

① 9 先飞, 飞到  $\angle 1 + \angle 2 = 60^\circ$

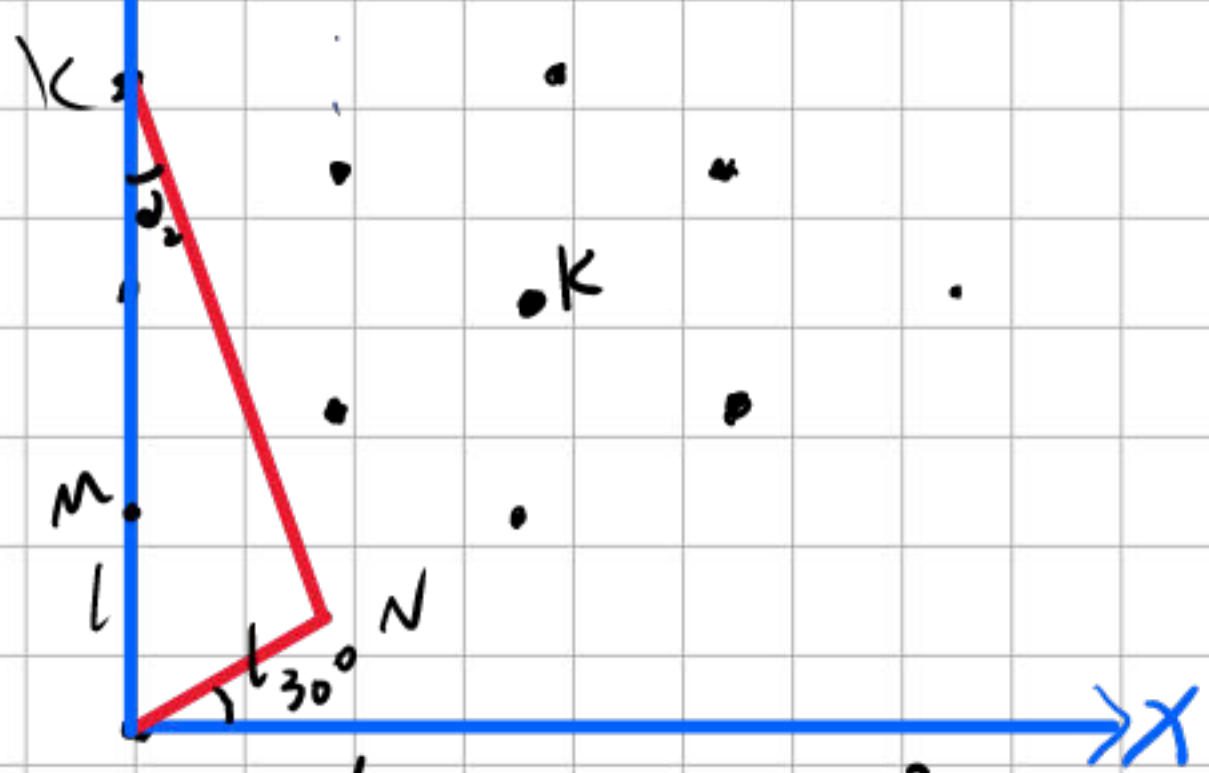
② 14 飞 (保持  $\angle 1 + \angle 2 = 60^\circ$ , 且  $\angle 3 + \angle 4 = 120^\circ$ )

③ 10 飞 (保持  $\angle 1 + \angle 2 = 60^\circ$ , 且  $\angle 5 + \angle 6 = 120^\circ$ )

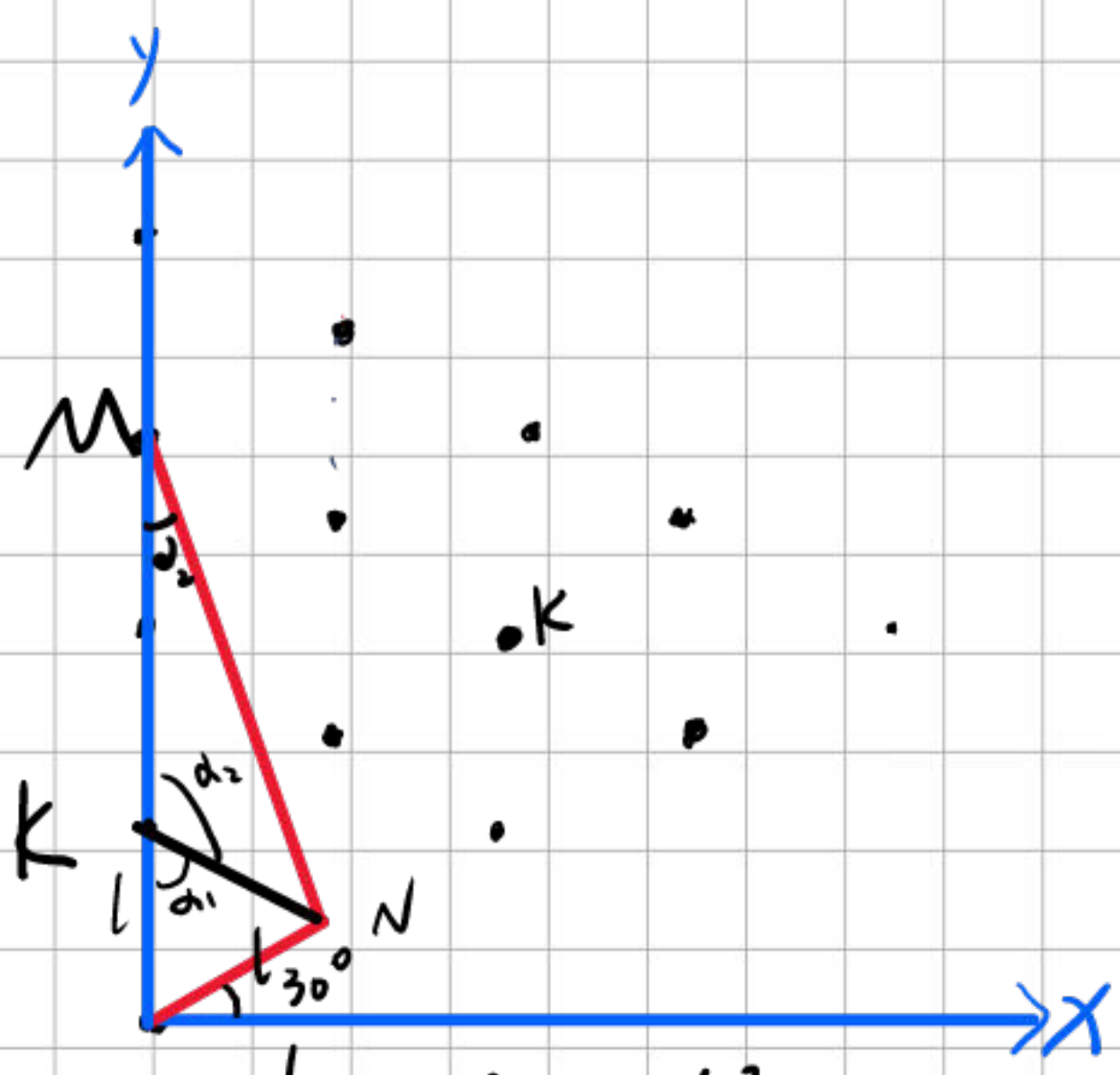
则 15, 14, 9, 10 四点之点在 2 号边上 (证略)

MN 都在 2 号边上

共线



$$OK = \frac{L}{\sin \alpha_2} \cdot \sin(\alpha_2 + 60^\circ)$$



$$OK = \frac{L}{\sin \alpha_1} \cdot \sin(\alpha_1 + 60^\circ)$$

OMN 在外部

$$\begin{cases} \frac{\sin \alpha_1}{OM} = \frac{\sin \angle MNK}{OK} \\ \frac{\sin \alpha_2}{ON} = \frac{\sin \angle MNK}{OK} \end{cases} \Rightarrow \frac{\sin \angle MNK}{\sin \angle ONK} = \frac{\sin \alpha_1 \cdot ON}{\sin \alpha_2 \cdot OM}$$

$$(\alpha_1 + \alpha_2 + 60^\circ) + \angle OMK + \angle ONK = 2\pi$$

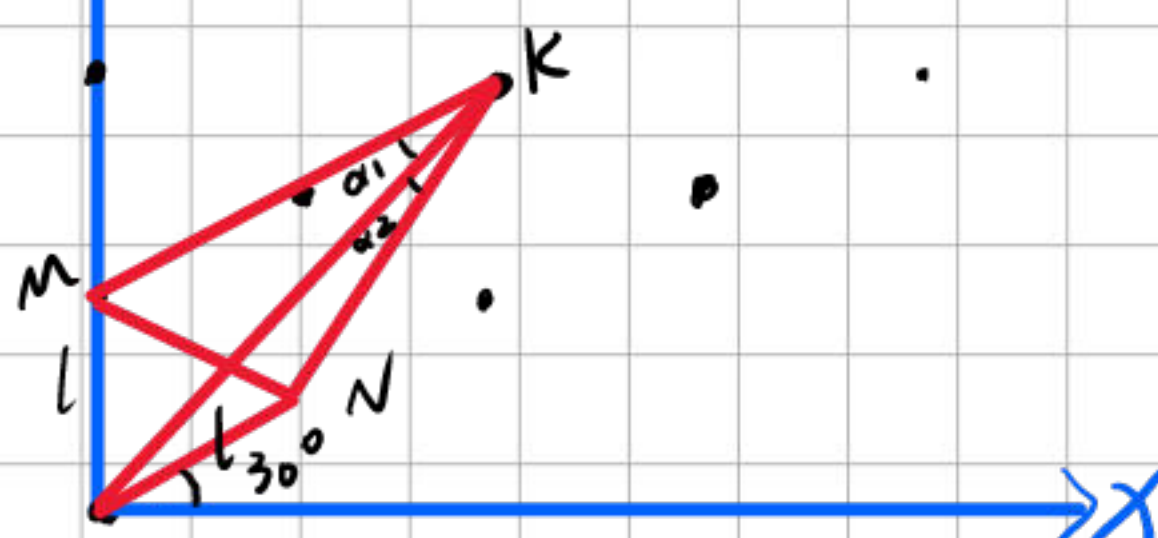
$$\angle OMK = 2\pi - [(\alpha_1 + \alpha_2 + 60^\circ) + \angle ONK]$$

$$\sin \angle OMK = -\sin[(\alpha_1 + \alpha_2 + 60^\circ) + \angle ONK]$$

$$\frac{ON \cdot \sin \alpha_1}{OM \cdot \sin \alpha_2} \sin \angle OMK = -\sin(\alpha_1 + \alpha_2 + 60^\circ) \cos \angle ONK - \cos(\alpha_1 + \alpha_2 + 60^\circ) \sin \angle ONK$$

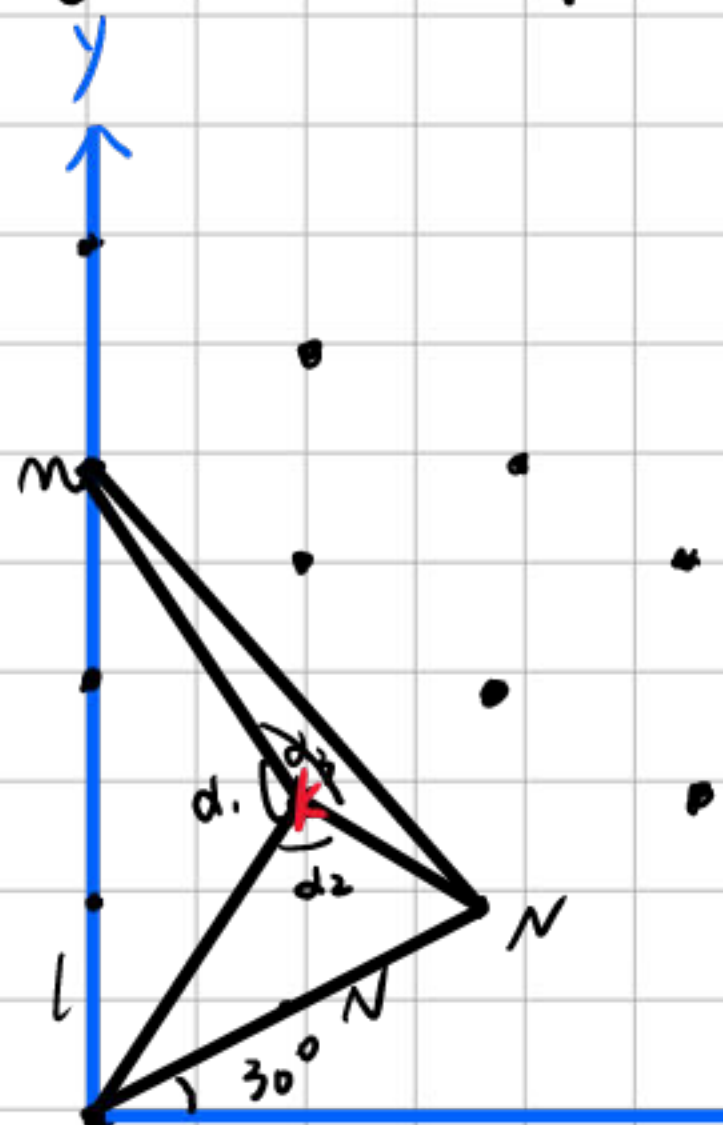
$$\tan \angle ONK = -\frac{\sin(\alpha_1 + \alpha_2 + 60^\circ)}{\frac{ON \cdot \sin \alpha_1}{OM \cdot \sin \alpha_2} + \cos(\alpha_1 + \alpha_2 + 60^\circ)}$$

$$OK = \sin \angle ONK \cdot \frac{ON}{\sin \alpha_2}$$





OMN 内部



$$\begin{cases} \frac{\sin \alpha_1}{OM} = \frac{\sin \angle OMK}{OK} \\ \frac{\sin \alpha_2}{ON} = \frac{\sin \angle ONK}{OK} \end{cases} \Rightarrow \frac{\sin \angle OMK}{\sin \angle ONK} = \frac{ON \cdot \sin \alpha_1}{OM \cdot \sin \alpha_2}$$

$$\alpha_1 + \alpha_2 + 60^\circ + \angle OMK + \angle ONK = 2\pi$$

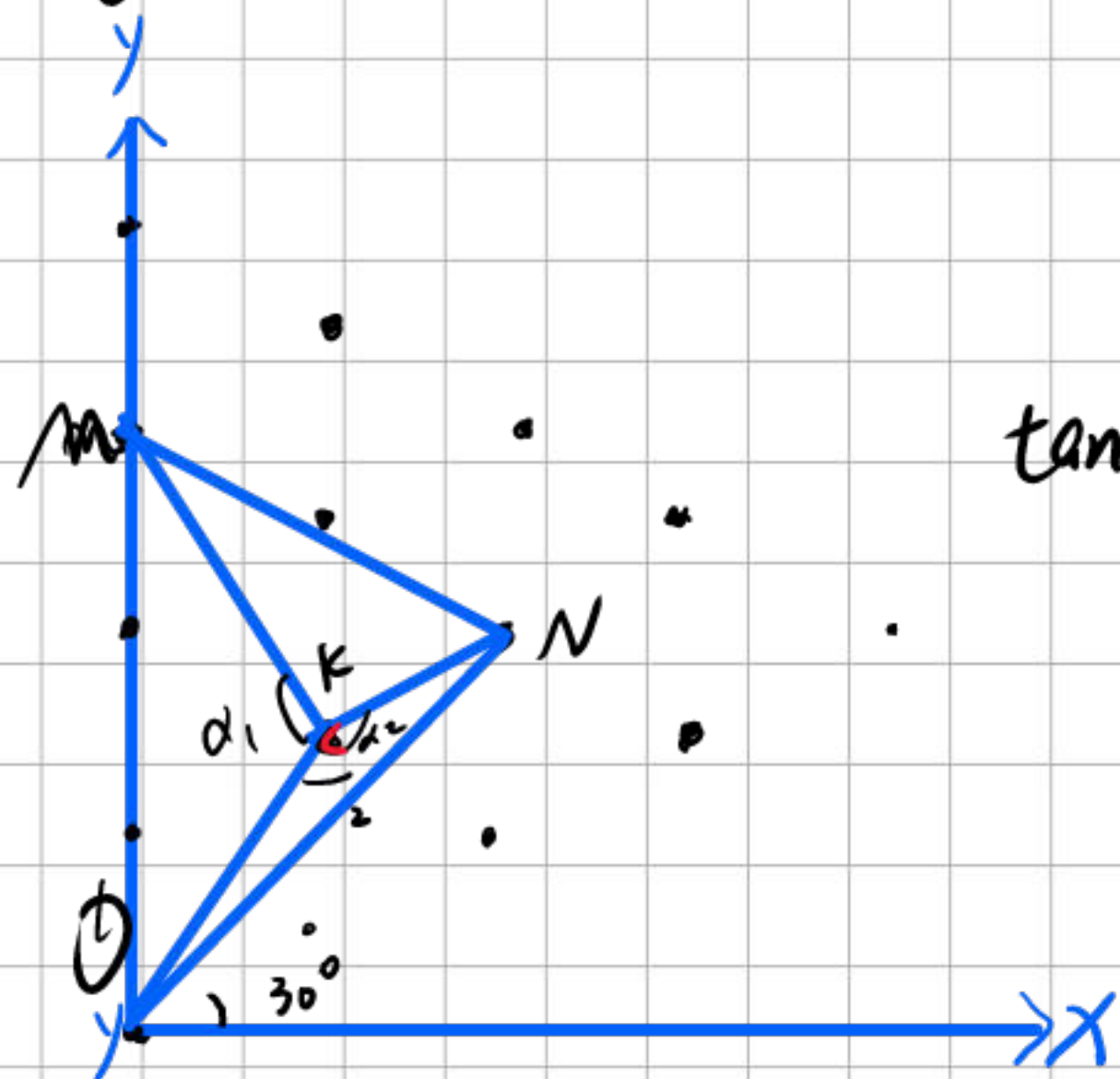
$$\angle OMK = 2\pi - (\alpha_1 + \alpha_2 + 60^\circ) + \angle ONK$$

$$\frac{ON \cdot \sin \alpha_1}{OM \cdot \sin \alpha_2} \sin \angle ONK = -\sin(\alpha_1 + \alpha_2 + 60^\circ) \cos \angle ONK - \cos(\alpha_1 + \alpha_2 + 60^\circ) \sin \angle ONK$$

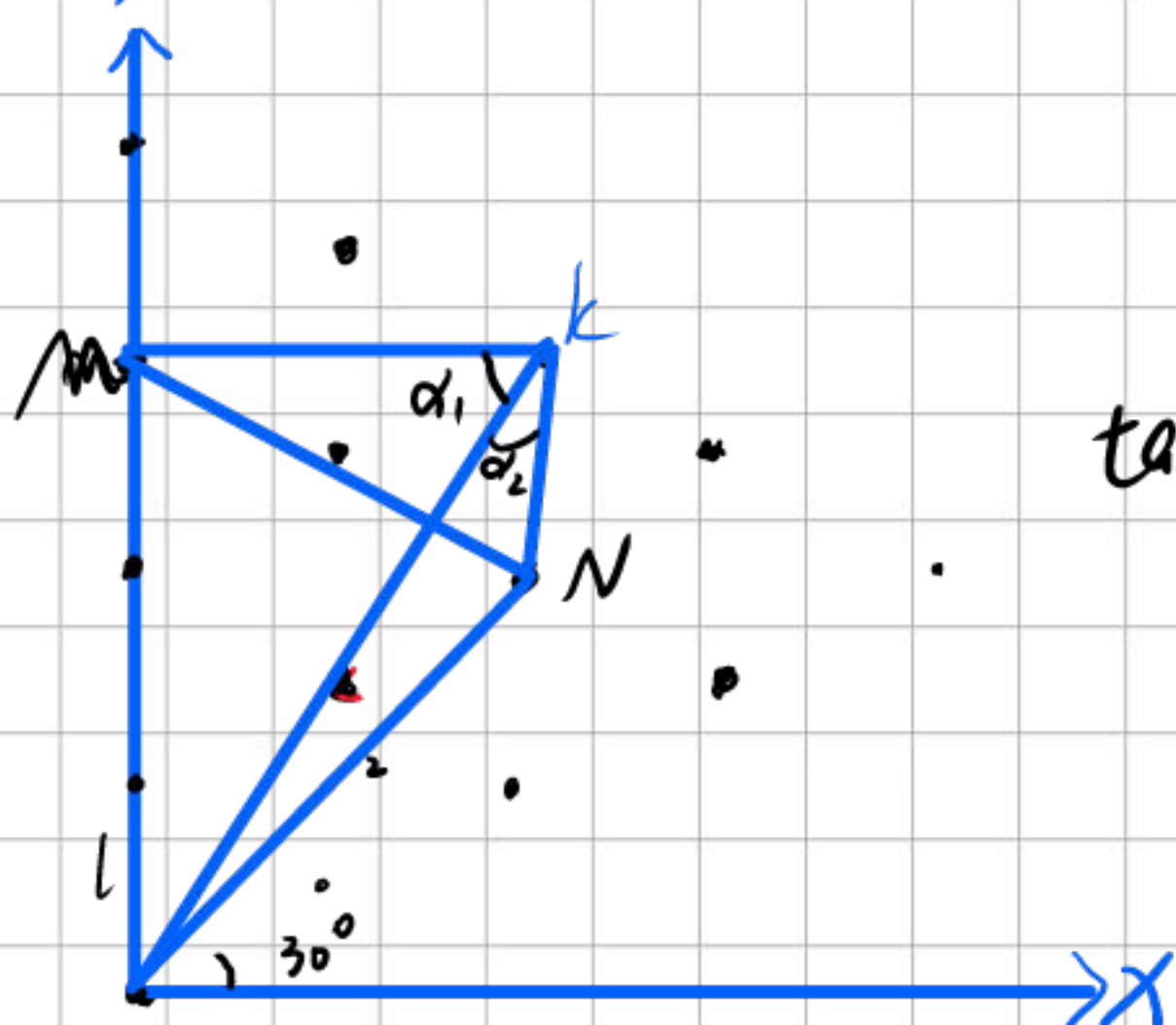
$$\tan \angle ONK = -\frac{\sin(\alpha_1 + \alpha_2 + 60^\circ)}{\frac{ON \cdot \sin \alpha_1}{OM \cdot \sin \alpha_2} + \cos(\alpha_1 + \alpha_2 + 60^\circ)}$$

$$OK = \sin \angle ONK \cdot \frac{ON}{\sin \alpha_2}$$

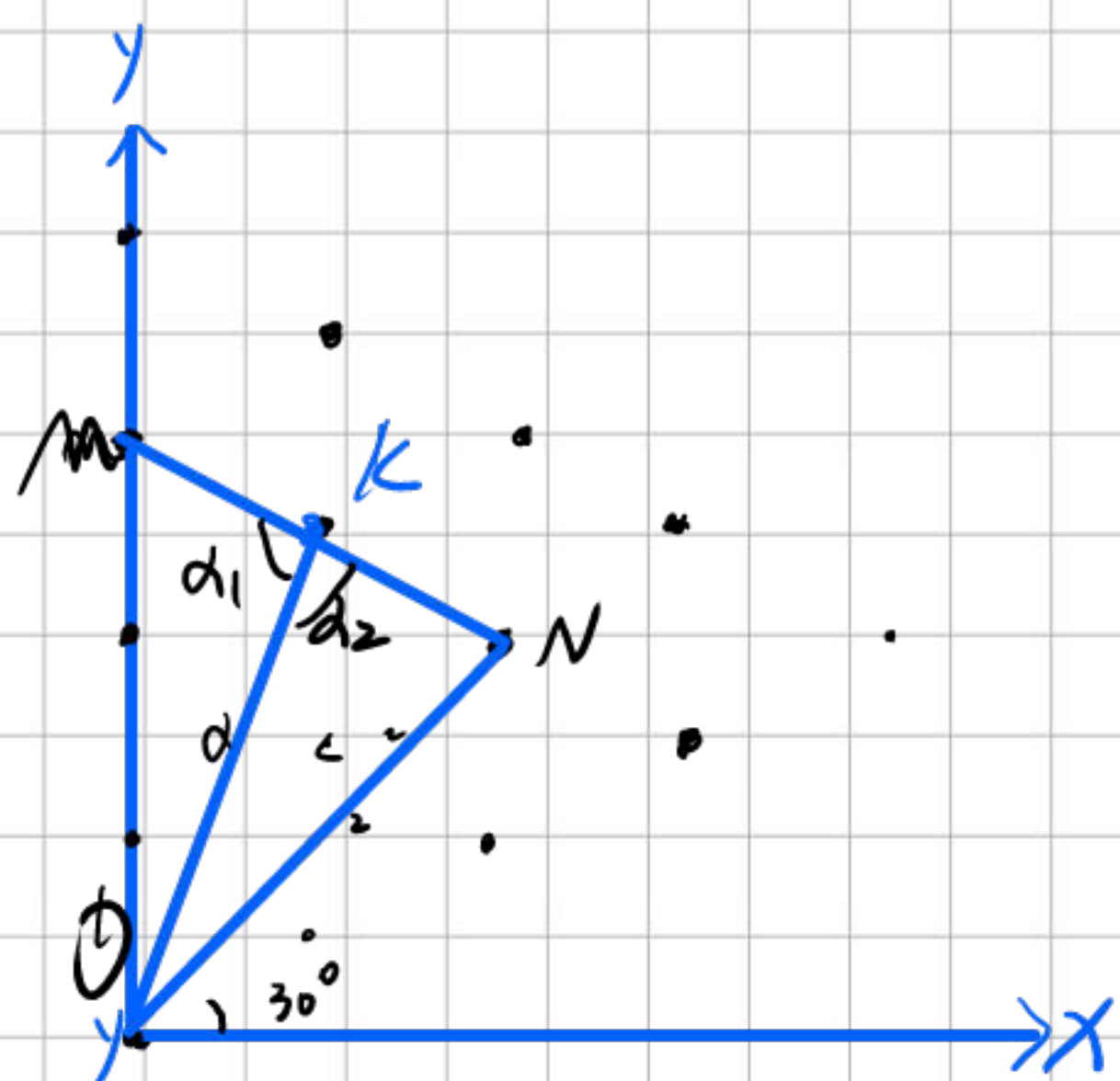
一个在边上, 一个不在边上



$$\tan \angle ONK = -\frac{\sin(\alpha_1 + \alpha_2 + 60^\circ)}{\frac{ON \cdot \sin \alpha_1}{OM \cdot \sin \alpha_2} + \cos(\alpha_1 + \alpha_2 + 60^\circ)} \quad OK = \sin \angle ONK \cdot \frac{ON}{\sin \alpha_2}$$



$$\tan \angle ONK = -\frac{\sin(\alpha_1 + \alpha_2 + 60^\circ)}{\frac{ON \cdot \sin \alpha_1}{OM \cdot \sin \alpha_2} + \cos(\alpha_1 + \alpha_2 + 60^\circ)} \quad OK = \sin \angle ONK \cdot \frac{ON}{\sin \alpha_2}$$



$$\begin{cases} \frac{\sin \alpha_1}{OM} = \frac{\sin \angle ONK}{OK} \\ \frac{\sin \alpha_2}{ON} = \frac{\sin \angle ONK}{OK} \end{cases} \Rightarrow \frac{\sin \angle ONK}{\sin \angle ONK} = \frac{ON \sin \alpha_1}{OM \sin \alpha_2} = \frac{ON}{OM}$$

$$\angle OMK + \angle ONK + \angle MON = \pi$$

$$\sin \angle ONK = \sin \angle ONK \cos \angle MON + \cos \angle ONK \sin \angle MON$$

$$\frac{ON}{OM} \tan \angle ONK = \tan \angle ONK \cos \angle MON + \sin \angle MON$$

$$\tan \angle ONK = \frac{\sin \angle MON}{\frac{ON}{OM} - \cos \angle MON}$$

$$OK = \frac{ON}{\sin \alpha_2} \cdot \sin \angle ONK$$

2个点在三角形

