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## Accelerated and interpretable oblique random survival forests --Manuscript Draft--

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Abstract:	The oblique random survival forest (RSF) is an ensemble supervised learning method for right censored outcomes. Trees in the oblique RSF are grown using linear combinations of predictors, whereas in the standard RSF, a single predictor is used. Oblique RSF ensembles have high prediction accuracy, but assessing many linear combinations of predictors induces high computational overhead. In addition, few methods have been developed for estimation of variable importance (VI) with oblique RSFs. We introduce a method to increase computational efficiency of the oblique RSF and a method to estimate VI with the oblique RSF. Our computational approach uses Newton-Raphson scoring in each non-leaf node, We estimate VI by negating each coefficient used for a given predictor in linear combinations, and then computing the reduction in out-of-bag accuracy. In benchmarking experiments, we find our implementation of the oblique RSF is hundreds of times faster, with equivalent prediction accuracy, compared to existing software for oblique RSFs. We find in simulation studies that 'negation VI' discriminates between relevant and irrelevant numeric predictors more accurately than permutation VI, Shapley VI, and a technique to measure VI using analysis of variance. All oblique RSF methods in the current study are available in the aorsf R package.
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November 16, 2022

#### Journal of Biomedical Informatics

#### Dear Editors:

We are writing to submit our manuscript "Accelerated and interpretable oblique random survival forests" to the *Journal of Biomedical Informatics*.

Our manuscript studies the computational efficiency and interpretability of oblique random survival forests, which is important because oblique random survival forests have high prediction accuracy but high computational overhead and few methods have been developed to interpret them. This paper extends our previous work in *Annals of Applied Statistics*, Oblique Random Survival Forests (DOI: 10.1214/19-AOAS1261), by addressing the computational inefficiency and difficulty of interpreting oblique random survival forests.

We suggest the following reviewers:

- Terry M. Therneau, Mayo Clinic (therneau@mayo.edu)
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Our submission has the following keywords: Oblique, Survival, Random Forests, Fast, Variable Importance

As the corresponding author, I confirm that none of the co-authors listed below have a conflict of interest with the action editors and referees I suggest above. Further, I confirm that all co-authors below consent to my submission of this manuscript to the *Journal of Biomedical Informatics*.

#### Sincerely,

Byron C. Jaeger (Wake Forest University School of Medicine)
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## ACCELERATED AND INTERPRETABLE OBLIQUE RSF

Oblique RSFs have excellent prediction accuracy but are computationally inefficient and difficult to interpret. We propose two methods to advance the oblique RSF:

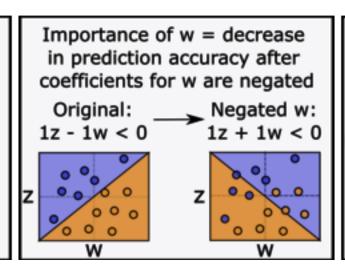
## Accelerate with partial Newton Raphson scoring

## Interpret with negation VI

### Results

Newton Raphson algorithm								
i	coefficients	converged						
0	0.0, 0.0	no						
1	0.2, -1.3	no						
2	0.4, -0.7	no						
3	0.3, -0.8	no						
4	0.3, -0.8	yes						

coefficients at i = 1 are good enough for oblique trees



1000x faster vs. SoA oblique RSF method (equivalent prediction accuracy)
12% increase in index of prediction accuracy vs. eight SoA ML methods.
2.8% increase in chance to rank signal over noise variable

vs five SoA VI methods

**Problem** Risk prediction may reduce the burden of disease by guiding strategies for prevention and treatment in a wide range of domains, but accurate and interpretable prediction models are needed.

**What is Already Known** The oblique random survival forest has exceptional prediction accuracy, but it is also computationally inefficient and lacks tools for interpretation.

What This Paper Adds This study introduces methodology that improves the computational efficiency and interpretation of oblique random survival forests. We show that fitting oblique random survival forests with partial Newton Raphson scoring is hundreds of times faster than existing methods with no loss of prediction accuracy. We also introduce a novel method to estimate variable importance with oblique random survival forests that outperforms state of the art methods when used to discriminate between relevant and irrelevant continuous predictors.

Conflict of Interest Statement

#### **Declaration of interests**

⊠The authors declare that they have no known competing financial interests or personal relationships
that could have appeared to influence the work reported in this paper.
□The authors declare the following financial interests/personal relationships which may be considered
as potential competing interests:

# ACCELERATED AND INTERPRETABLE OBLIQUE RANDOM SURVIVAL FORESTS

#### A PREPRINT

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#### **ABSTRACT**

The oblique random survival forest (RSF) is an ensemble supervised learning method for right-censored outcomes. Trees in the oblique RSF are grown using linear combinations of predictors, whereas in the standard RSF, a single predictor is used. Oblique RSF ensembles have high prediction accuracy, but assessing many linear combinations of predictors induces high computational overhead. In addition, few methods have been developed for estimation of variable importance (VI) with oblique RSFs. We introduce a method to increase computational efficiency of the oblique RSF and a method to estimate VI with the oblique RSF. Our computational approach uses Newton-Raphson scoring in each non-leaf node, We estimate VI by negating each coefficient used for a given predictor in linear combinations, and then computing the reduction in out-of-bag accuracy. In benchmarking experiments, we find our implementation of the oblique RSF is hundreds of times faster, with equivalent prediction accuracy, compared to existing software for oblique RSFs. We find in simulation studies that 'negation VI' discriminates between relevant and irrelevant numeric predictors more accurately than permutation VI, Shapley VI, and a technique to measure VI using analysis of variance. All oblique RSF methods in the current study are available in the aorsf R package.

Keywords Oblique · Survival · Random Forests · Fast · Variable Importance

#### 1 Introduction

Risk prediction may reduce the burden of disease by guiding strategies for prevention and treatment in a wide range of domains [Moons et al., 2012a,b]. The random survival forest (RSF; Ishwaran et al. [2008], Hothorn et al. [2006]) is a supervised learning algorithm that has been used frequently for risk prediction [Wang and Li, 2017]. Similar to random forests (RFs) for classification and regression [Breiman, 2001], The RSF is a large set of de-correlated and randomized decision trees, with each tree contributing to the ensemble's prediction function. Notable characteristics of the RSF include uniform convergence of its ensemble survival prediction function to the true survival function, first shown by Ishwaran and Kogalur [2010] and later by Cui et al. [2017] under more general conditions. However, Cui et al. [2017] noted that the RSF is at a disadvantage when predictors are correlated and some are not relevant to the censored outcome, which is a strong possibility when large clinical and 'omic' databases are leveraged for risk prediction.

A potential approach to improve the RSF when predictors are correlated and some are not relevant to the censored outcome is to use oblique trees instead of axis based trees. Axis based trees split data using a single predictor, creating decision boundaries that are perpendicular or parallel to axes of the predictor space [see Breiman et al., 2017, Chapter 2]. Oblique trees split data using a linear combination of predictors, creating decision boundaries that are neither parallel nor perpendicular to axes of their contributing predictors [see Breiman et al., 2017, Chapter 5]. Menze et al. [2011] examined prediction accuracy of RFs in the presence of correlated predictors and found that oblique RFs had substantially higher prediction accuracy compared to axis-based RFs. Similarly, Jaeger et al. [2019] found that growing RSFs with oblique rather than axis-based survival trees reduced the RSF's concordance error, with improvements ranging from 2.5% to 24.9% depending on the data analyzed.

Despite the potential for higher accuracy, oblique trees have at least two notable drawbacks compared to axis-based trees. First, finding a locally optimal oblique decision rule may require exponentially more computation than an axis-based rule. If p predictors are potentially used to split n observations, up to  $\mathcal{O}(n^p)$  oblique splits can be assessed versus  $\mathcal{O}(n \cdot p)$  axis-based splits [Heath et al., 1993, Murthy et al., 1994]. Second, estimating variable importance (VI) using permutation (a standard method for RFs) may be less effective in ensembles of oblique trees, as permuting the values of one predictor may not destabilize decisions that are based on linear combinations of predictors. Although VI is one of the most widely used strategies to interpret random forests [Ishwaran and Lu, 2019], few studies have investigated VI for oblique random forests [see Menze et al., 2011, Section 5], and fewer have investigated VI specifically for the oblique RSF.

The aim of this paper is to introduce methodology that improves the computational efficiency and interpretation of oblique RSFs. Section 2 reviews prior studies that have developed methods related to those introduced in the current study. In Section 3, we reduce the computational cost of oblique RSFs (*i.e.*, accelerate them) with a scalable algorithm to identify linear combinations of coefficients. In Section 4, we improve the interpretability of oblique RSFs with 'negation VI', a method to estimate VI that flips the sign of coefficients in linear combinations of predictors instead of permuting predictor values. We evaluate these methods with general benchmarking experiments and simulation studies in Section 5. In Section 6, we summarize results from the current study and present ideas connecting the current work to existing frameworks and methods for RSFs that future studies may engage with. All oblique RSF methods introduced are available in the aorsf R package [Jaeger et al., 2022].

#### 2 Related work

Sections 2.1 and 2.2 briefly summarize prior studies that have developed methods related to the oblique RSF and VI, respectively.

#### 2.1 Axis-based and oblique random forests

After Breiman [2001] introduced the axis-based and oblique RF, numerous methods were developed to grow oblique RFs for classification or regression tasks [Menze et al., 2011, Zhang and Suganthan, 2014, Rainforth and Wood, 2015, Zhu et al., 2015, Poona et al., 2016, Qiu et al., 2017, Tomita et al., 2020, Katuwal et al., 2020]. However, oblique splitting approaches for classification or regression may not generalize to censored outcomes [*e.g.*, see Zhu, 2013, Section 4.5.1], and most research involving the RSF has focused on forests with axis-based trees [Wang and Li, 2017].

Building on prior research for bagging survival trees [Hothorn et al., 2004], Hothorn et al. [2006] developed an axis-based RSF in their framework for unbiased recursive partitioning, more commonly referred to as the conditional inference forest (CIF). Zhou et al. [2016] developed a rotation forest based on the CIF and Wang and Zhou [2017] developed a method for extending the predictor space of the CIF. Ishwaran et al. [2008] developed an axis-based RSF with strict adherence to the rules for growing trees proposed in Breiman [2001]. Jaeger et al. [2019] developed the

oblique RSF following the bootstrapping approach described in Breiman's original RF and incorporating early stopping rules from the CIF.

Fast algorithms to fit axis-based RSFs are available in the randomForestSRC R package [Ishwaran and Kogalur, 2019] and the ranger [Wright and Ziegler, 2017] R package. randomForestSRC provides a unified interface to grow RFs in a wide range of analyses, and ranger is designed to grow RFs efficiently using high dimensional data. Fast algorithms to fit the CIF are provided by the party R package [Hothorn et al., 2010], which provides a computational toolbox for recursive partitioning using conditional inference trees. Jaeger et al. [2019] developed the obliqueRSF package and found it was approximately 30 times slower than party and nearly 200 times slower than randomForestSRC. Few studies have developed software with fast algorithms for oblique RSFs that have comparable speed compared to algorithms for axis-based RSFs.

#### 2.2 Variable importance

Several techniques to estimate VI have been developed since Breiman [2001] introduced permutation VI, which is defined for each predictor as the difference in a RF's estimated prediction error before versus after the predictor's values are randomly permuted. Strobl et al. [2007] identified bias in permutation VI driven by variable selection bias and effects induced by bootstrap sampling, and proposed an unbiased permutation VI measure based on unbiased recursive partitioning [Hothorn et al., 2006]. Menze et al. [2011] introduced an approach to estimate VI for oblique RFs that computes an analysis of variance (ANOVA) table in non-leaf nodes to obtain p-values for each predictor contributing to the node. The ANOVA VI¹ is then defined for each predictor as the number of times a p-value associated with the predictor is  $\leq 0.01$  while growing a forest. Lundberg and Lee [2017] introduced a method to estimate VI using SHapley Additive exPlanation (SHAP) values, which estimate the contribution of a predictor to a model's prediction for a given observation. SHAP VI is computed for each predictor by taking the mean absolute value of SHAP values for that predictor across all observations in a given set. With the exception of Menze et al. [2011], few studies have evaluated estimation of VI using oblique RFs, and fewer have examined VI specifically for the oblique RSF.

#### 3 The accelerated oblique random survival forest

This section describes our approach to reduce computational overhead of the oblique RSF. Consider the usual framework for right-censored time-to-event outcomes with training data

$$\mathcal{D}_{ ext{train}} = \{(T_i, \delta_i, oldsymbol{x}_i)\}_{i=1}^{N_{ ext{train}}}$$
 .

Here,  $T_i$  is the event time if  $\delta_i = 1$  or the censoring time if  $\delta_i = 0$ , and  $x_i$  is a vector of predictors values. Assuming there are no ties, let  $t_1 < \ldots < t_m$  denote the m unique event times in  $\mathcal{D}_{\text{train}}$ .

To accelerate the oblique RSF, we propose to identify linear combinations of predictor variables in non-leaf nodes by applying Newton Raphson scoring to the partial likelihood function of the Cox regression model:

$$L(\boldsymbol{\beta}) = \prod_{i=1}^{m} \frac{e^{\boldsymbol{x}_{j(i)}^{T} \boldsymbol{\beta}}}{\sum_{j \in R_{i}} e^{\boldsymbol{x}_{j}^{T} \boldsymbol{\beta}}},$$
(1)

where  $R_i$  is the set of indices, j, with  $T_j \ge t_i$  (i.e., those still at risk at time  $t_i$ ), and j(i) is the index of the observation for which an event occurred at time  $t_i$ . Newton Raphson scoring is an exceptionally fast estimation procedure, and the survival package [Therneau, 2022a] includes documentation that outlines how to efficiently program it [Therneau, 2022b]. Briefly, a vector of length mtry (i.e., the number of randomly selected predictors) with estimated regression coefficients,  $\hat{\beta}$ , is updated in each step of the procedure based on its first derivative,  $U(\hat{\beta})$ , and second derivative,  $H(\hat{\beta})$ :

$$\hat{\beta}^{k+1} = \hat{\beta}^k + U(\hat{\beta} = \hat{\beta}^k) H^{-1}(\hat{\beta} = \hat{\beta}^k)$$

For statistical inference, it is recommended to continue updating  $\hat{\beta}$  by completing additional iterations of Newton Raphson scoring until a convergence threshold is met. However, since an estimate of  $\hat{\beta}$  is created by the first iteration of Newton Raphson scoring, only one iteration of Newton Raphson scoring is needed to identify a valid linear combination of predictors. Moreover, computing U and H requires computation and exponentiation of the vector  $\boldsymbol{x}\hat{\beta}$ , but these steps can be skipped on the first iteration of Newton Raphson scoring if an initial value of  $\hat{\beta}=0$  is chosen, allowing for a reduction in computing operations and removing the need to scale predictor values prior to initiating the Newton

<sup>&</sup>lt;sup>1</sup>Menze et al. [2011] name their method 'oblique RF VI', but we use the name 'ANOVA VI' in this article to avoid confusing Menze's approach with other approaches to estimate VI for oblique RFs.

Raphson algorithm.<sup>2</sup> In Section 5.1.6, we formally test whether growing oblique survival trees using one iteration of Newton Raphson scoring provides equivalent prediction accuracy compared to trees where iterations are completed until a convergence threshold is met.

Algorithm 1 presents our approach to fitting an oblique survival tree in the accelerated oblique RSF using default values from the aorsf R package. Several steps are taken to reduce computational overhead. First, memory is conserved by conducting bootstrap resampling via random integer-valued weights, rather than using a bootstrapped copy of the original data. Memory conservation also takes place in terminal nodes, where we restrict estimation of the survival and cumulative hazard function to event times that occur among observations in the node. Second, early stopping is applied to the tree-growing procedure if a statistical criterion is not met. In our case, the criterion is based on the magnitude of a log-rank test statistic corresponding to splitting the data at a current node. Third, instead of greedy recursive partitioning, we use 'good enough' partitioning. More specifically, instead of computing a log-rank test statistic for several different linear combinations of variables and proceeding with the highest scoring option, we identify an optimal cut-point for one linear combination of variables and assess whether using this combination will create a split that passes the criterion for splitting a node. If it does not pass the criterion, then another linear combination will be tested, with the maximum number of attempts set by the parameter n\_retry. Often a 'good-enough' split can be found in just one attempt when the training set is large, which gives the accelerated oblique RSF a computational advantage in larger training sets compared to greedy partitioning.

#### 4 Negation variable importance

This Section introduces negation VI, which is similar to permutation VI in that it measures how much a model's prediction error increases when a variable's role in the model is de-stabilized. Specifically, negation VI measures the increase in an oblique RF's prediction error after flipping the sign of all coefficients linked to a variable (*i.e.*, negating them). As negating a coefficient effectively flips decision boundaries around the corresponding predictor's axis, scaling numeric predictors to have a mean of zero and standard deviation of one is recommended.<sup>3</sup> For the current study, we use Harrell's concordance (C)-statistic [Harrell et al., 1982] to measure change in prediction error when computing negation VI.

A motivating problem for negation VI is that of correlated, numeric predictors. When two predictors are correlated and only one of them is relevant for prediction of an outcome, VI methods based on permutation are known to have upward bias in estimating the importance of the irrelevant predictor [Hooker et al., 2021]. Permutation may distort the joint distribution of predictors, which may in turn increase a model's estimated prediction error due to extrapolation. On the other hand, negating coefficients modifies the decision rule rather than modifying the data. Thus, we hypothesize that negation VI can be more effective at identifying important predictors for correlated, numeric predictors.

Negation VI has several helpful characteristics. First, negation VI generalizes to any oblique RF (*i.e.*, not just RSFs) using any valid error function, making it both general and flexible. Second, negation is non-random and hence reproducible without setting a random seed. Third, since negation VI does not permute variables, the analyst need not worry about impossible combinations of predictors that may occur when one predictor is randomly permuted, such as having a negative status for type 2 diabetes and having Hemoglobin A1c level  $\geq 6.5\%$  (a value indicative of type 2 diabetes) as a result of randomly permuting the values of Hemoglobin A1c.

#### 5 Numeric experiments

Sections 5.1 and 5.2 present numerical experiments examining the accelerated oblique RSF and negation VI, respectively. The code used to run these experiments is available online at https://github.com/bcjaeger/aorsf-bench. All analyses were conducted using R version 4.1.3 with version 0.0.4 of aorsf [Jaeger et al., 2022], and coordinated by the targets R package [Landau, 2021]. To standardize comparisons of computational efficiency, all learners and VI techniques used up to 4 processing units.

<sup>&</sup>lt;sup>2</sup>Predictors are scaled prior to initiating the Newton Raphson algorithm to avoid exponentiation of large numbers. However, if only one iteration is completed with an initial value of 0 for  $\hat{\beta}$ , then  $\exp(x\hat{\beta}) = 1$ .

<sup>&</sup>lt;sup>3</sup>The aorsf package automatically scales numeric inputs to a mean of zero and standard deviation of one.

<sup>&</sup>lt;sup>4</sup>The aorsf package enables customized functions to be applied in lieu of the default C-statistic.

#### **Algorithm 1** Accelerated oblique random survival tree using default parameters.

```
Require: Training data \mathcal{D}_{\text{train}} = \{(T_i, \delta_i, \boldsymbol{x}_i)\}_{i=1}^{N_{\text{train}}}, \text{ mtry } = \sqrt{\text{ncol}(\boldsymbol{x}_{\text{train}})}, \text{ n\_split } = 5, \text{ n\_retry } = 3, \text{ and } = 1, \dots, n\_\text{noted}
       split min stat = 3.841459
  1: \mathcal{T} \leftarrow \emptyset
  2: w \leftarrow \text{sample}(\text{from} = \{0, \dots, 10\}, \text{ size} = \text{nrow}(\boldsymbol{x}_{\text{train}}), \text{ replace} = T)
  3: \mathcal{D}_{\text{in-bag}} \leftarrow \text{subset}(\mathcal{D}_{\text{train}}, \text{ rows} = \text{which}(w > 0))
  4: w \leftarrow \text{subset}(w, \text{which}(w > 0))
  5: node_assignments \leftarrow rep(1, times = nrow(x_{in-bag}))
  6: nodes_{to}_{split} \leftarrow \{1\}
  7: while nodes_to_split \neq \emptyset do
  8:
             for node \in nodes to split do
 9:
                   n \text{ try} \leftarrow 1
10:
                   node\_rows \leftarrow which(node\_assignments \equiv node)
11:
                   node\_cols \leftarrow sample(from = \{1, ..., ncol(x)\}, size = mtry, replace = F)
12:
                   \mathcal{D}_{\text{node}} \leftarrow \text{subset}(\mathcal{D}_{\text{in-bag}}, \text{ rows} = \text{node\_rows}, \text{ columns} = \text{node\_cols})
                   \beta \leftarrow \text{newt\_raph}(\mathcal{D}_{\text{node}}, \text{ weights} = \text{subset}(w, \text{node\_rows}), \text{ max\_iter} = 1)
13:
14:
                   \eta \leftarrow \boldsymbol{x}_{\text{node}} \times \beta
                   \mathcal{C} \leftarrow \text{sample}(\text{from} = \text{unique}(\eta), \text{size} = \text{n split, replace} = \text{F})
15:
                   c \leftarrow \operatorname{argmax}_{c^* \in \mathcal{C}} \left\{ \operatorname{log\_rank\_stat}(\eta, c^*) \right\}
16:
                   if \log_{\text{rank\_stat}}(\eta, c) \ge \text{split\_min\_stat} then
17:
                         \mathcal{T} \leftarrow \text{add\_node}(\mathcal{T}, \text{ name} = \text{node}, \text{ beta} = \beta, \text{ cutpoint} = c)
18:
19:
                        ▷ Right node logic omitted for brevity (identical to left node logic)
20:
                        node_left_name \leftarrow max(node_assignments) + 1
                        node left rows \leftarrow subset(node rows, which(\eta < c))
21:
22:
                        subset(node assignments, node left rows) \leftarrow node left name
23:
                        if is_splittable(subset(node_assignments, node_left_rows)) then
                               nodes to split \leftarrow nodes to split \cup node left name
24:
25:
                        else
                               \mathcal{T} \leftarrow add\_leaf(\mathcal{T}, data = subset(\mathcal{D}_{node}, rows = node\_left\_rows))
26:
                        end if
27:
                   else if n_{try} \le n_{try} then
28:
29:
                        n_{try} \leftarrow n_{try} + 1
30:
                        go to 11
31:
                   else
32:
                         \mathcal{T} \leftarrow \text{add\_leaf}(\mathcal{T}, \, \text{data} = \mathcal{D}_{\text{node}})
33:
34:
                   nodes\_to\_split \leftarrow nodes\_to\_split \setminus \{node\}
35:
             end for
36: end while
37: return \mathcal{T}
```

#### 5.1 Benchmark of prediction accuracy

The aim of this numeric experiment is to evaluate the prediction accuracy of the accelerated oblique RSF compared to its predecessor (the oblique RSF from the obliqueRSF R package) and to several other machine learning algorithms. Inferences drawn from this experiment include equivalence and inferiority tests based on Bayesian linear mixed models.

#### 5.1.1 Learners

We consider four classes of learners: RSFs (both axis-based and oblique), boosting ensembles, regression models, and neural networks. Specific learners from each class are summarized in Table 1. To facilitate fair comparisons, tuning parameters were harmonized within each class. For example, for RSF learners, we set the minimum node size (a parameter shared by all RSF learners) as 10. Additionally, for RSF learners, the number of randomly selected predictors was the square root of the total number of predictors rounded to the nearest integer, and the number of trees in the ensemble was 500 (a common default value for the number of trees). For boosting, regression, and neural network learners, nested cross-validation was applied to tune relevant model parameters. Specifically, tuning for boosting models included identifying the number of steps to complete. For regression models, tuning was used to identify the magnitude of penalization. For neural networks, the number and density of layers was tuned.

Learner Class	Software	Learners	Description
Random Surviv	al Forests		
Axis based	RandomForestSRC ranger party rotsf rsfse	rsf-standard rsf-extratrees cif-standard cif-rotate cif-spacextend	rsf-standard grows survival trees following Leo Breiman's original random forest algorithm with variables and cut-points selected to maximize a log-rank statistic. rsf-extratrees grows survival trees with randomly selected predictors and cut-points. cif-standard uses the framework of conditional inference to grow survival trees. cif-rotate extends cif-standard by applying principal component analysis to random subsets of data prior to growing each survival tree. cif-spacextend derives new predictors for each tree in the ensemble, separately.
Oblique	obliqueRSF aorsf	obliqueRSF-net aorsf-net aorsf-fast aorsf-cph aorsf-extratrees	Oblique survival trees following Leo Breiman's random forest algorithm. Linear combinations of inputs are derived using glmnet in obliqueRSF-net and aorsf-net, using Newton Raphson scoring for the Cox partial likelihood function in aorsf-fast (1 iteration of scoring) and aorsf-cph (up to 20 iterations), and chosen randomly from a uniform distribution in aorsf-extratrees. Cut-points are selected from 5 randomly selected candidates to maximize a log-rank statistic.
Boosting ensen	ıbles		
Trees	xgboost	xgboost-cox xgboost-aft	xgboost-cox maximizes the Cox partial likelihood function, whereas xgboost-aft maximizes the accelerated failure time likelihood function. Nested cross validation (5 folds) is applied to tune the number of trees grown, the minimum number of observations in a leaf node was 10, the maximum depth of trees was 6, and $\sqrt{p}$ variables were considered randomly for each tree split, where $p$ is the total number of predictors.
Regression mod	dels		
Cox Net	glmnet	glmnet-cox	The Cox proportional hazards model is fit using an elastic net penalty. Nested cross validation (5 folds) is applied to tune penalty terms.
Neural network	cs		
Cox Time	survivalmodels	nn-cox	A neural network based on the proportional hazards model with time-varying effects. Nested cross-validation was applied to select the number of layers (from 1 to 8), the number of nodes in each layer (from $\sqrt{p}/2$ to $\sqrt{p}$ ), and the number of epochs to complete (up to 500). A drop-out rate of 10% was applied during training.

Table 1: Learning algorithms assessed in numeric studies. aorsf-fast is the accelerated oblique random survival forest (see Algorithm 1), and each of the additional learners are compared to aorsf-fast in numeric studies.

#### 5.1.2 Evaluation of prediction accuracy

Our primary metric for evaluating the accuracy of predicted risk is the integrated and scaled Brier score [Graf et al., 1999], a proper scoring rule that combines discrimination and calibration in one value and improves interpretability by adjusting for a benchmark model [Kattan and Gerds, 2018]. Consider a testing data set:

$$\mathcal{D}_{\text{test}} = \left\{ (T_i, \delta_i, x_i) \right\}_{i=1}^{N_{\text{test}}}.$$

Let  $\widehat{S}(t \mid x_i)$  be the predicted probability of survival up to a given prediction time of t > 0. For observation i in  $\mathcal{D}_{\text{test}}$ , let  $\widehat{S}(t \mid x_i)$  be the predicted probability of survival up to a given prediction time of t > 0. Define

$$\widehat{BS}(t) = \frac{1}{N_{\text{test}}} \sum_{i=1}^{N_{\text{test}}} \{ \widehat{S}(t \mid \boldsymbol{x}_i)^2 \cdot I(T_i \leq t, \delta_i = 1) \cdot \widehat{G}(T_i)^{-1} + [1 - \widehat{S}(t \mid \boldsymbol{x}_i)]^2 \cdot I(T_i > t) \cdot \widehat{G}(t)^{-1} \}$$

where  $\widehat{G}(t)$  is the Kaplan-Meier estimate of the censoring distribution. As  $\widehat{BS}(t)$  is time dependent, integration over time provides a summary measure of performance over a range of plausible prediction times. The integrated  $\widehat{BS}(t)$  is defined as

$$\widehat{\mathcal{BS}}(t_1, t_2) = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} \widehat{\mathbf{BS}}(t) dt.$$
 (2)

In our results,  $t_1$  and  $t_2$  are the 25th and 75th percentile of event times, respectively.  $\widehat{\mathcal{BS}}(t_1, t_2)$ , a sum of squared prediction errors, can be scaled to produce a measure of explained residual variation (i.e., an  $R^2$  statistic) by computing

$$R^{2} = 1 - \frac{\widehat{\mathcal{BS}}(t_{1}, t_{2})}{\widehat{\mathcal{BS}}_{0}(t_{1}, t_{2})}$$

$$\tag{3}$$

where  $\widehat{\mathcal{BS}}_0(t_1,t_2)$  is the integrated Brier score when a Kaplan-Meier estimate for survival based on the training data is used as the survival prediction function  $\widehat{S}(t)$ . We refer to this  $R^2$  statistic as the index of prediction accuracy (IPA) [Kattan and Gerds, 2018].

Our secondary metric for evaluating predicted risk is the time-dependent concordance (C)-statistic. We compute the first time-dependent C-statistic proposed by Blanche et al. [2013, Equation 3], which is interpreted as the probability that a risk prediction model will assign higher risk to a case (i.e., an observation with  $T \le t$  and  $\delta = 1$ ) versus a non-case (i.e., an observation with T > t). Similar to the IPA, observations with  $T \le t$  and  $\delta = 0$  only contribute to inverse probability of censoring weights for the time-dependent C-statistic.

Both the IPA and time-dependent C-statistic generally take values between 0 and 1. To avoid presenting an excessive amount of leading zeroes in our tables, figures, and text, we scale both the IPA and time-dependent C-statistic by 100. For example, we present a value of 25 if the IPA is 0.25, 87 if the time-dependent C-statistic is 0.87, and present 10.2 if the difference between two IPA values is 0.102

#### 5.1.3 Data sets

We used a collection of 21 data sets containing a total of 35 risk prediction tasks (tasks per data set ranged from one to four). Participant-level data from the GUIDE-IT and SPRINT clinical trials and the ARIC, MESA, and JHS community cohort studies was obtained from the National Institute of Health Biologic Specimen and Data Repository Coordinating Center (BioLINCC). Designs and protocols for these studies have been made available [ARIC Investigators, 1989, Bild et al., 2002, Felker et al., 2017, SPRINT Research Group, 2015, Taylor Jr et al., 2005]. All other datasets were publicly available and obtained through R packages (see Appendix A.1). Across all prediction tasks, the number of observations ranged from 137 to 17,549 (median: 1,384), the number of predictors ranged from 7 to 1,692 (median: 41), and the percentage of censored observations ranged from 5.26 to 97.7 (median: 78.1) (Table A.1).

#### 5.1.4 Monte-Carlo cross validation

For each risk prediction task, we completed 25 runs of Monte-Carlo cross validation. In each run, we used a random sample containing 50% of the available data for training and the remaining 50% for testing each of the learners described in Section 5.1.1. Then, for each learner, we computed the IPA and time-dependent C-statistic. If any learner failed to obtain predictions on any particular split of data<sup>5</sup>, the results for that split were omitted from downstream analyses for all learners.

#### 5.1.5 Statistical analysis

After collecting data from 25 replications of Monte-Carlo cross validation for the 14 learners in all 35 risk prediction tasks, we analyzed the resulting 12,250 observations of IPA and, separately, time-dependent C-statistic, using a Bayesian linear mixed model. Our approach follows the ideas described by Benavoli et al. [2017] and Kuhn and Wickham [2020], who developed guidelines on making statistical comparisons between learners using Bayesian models. Specifically, we fit two models:

$$IPA = \widehat{\gamma}_0 + \widehat{\gamma} \cdot learner + (1 \mid data/run)$$

and

C-stat = 
$$\widehat{\gamma}_0 + \widehat{\gamma} \cdot \text{learner} + (1 \mid \text{data/run}).$$

Random intercepts for specific splits of data (*i.e.*, run in the model formula) were nested within datasets. The intercept,  $\widehat{\gamma}_0$ , was the expected value of the outcome using aorsf-fast, making the coefficients in  $\widehat{\gamma}$  the expected differences between aorsf-fast and other learners. Default priors from rstanarm were applied for model fitting [Goodrich et al., 2022].

**Hypothesis testing** For both the IPA and time-dependent C-statistic, we conducted equivalence and inferiority tests based on a 1 point region of practical equivalence. More specifically, we concluded that two learners had practically equivalent IPA or time-dependent C-statistic if there was a 95% or higher posterior probability that the absolute difference in the relevant metric was less than 1. We concluded that one learner was weakly superior when there was  $\geq 95\%$  posterior probability that the absolute difference in the relevant metric was non-zero, and concluded superiority when when there was  $\geq 95\%$  posterior probability that the absolute difference in the relevant metric was 1 or more.

#### 5.1.6 Results

A full summary of all results presented in this Section is provided in Table A.2. In total, 871 out of 875 Monte-Carlo cross validation runs were completed. On run 13, 18, 24 and 25 for the ACTG 320 data, the nn-cox learner encountered an error during its fitting procedure.

**Index of prediction accuracy** Compared to learners that were not oblique RSFs, aorsf-fast had the highest IPA in 17 out of 35 risk prediction tasks, with an overall mean IPA of 12.6 (Figure 1). Compared to the learner with the second highest mean IPA (cif-standard), aorsf-fast's mean was 1.33 points higher, a relative increase of 11.7%. The posterior probability of aorsf-fast and aorsf-cph having practically equivalent expected IPA was 0.99, and the posterior probability of aorsf-fast having a superior IPA to other learners ranged from 0.82 (versus cif-standard) to >0.999 (versus several other learners; see Figure 2)

<sup>&</sup>lt;sup>5</sup>For example, when the prediction task was to predict risk of death in the ACTG 320 clinical trial (26 events total), some splits did not leave enough events in the training data to fit complex learners such as neural networks

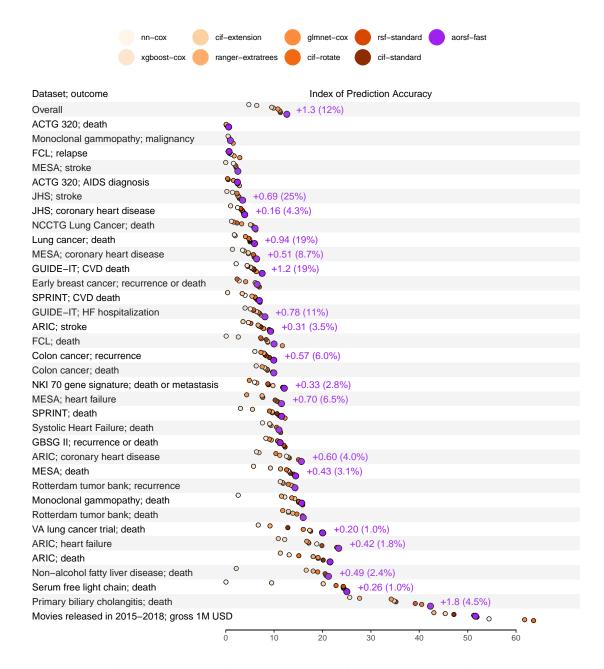


Figure 1: Index of prediction accuracy for the accelerated oblique random survival forest and other learning algorithms across multiple risk prediction tasks. Text appears in tasks where the accelerated oblique random survival forest obtained the highest index of prediction accuracy, showing the absolute and percent improvement over the second best learner. As predicted survival probabilities are not a standard output from xgboost-aft, it is not included in this figure. Also, since this figure is intended to compare aorsf-fast to learners that are not oblique random survival forests, aorsf-cph, aorsf-net, aorsf-random, and obliqueRSF-net are not included.

#### Posterior probability

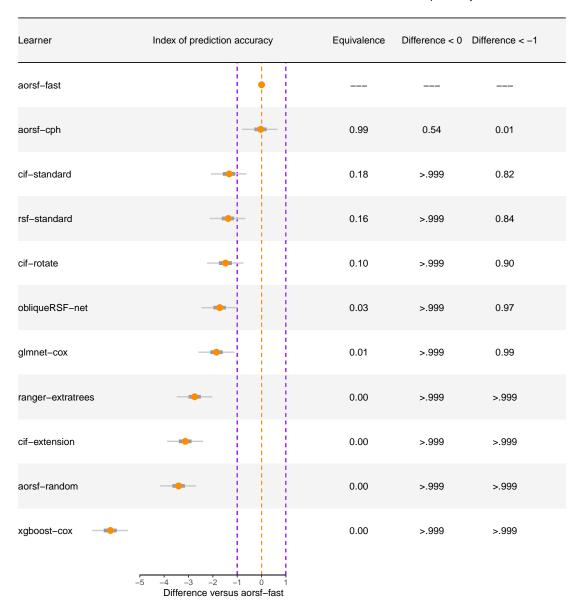


Figure 2: Expected differences in index of prediction accuracy between the accelerated oblique random survival forest and other learning algorithms. A region of practical equivalence is shown by purple dotted lines, and a boundary of non-zero difference is shown by an orange dotted line at the origin.

**Time-dependent concordance statistic** Compared to learners that were not oblique RSFs, aorsf-fast had the highest time-dependent C-statistic in 9 out of 35 risk prediction tasks, with an overall mean of 77.2 (Figure 3). Compared to the learner with the second highest mean C-statistic (cif-standard), aorsf-fast's mean was 0.668 points higher, a relative increase of 0.873%. The posterior probability of aorsf-fast and aorsf-cph having practically equivalent expected time-dependent C-statistics was > 0.999, and the posterior probability of aorsf-fast having a superior time-dependent C-statistic versus other learners ranged from 0.14 (versus cif-standard) to >0.999 (versus several other learners; see Figure 4)

#### 5.2 Benchmark of variable importance

The aim of this experiment is to evaluate negation VI and similar VI methods based on how well they can discriminate between relevant and irrelevant variables, where relevance is defined by having a relationship with the simulated outcome. We consider methods that are intrinsic to the oblique RF (*e.g.*, ANOVA VI), those that are intrinsic to the RF (*e.g.*, permutation VI), and those that are model-agnostic (*e.g.*, SHAP VI). VI methods with unavailable or still developing software were not included.<sup>6</sup>

#### 5.2.1 Variable importance techniques

We compute permutation VI for axis based RSFs using the randomForestSRC package. We compute ANOVA VI, negation VI, and permutation VI for oblique RSFs using the aorsf package. For ANOVA VI, we applied a p-value threshold of 0.01, following the threshold recommended by Menze et al. [2011]. We compute SHAP VI for boosted tree models using the xgboost package [Chen et al., 2022], which incorporates the tree SHAP approach proposed by Lundberg et al. [2018].

#### 5.2.2 Variable types

We considered five classes of predictor variables, with each class characterized by its variables' relationship to a right-censored outcome on the log-hazard scale. Specifically,

- irrelevant variables had no relationship with the outcome.
- main effect variables had a linear relationship to the outcome on the log-hazard scale.
- non-linear effect variables had a non-linear relationship to the outcome. A normally distributed variable x was generated with a linear relationship to the outcome on the log-hazard scale, then  $\tilde{x} = \sin(a \cdot \pi \cdot x)$  was retained for modeling. The constant a varied uniformly from 0.125 to 0.25.
- *combination effect* variables were formed by linear combinations of three other variables. While their combination was linearly related to the outcome on the log-hazard scale, each of the three variables contributing to the combination had no relation to the outcome.
- *interaction effect* variables were related to the outcome by multiplicative interaction with one other variable, which could have been a main effect, non-linear effect, or combination effect variable.

#### 5.2.3 Simulated data

We initiated each set of simulated data with a random draw of size n from a p-dimensional multivariate normal distribution, yielding n observations of p predictors. Each of p predictor variables had a mean of zero, standard deviation of 1, and correlation with other predictor variables drawn at random between a lower and upper boundary. A time-to-event outcome with roughly 45% of observations censored was generated using

<sup>&</sup>lt;sup>6</sup>Although the party package implements the approach to VI developed by Strobl et al. [2007], the developers of the party package note that the implementation of this approach for survival outcomes is "extremely slow and experimental" as of version 1.3.10. Therefore, it is not incorporated in the current simulation study.

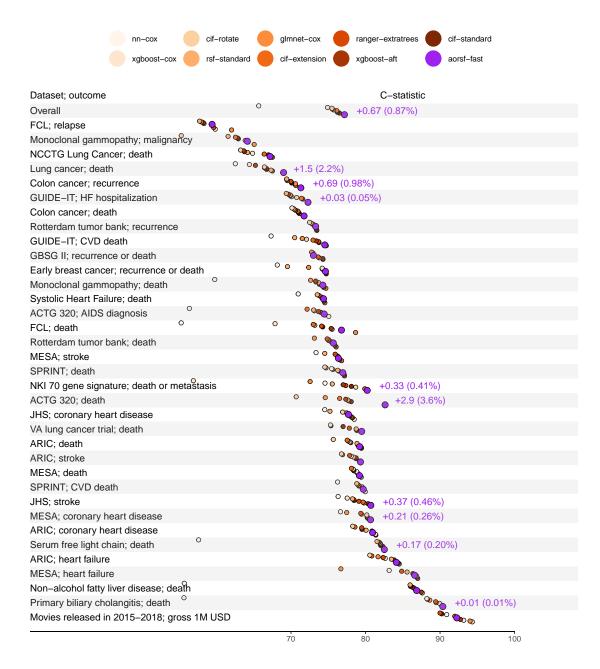


Figure 3: Time-dependent concordance statistic for the accelerated oblique random survival forest and other learning algorithms across multiple risk prediction tasks. Text appears in tasks where the accelerated oblique random survival forest obtained the highest concordance, showing the absolute and percent improvement over the second best learner. Since this figure is intended to compare aorsf-fast to learners that are not oblique random survival forests, aorsf-cph, aorsf-net, aorsf-random, and obliqueRSF-net are not included.

#### Posterior probability Learner Time-dependent C-statistic Equivalence Difference < 0 Difference < -1 aorsf-fast obliqueRSF-net >.999 0.35 0.00 aorsf-cph >.999 0.55 0.00 cif-standard 0.98 0.14 0.86 0.59 0.41 xgboost-aft >.999 0.52 >.999 0.48 ranger-extratrees cif-extension 0.47 >.999 0.53 0.09 >.999 0.91 glmnet-cox rsf-standard 0.03 0.97 >.999 cif-rotate 0.02 >.999 0.98 0.00 >.999 xgboost-cox >.999 0.00 aorsf-random >.999 >.999

Figure 4: Expected differences in time-dependent concordance statistic between the accelerated oblique random survival forest and other learning algorithms. A region of practical equivalence is shown by purple dotted lines, and a boundary of non-zero difference is shown by an orange dotted line at the origin.

Difference versus aorsf-fast

the simsurv package [Brilleman, 2018, Brilleman et al., 2020]. The full predictor matrix (*i.e.*, including interactions, non-linear mappings, and combinations) was used to generate the outcome. Interactions, non-linear mappings, and combinations were dropped from the predictor matrix after the outcome was generated so that VI techniques could be evaluated based on their ability to detect these effects.

#### **5.2.4** Parameter specifications

Parameters that varied in the current simulation study included the number of observations (500, 1000, and 2500) and the absolute value of the maximum correlation between predictors (0.3, 0.15, and 0). Parameters that remain fixed throughout the study included the number of predictors in each class (15) and the effect size of each predictor (one standard deviation increase associated with a 64% increase in relative risk). Using this design for simulated data, the Heller explained relative risk (95% confidence interval) of our covariates was 88.5 (88.2, 88.7) [Heller, 2012] with 2,500 observations.

#### **5.2.5** Evaluation of variable importance

We compared VI techniques based on their discrimination (*i.e.*, C-statistic) between relevant and irrelevant variables. Specifically, we generated a binary outcome for each predictor variable based on its relevance (*i.e.*, the binary outcome is 1 if the variable is relevant, 0 otherwise). Treating VI as if it were a 'prediction' for these binary outcomes yields a C-statistic which may be interpreted as the probability that the VI technique will rank a relevant variable higher than an irrelevant variable [Harrell et al., 1982].

#### 5.2.6 Results

The three techniques that used 'aorsf' to estimate VI were ranked first (aorsf-negate; C=75.9), second (aorsf-anova; C=73.9), and third (aorsf-permute; C=73.2) in overall mean C-statistic across all of the simulation scenarios, with aorsf-negate obtaining the highest C-statistic in 26 out of 36 VI tasks (Figure 5). Among the four relevant variable classes, aorsf-negate had the highest mean C-statistic for main effects, combination effects, and non-linear effects, with the greatest advantage of using aorsf-negate occurring among non-linear and combination variables. Full results from the experiment are provided in Table A.3. Computationally, ANOVA VI was faster than negation and permutation VI, with a median time of 2.88 seconds versus 20.4 and 21.8 seconds, respectively.

#### 5.3 Benchmark of computational efficiency

The aim of this numeric experiment is to evaluate the computational efficiency of the accelerated oblique RSF compared to its predecessor (the oblique RSF from the obliqueRSF R package) and to several other machine learning algorithms.

#### **5.3.1** Evaluation of computational efficiency

For each learner discussed in Section 5.1.1 and for each of the 35 risk prediction tasks analyzed in Section 5.1, we tracked the amount of time required to fit a prediction model (including time used to tune parameters) and compute predicted risk.

We performed additional benchmarks on the time required to fit 500 trees using aorsf, randomForestSRC, and ranger. The learners that represented these R packages were aorsf-fast, rsf-standard, and rsf-extratrees, respectively. To allow for controlled comparisons of computational efficiency with varying dimensions of training data, we used the same process to simulate data as described in Section 5.2.3, varying the number of observations from 100 to 10000 and the number of predictors from 10 to 1000. The minimum node size of trees in this experiment was dynamically set as the nearest integer to the number of observations in the training set divided by 10.

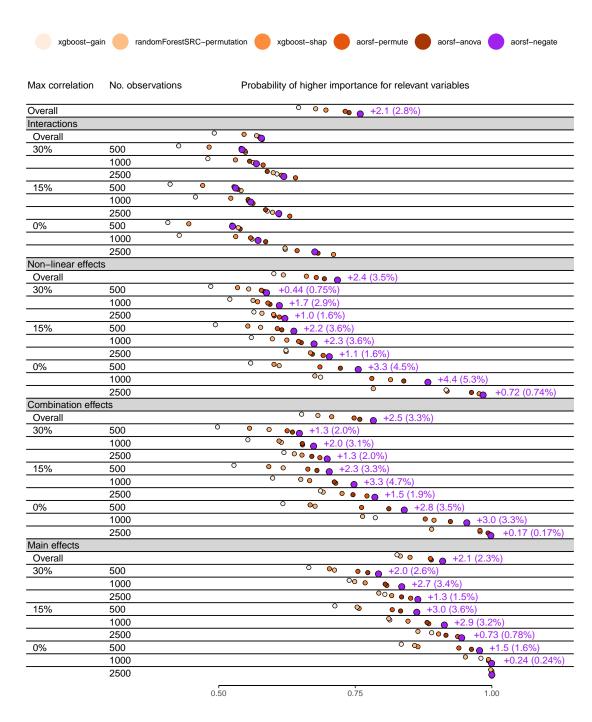


Figure 5: Concordance statistic for assigning higher importance to relevant versus irrelevant variables. Text appears in rows where negation importance obtained the highest concordance, showing absolute and percent improvement over the second best technique.

#### 5.3.2 Results

In the analysis of 35 risk prediction tasks, aorsf-fast was the second fastest learner overall, with a median time to develop a risk prediction model and compute predictions about 337 milliseconds longer than glmnet-cox (Figure 6). Comparing median computing times, aorsf-fast was 1,291.6 times faster than its predecessor, obliqueRSF-net. In addition, aorsf-fast was 19.8, 1.90, and 3.18 faster than axis based forests grown using the party, ranger, and randomForestSRC packages, respectively.

In the analysis of time to fit 500 trees using simulated data, the ranger package exhibited the fastest computation times overall (Figure 7). aorsf was the second fastest when the number of predictors was 10 or 100, and randomForestSRC had similar computation time versus aorsf when 1000 predictors were present.

#### 6 Discussion

In this paper, we have developed two contributions to the oblique RSF: (1) the accelerated oblique RSF (i.e., aorsf-fast) and (2) negation VI. Our technique to accelerate the oblique RSF reduces the number of operations required to find linear combinations of inputs using a single iteration of Newton Raphson scoring, while our VI technique directly engages with coefficients in linear combinations of inputs to measure importance of individual variables. In numeric experiments, we found that that aorsf-fast is approximately 1,291.6 times faster than its predecessor, obliqueRSF-net, with a practically equivalent C-statistic. We also found that negation VI, a technique to estimate VI using the oblique RSF, detected non-linear, combination, and main effects more effectively than three standard methods to estimate VI: permutation, ANOVA, and SHAP VI. Overall, we found that estimating VI using negation instead of ANOVA increased the C-statistic for ranking a relevant variable higher than an irrelevant variable by 2.05, a relative increase of 2.78%.

To understand potential differences in computational efficiency, we reviewed code in the aorsf, randomForestSRC, and ranger packages. We found differences in how survival outcome data are saved in leaf nodes. For each leaf node, aorsf stores data with one row per unique event time using training data that are stored in the leaf, whereas randomForestSRC and ranger store survival outcomes at a fixed grid of event times in each leaf. By default, ranger creates a grid that includes all event times in the training data. The grid strategy can cause higher computing time and memory usage when the grid of event times is large and a large number of leaf nodes are included in each tree, which can occur when minimum node size is small relative to the size of the training data. We kept minimum node size fixed in our benchmark of computational efficiency using real data, and dymanically increased minimum node size based on the size of the training set when we benchmarked computational efficiency using simulated data. Because of this decision, the randomForestSRC and ranger packages ran slower than aorsf in our benchmark of real data but not in the benchmark of simulated data.

#### 6.1 Implications of our results

Accurate risk prediction models have the potential to improve healthcare by directing timely interventions to patients who are most likely to benefit. However, prediction models that cannot scale adequately to large databases or cannot be interpreted and explained will struggle to gain acceptance in clinical practice [Moss et al., 2022]. The current study advances the oblique RSF, an accurate risk prediction model, towards being accurate, scalable, and interpretable. The improved computational efficiency of the accelerated oblique RSF increases the feasibility of applying oblique RSFs in a wide range of prediction tasks. Faster model evaluation and re-fitting also improve diagnosis and resolution of model-based issues (e.g., model calibration deteriorates over time). The introduction of negation VI also advances interpretability. VI is intrinsically linked to model fairness, as it can be used to identify when protected characteristics such as race, religion, and sexuality are inadvertently used (either directly or through correlates of these characteristics) by a prediction model. Since negation VI engages with the coefficients used in linear combinations of variables, a major component of

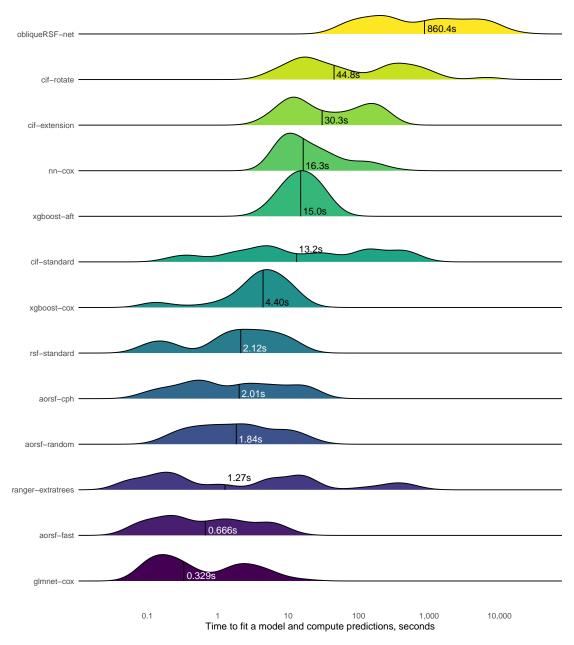


Figure 6: Distribution of time taken to fit a prediction model and compute predicted risk. The median time, in seconds, is printed and annotated for each learner by a vertical line.

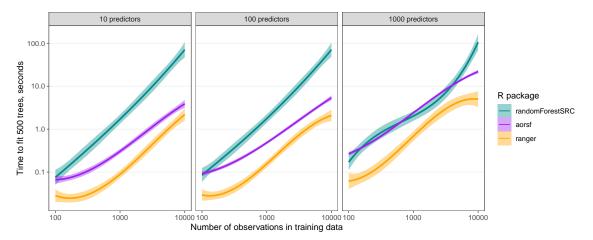


Figure 7: The expected time, in seconds, to fit an ensemble of 500 axis-based survival trees using the ranger or randomForestSRC package versus 500 oblique survival trees using the aorsf package. The ranger package is the most efficient overall, and aorsf appears to be relatively efficient in larger samples, particularly when 10 or 100 predictors are present in the training data. All three packages appear to scale linearly in computation time with the number of observations in the training data.

oblique RSFs, it may be more capable of diagnosing unfairness in oblique RSFs compared to permutation importance and model-agnostic VI techniques.

#### **6.2** Limitations and next steps

While the current study advances the oblique RSF towards being scalable and interpretable, there remain several limitations that can be targeted in future studies. The accelerated oblique RSF does not account for competing risks, and biased estimation of incidence may occur when competing risks are ignored. Thus, allowing the oblique RSF to account for competing risks is a high priority for future studies. In addition, the current study only considered data without missing values, only evaluated oblique RSFs that applied the log-rank statistic for node splitting, and only considered negation VI estimates based on Harrell's C-statistic. Few studies have developed strategies to deal with missing data while growing oblique survival trees. Prior studies have found that log-rank tests can be mis-informative when survival curves cross [Li et al., 2015], and that Harrell's C-statistic is dependent on the censoring distribution of the outcome [Uno et al., 2011]. Thus, a second item is to expand the range of options available to users of the aorsf package, enabling them to apply strategies for imputation of missing values and use a broad range of statistical criteria while growing oblique survival trees. Last, Cui et al. [2017] found that estimating an inverse-probability weighted hazard function at each non-leaf node of a survival tree allows the RSF to converge asymptotically to the true survival function when some variables contribute both to the risk of the event and the risk of censoring, a scenario that is very likely in the analysis of medical data. The accelerated oblique RSF could incorporate this splitting technique by using Newton Raphson scoring to fit a model for the censoring distribution after which a weighted model could be fit to the failure distribution. This final item has the highest priority, as Cui et al. [2017] showed it is a requisite condition for consistency of axis-based survival trees in fairly general settings.

#### 6.3 Conclusion

Oblique RSFs have exceptional prediction accuracy and this study has shown how they can be fit with computational efficiency that rivals their axis-based counterparts. We have also introduced a general and flexible method to estimate VI with oblique RFs, and demonstrated its effectiveness for numeric, correlated predictors. Code used for the current study is available at https://github.com/bcjaeger/aorsf-bench, and the aorsf package is available at https://github.com/bcjaeger/aorsf.

#### Acknowledgements

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#### **Appendix**

#### Data sources

- 1. The "VA lung cancer trial" data [Kalbfleisch and Prentice, 2011] were obtained from the randomForestSRC R package [Ishwaran and Kogalur, 2019].
- 2. The "Colon cancer" data [Moertel et al., 1995] were obtained from the survival R package [Therneau, 2022a].
- 3. The "Primary biliary cholangitis" data [Therneau and Grambsch, 2000] were obtained from the aorsf R package [Jaeger, 2022].
- 4. The "Movies released in 2015-2018" data were obtained from the censored R package [Hvitfeldt and Frick].
- 5. The "GBSG II" data [Schumacher, 1994] were obtained from the TH.data R package [Hothorn, 2022].
- 6. The "Systolic Heart Failure" data [Hsich et al., 2011] were obtained from the randomForestSRC R package [Ishwaran and Kogalur, 2019].
- 7. The "Serum free light chain" data [Dispenzieri et al., 2012, Kyle et al., 2006] were obtained from the survival R package [Therneau, 2022a].
- 8. The "Non-alcohol fatty liver disease" data [Allen et al., 2018] were obtained from the survival R package [Therneau, 2022a].
- 9. The "Rotterdam tumor bank" data [Royston and Altman, 2013] were obtained from the survival R package [Therneau, 2022a].
- 10. The "ACTG 320" data [Hosmer and Lemeshow, 2002] were obtained from the mlr3proba R package [Sonabend et al., 2021].
- 11. The "GUIDE-IT" data [Felker et al., 2017] were obtained from BioLINCC.
- 12. The "Early breast cancer" data [Desmedt et al., 2011, Hatzis et al., 2011, Ternès et al., 2017] were obtained from the biospear R package [Ternes et al., 2018].
- 13. The "SPRINT" data [SPRINT Research Group, 2015] were obtained from BioLINCC.
- 14. The "NKI 70 gene signature" data [Van De Vijver et al., 2002] were obtained from the OpenML R package [Casalicchio et al., 2017].
- 15. The "Lung cancer" data [Director's Challenge Consortium for the Molecular Classification of Lung Adenocarcinoma, 2008] were obtained from the OpenML R package [Casalicchio et al., 2017].
- 16. The "NCCTG Lung Cancer" data [Loprinzi et al., 1994] were obtained from the survival R package [Therneau, 2022a].
- 17. The "FCL" data [Pintilie, 2006] were obtained from the randomForestSRC R package [Ishwaran and Kogalur, 2019].
- 18. The "Monoclonal gammopathy" data [Kyle et al., 2002] were obtained from the survival R package [Therneau, 2022a].
- 19. The "MESA" data [Bild et al., 2002] were obtained from BioLINCC.
- 20. The "ARIC" data [ARIC Investigators, 1989] were obtained from BioLINCC.
- 21. The "JHS" data [Taylor Jr et al., 2005] were obtained from BioLINCC.

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Label	N observations	N predictors	Outcome	N Events	% Censored
VA lung cancer trial	137	8	Death	128	6.57
			Recurrence	468	49.6
Colon cancer	929	12	Death	452	51.3
Primary biliary cholangitis	276	19	Death	111	59.8
Movies released in 2015-2018	551	46	Gross 1M USD	522	5.26
GBSG II	686	10	Recurrence Or Death	299	56.4
Systolic Heart Failure	2,231	41	Death	726	67.5
Serum free light chain	7,874	10	Death	2,169	72.5
Non-alcohol fatty liver disease	17,549	24	Death	1,364	92.2
		11	Recurrence	1,518	49.1
Rotterdam tumor bank	2,982		Death	1,272	57.3
		12	AIDS Diagnosis	96	91.7
ACTG 320	1,151		Death	26	97.7
			Cardiovascular Death	110	87.7
GUIDE-IT	894	59	Hf Hospitalization	288	67.8
Early breast cancer	614	1,692	Recurrence Or Death	134	78.2
			Cardiovascular Death	521	94.4
SPRINT	9,361	174	Death	1,644	82.4
NKI 70 gene signature	144	77	Death Or Metastasis	48	66.7
Lung cancer	442	24	Death	236	46.6
NCCTG Lung Cancer	228	9	Death	165	27.6
			Death	76	86.0
FCL	541	7	Relapse	272	49.7
			Death	963	30.4

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Monoclonal gammopathy	1,384	8 Malignancy		115	91.7
			Heart Failure	339	95.0
			Coronary Heart Disease	439	93.5
MESA	6,783	48	Stroke	292	95.7
			Death	1,297	80.9
			Heart Failure	2,981	78.1
			Coronary Heart Disease	2,282	83.2
ARIC	13,623	41	Stroke	1,323	90.3
			Death	6,662	51.1
WY.C	2.504	0.0	Stroke	152	95.8
JHS	3,501	80	Coronary Heart Disease	190	94.6

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks.

	Performance	metric (SD)	Computation	n time, seconds
	Scaled Brier	C-Statistic	Model fitting	Risk prediction
Overall				
aorsf-fast	0.126 (0.109)	0.772 (0.071)	0.527	0.138
aorsf-cph	0.126 (0.109)	0.771 (0.070)	1.750	0.140
cif-standard	0.113 (0.098)	0.765 (0.071)	3.792	6.448
rsf-standard	0.113 (0.114)	0.755 (0.075)	1.945	0.196
cif-rotate	0.112 (0.124)	0.755 (0.081)	36.928	8.194
obliqueRSF-net	0.109 (0.081)	0.773 (0.069)	552.335	84.685
glmnet-cox	0.108 (0.119)	0.757 (0.077)	0.326	0.003
ranger-extratrees	0.099 (0.085)	0.762 (0.067)	0.790	1.109
cif-extension	0.095 (0.092)	0.761 (0.072)	21.977	6.922
aorsf-random	0.092 (0.079)	0.744 (0.065)	1.717	0.149
xgboost-cox	0.064 (0.100)	0.749 (0.094)	4.394	0.004
nn-cox	0.048 (0.106)	0.657 (0.136)	11.377	1.705
xgboost-aft		0.762 (0.076)	15.031	0.007
ACTG 320; AIDS di	agnosis, n = 115			
obliqueRSF-net	0.029 (0.015)	0.753 (0.037)	115.320	18.196
ranger-extratrees	0.028 (0.017)	0.740 (0.036)	0.086	0.133
aorsf-random	0.027 (0.020)	0.756 (0.036)	0.465	0.035
cif-standard	0.024 (0.031)	0.744 (0.040)	1.657	4.377
aorsf-cph	0.024 (0.029)	0.750 (0.042)	0.436	0.036
aorsf-fast	0.024 (0.028)	0.745 (0.045)	0.141	0.036
cif-extension	0.023 (0.015)	0.722 (0.038)	9.010	4.189
glmnet-cox	0.016 (0.030)	0.746 (0.037)	0.197	0.002
rsf-standard	0.005 (0.041)	0.730 (0.042)	0.179	0.061
cif-rotate	0.004 (0.040)	0.731 (0.038)	14.549	3.604
nn-cox	0.000 (0.011)	0.564 (0.101)	7.755	0.811
xgboost-cox	-0.001 (0.052)	0.751 (0.033)	3.729	0.003
xgboost-aft		0.737 (0.035)	11.383	0.006
ACTG 320; death, n	= 1151, p = 12	, ,		
aorsf-random	0.008 (0.012)	0.798 (0.073)	0.285	0.024
obliqueRSF-net	0.006 (0.009)	0.821 (0.049)	49.070	11.201
aorsf-fast	0.006 (0.019)	0.826 (0.057)	0.088	0.020
aorsf-cph	0.006 (0.018)	0.818 (0.062)	0.357	0.020
cif-extension	0.001 (0.020)	0.765 (0.066)	8.283	3.478
ranger-extratrees	0.001 (0.019)	0.777 (0.069)	0.041	0.122
xgboost-cox	-0.004 (0.004)	0.500 (0.000)	0.118	0.002
nn-cox	-0.004 (0.004)	0.547 (0.128)	7.487	0.717
cif-standard	-0.005 (0.025)	0.781 (0.062)	1.695	4.223
rsf-standard	-0.031 (0.051)	0.776 (0.073)	0.098	0.037
cif-rotate	-0.037 (0.049)	0.707 (0.090)	13.163	3.201
glmnet-cox	-0.065 (0.095)	0.746 (0.098)	0.286	0.002
xgboost-aft		0.774 (0.070)	10.124	0.005
ARIC; coronary hea	nrt disease, $n = 13$	3623, p = 41		

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction
aorsf-fast	0.156 (0.007)	0.810 (0.007)	4.590	1.434
aorsf-cph	0.153 (0.006)	0.809 (0.007)	14.582	1.450
rsf-standard	0.150 (0.007)	0.801 (0.007)	8.222	0.981
obliqueRSF-net	0.133 (0.005)	0.811 (0.008)	4468.696	1359.275
cif-standard	0.132 (0.005)	0.809 (0.007)	70.462	358.273
glmnet-cox	0.129 (0.011)	0.795 (0.008)	1.873	0.010
nn-cox	0.126 (0.012)	0.795 (0.007)	43.144	86.104
ranger-extratrees	0.112 (0.005)	0.795 (0.009)	283.364	69.939
aorsf-random	0.104 (0.005)	0.771 (0.008)	11.343	1.420
cif-rotate	0.104 (0.004)	0.783 (0.009)	558.249	68.510
cif-extension	0.069 (0.002)	0.786 (0.009)	164.161	50.420
xgboost-cox	0.064 (0.017)	0.813 (0.006)	9.660	0.015
xgboost-aft		0.814 (0.006)	29.321	0.013
C		0.814 (0.000)	29.321	0.013
ARIC; death, $n = 13$		0.700 (0.004)	10.250	1.160
rsf-standard	0.216 (0.006)	0.789 (0.004)	12.352	1.162
aorsf-fast	0.216 (0.006)	0.792 (0.004)	7.463	2.519
aorsf-cph	0.215 (0.006)	0.792 (0.004)	22.389	2.569
cif-standard	0.201 (0.004)	0.790 (0.004)	68.083	373.333
obliqueRSF-net	0.195 (0.004)	0.789 (0.004)	7373.936	1276.463
nn-cox	0.191 (0.008)	0.779 (0.005)	83.418	84.770
glmnet-cox	0.191 (0.015)	0.777 (0.007)	2.282	0.011
ranger-extratrees	0.181 (0.004)	0.780 (0.005)	356.276	61.525
cif-rotate	0.151 (0.007)	0.757 (0.006)	563.575	64.849
xgboost-cox	0.131 (0.012)	0.794 (0.004)	12.568	0.015
aorsf-random	0.128 (0.006)	0.725 (0.005)	20.291	2.298
cif-extension	0.113 (0.002)	0.775 (0.005)	176.867	50.345
xgboost-aft	_	0.794 (0.004)	35.380	0.013
ARIC; heart failure,				
aorsf-fast	0.233 (0.006)	0.841 (0.005)	5.478	1.709
rsf-standard	0.229 (0.006)	0.835 (0.005)	10.326	1.039
aorsf-cph	0.229 (0.006)	0.840 (0.005)	17.063	1.730
cif-standard	0.199 (0.005)	0.839 (0.005)	68.929	364.202
obliqueRSF-net	0.198 (0.005)	0.839 (0.005)	5341.195	1624.560
nn-cox	0.188 (0.018)	0.826 (0.006)	58.351	89.012
cif-rotate	0.172 (0.006)	0.806 (0.007)	569.166	67.654
ranger-extratrees	0.170 (0.004)	0.824 (0.005)	411.253	73.737
glmnet-cox	0.167 (0.044)	0.817 (0.018)	2.257	0.010
aorsf-random	0.151 (0.006)	0.792 (0.007)	14.023	1.686
xgboost-cox	0.122 (0.017)	0.845 (0.005)	11.985	0.015
cif-extension	0.109 (0.003)	0.808 (0.006)	169.620	49.957
xgboost-aft		0.844 (0.005)	30.837	0.012
ARIC; stroke, $n = 13$	3623, p = 41			
aorsf-fast	0.093 (0.004)	0.793 (0.007)	3.625	1.205
aorsf-cph	0.090 (0.004)	0.792 (0.007)	12.691	1.331
rsf-standard	0.090 (0.006)	0.784 (0.006)	8.134	0.916
	(0.000)	(0.000)		0.2.2

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction
glmnet-cox	0.078 (0.004)	0.787 (0.007)	1.781	0.010
obliqueRSF-net	0.073 (0.003)	0.789 (0.008)	3058.459	2338.694
cif-standard	0.073 (0.003)	0.787 (0.007)	69.723	355.372
nn-cox	0.068 (0.016)	0.781 (0.012)	29.662	78.191
ranger-extratrees	0.067 (0.003)	0.779 (0.008)	219.331	61.397
aorsf-random	0.061 (0.005)	0.750 (0.009)	9.153	1.186
cif-rotate	0.052 (0.003)	0.768 (0.009)	573.621	66.723
xgboost-cox	0.047 (0.014)	0.794 (0.006)	7.662	0.014
cif-extension	0.036 (0.002)	0.769 (0.009)	167.033	51.074
xgboost-aft	_	0.793 (0.006)	25.321	0.012
Colon cancer; death	n, n = 929, p = 12			
aorsf-random	0.103 (0.011)	0.724 (0.012)	0.974	0.048
aorsf-cph	0.100 (0.015)	0.717 (0.011)	0.631	0.050
aorsf-fast	0.099 (0.014)	0.718 (0.012)	0.235	0.052
cif-standard	0.097 (0.013)	0.710 (0.012)	0.698	3.233
obliqueRSF-net	0.087 (0.006)	0.717 (0.011)	227.346	90.031
cif-rotate	0.086 (0.017)	0.705 (0.014)	12.581	3.222
rsf-standard	0.086 (0.019)	0.704 (0.011)	1.899	0.150
ranger-extratrees	0.083 (0.007)	0.710 (0.012)	0.079	0.231
cif-extension	0.080 (0.006)	0.709 (0.011)	7.680	3.708
glmnet-cox	0.075 (0.016)	0.711 (0.019)	0.133	0.002
xgboost-cox	0.063 (0.013)	0.701 (0.013)	3.694	0.003
nn-cox	-0.003 (0.003)	0.510 (0.045)	9.217	1.188
xgboost-aft	— — — — — — — — — — — — — — — — — — —	0.706 (0.013)	12.025	0.006
Colon cancer; recur	rence. $n = 929$ . $p$	` /		
aorsf-fast	0.099 (0.017)	0.713 (0.016)	0.235	0.051
aorsf-cph	0.099 (0.016)	0.712 (0.015)	0.641	0.050
aorsf-random	0.094 (0.014)	0.706 (0.015)	0.989	0.047
cif-standard	0.091 (0.016)	0.701 (0.017)	0.685	3.216
obliqueRSF-net	0.086 (0.008)	0.712 (0.015)	220.136	52.240
cif-rotate	0.084 (0.020)	0.694 (0.017)	12.394	3.355
cif-extension	0.081 (0.009)	0.706 (0.017)	7.829	3.620
rsf-standard	0.081 (0.020)	0.694 (0.015)	1.839	0.152
ranger-extratrees	0.079 (0.011)	0.700 (0.016)	0.081	0.273
glmnet-cox	0.073 (0.011)	0.706 (0.024)	0.136	0.002
xgboost-cox	0.060 (0.010)	0.695 (0.018)	3.234	0.003
nn-cox	-0.020 (0.074)	0.533 (0.044)	9.225	1.019
xgboost-aft	—	0.701 (0.019)	12.802	0.006
Early breast cancer;	recurrence or de			
obliqueRSF-net	0.072 (0.022)	0.751 (0.027)	1772.643	38.287
cif-rotate	0.070 (0.018)	0.747 (0.027)	6243.357	338.140
cif-standard	0.067 (0.019)	0.747 (0.030)	8.875	4.293
aorsf-cph	0.067 (0.029)	0.747 (0.026)	1.614	0.300
aorsf-fast	0.065 (0.028)	0.746 (0.026)	1.325	0.297
cif-extension	0.064 (0.016)	0.746 (0.028)	42.920	6.083
	(0.010)	(2.220)		

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction			
ranger-extratrees	0.061 (0.022)	(22) 0.742 (0.031) 0.219		0.311			
glmnet-cox	0.041 (0.032)	0.724 (0.036)	5.782	0.005			
xgboost-cox	0.028 (0.032)	0.742 (0.032)	2.472	0.006			
aorsf-random	0.025 (0.016)	0.691 (0.042)	1.888	0.271			
rsf-standard	0.024 (0.037)	0.695 (0.033)	0.883	0.169			
nn-cox	-0.010 (0.071)	0.682 (0.067)	14.875	1.621			
xgboost-aft		0.744 (0.027)	10.373	0.009			
FCL; death, $n = 541$ ,	p = 7						
glmnet-cox	0.117 (0.028)	0.787 (0.037)	0.105	0.002			
aorsf-cph	0.100 (0.039)	0.769 (0.033)	0.165	0.018			
aorsf-fast	0.100 (0.037)	0.768 (0.033)	0.079	0.018			
obliqueRSF-net	0.091 (0.023)	0.769 (0.032)	78.242	6.014			
cif-rotate	0.087 (0.048)	0.755 (0.027)	5.839	1.758			
cif-extension	0.087 (0.036)	0.730 (0.034)	5.195	2.616			
aorsf-random	0.085 (0.029)	0.754 (0.034)	0.258	0.019			
cif-standard	0.084 (0.038)	0.743 (0.036)	0.281	1.194			
ranger-extratrees	0.073 (0.016)	0.741 (0.037)	0.031	0.081			
rsf-standard	0.072 (0.048)	0.732 (0.034)	0.113	0.039			
xgboost-cox	0.026 (0.053)	0.679 (0.120)	0.330	0.002			
nn-cox	0.001 (0.028)	0.553 (0.117)	7.201	0.403			
xgboost-aft		0.754 (0.038)	7.320	0.005			
FCL; relapse, $n = 541$ , $p = 7$							
glmnet-cox	0.029 (0.017)	0.620 (0.024)	0.107	0.002			
obliqueRSF-net	0.018 (0.014)	0.598 (0.024)	165.938	8.270			
ranger-extratrees	0.017 (0.016)	0.596 (0.025)	0.031	0.080			
aorsf-random	0.012 (0.017)	0.595 (0.023)	0.401	0.021			
xgboost-cox	0.011 (0.016)	0.598 (0.032)	1.548	0.002			
cif-standard	0.008 (0.021)	0.594 (0.023)	0.277	1.221			
aorsf-cph	0.007 (0.021)	0.595 (0.026)	0.260	0.023			
aorsf-fast	0.007 (0.019)	0.594 (0.025)	0.116	0.022			
cif-extension	-0.005 (0.023)	0.580 (0.028)	5.912	2.183			
nn-cox	-0.006 (0.014)	0.521 (0.059)	8.447	0.457			
cif-rotate	-0.012 (0.025)	0.583 (0.030)	6.486	2.537			
rsf-standard	-0.026 (0.032)	0.577 (0.024)	0.891	0.083			
xgboost-aft	_	0.582 (0.034)	6.799	0.005			
GBSG II; recurrence	e or death, $n = 68$	86, p = 10					
cif-standard	0.123 (0.020)	0.743 (0.020)	0.478	2.173			
obliqueRSF-net	0.121 (0.014)	0.747 (0.018)	234.738	19.092			
rsf-standard	0.120 (0.023)	0.738 (0.019)	1.362	0.114			
aorsf-cph	0.117 (0.022)	0.733 (0.017)	0.404	0.038			
	\ /			2 420			
cif-extension	0.114 (0.017)	0.743 (0.019)	7.544	3.429			
cif-extension aorsf-fast	0.114 (0.017) 0.112 (0.024)	0.730 (0.018)	0.180	0.040			
cif-extension	0.114 (0.017) 0.112 (0.024) 0.111 (0.017)	0.730 (0.018) 0.727 (0.018)		0.040 0.036			
cif-extension aorsf-fast	0.114 (0.017) 0.112 (0.024)	0.730 (0.018)	0.180	0.040			

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction
glmnet-cox	0.090 (0.019)	0.728 (0.021)	0.113	0.002
xgboost-cox	0.083 (0.015)	0.730 (0.020)	2.632	0.003
nn-cox	-0.015 (0.048)	0.504 (0.037)	8.139	0.727
xgboost-aft	_	0.729 (0.021)	12.179	0.006
GUIDE-IT; CVD de	ath, n = 894, p =	59		
aorsf-fast	0.075 (0.018)	0.745 (0.028)	0.154	0.036
aorsf-cph	0.071 (0.018)	0.742 (0.027)	0.386	0.037
glmnet-cox	0.063 (0.041)	0.715 (0.091)	0.489	0.003
obliqueRSF-net	0.060 (0.013)	0.741 (0.027)	209.529	11.066
cif-rotate	0.059 (0.016)	0.721 (0.025)	34.549	4.966
cif-standard	0.058 (0.014)	0.738 (0.022)	1.380	3.350
ranger-extratrees	0.054 (0.013)	0.737 (0.029)	0.082	0.196
cif-extension	0.052 (0.011)	0.730 (0.022)	13.080	5.523
rsf-standard	0.046 (0.023)	0.705 (0.025)	0.174	0.061
xgboost-cox	0.044 (0.041)	0.747 (0.020)	3.880	0.003
aorsf-random	0.030 (0.011)	0.675 (0.035)	0.510	0.038
nn-cox	0.022 (0.036)	0.673 (0.089)	8.663	0.566
xgboost-aft	_	0.734 (0.020)	11.747	0.006
GUIDE-IT; HF hos	pitalization, n = 8	, ,		
aorsf-fast	0.081 (0.019)	0.723 (0.024)	0.239	0.054
aorsf-cph	0.080 (0.018)	0.722 (0.024)	0.682	0.055
ranger-extratrees	0.073 (0.010)	0.722 (0.022)	0.243	0.187
obliqueRSF-net	0.071 (0.009)			22.308
cif-standard			1.282	3.415
cif-rotate	0.067 (0.019)	0.708 (0.029)	40.978	4.799
cif-extension	0.064 (0.009)	0.714 (0.022)	14.406	5.796
glmnet-cox	0.058 (0.020)	0.699 (0.025)	0.391	0.002
rsf-standard	0.058 (0.022)	0.694 (0.026)	1.601	0.122
nn-cox	0.051 (0.026)	0.701 (0.038)	9.103	0.579
xgboost-cox	0.040 (0.016)	0.699 (0.026)	3.449	0.003
aorsf-random	0.039 (0.012)	0.668 (0.028)	0.889	0.053
xgboost-aft	—	0.697 (0.025)	13.258	0.006
JHS; coronary hear	t disease, n = 350	· · · · · · · · · · · · · · · · · · ·	10.200	0.000
aorsf-cph	0.040 (0.007)	0.778 (0.014)	2.083	0.144
aorsf-fast	0.039 (0.007)	0.777 (0.015)	0.557	0.141
obliqueRSF-net	0.038 (0.005)	0.784 (0.017)	592.769	868.718
cif-standard	0.038 (0.006)	0.779 (0.017)	9.787	30.975
cif-extension	0.036 (0.004)	0.781 (0.019)	56.440	20.992
ranger-extratrees	0.035 (0.005)	0.777 (0.017)	3.678	2.536
cif-rotate	0.034 (0.010)	0.769 (0.018)	187.605	23.593
glmnet-cox	0.031 (0.010)	0.774 (0.020)	2.237	0.004
rsf-standard	0.031 (0.011)	0.752 (0.016)	2.011	0.215
nn-cox	0.025 (0.020)	0.745 (0.029)	10.189	6.685
aorsf-random	0.021 (0.004)	0.746 (0.021)	1.800	0.163
xgboost-cox	0.010 (0.023)	0.785 (0.022)	4.562	0.006
1500000 001	0.010 (0.023)	0.703 (0.022)	1.502	0.000

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier		Model fitting	Risk prediction
xgboost-aft		C-Statistic 0.782 (0.017)	18.309	0.007
JHS; stroke, $n = 363$	89  n = 80	0.702 (0.017)	10.50)	0.007
aorsf-cph	0.035 (0.006)	0.805 (0.017)	2.137	0.141
aorsf-fast	0.035 (0.000)	0.807 (0.018)	0.527	0.139
obliqueRSF-net	0.028 (0.004)	0.810 (0.016)	528.781	577.511
glmnet-cox	0.028 (0.004)	0.798 (0.017)	2.915	0.004
cif-standard	0.028 (0.005)	0.803 (0.016)	10.497	32.921
rsf-standard	0.027 (0.010)	0.782 (0.018)	1.632	0.159
cif-extension	0.027 (0.010)	0.797 (0.018)	56.277	22.158
aorsf-random	0.023 (0.003)	0.770 (0.013)	1.726	0.158
ranger-extratrees	0.024 (0.005)	0.791 (0.016)	3.510	2.689
cif-rotate	0.023 (0.003)	0.785 (0.017)	186.661	24.918
nn-cox	0.014 (0.022)	0.763 (0.017)	9.541	6.840
xgboost-cox	0.014 (0.022)	0.775 (0.023)	3.500	0.005
	0.002 (0.028)	0.773 (0.023)	16.110	
xgboost-aft		0.764 (0.016)	10.110	0.007
Lung cancer; death,		0.601.(0.010)	0.200	0.020
aorsf-cph	0.063 (0.031)	0.691 (0.019)	0.308	0.030
aorsf-fast	0.060 (0.033)	0.690 (0.019)	0.122	0.030
obliqueRSF-net	0.056 (0.018)	0.679 (0.021)	219.473	7.313
cif-extension	0.050 (0.018)	0.667 (0.019)	8.429	3.209
rsf-standard	0.050 (0.035)	0.673 (0.023)	1.081	0.072
cif-standard	0.050 (0.023)	0.667 (0.022)	0.318	0.924
ranger-extratrees	0.049 (0.016)	0.675 (0.019)	0.037	0.062
cif-rotate	0.047 (0.026)	0.664 (0.021)	16.753	2.820
aorsf-random	0.043 (0.021)	0.653 (0.024)	0.549	0.027
glmnet-cox	0.041 (0.024)	0.664 (0.034)	0.127	0.002
nn-cox	0.019 (0.038)	0.625 (0.062)	9.211	0.291
xgboost-cox	0.018 (0.019)	0.644 (0.027)	1.583	0.002
xgboost-aft	_	0.652 (0.026)	8.520	0.005
MESA; coronary he		6785, p = 48		
aorsf-fast	0.064 (0.010)	0.807 (0.011)	1.213	0.363
aorsf-cph	0.061 (0.010)	0.802 (0.012)	5.020	0.374
cif-standard	0.059(0.007)	0.803 (0.013)	23.531	96.894
obliqueRSF-net	0.058 (0.006)	0.809 (0.012)	1296.402	747.185
cif-rotate	0.058 (0.009)	0.802 (0.013)	284.179	37.551
rsf-standard	0.057 (0.012)	0.795 (0.013)	3.455	1.337
ranger-extratrees	0.047 (0.004)	0.794 (0.011)	7.979	6.588
cif-extension	0.047 (0.003)	0.805 (0.013)	97.660	28.300
aorsf-random	0.041 (0.008)	0.760 (0.015)	2.930	0.404
glmnet-cox	0.038 (0.017)	0.775 (0.016)	4.514	0.006
nn-cox	0.035 (0.016)	0.766 (0.019)	13.123	15.303
xgboost-cox	0.014 (0.027)	0.802 (0.013)	5.344	0.008
xgboost-aft		0.802 (0.012)	20.582	0.009
MESA; death, $n = 6$	793, $p = 48$			
aorsf-fast	0.144 (0.008)	0.792 (0.008)	1.725	0.541
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A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction		
aorsf-cph	0.143 (0.008)	0.791 (0.008)	6.596	0.543		
rsf-standard	0.140 (0.008)	0.784 (0.009)	4.936	0.480		
cif-standard	0.134 (0.007)	0.788 (0.009)	23.408	98.656		
obliqueRSF-net	0.132 (0.006)	0.790 (0.009)	2468.159	526.499		
glmnet-cox	0.131 (0.026)	0.789 (0.012)	1.373	0.006		
nn-cox	0.129 (0.019)			17.345		
cif-rotate	0.126 (0.007)	0.783 (0.010)	319.531	37.277		
ranger-extratrees	0.113 (0.004)	0.784 (0.008)	9.502	6.313		
cif-extension	0.092 (0.003)	0.781 (0.009)	108.674	28.132		
aorsf-random	0.086 (0.006)	0.741 (0.009)	5.817	0.577		
xgboost-cox	0.057 (0.029)	0.794 (0.009)	8.811	0.009		
xgboost-aft	_	0.793 (0.009)	24.056	0.009		
MESA; heart failure	n = 6785, n = 4	· · · · · · · · · · · · · · · · · · ·				
aorsf-fast	0.115 (0.010)	0.866 (0.012)	1.118	0.321		
aorsf-cph	0.109 (0.011)	0.858 (0.013)	4.817	0.334		
rsf-standard	0.108 (0.012)	0.856 (0.012)	3.228	1.248		
cif-rotate	0.105 (0.010)	0.869 (0.013)	254.592	36.536		
cif-standard	0.102 (0.009)	0.864 (0.013)	23.983	97.903		
obliqueRSF-net	0.099 (0.007)	0.870 (0.012)	1112.448	1225.449		
aorsf-random	0.082 (0.009)	0.819 (0.016)	2.432	0.372		
cif-extension	0.077 (0.005)	0.864 (0.011)	91.356	28.914		
nn-cox	0.075 (0.021)	0.832 (0.015)	12.343	14.955		
ranger-extratrees	0.075 (0.005)	0.849 (0.015)	7.105	6.412		
glmnet-cox	0.043 (0.044)	0.767 (0.139)	3.485	0.006		
xgboost-cox	-0.011 (0.019)	0.869 (0.011)	7.135	0.009		
xgboost-aft	—	0.870 (0.012)	22.191	0.008		
MESA; $stroke$ , $n = 6783$ , $p = 48$						
cif-rotate	0.025 (0.004)	0.764 (0.017)	267.261	37.143		
aorsf-fast	0.025 (0.006)	0.764 (0.016)	1.087	0.318		
cif-standard	0.025 (0.004)	0.762 (0.017)	23.820	97.317		
obliqueRSF-net	0.024 (0.003)	0.772 (0.017)	975.645	1212.002		
aorsf-cph	0.024 (0.006)	0.760 (0.018)	4.270	0.315		
ranger-extratrees	0.022 (0.003)	0.759 (0.016)	7.125	6.067		
glmnet-cox	0.021 (0.009)	0.765 (0.017)	3.417	0.006		
cif-extension	0.021 (0.002)	0.768 (0.017)	93.628	27.983		
rsf-standard	0.019 (0.009)	0.745 (0.018)	3.032	1.194		
aorsf-random	0.016 (0.004)	0.725 (0.023)	2.309	0.342		
nn-cox	0.016 (0.008)	0.734 (0.040)	11.686	18.015		
xgboost-cox	0.000 (0.027)			0.008		
xgboost-aft	_	0.764 (0.015)	20.407	0.008		
Monoclonal gammo	nathy: death. n =	` /				
cif-rotate	0.159 (0.019)	0.744 (0.014)	15.330	4.515		
aorsf-cph	0.158 (0.016)	0.743 (0.011)	1.176	0.092		
aorsf-fast	0.157 (0.016)	0.743 (0.011)	0.407	0.091		
cif-standard	0.151 (0.015)	0.738 (0.012)	1.512	6.113		
vii ovaliente	3.121 (0.013)	3.,23 (0.012)	1.012	0.110		

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction				
rsf-standard	0.151 (0.017)	0.737 (0.011)	2.305	0.203				
obliqueRSF-net	0.148 (0.009)	0.748 (0.011)	543.632	42.863				
aorsf-random	0.148 (0.013)	0.738 (0.012)	1.747	0.086				
cif-extension	0.143 (0.009)	0.747 (0.013)	10.794	4.507				
glmnet-cox	0.137 (0.021)	0.726 (0.014)	0.146	0.002				
xgboost-cox	0.122 (0.012)	0.733 (0.012)	4.230	0.003				
ranger-extratrees	0.115 (0.005)	0.744 (0.012)	0.052	0.169				
nn-cox	0.026 (0.051)	0.598 (0.100)	11.948	0.652				
xgboost-aft	—	0.733 (0.013) 13.595		0.006				
Monoclonal gammopathy; malignancy, $n = 1384$ , $p = 8$								
glmnet-cox	0.015 (0.011)	0.651 (0.055)	0.129	0.002				
obliqueRSF-net	0.012 (0.008)	0.649 (0.032)	143.443	22.157				
aorsf-cph	0.010 (0.013)	0.644 (0.036)	0.594	0.041				
aorsf-fast	0.010 (0.014)	0.641 (0.036)	0.190	0.041				
ranger-extratrees	0.008 (0.006)	0.642 (0.030)	0.054	0.156				
cif-extension	0.008 (0.010)	0.625 (0.028)	8.632	4.411				
aorsf-random	0.007 (0.013)	0.636 (0.032)	0.532	0.040				
cif-standard	0.006 (0.011)	0.628 (0.033)	1.490	5.778				
xgboost-cox	0.005 (0.011)	0.639 (0.040)	1.686	0.003				
nn-cox	-0.003 (0.005)	0.515 (0.056)	7.746	0.606				
rsf-standard	-0.009 (0.018)	· /		0.069				
cif-rotate	-0.024 (0.023)			4.047				
xgboost-aft	—	0.629 (0.039) 11.326		0.006				
Movies released in 2	015-2018: gross	` ′						
cif-rotate	0.636 (0.024)	0.943 (0.007)	19.882	3.487				
glmnet-cox	0.618 (0.034)	0.940 (0.009)	0.205	0.002				
nn-cox	0.544 (0.055)	0.909 (0.020)	13.922	0.580				
aorsf-cph	0.523 (0.024)	0.926 (0.011)	0.783	0.043				
rsf-standard	0.519 (0.022)	0.922 (0.010)	1.503	0.103				
aorsf-fast			0.227	0.043				
xgboost-cox	0.512 (0.029)	0.922 (0.012) 0.932 (0.009)	13.524	0.004				
cif-standard	0.472 (0.029)	0.902 (0.018)	0.354	1.715				
cif-extension	0.454 (0.025)	0.920 (0.013)	9.152	3.724				
ranger-extratrees	0.430 (0.025)	0.900 (0.019)	0.045	0.090				
obliqueRSF-net	0.309 (0.020)	0.912 (0.017)	124.706	10.004				
aorsf-random	0.303 (0.029)	0.851 (0.026)	0.950	0.042				
xgboost-aft	_	0.927 (0.010)	35.466	0.007				
NCCTG Lung Canc	er: death. n = 22							
ranger-extratrees	0.062 (0.028)	0.675 (0.033)	0.022	0.030				
aorsf-random	0.061 (0.029)	0.676 (0.027)	0.324	0.015				
aorsf-fast	0.061 (0.042)	0.672 (0.025)	0.066	0.017				
aorsf-cph	0.059 (0.040)	0.671 (0.024)	0.153	0.016				
obliqueRSF-net	0.056 (0.025)	0.678 (0.030)	88.165	3.793				
cif-standard	0.055 (0.032)	0.670 (0.030)	0.128	0.254				
cif-extension	0.051 (0.032)	0.664 (0.029)	3.845	1.378				
OH CAUCHSTON	3.031 (0.032)	0.001 (0.02))	5.075	1.570				

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

glmnet-cox						
rsf-standard 0.023 (0.039) 0.642 (0.025) 0.099 0.02 cif-rotate 0.017 (0.041) 0.632 (0.032) 4.906 1.27 xgboost-cox 0.012 (0.022) 0.648 (0.031) 1.076 0.00 nn-cox -0.020 (0.019) 0.517 (0.110) 7.701 0.22 xgboost-aft — 0.637 (0.034) 7.679 0.00 NKI 70 gene signature; death or metastasis, n = 144, p = 77  aorsf-cph 0.124 (0.049) 0.802 (0.051) 0.074 0.01 aorsf-fast 0.121 (0.052) 0.802 (0.054) 0.049 0.01 cif-rotate 0.118 (0.059) 0.787 (0.049) 26.703 2.97 obliqueRSF-net 0.098 (0.049) 0.790 (0.062) 77.169 0.55 cif-extension 0.098 (0.055) 0.799 (0.061) 8.367 3.55 cif-standard 0.088 (0.051) 0.781 (0.065) 0.141 0.11 rsf-standard 0.087 (0.044) 0.774 (0.054) 0.023 0.03 nn-cox 0.060 (0.065) 0.746 (0.059) 7.922 0.11 aorsf-random 0.051 (0.047) 0.733 (0.063) 0.150 0.03 glmnet-cox 0.049 (0.064) 0.726 (0.090) 0.271 0.06 xgboost-aft — 0.770 (0.056) 4.807 0.01 ygboost-aft — 0.770 (0.056) 4.807 0.01 ygboost-aft 0.213 (0.009) 0.869 (0.006) 17.803 1.37 aorsf-fast 0.212 (0.009) 0.869 (0.006) 17.803 1.37 aorsf-fast 0.212 (0.009) 0.869 (0.006) 4.902 1.33 rsf-standard 0.207 (0.009) 0.869 (0.006) 17.803 1.37 aorsf-fast 0.212 (0.009) 0.869 (0.006) 4.902 1.33 rsf-standard 0.207 (0.009) 0.869 (0.006) 4.902 1.33 ranger-extratrees 0.181 (0.007) 0.860 (0.005) 10.179 1.11 yglmnet-cox 0.207 (0.011) 0.860 (0.005) 10.179 1.13 yglmset-cox 0.207 (0.005) 0.868 (0.005) 2.59.239 60.3 aorsf-random 0.141 (0.006) 0.839 (0.007) 9.973 1.44 ygloost-co		Scaled Brier	C-Statistic	Model fitting	Risk prediction	
rsf-standard 0.023 (0.039) 0.642 (0.025) 0.099 0.02 cif-rotate 0.017 (0.041) 0.632 (0.032) 4.906 1.27 xgboost-cox 0.012 (0.022) 0.648 (0.031) 1.076 0.00 nn-cox -0.020 (0.019) 0.517 (0.110) 7.701 0.20 xgboost-aft — 0.637 (0.034) 7.679 0.00 NKI 70 gene signature; death or metastasis, n = 144, p = 77  aorsf-cph 0.124 (0.049) 0.802 (0.051) 0.074 0.01 aorsf-fast 0.121 (0.052) 0.802 (0.054) 0.049 0.01 cif-rotate 0.118 (0.059) 0.787 (0.049) 26.703 2.97 obliqueRSF-net 0.098 (0.049) 0.790 (0.062) 77.169 0.55 cif-extension 0.098 (0.055) 0.799 (0.061) 8.367 3.55 cif-standard 0.088 (0.051) 0.781 (0.065) 0.141 0.11 rsf-standard 0.088 (0.051) 0.781 (0.065) 0.141 0.12 rsf-standard 0.088 (0.051) 0.781 (0.065) 0.141 0.13 rsf-standard 0.087 (0.044) 0.774 (0.054) 0.023 0.03 nn-cox 0.060 (0.065) 0.746 (0.059) 7.922 0.11 aorsf-random 0.051 (0.047) 0.733 (0.063) 0.150 0.01 glmnet-cox 0.049 (0.064) 0.726 (0.090) 0.271 0.00 xgboost-aft — 0.770 (0.056) 4.807 0.00 0.07 (0.056) 4.807 0.00 0.05 (0.056) 0.05 (0.050) 0.066 0.00 0.05 (0.050) 0.056 0.00 0.05 (0.050) 0.056 0.00 0.05 (0.050) 0.056 0.00 0.05 (0.050) 0.056 0.00 0.05 (0.050) 0.056 0.00 0.05 (0.050) 0.056 0.00 0.05 (0.050) 0.056 0.00 0.05 (0.050) 0.056 0.00 0.050 (0.055) 0.746 (0.059) 7.922 0.11 0.00 0.050 (0.055) 0.0	glmnet-cox	0.033 (0.031)	0.638 (0.059)	0.097	0.002	
xgboost-cox         0.012 (0.022)         0.648 (0.031)         1.076         0.00           nn-cox         -0.020 (0.019)         0.517 (0.110)         7.701         0.20           xgboost-aft         —         0.637 (0.034)         7.679         0.00           NKI 70 gene signature; death or metastasis, n = 144, p = 77           aorsf-cph         0.124 (0.049)         0.802 (0.051)         0.074         0.01           aorsf-fast         0.121 (0.052)         0.802 (0.054)         0.049         0.01           cif-rotate         0.118 (0.059)         0.787 (0.049)         26.703         2.97           obliqueRSF-net         0.098 (0.049)         0.799 (0.061)         8.367         3.53           cif-extension         0.098 (0.055)         0.799 (0.061)         8.367         3.53           cif-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           anrsf-random         0.051 (0.047)         0.733 (0.063)         0.150           glmnet-cox         0.049 (0.064)         0.726 (0.099)         <				0.099	0.038	
nn-cox	cif-rotate	0.017 (0.041)	0.632 (0.032)	4.906	1.275	
xgboost-aft         —         0.637 (0.034)         7.679         0.00           NKI 70 gene signature; death or metastasis, n = 144, p = 77           aorsf-cph         0.124 (0.049)         0.802 (0.051)         0.074         0.01           aorsf-fast         0.121 (0.052)         0.802 (0.054)         0.049         0.01           cif-rotate         0.118 (0.059)         0.787 (0.049)         26.703         2.97           obliqueRSF-net         0.098 (0.049)         0.790 (0.062)         77.169         0.55           cif-extension         0.098 (0.055)         0.799 (0.061)         8.367         3.5           cif-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.774 (0.054)         0.023         0.03           nn-cox         0.060 (0.065)         0.746 (0.059)         7.922         0.11           glmnet-cox         0.049 (0.064)         0.726 (0.099)         0.271         0.00           xgboost-aft         —         0.770 (0.056)	xgboost-cox	0.012 (0.022)	0.648 (0.031)	1.076	0.002	
NKI 70 gene signature; death or metastasis, n = 144, p = 77           aorsf-cph         0.124 (0.049)         0.802 (0.051)         0.074         0.01           aorsf-fast         0.121 (0.052)         0.802 (0.054)         0.049         0.01           cif-rotate         0.118 (0.059)         0.787 (0.049)         26.703         2.97           obliqueRSF-net         0.098 (0.049)         0.790 (0.062)         77.169         0.55           cif-extension         0.098 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.774 (0.054)         0.023         0.03           nn-cox         0.060 (0.065)         0.746 (0.059)         7.922         0.11           aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.01           glmnet-cox         0.049 (0.064)         0.726 (0.090)         0.271         0.00           xgboost-aft         —         0.770 (0.056)         4.807         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24 <td>nn-cox</td> <td>-0.020 (0.019)</td> <td>0.517 (0.110)</td> <td>7.701</td> <td>0.203</td>	nn-cox	-0.020 (0.019)	0.517 (0.110)	7.701	0.203	
aorsf-cph         0.124 (0.049)         0.802 (0.051)         0.074         0.01           aorsf-fast         0.121 (0.052)         0.802 (0.054)         0.049         0.01           cif-rotate         0.118 (0.059)         0.787 (0.049)         26.703         2.97           obliqueRSF-net         0.098 (0.049)         0.790 (0.062)         77.169         0.55           cif-extension         0.098 (0.055)         0.799 (0.061)         8.367         3.53           cif-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.775 (0.054)         0.023         0.03           nn-cox         0.060 (0.065)         0.746 (0.059)         7.922         0.11           aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.00           glmnet-cox         0.049 (0.064)         0.726 (0.099)         0.271         0.00           xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           xgboost-aft         -         0.770 (0.056)         4.807         0.00           Non-alcohol f	xgboost-aft	_	0.637 (0.034)	7.679	0.005	
aorsf-fast         0.121 (0.052)         0.802 (0.054)         0.049         0.01           cif-rotate         0.118 (0.059)         0.787 (0.049)         26.703         2.95           obliqueRSF-net         0.098 (0.049)         0.790 (0.062)         77.169         0.55           cif-extension         0.098 (0.055)         0.799 (0.061)         8.367         3.53           cif-extension         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.774 (0.054)         0.023         0.03           nn-cox         0.0660 (0.065)         0.746 (0.059)         7.922         0.11           aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.01           glmnet-cox         0.049 (0.064)         0.726 (0.090)         0.271         0.00           xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24         24           aorsf-fast         0.213 (0.009)         0.869 (0.006)         1.807         0.00           Non-alcohol fatty liver disease; death,						
cif-rotate         0.118 (0.059)         0.787 (0.049)         26.703         2.97           obliqueRSF-net         0.098 (0.049)         0.790 (0.062)         77.169         0.55           cif-extension         0.098 (0.055)         0.799 (0.061)         8.367         3.52           cif-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.774 (0.054)         0.023         0.03           nn-cox         0.060 (0.065)         0.746 (0.059)         7.922         0.11           aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.01           glmnet-cox         0.049 (0.064)         0.726 (0.099)         0.271         0.00           xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           xgboost-aft         -         0.770 (0.056)         4.807         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24         24         aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006					0.014	
obliqueRSF-net         0.098 (0.049)         0.790 (0.062)         77.169         0.55           cif-extension         0.098 (0.055)         0.799 (0.061)         8.367         3.53           cif-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.774 (0.054)         0.023         0.03           nn-cox         0.060 (0.065)         0.746 (0.059)         7.922         0.11           aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.01           glmnet-cox         0.049 (0.064)         0.726 (0.090)         0.271         0.00           xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           xgboost-aft         —         0.770 (0.056)         4.807         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24         aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006)         17.803         1.32           rsf-standard         0.207 (0.011)         0.860 (0.005) <td< td=""><td></td><td>\ /</td><td></td><td></td><td>0.015</td></td<>		\ /			0.015	
cif-extension         0.098 (0.055)         0.799 (0.061)         8.367         3.55           cif-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.774 (0.054)         0.023         0.03           nn-cox         0.060 (0.065)         0.746 (0.059)         7.922         0.11           aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.01           glmnet-cox         0.049 (0.064)         0.726 (0.090)         0.271         0.00           xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           xgboost-aft         —         0.770 (0.056)         4.807         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24         aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006)         17.803         1.37           rsf-standard         0.207 (0.009)         0.869 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         10.			\ /	26.703	2.970	
cif-standard         0.088 (0.051)         0.781 (0.065)         0.141         0.13           rsf-standard         0.087 (0.048)         0.755 (0.050)         0.066         0.02           ranger-extratrees         0.064 (0.044)         0.774 (0.054)         0.023         0.03           nn-cox         0.060 (0.065)         0.746 (0.059)         7.922         0.11           aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.00           glmnet-cox         0.049 (0.064)         0.726 (0.090)         0.271         0.00           xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           xgboost-aft         —         0.770 (0.056)         4.807         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24         aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-stat         0.212 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         10.179         1.12           glmet-cox         0.207 (0.011)         0.860 (0.005)         10.3887<			` /		0.555	
rsf-standard 0.087 (0.048) 0.755 (0.050) 0.066 0.02 ranger-extratrees 0.064 (0.044) 0.774 (0.054) 0.023 0.03 nn-cox 0.060 (0.065) 0.746 (0.059) 7.922 0.11 aorsf-random 0.051 (0.047) 0.733 (0.063) 0.150 0.01 glmnet-cox 0.049 (0.064) 0.726 (0.090) 0.271 0.00 xgboost-cox -0.028 (0.029) 0.569 (0.094) 0.119 0.00 xgboost-aft — 0.770 (0.056) 4.807 0.00 Non-alcohol fatty liver disease; death, n = 17549, p = 24 aorsf-cph 0.213 (0.009) 0.869 (0.006) 17.803 1.37 rsf-standard 0.207 (0.009) 0.869 (0.006) 4.902 1.33 rsf-standard 0.207 (0.009) 0.869 (0.005) 10.179 1.12 glmnet-cox 0.207 (0.011) 0.860 (0.005) 10.179 1.12 glmnet-cox 0.207 (0.011) 0.860 (0.005) 1.330 0.01 cif-standard 0.205 (0.007) 0.863 (0.006) 64.986 621.6 obliqueRSF-net 0.204 (0.008) 0.868 (0.006) 2703.887 9972. cif-rotate 0.190 (0.008) 0.868 (0.006) 2703.887 9972. cif-rotate 0.190 (0.008) 0.865 (0.005) 259.239 60.3 ranger-extratrees 0.181 (0.007) 0.860 (0.005) 40.520 81.6 cif-extension 0.166 (0.003) 0.866 (0.006) 124.635 54.3 aorsf-random 0.141 (0.006) 0.839 (0.007) 9.973 1.49 xgboost-cox 0.022 (0.014) 0.876 (0.005) 9.315 0.01 nn-cox 0.000 (0.002) 0.557 (0.095) 19.415 103.2 xgboost-aft — 0.875 (0.005) 31.562 0.01 Primary biliary cholangitis; death, n = 276, p = 19 aorsf-fast 0.423 (0.035) 0.904 (0.021) 0.069 0.01 cif-rotate 0.405 (0.040) 0.899 (0.022) 9.295 2.06 rsf-standard 0.392 (0.034) 0.901 (0.022) 0.151 0.01 cif-rotate 0.405 (0.040) 0.899 (0.022) 9.295 2.06 rsf-standard 0.392 (0.034) 0.901 (0.022) 0.151 0.01 cif-rotate 0.405 (0.040) 0.899 (0.022) 9.295 2.06 rsf-standard 0.392 (0.034) 0.904 (0.025) 0.188 0.33 cif-extension 0.344 (0.031) 0.891 (0.020) 0.277 0.01 glmnet-cox 0.342 (0.044) 0.886 (0.028) 0.117 0.00					3.531	
ranger-extratrees 0.064 (0.044) 0.774 (0.054) 0.023 0.03 nn-cox 0.060 (0.065) 0.746 (0.059) 7.922 0.11 aorsf-random 0.051 (0.047) 0.733 (0.063) 0.150 0.01 glmnet-cox 0.049 (0.064) 0.726 (0.090) 0.271 0.00 xgboost-cox -0.028 (0.029) 0.569 (0.094) 0.119 0.00 xgboost-aft					0.130	
nn-cox	rsf-standard				0.025	
aorsf-random         0.051 (0.047)         0.733 (0.063)         0.150         0.01           glmnet-cox         0.049 (0.064)         0.726 (0.090)         0.271         0.00           xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           xgboost-aft         —         0.770 (0.056)         4.807         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24           aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006)         4.902         1.33           rsf-standard         0.207 (0.009)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)	ranger-extratrees				0.030	
glmnet-cox		0.060 (0.065)			0.115	
xgboost-cox         -0.028 (0.029)         0.569 (0.094)         0.119         0.00           Non-alcohol fatty liver disease; death,         n = 17549, p = 24           aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006)         4.902         1.33           rsf-standard         0.207 (0.009)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         1.330         0.01           cif-standard         0.205 (0.007)         0.863 (0.006)         64.986         621.6           obliqueRSF-net         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000	*****		0.733 (0.063)		0.015	
xgboost-aft         —         0.770 (0.056)         4.807         0.00           Non-alcohol fatty liver disease; death, n = 17549, p = 24           aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006)         4.902         1.33           rsf-standard         0.207 (0.009)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         1.330         0.01           cif-standard         0.205 (0.007)         0.863 (0.006)         64.986         621.6           obliqueRSF-net         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.55		\ /			0.002	
Non-alcohol fatty liver disease; death, n = 17549, p = 24           aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006)         4.902         1.33           rsf-standard         0.207 (0.009)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         1.330         0.01           cif-standard         0.205 (0.007)         0.863 (0.006)         64.986         621.6           obliqueRSF-net         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —		-0.028 (0.029)			0.002	
aorsf-cph         0.213 (0.009)         0.869 (0.006)         17.803         1.37           aorsf-fast         0.212 (0.009)         0.869 (0.006)         4.902         1.33           rsf-standard         0.207 (0.009)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         1.330         0.01           cif-standard         0.205 (0.007)         0.863 (0.006)         64.986         621.6           obliqueRSF-net         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01 <td< td=""><td>xgboost-aft</td><td>_</td><td>0.770(0.056)</td><td>4.807</td><td>0.005</td></td<>	xgboost-aft	_	0.770(0.056)	4.807	0.005	
aorsf-fast         0.212 (0.009)         0.869 (0.006)         4.902         1.33           rsf-standard         0.207 (0.009)         0.860 (0.005)         10.179         1.12           glmnet-cox         0.207 (0.011)         0.860 (0.005)         1.330         0.01           cif-standard         0.205 (0.007)         0.863 (0.006)         64.986         621.6           obliqueRSF-net         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01           Primary biliary cholangitis; death, n = 276, p = 19         aorsf-fast         0.423 (0.035)         0.904 (0.021)						
rsf-standard 0.207 (0.009) 0.860 (0.005) 10.179 1.12 glmnet-cox 0.207 (0.011) 0.860 (0.005) 1.330 0.01 cif-standard 0.205 (0.007) 0.863 (0.006) 64.986 621.6 obliqueRSF-net 0.204 (0.008) 0.868 (0.006) 2703.887 9972. cif-rotate 0.190 (0.008) 0.865 (0.005) 259.239 60.3 ranger-extratrees 0.181 (0.007) 0.860 (0.005) 40.520 81.6 cif-extension 0.166 (0.003) 0.866 (0.006) 124.635 54.3 aorsf-random 0.141 (0.006) 0.839 (0.007) 9.973 1.49 xgboost-cox 0.022 (0.014) 0.876 (0.005) 9.315 0.01 nn-cox 0.000 (0.002) 0.557 (0.095) 19.415 103.2 xgboost-aft — 0.875 (0.005) 31.562 0.01 Primary biliary cholangitis; death, n = 276, p = 19  aorsf-fast 0.423 (0.035) 0.904 (0.021) 0.069 0.01 cif-rotate 0.405 (0.040) 0.899 (0.022) 9.295 2.06 rsf-standard 0.392 (0.034) 0.895 (0.023) 0.094 0.03 obliqueRSF-net 0.359 (0.030) 0.908 (0.022) 101.477 1.86 cif-standard 0.352 (0.034) 0.901 (0.025) 0.188 0.33 cif-extension 0.348 (0.033) 0.901 (0.023) 5.399 2.04 aorsf-random 0.344 (0.031) 0.891 (0.020) 0.277 0.01 glmnet-cox 0.342 (0.044) 0.886 (0.028) 0.117 0.000					1.370	
glmnet-cox					1.336	
cif-standard         0.205 (0.007)         0.863 (0.006)         64.986         621.6           obliqueRSF-net         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01           Primary biliary cholangitis; death, n = 276, p = 19         19           aorsf-fast         0.423 (0.035)         0.904 (0.021)         0.069         0.01           aorsf-fast         0.423 (0.034)         0.901 (0.022)         0.151         0.01           cif-rotate         0.405 (0.040)         0.889 (0.022)         9.295         2.06           rsf-standard         0.352 (0.034)					1.126	
obliqueRSF-net         0.204 (0.008)         0.868 (0.006)         2703.887         9972.           cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01           Primary biliary cholangitis; death, n = 276, p = 19         19         19         10.00         10.00           aorsf-fast         0.423 (0.035)         0.904 (0.021)         0.069         0.01           aorsf-cph         0.413 (0.034)         0.901 (0.022)         0.151         0.01           cif-rotate         0.405 (0.040)         0.899 (0.022)         9.295         2.06           rsf-standard         0.392 (0.034)         0.895 (0.023)         0.094         0.03 <tr< td=""><td>0</td><td></td><td></td><td></td><td>0.012</td></tr<>	0				0.012	
cif-rotate         0.190 (0.008)         0.865 (0.005)         259.239         60.3           ranger-extratrees         0.181 (0.007)         0.860 (0.005)         40.520         81.6           cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01           Primary biliary cholangitis; death, n = 276, p = 19         19         19         10					621.600	
ranger-extratrees 0.181 (0.007) 0.860 (0.005) 40.520 81.6 cif-extension 0.166 (0.003) 0.866 (0.006) 124.635 54.3 aorsf-random 0.141 (0.006) 0.839 (0.007) 9.973 1.49 xgboost-cox 0.022 (0.014) 0.876 (0.005) 9.315 0.01 nn-cox 0.000 (0.002) 0.557 (0.095) 19.415 103.2 xgboost-aft — 0.875 (0.005) 31.562 0.01 Primary biliary cholangitis; death, n = 276, p = 19 aorsf-fast 0.423 (0.035) 0.904 (0.021) 0.069 0.01 cif-rotate 0.405 (0.040) 0.899 (0.022) 9.295 2.06 rsf-standard 0.392 (0.034) 0.895 (0.023) 0.094 0.03 obliqueRSF-net 0.359 (0.030) 0.908 (0.022) 101.477 1.86 cif-standard 0.352 (0.034) 0.904 (0.025) 0.188 0.33 cif-extension 0.348 (0.033) 0.901 (0.023) 5.399 2.04 aorsf-random 0.344 (0.031) 0.891 (0.020) 0.277 0.01 glmnet-cox 0.342 (0.044) 0.886 (0.028) 0.117 0.00					9972.393	
cif-extension         0.166 (0.003)         0.866 (0.006)         124.635         54.3           aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01           Primary biliary cholangitis; death, n = 276, p = 19           aorsf-fast         0.423 (0.035)         0.904 (0.021)         0.069         0.01           aorsf-cph         0.413 (0.034)         0.901 (0.022)         0.151         0.01           cif-rotate         0.405 (0.040)         0.899 (0.022)         9.295         2.06           rsf-standard         0.392 (0.034)         0.895 (0.023)         0.094         0.03           obliqueRSF-net         0.359 (0.030)         0.908 (0.022)         101.477         1.86           cif-standard         0.352 (0.034)         0.904 (0.025)         0.188         0.33           cif-extension         0.348 (0.033)         0.901 (0.023)         5.399         2.04           aorsf-random         0.342 (0.044)         0.886					60.313	
aorsf-random         0.141 (0.006)         0.839 (0.007)         9.973         1.49           xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01           Primary biliary cholangitis; death, n = 276, p = 19           aorsf-fast         0.423 (0.035)         0.904 (0.021)         0.069         0.01           aorsf-cph         0.413 (0.034)         0.901 (0.022)         0.151         0.01           cif-rotate         0.405 (0.040)         0.899 (0.022)         9.295         2.06           rsf-standard         0.392 (0.034)         0.895 (0.023)         0.094         0.03           obliqueRSF-net         0.359 (0.030)         0.908 (0.022)         101.477         1.86           cif-standard         0.352 (0.034)         0.904 (0.025)         0.188         0.33           cif-extension         0.348 (0.033)         0.901 (0.023)         5.399         2.04           aorsf-random         0.344 (0.031)         0.891 (0.020)         0.277         0.01           glmnet-cox         0.342 (0.044)         0.886 (0.02					81.674	
xgboost-cox         0.022 (0.014)         0.876 (0.005)         9.315         0.01           nn-cox         0.000 (0.002)         0.557 (0.095)         19.415         103.2           xgboost-aft         —         0.875 (0.005)         31.562         0.01           Primary biliary cholangitis; death, n = 276, p = 19           aorsf-fast         0.423 (0.035)         0.904 (0.021)         0.069         0.01           aorsf-cph         0.413 (0.034)         0.901 (0.022)         0.151         0.01           cif-rotate         0.405 (0.040)         0.899 (0.022)         9.295         2.06           rsf-standard         0.392 (0.034)         0.895 (0.023)         0.094         0.03           obliqueRSF-net         0.359 (0.030)         0.908 (0.022)         101.477         1.86           cif-standard         0.352 (0.034)         0.904 (0.025)         0.188         0.33           cif-extension         0.348 (0.033)         0.901 (0.023)         5.399         2.04           aorsf-random         0.344 (0.031)         0.891 (0.020)         0.277         0.01           glmnet-cox         0.342 (0.044)         0.886 (0.028)         0.117         0.00			(0.003) $0.866$ $(0.006)$ $124$		54.345	
nn-cox					1.490	
xgboost-aft— $0.875 (0.005)$ $31.562$ $0.016$ Primary biliary cholangitis; death, $n = 276$ , $p = 19$ aorsf-fast $0.423 (0.035)$ $0.904 (0.021)$ $0.069$ $0.016$ aorsf-cph $0.413 (0.034)$ $0.901 (0.022)$ $0.151$ $0.016$ cif-rotate $0.405 (0.040)$ $0.899 (0.022)$ $9.295$ $2.066$ rsf-standard $0.392 (0.034)$ $0.895 (0.023)$ $0.094$ $0.036$ obliqueRSF-net $0.359 (0.030)$ $0.908 (0.022)$ $101.477$ $1.866$ cif-standard $0.352 (0.034)$ $0.904 (0.025)$ $0.188$ $0.336$ cif-extension $0.348 (0.033)$ $0.901 (0.023)$ $5.399$ $2.046$ aorsf-random $0.344 (0.031)$ $0.891 (0.020)$ $0.277$ $0.016$ glmnet-cox $0.342 (0.044)$ $0.886 (0.028)$ $0.117$ $0.006$	xgboost-cox				0.017	
Primary biliary cholangitis; death, $n = 276$ , $p = 19$ aorsf-fast $0.423$ ( $0.035$ ) $0.904$ ( $0.021$ ) $0.069$ $0.01$ aorsf-cph $0.413$ ( $0.034$ ) $0.901$ ( $0.022$ ) $0.151$ $0.01$ cif-rotate $0.405$ ( $0.040$ ) $0.899$ ( $0.022$ ) $9.295$ $2.06$ rsf-standard $0.392$ ( $0.034$ ) $0.895$ ( $0.023$ ) $0.094$ $0.03$ obliqueRSF-net $0.359$ ( $0.030$ ) $0.908$ ( $0.022$ ) $101.477$ $1.86$ cif-standard $0.352$ ( $0.034$ ) $0.904$ ( $0.025$ ) $0.188$ $0.33$ cif-extension $0.348$ ( $0.033$ ) $0.901$ ( $0.023$ ) $5.399$ $2.04$ aorsf-random $0.344$ ( $0.031$ ) $0.891$ ( $0.020$ ) $0.277$ $0.01$ glmnet-cox $0.342$ ( $0.044$ ) $0.886$ ( $0.028$ ) $0.117$ $0.00$		0.000 (0.002)			103.251	
aorsf-fast         0.423 (0.035)         0.904 (0.021)         0.069         0.01           aorsf-cph         0.413 (0.034)         0.901 (0.022)         0.151         0.01           cif-rotate         0.405 (0.040)         0.899 (0.022)         9.295         2.06           rsf-standard         0.392 (0.034)         0.895 (0.023)         0.094         0.03           obliqueRSF-net         0.359 (0.030)         0.908 (0.022)         101.477         1.86           cif-standard         0.352 (0.034)         0.904 (0.025)         0.188         0.33           cif-extension         0.348 (0.033)         0.901 (0.023)         5.399         2.04           aorsf-random         0.344 (0.031)         0.891 (0.020)         0.277         0.01           glmnet-cox         0.342 (0.044)         0.886 (0.028)         0.117         0.00		_	* * * * * * * * * * * * * * * * * * * *	31.562	0.014	
aorsf-cph         0.413 (0.034)         0.901 (0.022)         0.151         0.01           cif-rotate         0.405 (0.040)         0.899 (0.022)         9.295         2.06           rsf-standard         0.392 (0.034)         0.895 (0.023)         0.094         0.03           obliqueRSF-net         0.359 (0.030)         0.908 (0.022)         101.477         1.86           cif-standard         0.352 (0.034)         0.904 (0.025)         0.188         0.33           cif-extension         0.348 (0.033)         0.901 (0.023)         5.399         2.04           aorsf-random         0.344 (0.031)         0.891 (0.020)         0.277         0.01           glmnet-cox         0.342 (0.044)         0.886 (0.028)         0.117         0.00						
cif-rotate         0.405 (0.040)         0.899 (0.022)         9.295         2.06           rsf-standard         0.392 (0.034)         0.895 (0.023)         0.094         0.03           obliqueRSF-net         0.359 (0.030)         0.908 (0.022)         101.477         1.86           cif-standard         0.352 (0.034)         0.904 (0.025)         0.188         0.33           cif-extension         0.348 (0.033)         0.901 (0.023)         5.399         2.04           aorsf-random         0.344 (0.031)         0.891 (0.020)         0.277         0.01           glmnet-cox         0.342 (0.044)         0.886 (0.028)         0.117         0.00					0.018	
rsf-standard 0.392 (0.034) 0.895 (0.023) 0.094 0.03 obliqueRSF-net 0.359 (0.030) 0.908 (0.022) 101.477 1.86 cif-standard 0.352 (0.034) 0.904 (0.025) 0.188 0.33 cif-extension 0.348 (0.033) 0.901 (0.023) 5.399 2.04 aorsf-random 0.344 (0.031) 0.891 (0.020) 0.277 0.01 glmnet-cox 0.342 (0.044) 0.886 (0.028) 0.117 0.00					0.018	
obliqueRSF-net         0.359 (0.030)         0.908 (0.022)         101.477         1.86           cif-standard         0.352 (0.034)         0.904 (0.025)         0.188         0.33           cif-extension         0.348 (0.033)         0.901 (0.023)         5.399         2.04           aorsf-random         0.344 (0.031)         0.891 (0.020)         0.277         0.01           glmnet-cox         0.342 (0.044)         0.886 (0.028)         0.117         0.00			\ /		2.069	
cif-standard       0.352 (0.034)       0.904 (0.025)       0.188       0.33         cif-extension       0.348 (0.033)       0.901 (0.023)       5.399       2.04         aorsf-random       0.344 (0.031)       0.891 (0.020)       0.277       0.01         glmnet-cox       0.342 (0.044)       0.886 (0.028)       0.117       0.00					0.038	
cif-extension       0.348 (0.033)       0.901 (0.023)       5.399       2.04         aorsf-random       0.344 (0.031)       0.891 (0.020)       0.277       0.01         glmnet-cox       0.342 (0.044)       0.886 (0.028)       0.117       0.00			\ /		1.862	
aorsf-random 0.344 (0.031) 0.891 (0.020) 0.277 0.01 glmnet-cox 0.342 (0.044) 0.886 (0.028) 0.117 0.00			` /		0.331	
glmnet-cox 0.342 (0.044) 0.886 (0.028) 0.117 0.00					2.040	
		` ,	\ /		0.019	
	_				0.002	
ranger-extratrees 0.277 (0.027) 0.894 (0.027) 0.026 0.03	ranger-extratrees	0.277 (0.027)	0.894 (0.027)	0.026	0.036	

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Canta J.D. C.	C Chair	M- 4-1 Cu!	Dialogue 4' ce'
	Scaled Brier	C-Statistic	Model fitting	Risk prediction
xgboost-cox	0.256 (0.103)	0.882 (0.026)	5.057	0.002
nn-cox	-0.024 (0.033)	0.556 (0.123)	8.423	0.195
xgboost-aft	_	0.883 (0.024)	9.373	0.006
Rotterdam tumor ba	nk; death, $n = 29$	982, p = 11		
aorsf-cph	0.163 (0.012)	0.759 (0.009)	2.494	0.205
aorsf-random	0.161 (0.011)	0.759 (0.010)	3.004	0.189
aorsf-fast	0.160 (0.012)	0.757 (0.009)	0.806	0.205
cif-standard	0.159 (0.010)	0.759 (0.009)	4.694	22.024
rsf-standard	0.159 (0.014)	0.756 (0.009)	2.995	0.391
obliqueRSF-net	0.156 (0.007)	0.759 (0.009)	931.931	64.305
cif-rotate	0.147 (0.011)	0.751 (0.011)	34.565	8.675
ranger-extratrees	0.139 (0.006)	0.749 (0.009)	3.211	2.477
xgboost-cox	0.130 (0.014)	0.753 (0.009)	4.472	0.004
cif-extension	0.129 (0.004)	0.751 (0.008)	22.084	8.110
glmnet-cox	0.118 (0.008)	0.731 (0.009)	0.247	0.003
nn-cox	-0.001 (0.001)	0.507 (0.049)	13.019	7.622
xgboost-aft	_	0.761 (0.009)	16.743	0.006
Rotterdam tumor ba			2.225	0.405
aorsf-random	0.145 (0.011)	0.734 (0.009)	3.327	0.197
aorsf-cph	0.145 (0.012)	0.734 (0.009)	2.801	0.221
cif-standard	0.144 (0.011)	0.734 (0.009)	4.829	22.205
aorsf-fast	0.143 (0.011)	0.733 (0.009)	0.883	0.217
obliqueRSF-net rsf-standard	0.142 (0.008)	0.737 (0.009)	870.086	81.412
	0.139 (0.012) 0.135 (0.007)	0.731 (0.008) 0.734 (0.009)	3.113 3.100	0.947 2.527
ranger-extratrees cif-rotate	0.133 (0.007)	0.734 (0.009)	36.405	8.349
cif-extension	0.129 (0.010)	0.723 (0.009)	22.537	8.390
glmnet-cox	0.117 (0.008)	0.731 (0.008)	0.227	0.004
xgboost-cox	0.117 (0.008)	0.727 (0.008)	4.123	0.004
nn-cox	-0.002 (0.002)	0.515 (0.029)	13.602	8.901
xgboost-aft	· · · · · · · · · · · · · · · · · · ·		16.138	0.006
Serum free light cha	$\sin \cdot death  n = 78$			2.000
aorsf-fast	0.250 (0.014)	0.825 (0.008)	2.063	0.635
aorsf-cph	0.250 (0.011)	0.825 (0.008)	6.461	0.629
glmnet-cox	0.248 (0.012)	0.820 (0.007)	0.503	0.006
obliqueRSF-net	0.247 (0.011)	0.824 (0.007)	2219.216	1284.916
ranger-extratrees	0.243 (0.009)	0.820 (0.007)	11.176	10.433
cif-standard	0.243 (0.011)	0.818 (0.008)	19.000	116.158
rsf-standard	0.243 (0.013)	0.815 (0.008)		
cif-rotate	0.228 (0.009)	0.819 (0.007)	63.456	0.562 20.143
aorsf-random	0.209 (0.011)	0.813 (0.008)	6.607	0.610
cif-extension	0.201 (0.005)	0.820 (0.008)	40.190	19.948
xgboost-cox	0.095 (0.038)	0.824 (0.007)	6.464	0.008
nn-cox	0.001 (0.003)	0.576 (0.111)	19.271	22.093
xgboost-aft	_	0.823 (0.008)	21.594	0.008

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction
SPRINT; CVD death	n, n = 9361, p = 1	174		
glmnet-cox	0.071 (0.011)	0.795 (0.011)	13.048	0.010
aorsf-cph	0.070 (0.006)	0.797 (0.011)	8.638	0.627
aorsf-fast	0.069 (0.006)	0.797 (0.011)	2.365	0.643
rsf-standard	0.065 (0.007)	0.788 (0.014)	4.277	1.394
obliqueRSF-net	0.064 (0.004)	0.799 (0.011)	2639.976	3402.983
cif-standard	0.061 (0.003)	0.798 (0.011)	49.621	182.059
cif-rotate	0.060 (0.005)	0.791 (0.012)	924.836	113.844
ranger-extratrees	0.054 (0.003)	0.791 (0.012)	8.222	7.874
nn-cox	0.040 (0.015)	0.763 (0.022)	16.891	22.686
aorsf-random	0.038 (0.003)	0.768 (0.013)	5.475	0.742
cif-extension	0.034 (0.002)	0.789 (0.011)	120.288	32.189
xgboost-cox	0.004 (0.019)	0.800 (0.011)	7.700	0.013
xgboost-aft		0.796 (0.012)	25.017	0.012
SPRINT; death, n =	9361, p = 174			
glmnet-cox	0.123 (0.012)	0.771 (0.009)	5.430	0.010
aorsf-cph	0.117 (0.008)	0.770 (0.008)	12.921	0.996
aorsf-fast	0.115 (0.008)	0.770 (0.008)	4.217	0.977
rsf-standard	0.110 (0.008)	0.763 (0.009)	7.137	0.691
obliqueRSF-net	0.108 (0.006)	0.766 (0.008)	4500.673	664.611
cif-standard	0.106 (0.006)	0.764 (0.008)	49.263	185.385
nn-cox	0.097 (0.012)	0.755 (0.011)	28.348	28.860
ranger-extratrees	0.096 (0.005)	0.756 (0.009)	9.647	8.153
cif-rotate	0.090 (0.007)	0.745 (0.009)	1039.879	113.336
aorsf-random	0.072 (0.003)	0.741 (0.009)	8.907	1.067
cif-extension	0.055 (0.002)	0.747 (0.009)	135.763	32.580
xgboost-cox	0.030 (0.022)	0.772 (0.008)	10.871	0.013
xgboost-aft	—	0.772 (0.007)	27.708	0.012
Systolic Heart Failur	re: death, n = 22.	· · · · · · · · · · · · · · · · · · ·		
glmnet-cox	0.113 (0.013)	0.745 (0.012)	0.268	0.003
cif-rotate	0.113 (0.013)	0.741 (0.011)	69.724	10.269
aorsf-cph	0.111 (0.014)	0.745 (0.012)	1.939	0.156
aorsf-fast	0.110 (0.015)	0.744 (0.012)	0.611	0.150
cif-standard	0.110 (0.011)	0.744 (0.011)	3.777	14.994
obliqueRSF-net	0.108 (0.009)	0.748 (0.012)	774.433	96.195
rsf-standard	0.105 (0.011)	0.735 (0.011)	2.783	0.272
aorsf-random	0.095 (0.008)	0.739 (0.012)	2.375	0.149
cif-extension	0.094 (0.006)	0.744 (0.012)	27.865	9.373
ranger-extratrees	0.091 (0.008)	0.738 (0.012)	3.445	1.214
xgboost-cox	0.091 (0.010)	0.744 (0.010)	4.688	0.004
nn-cox	0.076 (0.021)	0.710 (0.021)	14.766	4.725
xgboost-aft		0.741 (0.009)	14.633	0.006
VA lung cancer trial	death, n = 137	` ′	1055	0.000
aorsf-cph	0.201 (0.052)	0.795 (0.034)	0.093	0.011
aorsf-fast	0.201 (0.052)	0.795 (0.034)	0.047	0.011
u0151-145t	0.200 (0.030)	0.175 (0.054)	0.04/	0.011

A.2: Index of prediction accuracy, time-dependent concordance statistic, and computational time required to fit and compute predictions for several learning algorithms across 35 risk prediction tasks. (continued)

	Scaled Brier	C-Statistic	Model fitting	Risk prediction
cif-rotate	0.198 (0.065)	0.789 (0.036)	4.005	1.004
rsf-standard	0.176 (0.048)	0.787 (0.037)	0.065	0.026
cif-extension	0.174 (0.048)	0.795 (0.034)	3.264	1.159
glmnet-cox	0.160 (0.036)	0.788 (0.037)	0.083	0.002
aorsf-random	0.151 (0.044)	0.777 (0.035)	0.205	0.012
cif-standard	0.128 (0.040)	0.770 (0.037)	0.093	0.119
obliqueRSF-net	0.114 (0.033)	0.799 (0.029)	53.069	0.734
ranger-extratrees	0.092 (0.033)	0.778 (0.038)	0.020	0.026
xgboost-cox	0.067 (0.076)	0.753 (0.045)	1.515	0.002
xgboost-aft	_	0.754 (0.047)	5.770	0.005
nn-cox	-0.030 (0.028)	0.521 (0.093)	7.791	0.118

A.3: Discrimination of relevant versus irrelevant variables for several techniques to estimate variable importance.

		acce	lerated oblid	que RSF	xgbo	oost	RSF
Max correlation	No. observations	Negation	ANOVA	Permutation	SHAP	Gain	Permutation
Overall	Overall	75.9	73.9	73.2	69.6	64.6	67.7
Interactions							
Overall	Overall	57.8	57.4	58.0	54.6	49.2	56.9
30	500	54.3	54.1	54.8	48.2	42.7	54.9
30	1,000	56.9	55.7	58.1	53.1	48.0	56.3
30	2,500	61.9	58.9	64.1	61.5	60.7	60.0
15	500	53.1	53.5	52.8	47.1	41.1	54.1
15	1,000	55.9	55.4	56.3	52.2	45.8	55.4
15	2,500	61.0	58.6	63.0	61.0	58.9	59.9
0	500	52.5	53.9	52.4	44.5	40.7	53.6
0	1,000	57.2	58.6	55.8	53.1	42.8	56.1
0	2,500	67.6	68.2	64.4	71.0	62.2	62.1
Non-linear effect	ts						
Overall	Overall	71.7	69.3	67.9	66.1	60.1	61.8
30	500	58.8	58.3	57.8	53.4	48.5	55.5
30	1,000	61.1	59.4	59.0	57.1	52.0	56.3
30	2,500	62.1	60.2	61.1	60.0	56.4	57.9
15	500	63.8	61.5	60.7	55.3	49.4	57.7
15	1,000	67.5	65.1	64.6	62.5	56.0	59.8
15	2,500	70.2	67.2	69.1	66.8	62.3	62.3
0	500	75.5	72.3	68.5	60.1	55.8	61.1
0	1,000	88.3	83.9	78.0	81.5	68.6	67.6
0	2,500	98.4	96.3	91.8	97.7	91.6	78.3
Combination eff	ects						
Overall	Overall	78.3	75.8	74.8	70.7	65.2	68.2
30	500	64.8	63.5	62.5	55.6	49.8	59.2
30	1,000	67.4	65.3	65.3	61.0	55.3	61.5
30	2,500	69.9	67.0	68.5	65.2	61.9	63.8
15	500	70.2	68.0	66.3	59.2	52.8	61.8
15	1,000	74.8	71.2	71.4	66.6	59.9	65.0
15	2,500	78.6	74.6	77.1	72.6	68.6	69.1
0	500	84.0	81.1	76.2	66.7	61.7	67.6
0	1,000	95.4	92.4	87.8	89.4	78.7	76.3

A.3: Discrimination of relevant versus irrelevant variables for several techniques to estimate variable importance. (continued)

Max correlation	No. observations	Negation	ANOVA	Permutation	SHAP	Gain	Permutation
0	2,500	99.8	99.3	97.8	99.7	97.9	89.0
Main effects							
Overall	Overall	91.0	88.9	88.7	85.0	82.6	83.2
30	500	79.3	77.3	75.5	70.3	66.5	71.2
30	1,000	83.5	80.5	80.8	76.8	73.9	74.9
30	2,500	86.5	83.5	85.1	81.7	80.4	79.3
15	500	86.3	83.3	81.8	75.7	71.3	75.3
15	1,000	91.3	88.1	88.5	84.6	81.3	81.1
15	2,500	94.5	91.6	93.7	90.2	89.0	86.5
0	500	97.8	96.3	94.0	86.5	83.4	85.9
0	1,000	100.0	99.7	99.4	99.4	98.0	95.2
0	2,500	100.0	100.0	100.0	100.0	100.0	99.8

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