

1. Write a program that finds the closest pair of points in a set of 2D points using the brute force approach.

Input:

- A list or array of points represented by coordinates (x, y).

Points: [(1, 2), (4, 5), (7, 8), (3, 1)]

Output:

- The two points with the minimum distance between them.
- The minimum distance itself.

Closest pair: (1, 2) - (3, 1) Minimum distance: 1.4142135623730951

2. Write a program to find the closest pair of points in a given set using the brute force approach. Analyze the time complexity of your implementation. Define a function to calculate the Euclidean distance between two points. Implement a function to find the closest pair of points using the brute force method. Test your program with a sample set of points and verify the correctness of your results. Analyze the time complexity of your implementation. Write a brute-force algorithm to solve the convex hull problem for the following set S of points? P1 (10,0)P2 (11,5)P3 (5, 3)P4 (9, 3.5)P5 (15, 3)P6 (12.5, 7)P7 (6, 6.5)P8 (7.5, 4.5).How do you modify your brute force algorithm to handle multiple points that are lying on the sameline?

**Given points:** P1 (10,0), P2 (11,5), P3 (5, 3), P4 (9, 3.5), P5 (15, 3), P6 (12.5, 7), P7 (6, 6.5), P8 (7.5, 4.5).

**output:** P3, P4, P6, P5, P7, P1

3. Write a program that finds the convex hull of a set of 2D points using the brute force approach.

**Input:**

- A list or array of points represented by coordinates (x, y).

Points: [(1, 1), (4, 6), (8, 1), (0, 0), (3, 3)]

**Output:**

- The list of points that form the convex hull in counter-clockwise order.

Convex Hull: [(0, 0), (1, 1), (8, 1), (4, 6)]

4. You are given a list of cities represented by their coordinates. Develop a program that utilizes exhaustive search to solve the TSP. The program should:

1. Define a function distance(city1, city2) to calculate the distance between two cities (e.g., Euclidean distance).
2. Implement a function tsp(cities) that takes a list of cities as input and performs the following:
  - Generate all possible permutations of the cities (excluding the starting city) using itertools.permutations.
  - For each permutation (representing a potential route):
    - Calculate the total distance traveled by iterating through the path and summing the distances between consecutive cities.
    - Keep track of the shortest distance encountered and the corresponding path.

- Return the minimum distance and the shortest path (including the starting city at the beginning and end).
- 3. Include test cases with different city configurations to demonstrate the program's functionality. Print the shortest distance and the corresponding path for each test case.

**Test Cases:**

1. **Simple Case:** Four cities with basic coordinates (e.g., [(1, 2), (4, 5), (7, 1), (3, 6)])
2. **More Complex Case:** Five cities with more intricate coordinates (e.g., [(2, 4), (8, 1), (1, 7), (6, 3), (5, 9)])

**Output:**

**Test Case 1:**

Shortest Distance: 7.0710678118654755

Shortest Path: [(1, 2), (4, 5), (7, 1), (3, 6), (1, 2)]

**Test Case 2:**

Shortest Distance: 14.142135623730951

Shortest Path: [(2, 4), (1, 7), (6, 3), (5, 9), (8, 1), (2, 4)]

5. You are given a cost matrix where each element  $\text{cost}[i][j]$  represents the cost of assigning worker  $i$  to task  $j$ . Develop a program that utilizes exhaustive search to solve the assignment problem. The program should Define a function `total_cost(assignment, cost_matrix)` that takes an assignment (list representing worker-task pairings) and the cost matrix as input. It iterates through the assignment and calculates the total cost by summing the corresponding costs from the cost matrix Implement a function `assignment_problem(cost_matrix)` that takes the cost matrix as input and performs the following Generate all possible permutations of worker indices (excluding repetitions).

**Test Cases:**

**Input**

1. **Simple Case:** Cost Matrix:  
[[3, 10, 7],  
[8, 5, 12],  
[4, 6, 9]]
2. **More Complex Case:** Cost Matrix:  
[[15, 9, 4],  
[8, 7, 18],  
[6, 12, 11]]

**Output:**

**Test Case 1:**

Optimal Assignment: [(worker 1, task 2), (worker 2, task 1), (worker 3, task 3)]

Total Cost: 19

**Test Case 2:**

Optimal Assignment: [(worker 1, task 3), (worker 2, task 1), (worker 3, task 2)]

Total Cost: 24

6. You are given a list of items with their weights and values. Develop a program that utilizes exhaustive search to solve the 0-1 Knapsack Problem. The program should:
1. Define a function `total_value(items, values)` that takes a list of selected items (represented by their indices) and the value list as input. It iterates through the selected items and calculates the total value by summing the corresponding values from the value list.
  2. Define a function `is_feasible(items, weights, capacity)` that takes a list of selected items (represented by their indices), the weight list, and the knapsack capacity as input. It checks if the total weight of the selected items exceeds the capacity.

**Test Cases:**

1. **Simple Case:**

- Items: 3 (represented by indices 0, 1, 2)
- Weights: [2, 3, 1]
- Values: [4, 5, 3]
- Capacity: 4

2. **More Complex Case:**

- Items: 4 (represented by indices 0, 1, 2, 3)
- Weights: [1, 2, 3, 4]
- Values: [2, 4, 6, 3]
- Capacity: 6

Output:

**Test Case 1:**

Optimal Selection: [0, 2] (Items with indices 0 and 2)

Total Value: 7

**Test Case 2:**

Optimal Selection: [0, 1, 2] (Items with indices 0, 1, and 2)

Total Value: 10