

1 ER Diagrams

We want to store sports teams and their players in our database. Draw an ER diagram corresponding to data given below:

- Every Team in our database will have a unique `team_name` and a stadium where they play their games.
- Each Coach has a name.
- Each Player will have a unique `player_id`, a name and an average score.
- Our database will contain who `Plays_For` which team and also the “position” that the player plays in. We also need to store who `Captains` a team, and who `Coaches` a team.
- Every Team needs players, and needs exactly one captain.
- Each Player can be on at most one team, but may currently be a free agent and not on any team.
- Each team needs coaches and may have many.
- A Coach is uniquely identified by which team they coach.

2 Functional Dependencies

- Consider a set of functional dependencies $F = \{X \rightarrow Y, Y \rightarrow Z\}$. For each of the following symbols or expressions, indicate whether it is (a) an attribute, (b) a set of attributes, (c), a set of sets of attributes, (d) a functional dependency, (e) a set of functional dependencies, or (f) none of the above.
 - X
 - XY
 - $X \rightarrow Y$
 - F
 - F^+
 - X^+
 - Armstrong's reflexivity axiom
- Consider a relation $R(x, y, z)$ and the list of functional dependencies $X \rightarrow Y$, $XY \rightarrow YZ$, and $Y \rightarrow X$ where $X = \{x\}$, $Y = \{y\}$, and $Z = \{z\}$. For each of the following relations, indicate which functional dependencies it might satisfy.

| x | y | z |
|---|---|---|
| 1 | 2 | 0 |
| 1 | 2 | 1 |
| 1 | 3 | 0 |
| 2 | 3 | 0 |

| x | y | z |
|---|---|---|
| 1 | 2 | 1 |
| 1 | 3 | 1 |
| 2 | 3 | 0 |

| x | y | z |
|---|---|---|
| 1 | 3 | 1 |
| 2 | 3 | 0 |

| x | y | z |
|---|---|---|
| 1 | 3 | 1 |

- Consider the set $F = \{A \rightarrow B, AB \rightarrow AC, BC \rightarrow BD, DA \rightarrow C\}$ of functional dependencies. Compute the following attribute closures.
 - A^+
 - B^+, C^+, D^+
 - AB^+, AC^+, AD^+
 - BC^+
 - BD^+
 - CD^+
 - BCD^+

4. Consider again the set F of functional dependencies from Question 3. Indicate whether the following sets of attributes are candidate keys, superkeys (but not candidate keys), or neither.

- (a) A
- (b) B, C, D
- (c) AB, AC, AD
- (d) BC
- (e) BD
- (f) CD
- (g) BCD

3 Normal Forms

1. Decompose $R = ABCDEFG$ into BCNF, given the functional dependency set: $F = AB \rightarrow CD, C \rightarrow EF, G \rightarrow A, G \rightarrow F, CE \rightarrow F$.