

# Formal Concept Analysis in R

Motivation, success stories and future work with the **fcaR** library

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# Motivation

# Why to develop an R package for FCA?

- R, together with Python, are the two most widely used programming languages in Machine Learning and Data Science.
- In R there are already libraries for association rule mining that have become standard: **arules**.
- There is no library in R that implements the basic ideas and functions of FCA and allows them to be used in other contexts.

## Our purpose

- To help disseminate FCA as a knowledge discovery tool.
- To be able to perform rapid testing of new ideas, algorithms, etc., both from a theoretical and practical point of view.
- Rapid prototyping of new solutions that can be integrated into more complex computational systems.
- To enable the application of FCA to real problems: automatic reasoning and recommender systems.

# Design principles

## Usability

- Direct execution of most classical algorithms (even in the fuzzy setting).
- Provide methods to operate on contexts, concept lattice and implications.
- **Logic:** include the  $SL_{FD}$  logic to compute closure wrt implication sets.
- Interoperability:
  - Read/write datasets in various formats (CSV, CTX, . . . ).
  - Import and export to **arules**.
- Allow reproducible research.
- Provide lots of documentation with examples.

## Implementation

- Modern programming paradigms (object-oriented).
- Classes representing entities: contexts, lattices, implications. . .
- Allow for extensions: new algorithms, new ideas. . .
- Use base R for the interface, but bottlenecks implemented in C.

## The **fcaR** library

# Library availability



Contributed Packages

Available Packages

Currently, the CRAN package repository features 18994 available packages.

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The package is in a stable phase in a repository on Github and on CRAN.

- Unit tests
- Vignettes with demos
- Status:
  - lifecycle: stable
  - CRAN version: 1.1.1
  - downloads: ~19K

# Classes and methods

## Classes

Class name	Use
"Set"	A basic class to store a fuzzy set using sparse matrices
"Concept"	A pair of sets (extent, intent) forming a concept for a given formal context
"ConceptLattice"	A set of concepts with their hierarchical relationship. It provides methods to compute notable elements, sublattices and plot the lattice graph
"ImplicationSet"	A set of implications, with functions to apply logic and compute closure of attribute sets
"FormalContext"	It stores a formal context, given by a table, and provides functions to use derivation operators, simplify the context, compute the concept lattice and the Duquenne-Guigues basis of implications

Table 1: Main classes found in **fcaR**.

## Main methods

---

### Formal Contexts

---

intent  
extent  
closure  
clarify  
reduce  
standardize  
find\_concepts  
find\_implications

---

---

### Concept Lattice

---

supremum  
infimum  
sublattice  
meet\_irreducibles  
join\_irreducibles  
subconcepts  
superconcepts  
lower\_neighbours  
upper\_neighbours

---

---

### Implication Set

---

closure  
recommend  
apply\_rules  
to\_basis

---

# A remark on the Simplification Logic

$SL_{FD}$	Equivalence rules
[Ref] $\frac{A \supseteq B}{A \Rightarrow B}$	
[Frag] $\frac{A \Rightarrow B \cup C}{A \Rightarrow B}$	$\{A \Rightarrow B\} \equiv \{A \Rightarrow B \setminus A\}$
[Comp] $\frac{A \Rightarrow B, C \Rightarrow D}{A \cup C \Rightarrow B \cup D}$	$\{A \Rightarrow B, A \Rightarrow C\} \equiv \{A \Rightarrow BC\}$
[Simp] $\frac{A \Rightarrow B, C \Rightarrow D}{A(C \setminus B) \Rightarrow D \setminus B}$	$A \subseteq C \Rightarrow \{A \Rightarrow B, C \Rightarrow D\} \equiv \{A \Rightarrow B, A(C \setminus B) \Rightarrow D \setminus B\}$
	$A \subseteq D \rightarrow \{A \Rightarrow B, C \Rightarrow BD\} \equiv \{A \Rightarrow B, C \Rightarrow D\}$

The  $SL_{FD}$  closure algorithm makes use of the above equivalence rules to compute the closure  $X^+$  of a set  $X$  using a set of implications  $\Sigma$ , and return a simplified  $\Sigma'$  where the attributes in  $X^+$  do not appear, and such that:

$$\{\emptyset \Rightarrow X\} \cup \Sigma \equiv \{\emptyset \Rightarrow X^+\} \cup \Sigma'$$

# Practical example of the functionalities

Context and derivation operators

Concept lattice

Implications and logic

Conceptual scaling

# Reproducible research with fcaR and interoperability

All classes have a `to_latex()` method to export in a suitable form to a `\LaTeX` document:

- Tables (for formal contexts):

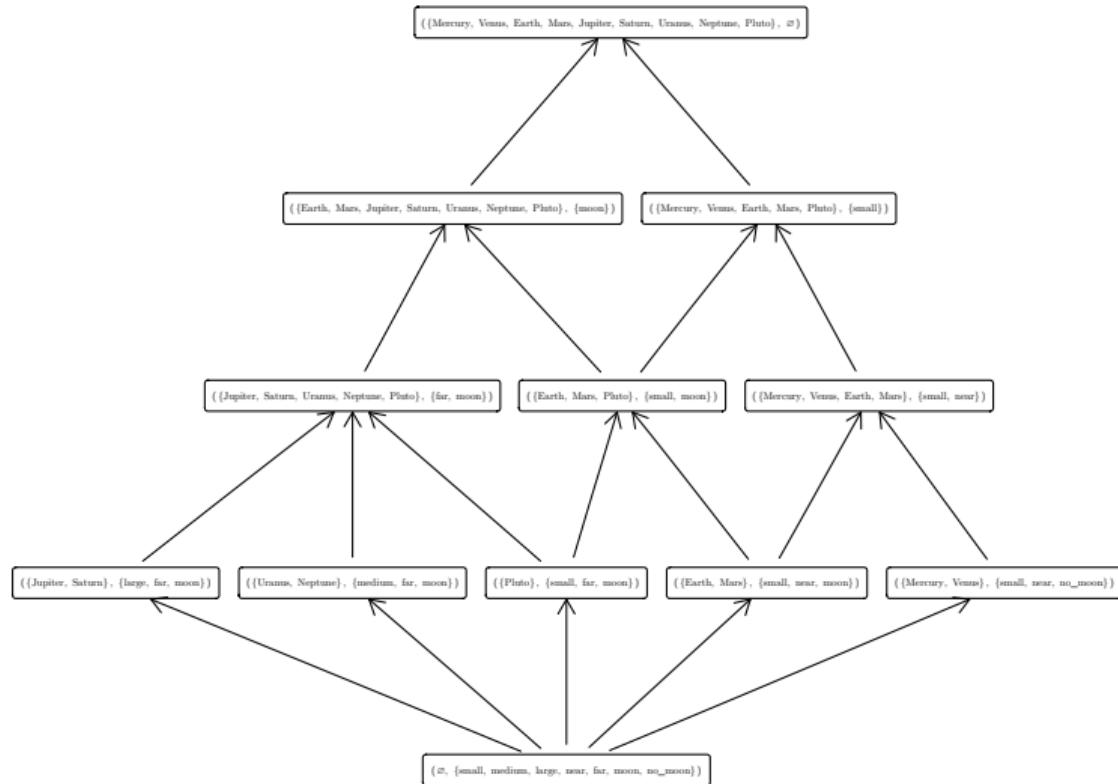
	small	medium	large	near	far	moon	no_moon
Mercury	×			×			×
Venus	×			×			×
Earth	×			×		×	
Mars	×			×		×	
Jupiter			×		×	×	
Saturn			×		×	×	
Uranus		×			×	×	
Neptune		×			×	×	
Pluto	×				×	×	

Table 2

- Listings (for concepts, implications...):

1:	{no_moon}	$\Rightarrow$	{small, near}
2:	{far}	$\Rightarrow$	{moon}
3:	{near}	$\Rightarrow$	{small}
4:	{large}	$\Rightarrow$	{far, moon}
5:	{medium}	$\Rightarrow$	{far, moon}
6:	{medium, large, far, moon}	$\Rightarrow$	{small, near, no_moon}
7:	{small, near, moon, no_moon}	$\Rightarrow$	{medium, large, far}
8:	{small, near, far, moon}	$\Rightarrow$	{medium, large, no_moon}
9:	{small, large, far, moon}	$\Rightarrow$	{medium, near, no_moon}
10:	{small, medium, far, moon}	$\Rightarrow$	{large, near, no_moon}

- Plots (for formal contexts, lattice):



- fcaR code can be embedded in RMD files (plain text + code + results) and produce a presentation (such as this one!) or a complete paper:

# fcaR, Formal Concept Analysis with R

by Pablo Cordero, Manuel Enciso, Domingo López-Rodríguez, and Ángel Mora

## Implications and logic

The knowledge stored in a formal context can also be represented as a set of implications, which are expressions of the form  $A \rightarrow B$  where A and B are sets of attributes or items, indicating that, for every object in which the set of attributes A is present, also B is present. This interpretation is similar to the one defined in data mining/machine learning over the so-called association rule. The confidence (a well-known measure of quality for association rules) is given by

For instance,  $\{P1\} \rightarrow \{P4\}$  is a valid implication in the previous example, having the following interpretation: when the attribute P1 has degree at least 0.5 then we have P4 with degree 1.

The Dauphiné-Guitart basis of implications (Guitart and Dauphiné, 1989) is a set of valid implications from which all other valid implications can be deduced. The Dauphiné-Guitart basis in our example has given by:

1.	$\{P1\} \rightarrow \emptyset$	$\Rightarrow \{P1, P2, P3, P4\}$
2.	$\{P2\} \rightarrow \{P1\}$	$\Rightarrow \{P2\}$
3.	$\{P3\} \rightarrow \{P1\}$	$\Rightarrow \{P3\}$
4.	$\{P4\} \rightarrow \{P1\}$	$\Rightarrow \{P4\}$
5.	$\{P1, P2\} \rightarrow \{P3\}$	$\Rightarrow \{P2, P4\}$
6.	$\{P1, P3\} \rightarrow \{P2\}$	$\Rightarrow \{P2, P4\}$

In Cordero et al. (2019), the simplification logic, denoted as  $fcl_{fca}$ , was introduced as a method to manipulate implications (functional dependencies or if-then rules), removing redundancies or computing closures of attributes. This logic is equivalent to Armstrong's Axioms (Armstrong, 1970), which are well known from the 80s in databases and artificial intelligence, formal concept analysis, and others. The axiomatic system of this logic can be referred to as the axioms below.

$$\begin{array}{c} 1. \\ 2. \\ 3. \\ 4. \\ 5. \end{array}$$

together with the following inference rules called fragmentation, composition and simplification, respectively, which are equivalent to the classical Armstrong's axioms of augmentation and, more importantly, transitivity.

$$\frac{\begin{array}{c} A \rightarrow B \\ A \rightarrow C \end{array}}{A \rightarrow B \cup C} \text{ (fragmentation)} \quad \frac{\begin{array}{c} A = B \\ A = C \end{array}}{A = B \cup C} \text{ (composition)} \quad \frac{\begin{array}{c} A = B \\ A = C \end{array}}{A = B \cap C} \text{ (simplification)}$$

The main advantage of  $fcl_{fca}$  with respect to Armstrong's Axioms is that the inference rules may be considered as equivalence rules (see the work by Mora et al. (2012) for further details and proofs), that is, given two implications  $A \rightarrow B$  and  $C \rightarrow D$ , the software translates it into an equivalent rule. In the package presented in this paper, we develop the following equivalences:

1. Fragmentation Equivalence [fEq1]:  $\{A \cup B\} \rightarrow \{A\}$
2. Composition Equivalence [fEq2]:  $\{A \cup B\} \rightarrow C \Leftrightarrow \{A \cup B, C\} \rightarrow \{C\}$
3. Simplification Equivalence [fEq3]:  $B \subseteq C \Leftrightarrow B \rightarrow C$

$$\{A, B, C \cup D\} \rightarrow \{A \cup B, A \cup C \rightarrow D\}$$

4. Right-Simplification Equivalence [fEq4]:  $A \cap C \cup D \rightarrow A \cap C$

$$\{A, B, C \cup D\} \rightarrow \{A \cap C, B \cup D\}$$

Usually many axioms, the implications always associate attributes on the right-hand side. We emphasize that this logic can manage aggregated implications, i.e., the implications' consequents do not have to be singletons. This represents an increase of the logic efficiency.

This logic removes attribute redundancies in some of the implications in the Dauphiné-Guitart basis presented below. Particularly, the implications with numbers 1, 3, 4, 5 and 6 are simplified to:

2.	$\{P4\} \rightarrow \{P2\}$
3.	$\{P3\} \rightarrow \{P1\}$
4.	$\{P4\} \rightarrow \{P3\}$
5.	$\{P1\} \rightarrow \{P1\}$

One of the primary uses of a set of implications is computing the closure of a set of attributes, the maximal fuzzy set that we can arrive at from these attributes using the given implications.

## Derivation operators

The methods that implement the derivation operators are named after them: `intert()`, `extant()` and `closure()`. They can be applied on objects of type "set", representing fuzzy sets of objects or attributes.

```
> S <- lattice(fcaSubjects, P1 == 1, G2 == 1)
> S
[1] {P1}
> fclIntert(S)
[2] {P1, P4, P4, {P1, P2, P3, P4}}
> T <- lattice(fcaAttributes, P1 == 1, P3 == 1)
> T
[1] {P1, P3}
> fclExtant(T)
[1]
> fcLClosure(T)
[1] {P1, P2, P1, P4}
```

In addition, we can perform classification on the formal context, by using `fclClarify()`, giving:

```
FormalContextWith 3 objects and 3 attributes.
> fclClarify(F, 3, 3)
[1] P1 P2 {P2, P4}
[2] P3 P1 P3
[3] G1 G2 1 0 8.5
[4] G2 G1 8.5 0 1
```

The duplicated rows and columns in the formal context have been collapsed, and the corresponding attributes and object's names are grouped together between brackets, e.g., {P2, P4}.

## Concept lattice

The command to compute the concept lattice for a "FormalContext" object is `fcaFindConcepts()`. The function returns a `conceptLattice`, which is of the "ConceptLattice" class.

### 1. Concept lattice

The command to compute the concept lattice for a "FormalContext" object is `fcaFindConcepts()`. The function returns a `conceptLattice`, which is of the "ConceptLattice" class.

### 2. A set of 8 concepts:

1. ({P1, G2, G3, G4}, {P2, {P2, P4}, {P1, P2, P3, P4}})
2. ({P1, G4}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
3. ({P1, G1, G2, G3}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
4. ({P1, G1}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
5. ({P1, G1, G2}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
6. ({P1, G1, G2, G3}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
7. ({P1, G1, G2, G3, G4}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
8. ({}, {P1, P2, P3, P4}, {P1, P2, P3, P4})

In order to know the cardinality of the set of concepts (that is, the number of concepts), we can use `fcaConceptsSize()`, which gives 8 in this case. The complete list of concepts can be printed with `fcaConcepts()` and the user can filter the concepts. Also, they can be translated to RIDs using the `getLattice()` method, as mentioned before.

The typical subsetting operation in R with brackets is implemented to select specific concepts from the lattice, giving the address or a boolean vector indicating which concepts to keep. The same rules apply for the other operators.

### 3. fcaConcepts({P1, P2, P3, P4})

### 4. A set of 5 concepts:

1. ({P1, G2, G3, G4}, {P2, {P2, P4}, {P1, P2, P3, P4}})
2. ({P1, G4}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
3. ({P1, G1, G2, G3}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
4. ({P1, G1}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})
5. ({P1, G1, G2}, {P2, {P1, P2, P3, P4}, {P1, P2, P3, P4}})

In addition, the user can compute concepts' support (the proportion of objects whose set of attributes contains the intent of a given concept) by means of `fcaConceptsSupport()`.

```
> fcaConceptsSupport(F)
[1] 1.00 0.48 0.35 0.58 0.50 0.80 0.80 0.80
```



Figure 4: Hasse diagram for a subtree of the crite12 formal context.

an individual) and returns the degree of the diagnosis attributes using the implications extracted from the formal context as an inference engine.

Next, we use the `NEXT_CLOSURE` algorithm to extract implications and compute the set of concepts, using `fcaFindImplications()`.

The number of implications is big (47400 concepts), therefore, it cannot be plotted here for space and readability reasons. For this reason, we only plot a subtree of small size in Figure 4.

There is an aggregate of 985 implications in the LHS and the RHS of the extracted rules:

```
> nImplications(fcaFindImplications())
[1] 985
> nRHS(fcaFindImplications())
[1] 47400
> nLHS(fcaFindImplications())
[1] 47400
```

Note that our paradigm can deal with non-unit implications, that is, where there is more than one attribute in the RHS of the implication. This feature is an extension of what is usual in other paradigms, for example, in transactional databases.

We can use the simplification logic to remove redundancies and reduce the LHS and RHS size of the implications. The next section is devoted to this to decrease the computational cost of computing closures:

```
> fcaImplicationsSimplify(rules = c("simplification", "resimplification"))
> nImplications(fcaFindImplications())
[1] 869
> nRHS(fcaFindImplications())
[1] 1998
> nLHS(fcaFindImplications())
[1] 55719
```

We can see that the average cardinality of the LHS has been reduced from 2.418 to 1.998 and that the one of the RHS, from 1.854 to 1.537.

With the simplified implication set, we can build a recommendation system by simply swapping the `recommend` method with `simplify`:

```
> diagnosis <- function(x) {
+   +
+   fcaImplicationsSimplify(rules = c("simplification",
+                                     "resimplification"))
+   +
+   attribute_filter =
+     c("G1", "G2", "G3", "G4")
+   +
+   getLattice()
+ }
```

This function can be applied to "set"s that have the same attributes as those of the formal context.

attribute\_filter argument specifies which attributes are of interest, in our case, the diagnosis attributes.

Let us generate some sets of attributes and get the recommendation (diagnosis) for each one:

```
> S1 <- setAttributes(fcaAttributes)
> S2 <- setAttributes(fcaAttributes)
> S3 <- setAttributes(fcaAttributes)
> S4 <- setAttributes(fcaAttributes)
> S5 <- setAttributes(fcaAttributes)
> S6 <- setAttributes(fcaAttributes)
> S7 <- setAttributes(fcaAttributes)
> S8 <- setAttributes(fcaAttributes)
> S9 <- setAttributes(fcaAttributes)
> S10 <- setAttributes(fcaAttributes)
```

diagnosis

deals with

1

## Integration with **arules**

**arules** is a standard in R to compute and manage (unit) association rules. The implications computed *or simplified* using **fcaR** can be exported to the **arules** format.

- Since, in many cases, other people know about association rules mining and its terminology, it is easy to introduce FCA and its methods with this integration.

# Where to find help

<https://malaga-fca-group.github.io/fcaR/>



## fcaR: Tools for Formal Concept Analysis

The aim of this package is to provide tools to perform fuzzy formal concept analysis (FCA) from within R. It provides functions to load and save a Formal Context, extract its concept lattice and implications. In addition, one can use the implications to compute semantic closures of fuzzy sets and, thus, build recommendation systems.

## Stories of success

# Where have we used **fcaR**?

The ways in which we have used **fcaR** so far are:

- From a theoretically point of view:
  - Rapid development and checking of new ideas: **fcaR** allows for a fast iteration of the cycle **theory - practice - theory**.
- With practical purposes:
  - Use the simplification logic for automated reasoning and creation of recommender systems.
  - Explore the concept lattice in real-world problems to model and extract knowledge.

# Recommender systems



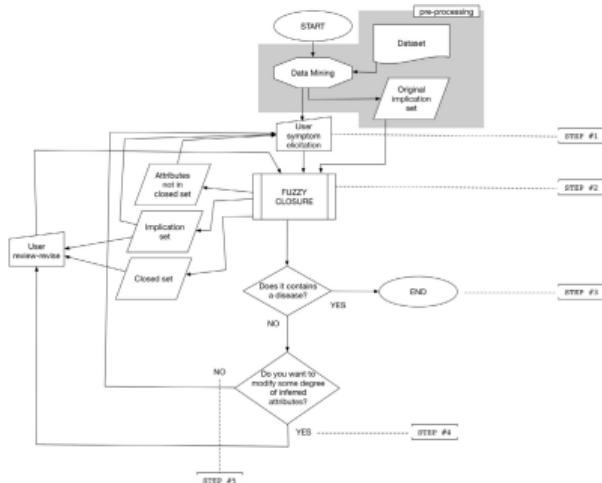
## A conversational recommender system for diagnosis using fuzzy rules

P. Cordero<sup>a</sup>, M. Enciso<sup>b</sup>, D. López<sup>a,\*</sup>, A. Mora<sup>a</sup>



<sup>a</sup>Dept. of Applied Mathematics, Universidad de Málaga, Andalucía Tech, Málaga, Spain

<sup>b</sup>Dept. of Computer Science, Universidad de Málaga, Andalucía Tech, Málaga, Spain



Comparison of the current proposal to other recommender systems and machine learning methods.

	Accuracy	Sensitivity	Specificity	Precision
ALS	0.360	0.333	0.380	0.290
IBCF (Cosine)	0.555	0.475	0.615	0.483
IBCF (Pearson)	0.770	0.466	1.000	1.000
LIBMF	0.491	0.901	0.181	0.455
SVD	0.376	0.515	0.271	0.349
SVD <sup>F</sup>	0.431	1.000	0.000	0.431
UBCF (Cosine)	0.608	0.967	0.335	0.524
UBCF (Pearson)	0.525	0.783	0.330	0.470
C5.0	0.674	0.636	1.000	1.000
PART	0.883	0.847	0.950	0.970
JRip	0.752	0.814	0.688	0.731
Random Forest	0.953	0.924	1.000	1.000
xgboost	0.818	0.963	0.713	0.706
k-nn	0.589	0.603	0.544	0.815
<b>Proposal</b>	<b>0.982</b>	<b>0.996</b>	<b>0.948</b>	<b>0.955</b>

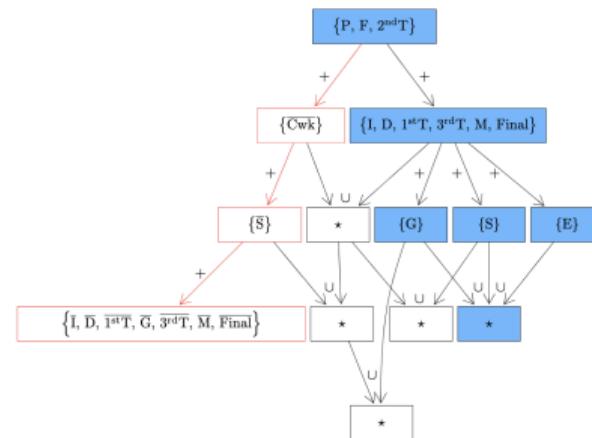
# Mixed attributes

Used for knowledge spaces and learning paths (IJCIS, submitted)

Minimal generators from positive and negative attributes: analysing the knowledge space of a maths course

Closed set	Min. gen.	Closed set	Min. gen.
$\{c, \bar{a}, \bar{d}\}$	$\{\bar{a}, \bar{d}\}$	$\{b, d, \bar{a}, \bar{c}\}$	$\{\bar{a}, \bar{c}\}$
$\{c, \bar{a}, \bar{b}, \bar{d}\}$	$\{\bar{a}, \bar{b}\}$	$\{c, \bar{b}, \bar{d}\}$	$\{\bar{b}, \bar{d}\}, \{c, \bar{b}\}$
$\{b, c, d, \bar{a}\}$	$\{c, d\}$	$\{b, d, \bar{a}\}$	$\{d, \bar{a}\}, \{b, d\}$
$\{b, c, \bar{a}\}$	$\{b, c\}$	$\{a, d, \bar{b}, \bar{c}\}$	$\{\bar{b}, \bar{c}\}, \{d, \bar{b}\}, \{a, d\}$
$\{a, c, \bar{b}, \bar{d}\}$	$\{a, c\}$	$\{a, b, \bar{c}, \bar{d}\}$	$\{\bar{c}, \bar{d}\}, \{a, b\}$

Closed set	Minimal generators
$M \cup \bar{M}$	$\{\bar{b}, \bar{c}, \bar{d}\}, \{\bar{a}, \bar{c}, \bar{d}\}, \{\bar{a}, \bar{b}, \bar{c}\}, \{d, \bar{a}, \bar{b}\}, \{d, \bar{d}\}, \{c, d, \bar{b}\}, \{c, \bar{c}\}, \{a, c, d\}, \{b, \bar{b}\}, \{a, b, d\}, \{a, b, c\}, \{a, \bar{a}\}$



## Article

# Simplifying Implications with Positive and Negative Attributes: A Logic-Based Approach

Francisco Pérez-Gámez , Domingo López-Rodríguez , Pablo Cordero , Ángel Mora  and Manuel Ojeda-Aciego \*

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**Theorem 3.** Consider  $A, B, C, D \subseteq M\bar{M}$ :

[KeyEq'] If there exist  $x \in A \cap D$ ,  $y \in B \cap \bar{C}$  with  $A \setminus x = C \setminus \bar{y}$ , then

$$\{A \rightarrow B, C \rightarrow D\} \equiv \{A \rightarrow B \setminus y, C \setminus \bar{y} \rightarrow y\} \equiv \{A \rightarrow B \setminus y, C \rightarrow M\bar{M}\}.$$

[KeyEq''] If  $A \subseteq C \neq \emptyset$  and  $B \cap \bar{D} \neq \emptyset$ , for any  $x \in C$  we have that then

$$\{A \rightarrow B, C \rightarrow D\} \equiv \{A \rightarrow B, C \setminus x \rightarrow \bar{x}\}.$$

[RedEq'] If  $D \subseteq B$  and there exists  $x \in A \cap \bar{C}$  such that  $A \setminus x = C \setminus \bar{x}$ , then

$$\{A \rightarrow B, C \rightarrow D\} \equiv \{A \rightarrow B \setminus D, C \setminus \bar{x} \rightarrow D\}.$$

[RftEq] If there exist  $x \in A$ ,  $y \in B \cap \bar{C}$  and  $A \setminus x = C \setminus \bar{y}$ , then

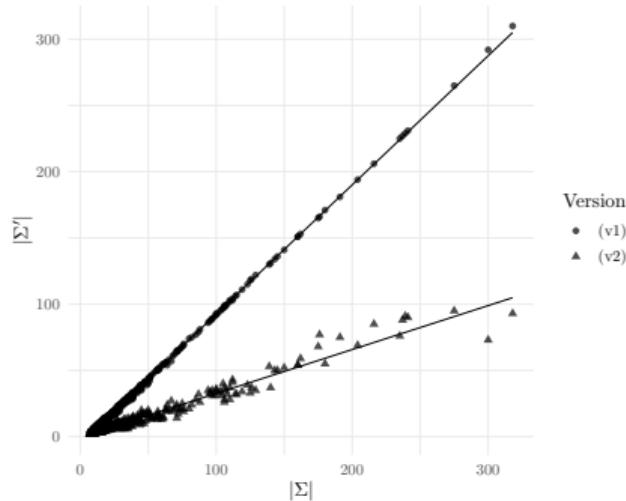
$$\{A \rightarrow B, C \rightarrow D\} \equiv \{A \rightarrow B \setminus y, C \rightarrow D\bar{x}\}.$$

[RftEq'] If there exist  $x \in A \cap \bar{D}$ ,  $y \in B \cap \bar{C}$  and  $A \setminus x \subseteq C \setminus \bar{y}$ , then

$$\{A \rightarrow B, C \rightarrow D\} \equiv \{A \rightarrow B, C \rightarrow D \setminus \bar{x}\}.$$

[MixUnEq] If there exist  $x \in A$ ,  $y \in C$  such that  $A \setminus x = C \setminus y$  and  $b \in D$ , then

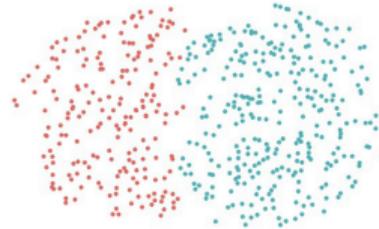
$$\{A \rightarrow b, C \rightarrow D\} \equiv \{(A \setminus x)\bar{b} \rightarrow \bar{x}\bar{y}, C \rightarrow D \setminus b\}.$$



# Clustering of implications applied to Social Network Analysis

## Clustering and Identification of Core Implications

Domingo López-Rodríguez<sup>(✉)</sup>, Pablo Cordero, Manuel Enciso, and Ángel Mora



## Sentiment Analysis



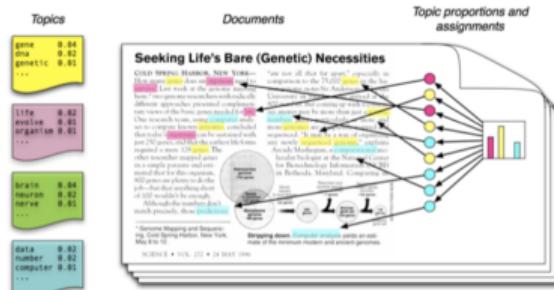
Positive



Negative



Neutral



# Collaborations

- Construction companies: Integration of FCA-based recommendation systems within the *Building Information Modelling* (BIM) methodology.

*Panel de Control*

**Datos**

Titulo Obra:

Organismo:  Tipo Contratación:  Importe Licitación:

Propuesta económica:  Propuesta técnica:  Puntuación total:

Baja:  Fecha:  dd/mm/aaaa

**Resultados**

Baja:  Importe/Oferenda:  Fecha:

Tipo de Obra:  Organismo:  Tipo Contratación:

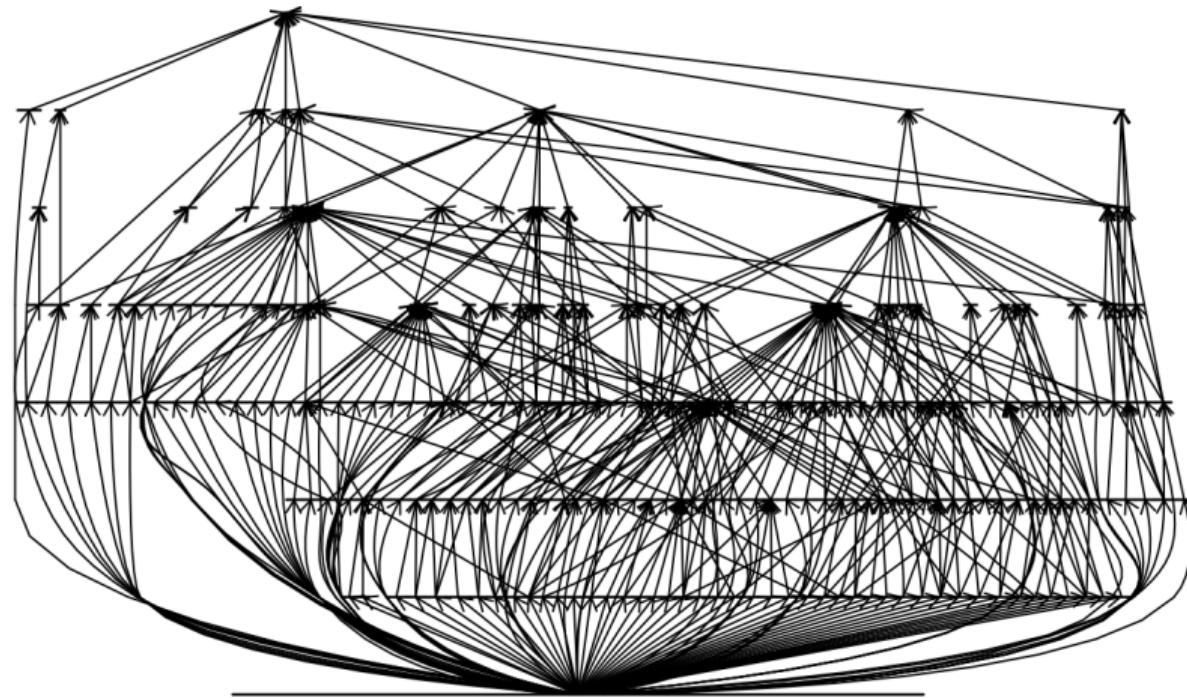
Valor TM:  Es Baja Temeraria:

Prop. económica:  Prop. técnica:  Ganador:

Punt. total:

- Cybersecurity company: Creation of an ontology of malware threats.



{Sophos = bckdr-rxm}  $\Rightarrow$  {Avast = metasploit-g, Kaspersky = heur:downloader.os.}

- Other research groups:
  - a. Application of fuzzy FCA to neuroimage processing and understanding.
  - b. Use of recommender systems and logic tools to analyse and reduce the Urban Heat Island (UHI) effect for urban planning.
  - c. FCA for concept drift detection in online unsupervised machine learning.

## Future works

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We are exploring several lines:

- Improve the usability by non-experts.
- Better integration for external tools (both in R and other languages or via web).
- Develop new algorithms and extensions.

# Future developments

## Web application

- Web app for **fcaR** (demo)

## Some extensions

- Integrate association rules in the library (Luxenburger's basis).
- Logic for mixed attributes: new algorithms to compute bases of mixed implications, iterative closure algorithm...
- Other extensions:  $\{\circ, +, -, \imath\}$ .

## Other algorithms

- Concept lattice (InClose, FastCbO, NextNeighbour)
- Canonical basis of implications
- Direct bases and minimal generators.
- Parallelization of the above.

THANK YOU VERY MUCH