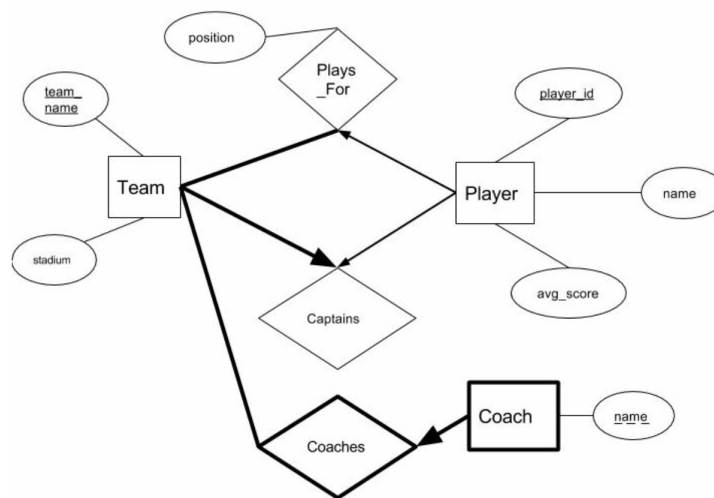


## 1 ER Diagrams

We want to store sports teams and their players in our database. Draw an ER diagram corresponding to data given below:

- Every Team in our database will have a unique team\_name and a stadium where they play their games.
- Each Coach has a name.
- Each Player will have a unique player\_id, a name and an average score.
- Our database will contain who Plays\_For which team and also the “position” that the player plays in. We also need to store who Captains a team, and who Coaches a team.
- Every Team needs players, and needs exactly one captain.
- Each Player can be on at most one team, but may currently be a free agent and not on any team.
- Each team needs coaches and may have many.
- A Coach is uniquely identified by which team they coach.



## 2 Functional Dependencies

- Consider a set of functional dependencies  $F = \{X \rightarrow Y, Y \rightarrow Z\}$ . For each of the following symbols or expressions, indicate whether it is (a) an attribute, (b) a set of attributes, (c), a set of sets of attributes, (d) a functional dependency, (e) a set of functional dependencies, or (f) none of the above.
  - X (b) a set of attributes
  - XY (b) a set of attributes
  - $X \rightarrow Y$  (d) a functional dependency
  - F (e) a set of functional dependencies
  - $F^+$  (e) a set of functional dependencies
  - $X^+$  (b) a set of attributes
  - Armstrong's reflexivity axiom (f) an axiom
- Consider a relation  $R(x, y, z)$  and the list of functional dependencies  $X \rightarrow Y$ ,  $XY \rightarrow YZ$ , and  $Y \rightarrow X$  where  $X = \{x\}$ ,  $Y = \{y\}$ , and  $Z = \{z\}$ . For each of the following relations, indicate which functional dependencies it might satisfy.

x	y	z
1	2	0
1	2	1
1	3	0
2	3	0

x	y	z
1	2	1
1	3	1
2	3	0

x	y	z
1	3	1
2	3	0

x	y	z
1	3	1

- None
  - $XY \rightarrow YZ$
  - $X \rightarrow Y, XY \rightarrow YZ$
  - $X \rightarrow Y, XY \rightarrow YZ, Y \rightarrow X$
- Consider the set  $F = \{A \rightarrow B, AB \rightarrow AC, BC \rightarrow BD, DA \rightarrow C\}$  of functional dependencies. Compute the following attribute closures.
    - $A^+$  ABCD
    - $B^+, C^+, D^+$  B, C, D; B, C, and D do not appear alone on the left of any functional dependency, so nothing is in their attribute closures besides themselves.
    - $AB^+, AC^+, AD^+$  ABCD;  $A^+ = ABCD$ , so  $AX = ABCD$  for any X.
    - $BC^+$  BCD

- (e)  $BD + BD$
  - (f)  $CD + CD$
  - (g)  $BCD + BCD$
4. Consider again the set  $F$  of functional dependencies from Question 3. Indicate whether the following sets of attributes are candidate keys, superkeys (but not candidate keys), or neither.
- (a)  $A$  **candidate key** because  $A+$  is the minimal number of keys to cover all symbols in  $F$
  - (b)  $B, C, D$  **neither** because neither of them cover all symbols in  $F$
  - (c)  $AB, AC, AD$  **superkeys** because  $A$  is a candidate key, so any more symbols added to  $A$  is not the minimal set of symbols to cover all symbols in  $F$  and thus, a superkey
  - (d)  $BC$  **neither**
  - (e)  $BD$  **neither**
  - (f)  $CD$  **neither**
  - (g)  $BCD$  **neither**

### 3 Normal Forms

1. Decompose  $R = ABCDEFG$  into BCNF, given the functional dependency set:  $F = AB \rightarrow CD, C \rightarrow EF, G \rightarrow A, G \rightarrow F, CE \rightarrow F$ .
- $AB \rightarrow CD \Rightarrow$  decompose  $ABCDEFG$  into  $ABCDEF, ABG$   
 $C \rightarrow EF \Rightarrow$  decompose  $ABCDEF$  into  $ABCD, CEF$   
 $G \rightarrow A \Rightarrow$  decompose  $ABG$  into  $AG, BG$   
 Final relations:  $ABCD, CEF, AG, BG$ .