



# Continuous control of a Robot Manipulator using Deep Deterministic Policy Gradient

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# Outline



- Introduction
- Mathematical Preliminaries
- 3 Deep Deterministic Policy Gradient
- Description of Uncertainties
- Simulation Results
- **6** Concluding Remarks



### Motivation



## Few applications of Robot Manipulator

- Industrial: welding, painting, assembly, disassembly, pick and place
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#### Reinforcement Learning:-

- Ability to generate optimal policies with no prior knowledge of the environment
- Deep RL addresses the issues of scalability, memory and computational complexity
- Can extend to multiple degrees-of-freedom





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- **DDPG**: trajectory-tracking control of a SCARA and mobile robot [4], reaching task of a 6-DoF robot manipulator in 3D space [5]
- No performance evaluation in the presence of uncertainties and disturbances



# Robot Manipulator Dynamics



The dynamics of the robot manipulator is described as follows:

$$M_{11}\ddot{\theta}_1 + M_{12}\ddot{\theta}_2 + V_1 + G_1 = \tau_1 \tag{1}$$

$$M_{12}\ddot{\theta}_1 + M_{22}\ddot{\theta}_2 + V_2 + G_2 = \tau_2 \tag{2}$$

In a more standard form:

$$M(\theta)\ddot{\theta} + V(\theta,\dot{\theta}) + G(\theta) = \tau$$
 (3)

where,

$$M = \begin{pmatrix} M_{11} & M_{12} \\ M_{12} & M_{22} \end{pmatrix}, V = \begin{pmatrix} V_1 \\ V_2 \end{pmatrix}, G = \begin{pmatrix} G_1 \\ G_2 \end{pmatrix}, \tau = \begin{pmatrix} \tau_1 \\ \tau_2 \end{pmatrix}$$

Goal: Track a desired reference,  $\theta^* = [\theta_1^*, \theta_2^*]^T$ 

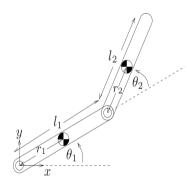


Figure: TLRM





- Learning takes place through agent-environment interactions
- At each time-step t, agent takes an action  $A_t$  based on the current state  $S_t$ , giving rise to a new state  $S_{t+1}$  receiving an immediate reward of  $r_t$  while following a policy  $\pi$





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- Cumulative reward:

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• The goodness of a state is determined by its value function:

$$V_{\pi}(s) = \mathbb{E}_{\pi} \left[ R_{\pi} | S_t = s \right] = \mathbb{E}_{\pi} \left[ \sum_{t=0}^{\infty} \gamma^k r_{t+i+1} | S_t = s \right]$$
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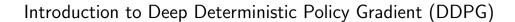
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• Similarly, the value of taking an action a in state s while following a policy  $\pi$  is given by:

$$Q_{\pi}(s, a) = \mathbb{E}_{\pi} [R_{\pi} | S_t = s, A_t = a] = \mathbb{E}_{\pi} [\sum_{k=0}^{\infty} \gamma^k r_{t+i+1} | S_t = s, A_t = a]$$
 (6)



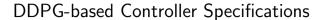




## Why DDPG?

- 1. Proposed as a simple integration of deep Q-networks and actor-critic
- 2. Successful in operating over continuous action spaces
- 3. As the uncertainties and disturbances are deterministic in nature, a deterministic policy is sufficient to achieve our targets
- There are 4 main steps to this process:
  - 1. Experience replay; Finite-sized cache D
  - 2. Actor & critic networks:  $\mu(s|\theta^{\mu})$  and Q(s,a)
  - 3. Target network updates: Added stability during training,  $\theta_t = \rho\theta + (1-\rho)\theta_t$
  - 4. Exploration: Adding an appropriate noise signal,  ${\cal N}$







- DDPG-based controller is augmented with a stabilizing PD controller
- $\Delta \tau_1$  and  $\Delta \tau_2$  compensate for the uncertainties in the system

$$R = -e^T Q e (7)$$

where  $e = \theta - \theta^*$  and Q is a positive definite matrix.

• Few of the DDPG parameters:

Parameter	Description	Values	
$(\alpha_a, \alpha_c)$	Learning rates	(0.001, 0.002)	
$\gamma$	Discount factor	0.99	
$\Delta  au$	Action Space	[-1,1] <i>Nm</i>	

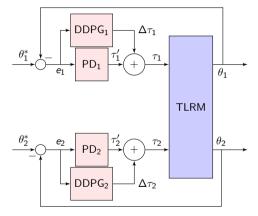


Figure: TLRM controller framework



# Description of Uncertainties



## Frictional Forces

- Friction that is present between the joints of the robot manipulator can severely affect motion quality
- 2. The frictional matrix can be modelled as:

$$F(\dot{\theta}) = \begin{bmatrix} \nu_1 \dot{\theta}_1 + k_1 \operatorname{sgn}(\dot{\theta}_1) \\ \nu_2 \dot{\theta}_2 + k_2 \operatorname{sgn}(\dot{\theta}_2) \end{bmatrix}$$
(8)

3. The combined TLRM dynamics can be written as:

$$M(\theta)\ddot{\theta} + V(\theta,\dot{\theta}) + G(\theta) + F(\dot{\theta}) = \tau$$

## Torque Disturbances

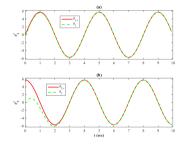
- An external torque disturbance is introduced into the system after a duration of 5 seconds
- 2. It is modelled as a sinusoidal signal with a frequency of  $2\pi$  rad/sec
- 3. The amplitude of the disturbance is taken to be 20% of the torque  $(\tau)$  input

$$\tau_d = \begin{bmatrix} 0.2\tau_1 \sin 2\pi t \\ 0.2\tau_2 \sin 2\pi t \end{bmatrix} \tag{9}$$







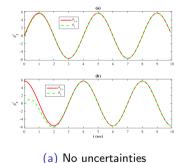


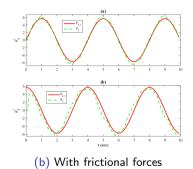
(a) No uncertainties

















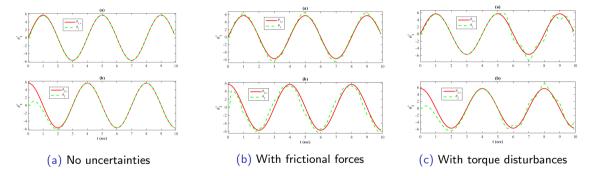
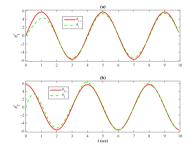


Figure: Tracking performance of PD controller







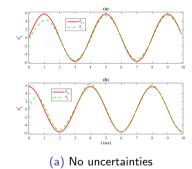


(a) No uncertainties









(b) With frictional forces







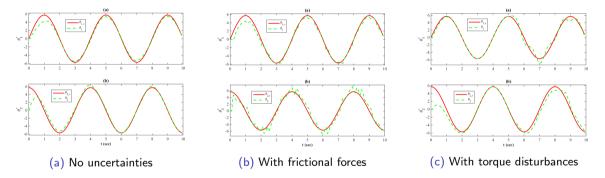


Figure: Tracking performance of DDPG controller







Table: Performance Comparison

Uncertainty	Angle	PD		DDPG	
		MSE	VAF	MSE	VAF
None	$ heta_{ extbf{1}}$	0.399	97.493	0.581	96.726
	$ heta_2$	1.940	89.798	0.830	94.970
Friction $F(\dot{\theta})$	$ heta_{ extbf{1}}$	0.765	95.199	0.763	96.101
	$ heta_2$	2.522	85.232	0.886	94.604
Torque $ au_d$	$ heta_{ extbf{1}}$	0.793	95.161	0.668	95.798
	$\theta_2$	2.744	84.963	1.855	90.635





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  - 2. several other disturbances such as measurement noise, and wind disturbances
  - 3. comparison with several other RL algorithms



# References



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