
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

4.0.1 Chow break test

$$F = \frac{(S_0 - S_1 - S_2)/k}{(S_1 + S_2)/(n - 2k)}$$

```
In [22]: X = pd.concat([df['INFL'], df['PROD']], axis=1)
        y = df['INTRATE']
        X = sm.add_constant(X)
        model = sm.OLS(y, X).fit()
        y_pred = model.predict(X)
        print(model.summary())
```

```

                                OLS Regression Results
=====
Dep. Variable:                  INTRATE    R-squared:                  0.575
Model:                          OLS        Adj. R-squared:              0.573
Method:                        Least Squares    F-statistic:                  443.9
Date:                          Tue, 10 Apr 2018    Prob (F-statistic):          1.06e-122
Time:                          00:08:19        Log-Likelihood:              -1502.8
No. Observations:              660            AIC:                        3012.
Df Residuals:                  657            BIC:                        3025.
Df Model:                      2
Covariance Type:               nonrobust
=====
               coef    std err          t      P>|t|      [0.025      0.975]
-----
const          1.2489      0.176       7.088     0.000      0.903      1.595
INFL           0.9750      0.033     29.785     0.000      0.911      1.039
PROD           0.0947      0.020      4.805     0.000      0.056      0.133
=====
Omnibus:                 12.297    Durbin-Watson:              0.065
Prob(Omnibus):            0.002    Jarque-Bera (JB):           12.444
Skew:                    0.326    Prob(JB):                   0.00199
Kurtosis:                3.168    Cond. No.                   11.9
=====
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [23]: X1 = X[:240]
        y1 = y[:240]
        X2 = X[240:]
        y2 = y[240:]
```

```
In [24]: model1 = sm.OLS(y1, X1).fit()
        print(model1.summary())
```

```

                                OLS Regression Results
=====
Dep. Variable:                  INTRATE    R-squared:                  0.794
Model:                          OLS        Adj. R-squared:              0.792
Method:                        Least Squares    F-statistic:                  457.2
Date:                          Tue, 10 Apr 2018    Prob (F-statistic):          4.50e-82
```

Time: 00:08:19 Log-Likelihood: -382.71
 No. Observations: 240 AIC: 771.4
 Df Residuals: 237 BIC: 781.9
 Df Model: 2
 Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]
const	1.4490	0.182	7.959	0.000	1.090	1.808
INFL	0.7833	0.026	29.781	0.000	0.732	0.835
PROD	0.1160	0.016	7.225	0.000	0.084	0.148
Omnibus:	2.436		Durbin-Watson:		0.146	
Prob(Omnibus):	0.296		Jarque-Bera (JB):		2.351	
Skew:	0.080		Prob(JB):		0.309	
Kurtosis:	3.458		Cond. No.		17.7	

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [25]: y2 = df['INTRATE'][240:]
        model2 = sm.OLS(y2, X2).fit()
        print(model2.summary())
```

OLS Regression Results

Dep. Variable:	INTRATE	R-squared:	0.582			
Model:	OLS	Adj. R-squared:	0.580			
Method:	Least Squares	F-statistic:	290.2			
Date:	Tue, 10 Apr 2018	Prob (F-statistic):	1.09e-79			
Time:	00:08:19	Log-Likelihood:	-1001.9			
No. Observations:	420	AIC:	2010.			
Df Residuals:	417	BIC:	2022.			
Df Model:	2					
Covariance Type:	nonrobust					
=====						
	coef	std err	t	P> t	[0.025	0.975]

const	0.7068	0.234	3.022	0.003	0.247	1.167
INFL	1.2330	0.051	24.085	0.000	1.132	1.334
PROD	0.0932	0.031	3.040	0.003	0.033	0.153
=====						
Omnibus:	5.956	Durbin-Watson:	0.075			
Prob(Omnibus):	0.051	Jarque-Bera (JB):	4.958			
Skew:	-0.179	Prob(JB):	0.0838			
Kurtosis:	2.607	Cond. No.	9.67			

=====

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [26]: S0 = sum((df['INTRATE'] - y_pred)**2)
```

```
In [27]: y_pred1 = model1.predict(X1)
         y_pred2 = model2.predict(X2)
```

```
In [28]: S1 = sum((y1 - y_pred1)**2)
         S2 = sum((y2 - y_pred2)**2)
```

```
In [29]: F = ((S0 - S1 - S2)*(660 - 4))/((S1 + S2)*2)
         print("Chow break test = {:.4f}".format(F))
```

Chow break test = 43.2343

Chow break test = 43.2343

We can safely reject the null hypothesis (H0). We do not reject the alternative hypothesis that the models is a combination of two linear regression model over two sets of data divided at the break date Januray 1980.

4.0.2 Chow Forecast test

$$F = \frac{(S0 - S1)/n_2}{S1/(n_1 - k)}$$

```
In [30]: F = ((S0 - S1)*(240 - 2))/(S1*420)
         print("Chow forecast test = {:.4f}".format(F))
```

Chow forecast test = 5.5338

Chow forecast test = 5.5338

We can safely reject the null hypothesis (H0). We can say that the alternative hypothesis is true that the 2nd regression line after the break provides a good fit as the coefficient is significant.

4.0.3 Jarque-Bera test

The high JB test value, 12.44 from Taylor equation suggests that the residuals are not normally distributed. This tells us that the model is not good.

The JB test values in the Chow break test gives JB values of 2.31 and 4.96. This indicates that the regression model is a better fit when the data is divided into 2 parts on the basis of time (break date January 1980).