## Bits, Bytes and Words

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Based on slides by Randal E. Bryant and David R. O'Hallaron

## Agenda

Representing information as bits

Bit-level manipulation

Integers

Representation: unsigned and signed

Conversion, casting

Expanding, truncating

### Representing information as bits

Bit-level manipulation

### Integers

Representation: unsigned and signed Conversion, casting Expanding, truncating

## **Everything is bits**

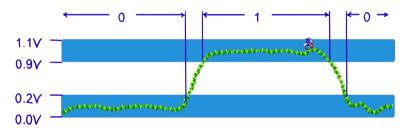
- Each bit is 0 or 1
- By interpreting sets of bits in various ways...
  - ...computers determine what to do.
  - ► ...represent and manipulate numbers, sets, strings—data.

Why bits? Why not decimals? Could it have been some other way?

## **Everything is bits**

#### Why bits? Electronic implementation.

- Easy to store with bistable elements.
- ► Reliably transmitted on noisy and inaccurate wires via *error correction*.



#### ... But there exist models that do not use bits.

- ► The Setun computer developed in the Soviet Union used ternary *trits*.
- Quantum computers use *qubits* that are in a superposition of the two states.
  - ...error correction is the main challenge here.

## **Everything is bit vectors**

### A sequence of bits is called a bit vector

$$\langle x_{w-1},\ldots,x_0\rangle$$

- Number bits from 0 to w-1.
- Bit  $x_0$  typically called *least significant* and  $x_{w-1}$  *most significant*.
  - ▶ Due to how bit vectors can be interpreted as binary numbers.
- Bit vectors are not numbers.
  - ► Can represent many kinds of objects.
  - ...but we will mostly focus on number representations.

## **Binary numbers**

#### Base 2 numbers.

- ► Represent 15213<sub>10</sub> as 11101101101101<sub>2</sub>
  - ightharpoonup (0011 1011 0110 1101) (with w = 16)
- ► Represent  $\frac{15_{10}}{213_{10}}$  as  $\frac{1111_2}{11010101_2}$ 
  - ightharpoonup (0000 0000 0000 1111 0000 0000 1101 0101) (w = 32)
  - ▶ 16 bits for each of numerator and denominator.
  - (This is not how we actually represent rational numbers in a computer-we'll see how next week.)

#### Machine numbers are of some finite size.

- ightharpoonup If we use w bits to represent a number, only  $2^w$  distinct values are possible.
- How we interpret those bits can vary.
- Why do we use finite-sized numbers?
  - ► A "w-bit machine" handles numbers of up to w bits "natively" (meaning fast).
  - ► A bit vector of some natively supported size is called a word.

# **Encoding byte values**

	Hex	Dec	Bits
Byte = 8 bit word	0	0	⟨0000⟩
•	1	1	$\langle 0001 \rangle$
<ul><li>(Machine-specific, but is true for all</li></ul>	2	2	(0010)
mainstream machines.)	3	3	⟨0011⟩
<ul> <li>256 different values.</li> </ul>	4	4	$\langle 0100 \rangle$
	5	5	$\langle 0101 \rangle$
<ul> <li>Binary 00000000<sub>2</sub> to 11111111<sub>2</sub>.</li> </ul>	6	6	$\langle 0110 \rangle$
<ul> <li>Decimal 0<sub>10</sub> to 255<sub>10</sub>.</li> </ul>	7	7	$\langle 0111 \rangle$
<ul> <li>Hexadecimal 00<sub>16</sub> to FF<sub>16</sub>.</li> </ul>	8	8	$\langle 1000 \rangle$
10 10	9	9	$\langle 1001 \rangle$
► Base 16 number representation.	Α	10	$\langle 1010 \rangle$
► Uses characters 0−9 and A−F.	В	11	$\langle 1011 \rangle$
► In C we write FA1D37B <sub>16</sub> as	C	12	<b>(1100)</b>
• 0xFA1D37B	D	13	<b>(1101)</b>
0xfa1d37b (case does not matter)	E	14	$\langle 1110 \rangle$
	F	15	$\langle 1111 \rangle$

## Let's play a game

http://topps.diku.dk/compsys/integers.html

# **Example data representations**

C data type	Typical 16-bit	Typical 32-bit	Typical 64-bit	x86-64
char	1	1	1	1
short	1	2	2	2
int	2	4	4	4
long	4	4	8	8
int32_t	4	4	4	4
int64_t	8	8	8	8
float	4	4	4	4
double	8	8	8	8
pointer	2	4	8	8

### Representing information as bits

### Bit-level manipulation

### Integers

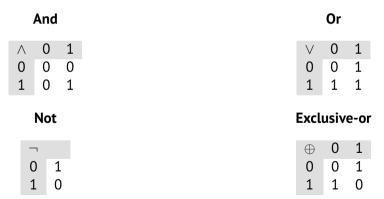
Representation: unsigned and signed Conversion, casting

Expanding, truncating

## Boolean algebra

### Developed by George Boole in the 19th century

- Algebraic representation of logic ("truth values").
- Encode *true* as 1 and *false* as 0.



■ These operations can be implemented with tiny electronic *gates*.

## Boolean algebra on bit vectors

• The truth tables generalise to bit vectors, applied elementwise.

- This is the form they take when available in programming languages such as C.
- ...although C uses different symbols.

## Bit-level operations in C

### Operators & ( $\land$ ), | ( $\lor$ ), $^{\land}$ ( $\oplus$ ), $^{\sim}$ ( $\neg$ ) available in C.

- Apply to any integral type.
  - ► E.g. long, int, short, char...
- Interpret operands as bit vectors.
- Applied element-wise.

#### **Examples**

- $\sim 0 \times 41 = 0 \times BE$ 
  - $ightharpoonup \neg \langle 01000001 \rangle = \langle 101111110 \rangle$
- $\sim 0 \times 00 = 0 \times FF$ 
  - ightharpoonup  $\langle 000000000 \rangle = \langle 1111111111 \rangle$
- -0x69 & 0x55 = 0x41
  - ightharpoonup  $\langle 01101001 \rangle \wedge \langle 01010101 \rangle = \langle 01000001 \rangle$
- -0x69 & 0x55 = 0x7D
  - $\blacktriangleright \ \langle 01101001 \rangle \land \langle 01010101 \rangle = \langle 01111101 \rangle$

## Contrast: logical operators in C

The logical operators interpret numbers as *single boolean values*, not as bit vectors!

- **&** & & , | | , !
  - ► View 0 as false.
  - Anything nonzero as true.
  - ► Always produce 0 or 1.
  - ► Short circuiting:  $1 \mid \mid (0/0)$  is safe.

#### Examples

- $\triangleright$  !0x41 = 0x00
- $\triangleright$  !0x00 = 0x01
- $\triangleright$  !!0x41 = 0x01
- $\triangleright$  0x69 && 0x55 = 0x01
- $\triangleright$  0x69 || 0x55 = 0x01
- Do not confuse the logical and bitwise operators!

## **Shift operations**

#### Left shift x << y</p>

- ► Shift bit-vector x left by y positions.
  - ► Throws away excess bits on the left.
  - Fills with zeroes on right.

#### Right shift x >> y

- ► Shift bit-vector x right by y positions.
  - ► Throws away excess bits on the left.
- ► Logical shift: Fill with 0s on left.
- Arithmetic shift: Replicate most significant bit on left.

#### Undefined behaviour in C

Shifting a negative amount or by the vector size or more.

X	$\langle 01100010 \rangle$
x < < 3	(00010000)

- x << 3  $\langle 00010000 \rangle$ x >> 2  $\langle 00011000 \rangle$
- $x >> a 2 \langle 00011000 \rangle$

- $\frac{x}{x << 3} \quad \langle 10100010 \rangle$
- x >> 2  $\langle 00101000 \rangle$
- $x>>^a 2 \quad \langle 11101000 \rangle$

### Representing information as bits

Bit-level manipulation

### Integers

Representation: unsigned and signed

Conversion, casting Expanding, truncating

## **Encoding integers**

Suppose  $x_i$  is the *i*th bit of a *w*-bit word (with  $x_0$  being the least significant bit).

### Unsigned

### Two's complement (AKA *signed*)

	Decimal	Hex	Bits
Х	15213	3 B 5 D	〈0011 1011 0110 1101〉
У	-15213	C 4 9 3	〈1100 0100 1001 0011〉

### Sign bit

- For 2's complement, most significant bit  $(x_{w-1})$  indicates sign.
  - ▶ 0 for non-negative.
  - ▶ 1 for negative.

## Two's complement encoding example

```
int16_t x = 15213; // 0011 1011 0110 1101 int16_t y = -15213; // 1100 0100 1001 0011
```

Weight	1	.5213		-15213
1	1	1	1	1
2	0	0	1	2
4	1	4	0	0
8	1	8	0	0
16	0	0	1	16
32	1	32	0	0
64	1	64	0	0
128	0	0	1	128
256	1	256	0	0
512	1	512	0	0
1024	0	0	1	1024
2048	1	2047	0	0
4096	1	4096	0	0
8192	1	8192	0	0
16384	0	0	1	16384
-32768	0	0	1	-32768
Sum		15213		-15213

## Numeric ranges

### Unsigned

### Two's complement

UMin =
 
$$0 = 0 \dots 0_2$$
 SMin =
  $-2^{w-1} = 10 \dots 0_2$ 

 UMax =
  $2^w - 1 = 1 \dots 1_2$ 
 SMax =
  $2^{w-1} - 1 = 01 \dots 1_2$ 
 $-1$ 
 $= 1 \dots 1_2$ 

Values for w = 16:

	Decimal	Hex	Bits
UMax	65535	FFFF	$\langle 1111\ 1111\ 1111\ 1111 \rangle$
SMax	32767	7 F F F	〈0111 1111 1111 1111〉
SMin	-32768	8 0 0 0	⟨1000 0000 0000 0000⟩
-1	-1	FFFF	<b>(1111 1111 1111 1111)</b>
0	0	0 0 0 0	⟨0000 0000 0000 0000⟩

## Values for different word sizes

	W					
	8	16	32	64		
UMax	255	65,535	4,294,967,295	18,446,744,073,709,551,615		
SMax	127	32,767	2,147,483,647	9,223,372,036,854,775,807		
SMin	-128	-32,768	-2,147,483,648	-9,223,372,036,854,775,808		

#### **Observations**

$$\begin{aligned} |\mathsf{SMin}| &= \mathsf{SMax} + 1 \\ |\mathsf{UMax}| &= 2 \cdot \mathsf{SMax} + 1 \end{aligned}$$

### Note the asymmetric range.

### **C Programming**

- #include <limits.h>
- Declares constants, e.g:
  - ► ULONG\_MAX
  - ► LONG\_MAX
    - ► LONG\_MIN
- Values are platform-specific.

# Unsigned and signed numeric values (here w=4)

X	Bits2N( $x$ )	TC2Int(x)
⟨0000⟩	0	0
⟨0001⟩	1	1
⟨0010⟩	2	2
⟨0011⟩	3	3
⟨0100⟩	4	4
⟨0101⟩	5	5
⟨0110⟩	6	6
$\langle 0111 \rangle$	7	7
⟨1000⟩	8	-8
$\langle 1001 \rangle$	9	-7
$\langle 1010 \rangle$	10	-6
⟨1011⟩	11	-5
$\langle 1100 \rangle$	12	-4
<b>(1101)</b>	13	-3
<b>〈1110</b> 〉	14	-2
$\langle 1111 \rangle$	15	-1

#### Equivalence

► Same encoding for non-negative values.

#### Uniqueness

- ► Every bit vector represents distinct integer value.
- ► Each representable integer has unique bit encoding.
- ► The representation is **bijective**.

### Can invert mappings

- $N2Bits(x) = Bits2N^{-1}(x)$ 
  - Bit vector for unsigned integer in range.
- ► Int2TC(x) = TC2Int<sup>-1</sup>(x)
  - ► Bit vector for Two's Complement integer in range.

### Representing information as bits

### Bit-level manipulation

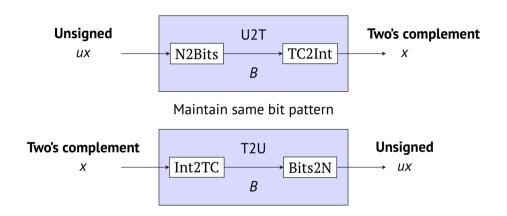
### Integers

Representation: unsigned and signed

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## Mapping between signed and unsigned

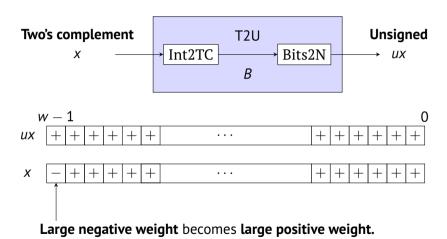


Mapping between unsigned and two's complement numbers: **Keep bit representations and reinterpret.** 

# Mapping signed ⇔ unsigned

Bits	Signed		Unsigned
⟨0000⟩	0		0
⟨0001⟩	1		1
⟨0010⟩	2		2
⟨0011⟩	3		3
⟨0100⟩	4		4
⟨0101⟩	5		5
⟨0110⟩	6	$\longrightarrow$ T2U $\longrightarrow$	6
⟨0111⟩	7		7
$\langle 1000 \rangle$	-8	← <u>U2T</u> ←	8
$\langle 1001 \rangle$	-7		9
$\langle 1010 \rangle$	-6		10
$\langle 1011 \rangle$	-5		11
$\langle 1100 \rangle$	-4		12
$\langle 1101 \rangle$	-3		13
$\langle 1110 \rangle$	-2		14
$\langle 1111 \rangle$	-1		15

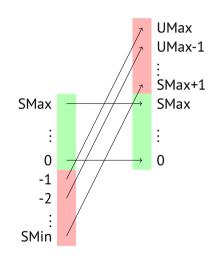
## Relation between signed and unsigned



## Conversion (that is, reinterpretation) visualized

### Two's complement to unsigned

- Ordering inversion.
- Negative numbers become large positive numbers.



## Signed versus unsigned in C

### C makes working with this more error-prone than it should be.

### Types Constants

- Signedness part of type: unsigned int, int32\_t, uint32\_t.
- By default are considered signed integers.
- Unsigned with U suffix: 0U, 4294967259U

#### Casting

Explicit casting between signed and unsigned:

```
int tx, ty;
unsigned int ux, uy;
tx = (int) ux;
uy = (unsigned int) ty;
```

Implicit casting due to assignments and other expressions:

```
tx = ux;

uy = ty;
```

- If there is a mix of unsigned and signed in single expression, *signed* values implicitly cast to unsigned.
- Including comparison operations <, >, ==, <=, >=.
- Examples for w = 32: SMin = -2, 147, 483, 648, <math>SMax = 2, 147, 483, 647:

Const LHS	Relation	Const RHS	Evaluation
0	==	0U	

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0	==	0U	unsigned

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- Examples for w = 32: SMin = 2

$$w = 32$$
:  $SMin = -2, 147, 483, 648$ ,  $SMax = 2, 147, 483, 647$ :

Const LHS	Relation	Const RHS	<b>Evaluation</b>
0	==	0U	unsigned
-1	<	0	

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0	==	0U	unsigned
-1	<	0	signed

#### **Evaluation**

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- Examples for w = 32: SMin = -2

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Const LHS	Relation	Const RHS	<b>Evaluation</b>
0	==	0U	unsigned
-1	<	0	signed
-1	>	0U	

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Const LHS	Relation	Const RHS	<b>Evaluation</b>
0	==	0U	unsigned
-1	<	0	signed
-1	>	0U	unsigned

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w = 32: SMin = -2, 147, 483, 648, <math>SMax = 2, 147, 483, 647:

Const LHS	Relation	Const RHS	<b>Evaluation</b>
0	==	0U	unsigned
-1	<	0	signed
-1	>	0U	unsigned
2147483647	>	-2147483647-1	

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w = 32: SMin =	-2, 147, 483	3, 648, <i>SMa</i>	x = 2,147	, 483, 647:

Const LHS	Relation	Const RHS	Evaluation
0	==	0U	unsigned
-1	<	0	signed
-1	>	0U	unsigned
2147483647	>	-2147483647-1	signed
2147483647U	<	-2147483647-1	unsigned
-1	>	-2	

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- Examples for

w = 32: SMin =	= -2, 147, 483	5, 648, <i>SM</i>	ax = 2, 14	47, 483,	647:

Const LHS	Relation	Const RHS	Evaluation
0	==	0U	unsigned
-1	<	0	signed
-1	>	0U	unsigned
2147483647	>	-2147483647-1	signed
2147483647U	<	-2147483647-1	unsigned
-1	>	-2	signed

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2147483647U	<	-2147483647-1	unsigned
-1	>	-2	signed
(unsigned int)-1	>	-2	

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2147483647	<	2147483648U	

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2147483647U	<	-2147483647-1	unsigned
-1	>	-2	signed
(unsigned int)-1	>	-2	unsigned
2147483647	<	2147483648U	unsigned
2147483647	>	(int) 2147483648U	

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  - Evamples for

Examples for			
w = 32: SMin = 1	-2, 147, 483, 64	8, $SMax = 2, 1$	L47, 483, 647:

Const LHS	Relation	Const RHS	Evaluation
0	==	0U	unsigned
-1	<	0	signed
-1	>	0U	unsigned
2147483647	>	-2147483647-1	signed
2147483647U	<	-2147483647-1	unsigned
-1	>	-2	signed
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# Casting between signed and unsigned: basic rules

- Bit representation is maintained.
- ...but reinterpreted.
- Can have unexpected effects: adding or subtracting  $2^w$ .
- Expression containing signed and unsigned int:
  - ▶ int is cast to unsigned int!
  - ► When can this go bad?

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for (unsigned int i = n-1; i >= 0; i--) {
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for (unsigned int i = n-1; i >= 0; i--) {
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```

**Advice:** Avoid arithmetic on unsigned types—only use them for bit operations.

**But:** Some C operators (sizeof) and many functions return unsigned types (e.g. size\_t). C is always ready to stab you in the back.

### Representing information as bits

Bit-level manipulation

### Integers

Representation: unsigned and signed Conversion, casting Expanding, truncating

### **Truncation**

#### Task

- Given k + w-bit signed integer x.
- Convert it to w-bit integer x' with same value i possible.

#### Approach

- Remove the *k* most significant bits.
- Equivalent to computing  $x' = x \mod 2^w$ .
- Numerical change if number has no representation in w bits.
- Otherwise safe.

W	X	TC2Int(x)
8	$\langle 11111111 \rangle$	-1
4	$\langle 1111 \rangle$	-1
8	⟨10000000⟩	-128
4	⟨0000⟩	0

## Sign extension

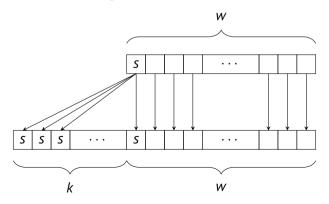
#### Task

- Given *w*-bit signed integer *x*.
- Convert it to w + k-bit integer x' with same value.

#### Approach

■ Make *k* copies of sign bit (most significant bit):

$$x' = \langle \underbrace{x_{w-1}, \dots, x_{w-1}}_{k \text{ copies of sign bit.}} x_{w-1} \cdots x_0 \rangle$$



# Sign extension example

```
short int x = 15213;
int         ix = (int) x;
short int y = -15213;
int         iy = (int) y;
```

	Decimal	Hex	Bits
Х	15213 <sub>10</sub>	3B 6D	(0011 1011 0110 1101)
ix	15213 <sub>10</sub>	00 00 3B 6D	(0000 0000 0000 0000 0011 1011 0110 1101)
У	$-15213_{10}$	C4 93	〈1100 0100 1001 0011〉
iy	$-15213_{10}$	FF FF C4 93	〈1111 1111 1111 1111 1100 0100 1001 0011〉

# Summary: basic rules for expanding and truncating

### Expanding (e.g. short to int)

- Unsigned: zeros added.
- Signed: sign extension.
- Both yield expected result.

### Truncating (e.g. unsigned int to unsigned short)

- Bits are truncated.
- Result reinterpreted.
- Unsigned: modulo operation.
- Signed: similar to a modulo operation.
- For small numbers yield expected behaviour.