

**Quick Reference (What students saw)****Relation:** any set of ordered pairs  $(x, y)$ .**Function:** each input  $x$  has exactly one output  $y$ .**Domain:** all inputs.    **Range:** all outputs.**Notation:**  $f(x)$  is the output when input is  $x$ . Substitute with parentheses.

1. (10 points)
- Is it a function? Domain & Range.**

$$R = \{(0, 2), (1, 5), (2, 5), (1, 5)\}.$$

**Solution: (a)** Yes,  $R$  is a function. Every input used  $(0, 1, 2)$  maps to exactly one output. The pair  $(1, 5)$  appears twice, but that's not a problem—there aren't two *different* outputs for the same input.

**(b)** Domain =  $\{0, 1, 2\}$ . Range =  $\{2, 5\}$ .

2. (12 points)
- Fix the relation (table view).**

$x$	$y$
-1	3
0	0
1	4
1	<input type="text"/>

**Solution: (a)** To be a function, the repeated input  $x = 1$  must produce the *same* output both times. So the blank must be 4.

**(b)** New relation:  $\{(-1, 3), (0, 0), (1, 4)\}$  (we can omit duplicates).

3. (14 points)
- Function evaluation (numbers and constants).**

$$f(x) = 3x - 4.$$

**Solution: (a)**  $f(0) = 3(0) - 4 = -4$ .    **(b)**  $f(5) = 15 - 4 = 11$ .    **(c)**  $f(-2) = 3(-2) - 4 = -6 - 4 = -10$ .

**(d)**  $f(a) = 3a - 4$  (treat  $a$  like a number).

**(e)**  $f(2a + 1) = 3(2a + 1) - 4 = 6a + 3 - 4 = 6a - 1$ .

4. (12 points)
- Solve for the missing number.**

$$g(x) = k - 2x.$$

**Solution:** (a)  $g(4) = k - 2(4) = k - 8 = 9 \Rightarrow k = 17$ .

(b)  $g(x) = 1 \Rightarrow k - 2x = 1 \Rightarrow -2x = 1 - k \Rightarrow x = \frac{k - 1}{2}$ .

(If using  $k = 17$  from part (a), then  $x = \frac{16}{2} = 8$ .)

5. (12 points) **Plain-English interpretation.**

$$p(x) = 2x + 6.$$

**Solution:** (A) **True.**  $p(4) = 2 \cdot 4 + 6 = 14$  means input 4 gives output 14.

(B) **True.**  $p(a) = 2a + 6$  even if  $a$  is unknown—function rules work for any input.

(C) **True.** Solve  $2x + 6 = 10 \Rightarrow 2x = 4 \Rightarrow x = 2$ .