



## Dieting Model

Dieting is now days a concern to many individuals in which they practice the intake of food in a regulated way to prevent and treat diseases and to maintain body mass.

So our aim here is to construct a mathematical model of dieting process and investigate the properties of its solutions. The main significance of the model is to provides important insights (and guides to a biomedical issue that is of interest to the general public).

~~First~~ To start with model we have to make some assumptions as below.

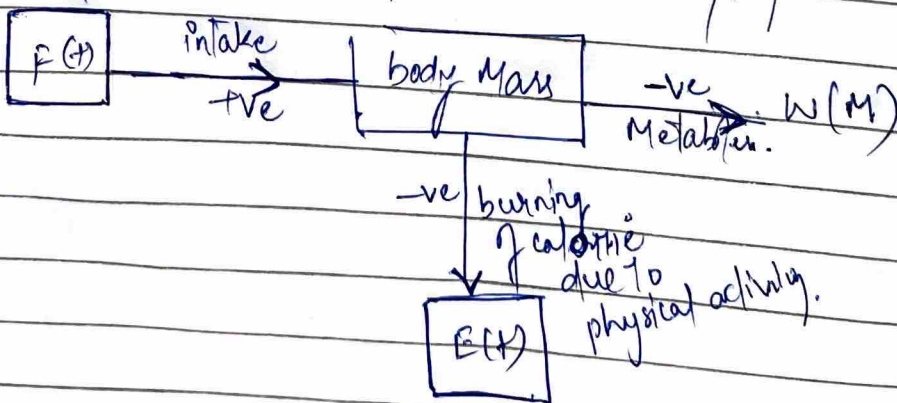
- $M(t)$ : body mass of the individual at time  $t$
- $F(t)$ : food intake of the individual at time  $t$
- $E(t)$ : physical activity level at time  $t$
- $W(M)$ : Metabolism level which depends on  $M(t)$ .

Our aim is to find the mass at time  $t$ .

i.e we construct a ymc of the form

$$\frac{dM}{dt} = f(F(t), E(t), W(M))$$

and by try to represent it graphically then





Then  $\frac{dM}{dt}$  can be written as

$$\frac{dM}{dt} = F(M) - E(M) - W(M) \quad \text{--- (I)}$$

where  $W(M) \propto M^{3/4}$  for our case.

i.e.  $W(M) = BM^{3/4}$ , as  $B$  is a true constant.

$\therefore$  (I) becomes

$$\boxed{\frac{dM}{dt} = F(M) - E(M) - BM^{3/4}} \rightarrow \text{(II)}$$

Simplification Condition:

The main Issue is what are  $F(M)$  and  $E(M)$ , as we have to consumed fixed quantity of calories in a Dieting within some fixed interval of time. i.e. the intake of food is fixed in a day,  $F(M)$  is fixed say  $\bar{F}$ . and Also in a Dieting the physical activity is done with a target to burn some fixed value of calories, within the so say  $E(M)$  is fixed as  $\bar{E}$  in a day.

Then the result-value of  $[F(M) - E(M)]$  is

$$\underbrace{[F(M) - E(M)]}_{\text{average}} \approx \bar{F} - \bar{E} = \lambda \quad \text{(say)} \\ \text{--- constant}$$

where  $\lambda$  is the average value of energy (calories) needed for an individual under normal Dieting circumstances.

Now eq (II) becomes

$$\frac{dM}{dt} = F(M) - E(M) - BM^{3/4} = \lambda - BM^{3/4}$$

Time Scale: Here we try to find the number of days required for an individual to make an significant changes in their body-mass.





and we denote these parameters as  $T^x$  with  
 $T^x = c \lambda^a \beta^b$ ;  $c = \text{constant}$

where  $a$  &  $b$  are constants to be determined

Now by  $[M] = \#$  i.e. the physical unit of mass is  
"#", then

physical unit of  $\lambda = [\lambda] = \frac{\#}{T} = \text{mass per time}$  and

physical unit of  $\beta = [\beta] = \frac{\#^{1/4}}{T}$ , for  $T = \text{time unit}$ .

$$\text{Thus } T^x = c \lambda^a \beta^b \Rightarrow [T^x] = [c] [\lambda]^a [\beta]^b$$
$$T = 1 \left( \frac{\#}{T} \right)^a \left( \frac{\#^{1/4}}{T} \right)^b$$

$$\Rightarrow T = \frac{\#^{a+b/4}}{T^{a+b}} \Rightarrow T = \#^{a+b/4} T^{-a-b}$$

Comparing LHS & RHS, we have

$$a+b/4 = 0 \quad -a-b = 0$$

solving for  $a$  &  $b$  we get  $a = \frac{1}{3}$  &  $b = -\frac{4}{3}$

$$\text{i.e. } T^x = \frac{\lambda^{1/3}}{\beta^{4/3}} \text{ by choosing } c=1.$$