## ZajecieSVD

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```
Sprawozdanie
Matematyka Konkretna
Prowadzący: prof. dr hab. Vasyl Martsenyuk
Laboratorium 1
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Analiza macierzowa w informatyce
Wariant 10
http://databookuw.com/page-2/page-4/
https://machinelearningmastery.com/singular-value-decomposition-for-machine-learning/
```

## 1 Calculation of SVD

```
[2]: # Singular-value decomposition
     from numpy import array
     from scipy.linalg import svd
     # define a matrix
     A = array([[1, 2], [3, 4], [5, 6]])
     print(A)
     # SVD
     U, s, VT = svd(A)
     print(U)
     print(s)
     print(VT)
    [[1 \ 2]]
     [3 4]
     [5 6]]
    [[-0.2298477
                   0.88346102 0.40824829]
     [-0.52474482 0.24078249 -0.81649658]
     [-0.81964194 -0.40189603 0.40824829]]
    [9.52551809 0.51430058]
    [[-0.61962948 -0.78489445]
     [-0.78489445 0.61962948]]
```

## 2 Pseudoinverse matrix

If  $A = U\Sigma V^T$  then pseudoinverse matrix is defind as

```
A^+ = VD^+U^T
     If \Sigma = \begin{bmatrix} s11 & 0 & 0\\ 0 & s22 & 0\\ 0 & 0 & s33 \end{bmatrix}
     then
    D^+ = \begin{bmatrix} 1/s11 & 0 & 0 \\ 0 & 1/s22 & 0 \\ 0 & 0 & 1/s33 \end{bmatrix}
[3]: # Pseudoinverse
     from numpy import array
     from numpy.linalg import pinv
     # define matrix
     A = array([
               [0.1, 0.2],
               [0.3, 0.4],
               [0.5, 0.6],
               [0.7, 0.8]])
     print(A)
     # calculate pseudoinverse
     B = pinv(A)
     print(B)
     [[0.1 0.2]
      [0.3 \ 0.4]
      [0.5 0.6]
      [0.7 0.8]]
     [[-1.00000000e+01 -5.00000000e+00 1.28785871e-14 5.00000000e+00]
      [8.50000000e+00 4.50000000e+00 5.00000000e-01 -3.50000000e+00]]
[4]: # Pseudoinverse via SVD
     from numpy import array
     from numpy.linalg import svd
     from numpy import zeros
     from numpy import diag
     # define matrix
     A = array([
      [0.1, 0.2],
      [0.3, 0.4],
       [0.5, 0.6],
       [0.7, 0.8]])
     print(A)
     # calculate svd
     U, s, VT = svd(A)
     # reciprocals of s
     d = 1.0 / s
```

# create m x n D matrix

```
D = zeros(A.shape)
# populate D with n x n diagonal matrix
D[:A.shape[1], :A.shape[1]] = diag(d)
# calculate pseudoinverse
B = VT.T.dot(D.T).dot(U.T)
print(B)

[[0.1 0.2]
[0.3 0.4]
[0.5 0.6]
[0.7 0.8]]
[[-1.00000000e+01 -5.00000000e+00 1.28508315e-14 5.0000000e+00]
[ 8.50000000e+00 4.50000000e+00 5.00000000e-01 -3.50000000e+00]]
```

## 3 Reduction of dimension

```
[5]: from matplotlib.image import imread
   import matplotlib.pyplot as plt
   import numpy as np
   import os
   plt.rcParams['figure.figsize'] = [16,8]
[6]: A = imread('10.webp')
```

```
[6]: A = imread('10.webp')
X = np.mean(A,-1) # convert RGB to grayscale

#img = plt.imshow(256-X)
img = plt.imshow(X)
img.set_cmap('gray')
plt.axis('off')
plt.show()
```

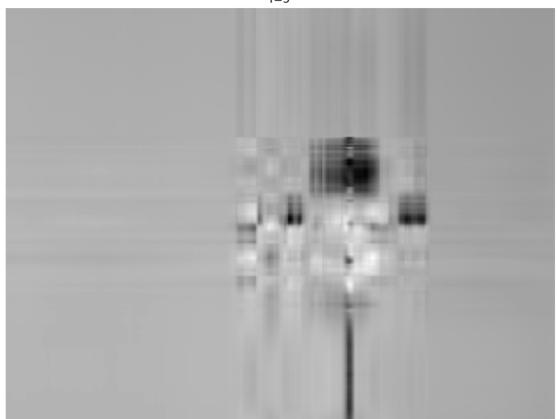


```
[7]: U, S, VT = np.linalg.svd(X,full_matrices=False)
    print(S.shape)
    S = np.diag(S)

j=0
    for r in (5,20,38,100,650):
        # Construct approximate image
        Xapprox = U[:,:r]@S[0:r,:r]@VT[:r,:]
        plt.figure(j+1)
        j += 1
        #img = plt.imshow(256-Xapprox)
        img = plt.imshow(Xapprox)
        img.set_cmap('gray')
        plt.axis('off')
        plt.title('r='+str(r))
        plt.show()
```

(600,)



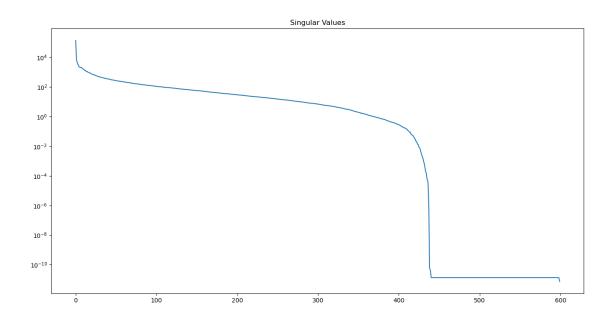


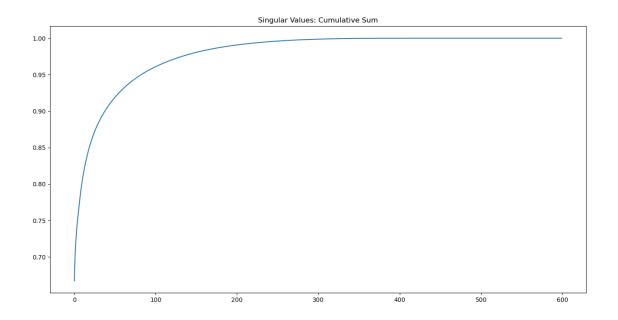












Aby zachować 90% informacji, należy użyć około 38 wartości singularnych