

Data Structures (Theory)

SORTING:

→ Makes searching fast.
Linear Data Structures → Linear Search

Linear Algorithms:

- Non-
Recursive
- + ↗ Easy coding
 - o Bubble Sort
 - o Insertion sort
 - o Selection Sort
- We will calculate time complexity of every sorting algorithm.
→ Response time of processor.

There is no best, worst or average case so there is every case. If ~~algo~~ ^{algo} has same time for sorted, unsorted & mixed data.

Non Linear Sort:

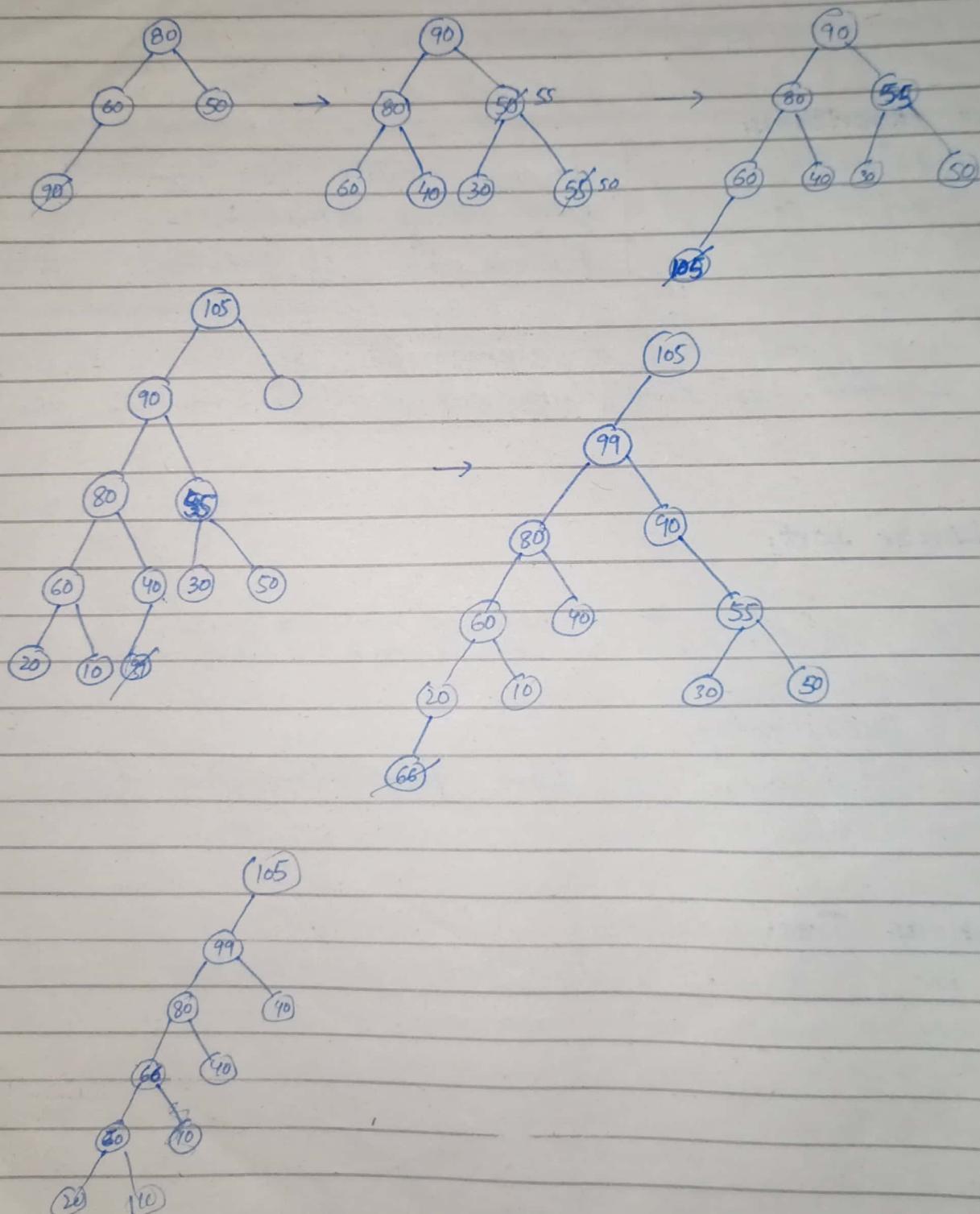
- 1. BST Sort
 - 2. Heap Sort
 - ↗ Max heap tab when we need ascending data
 - Min heap tab when we need descending order.
 - 3. Merge Sort
- Recursive code + difficult coding

Linear Sorting algorithms have better time complexity than non-linear.

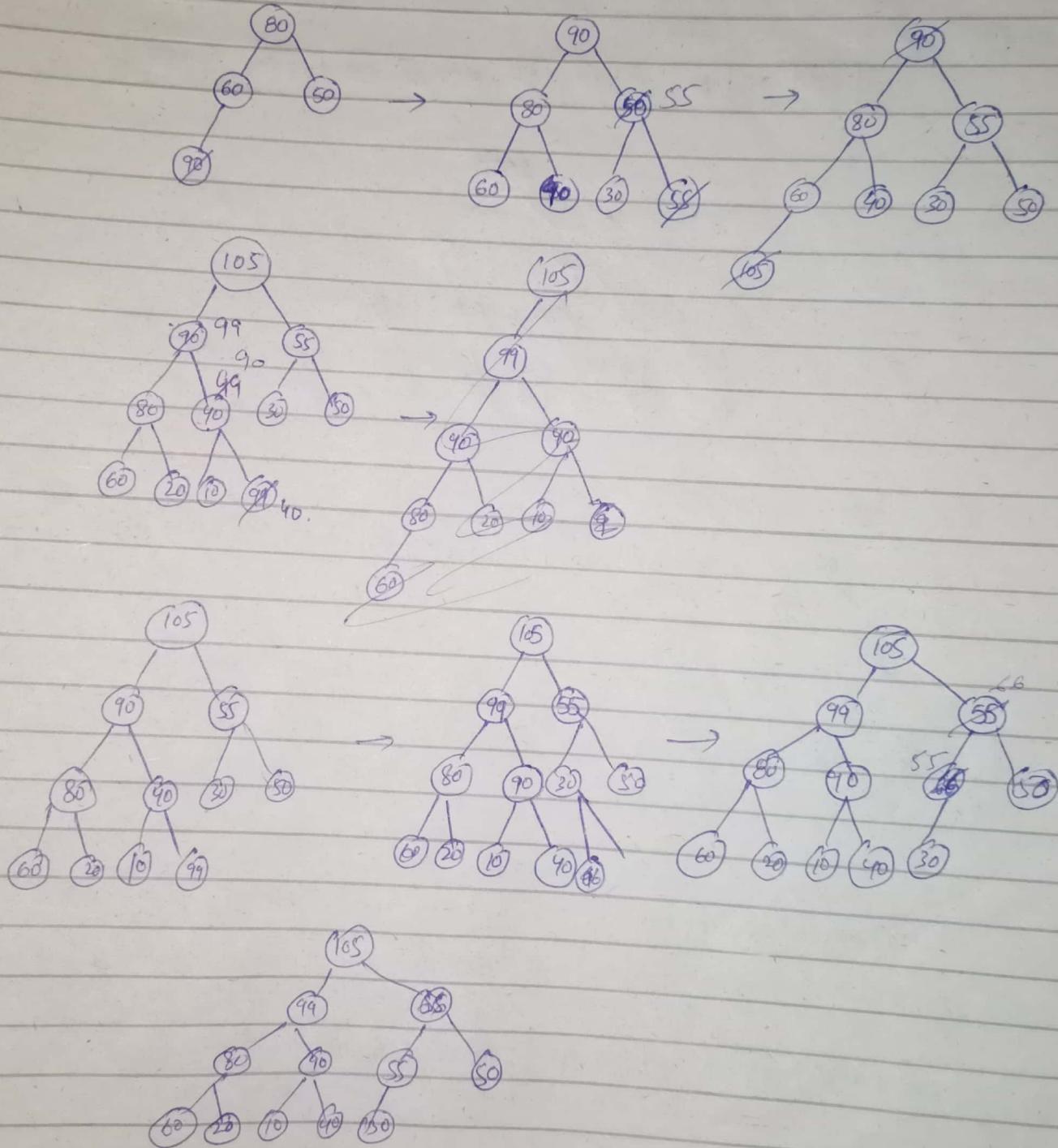
Max Heap Tree:

- Every root is greater than its children.
- Left to right node insertion.

80, 60, 50; 90, 40, 30, 55, 105, 20, 10, 99, 66



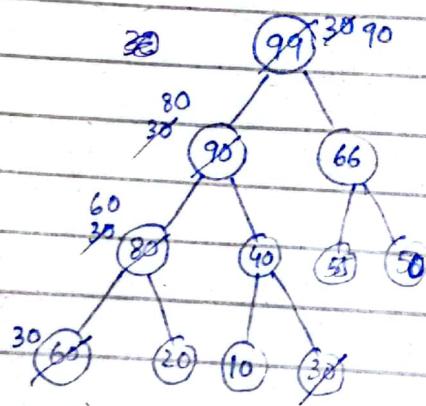
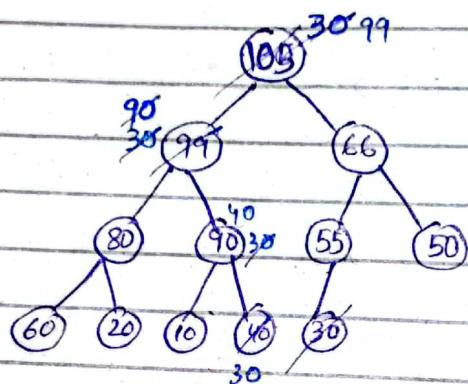
80, 60, 50, 90, 40, 30, 55, 105, 20, 10, 99, 66



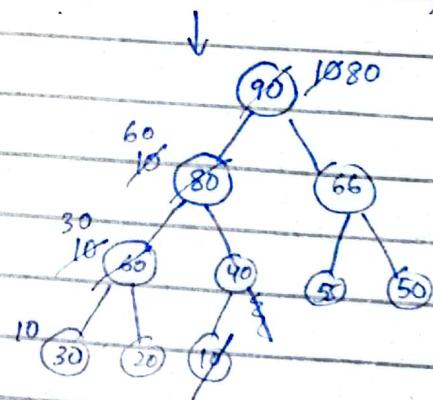
105	99	66	80	90	55	50	60	20	10	40	30
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Replace with last node.

30	99	66	80	90	55	50	60	20	10	40	105
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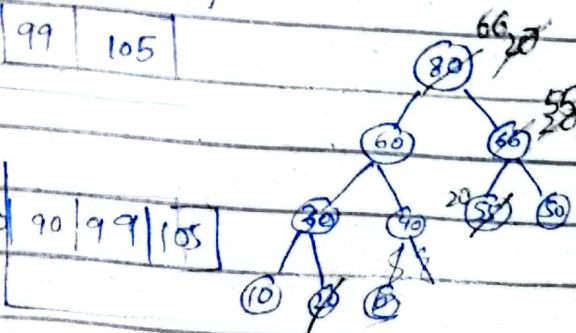
99	90	66	80	40	55	50	60	20	10	30	105
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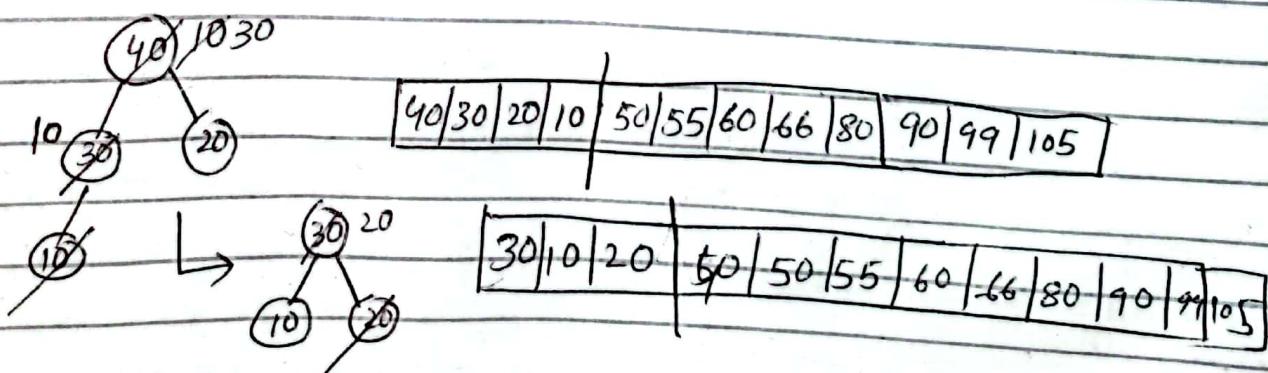
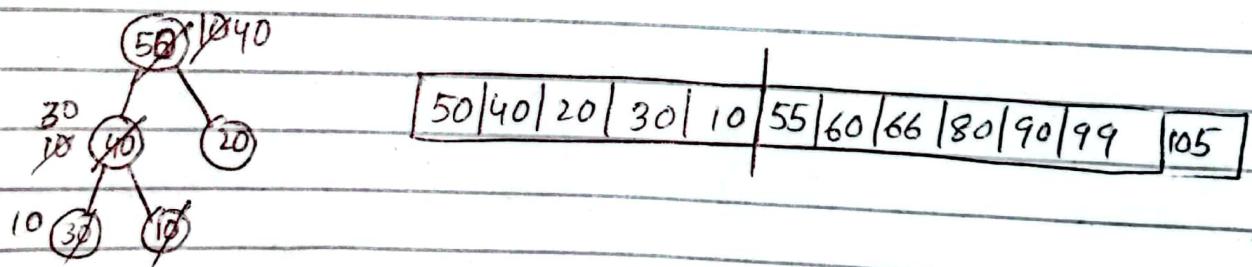
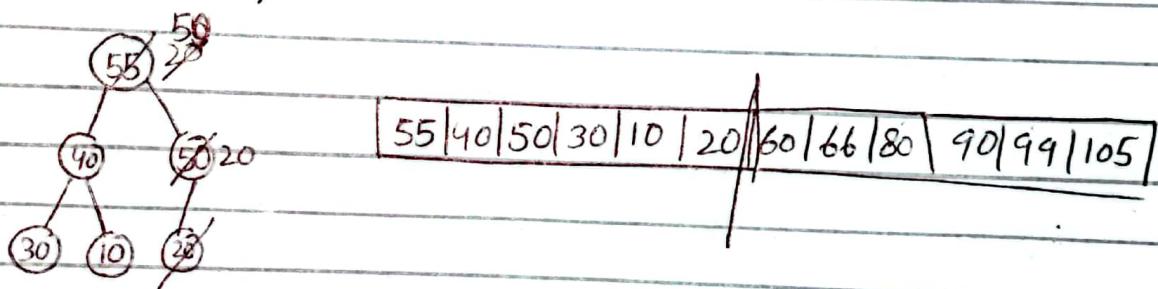
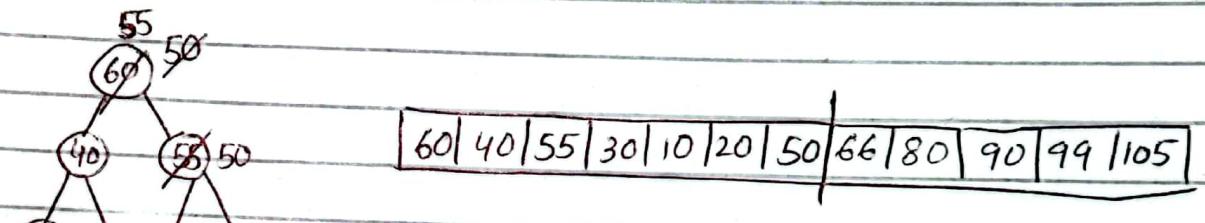
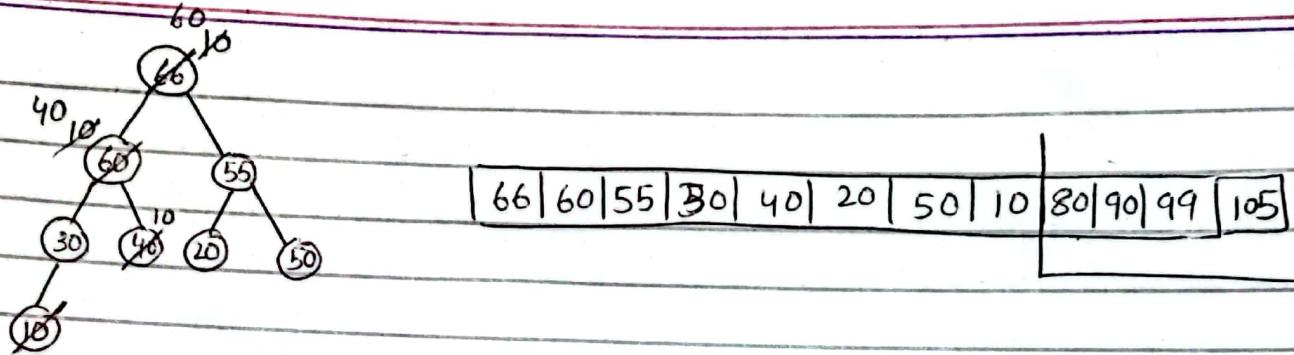


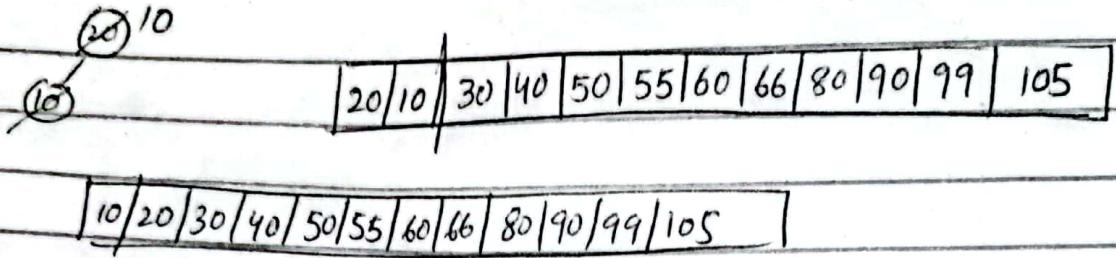
90	80	66	60	40	30	20	10
----	----	----	----	----	----	----	----

99	105
----	-----

80	60	66	30	40	55	50	10	20	90	99	105
----	----	----	----	----	----	----	----	----	----	----	-----

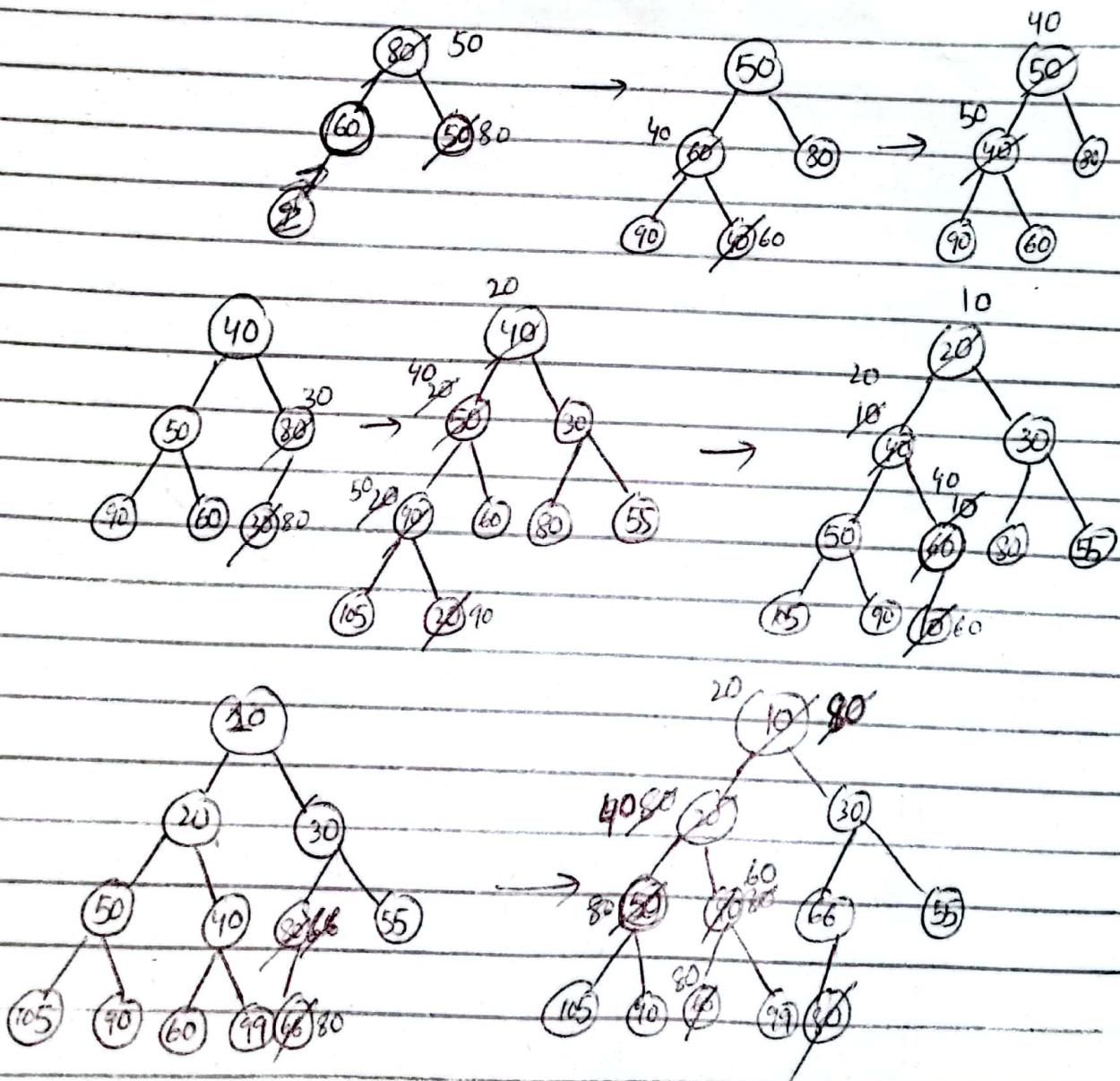




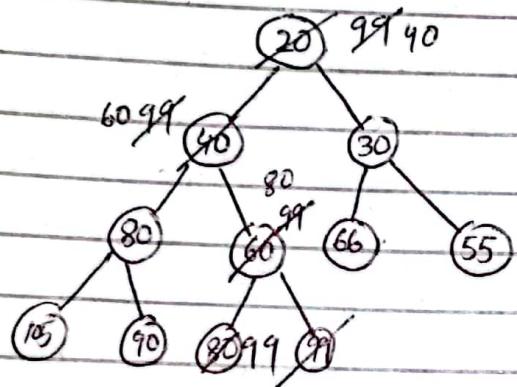


Min heap tree:

80, 60, 50, 90, 40, 30, 55, 105, 20, 10, 99, 66



10	20	30	50	40	66	55	105	90	60	99	80
----	----	----	----	----	----	----	-----	----	----	----	----



20	40	30	80	60	66	55	105	90	80	99	10
----	----	----	----	----	----	----	-----	----	----	----	----

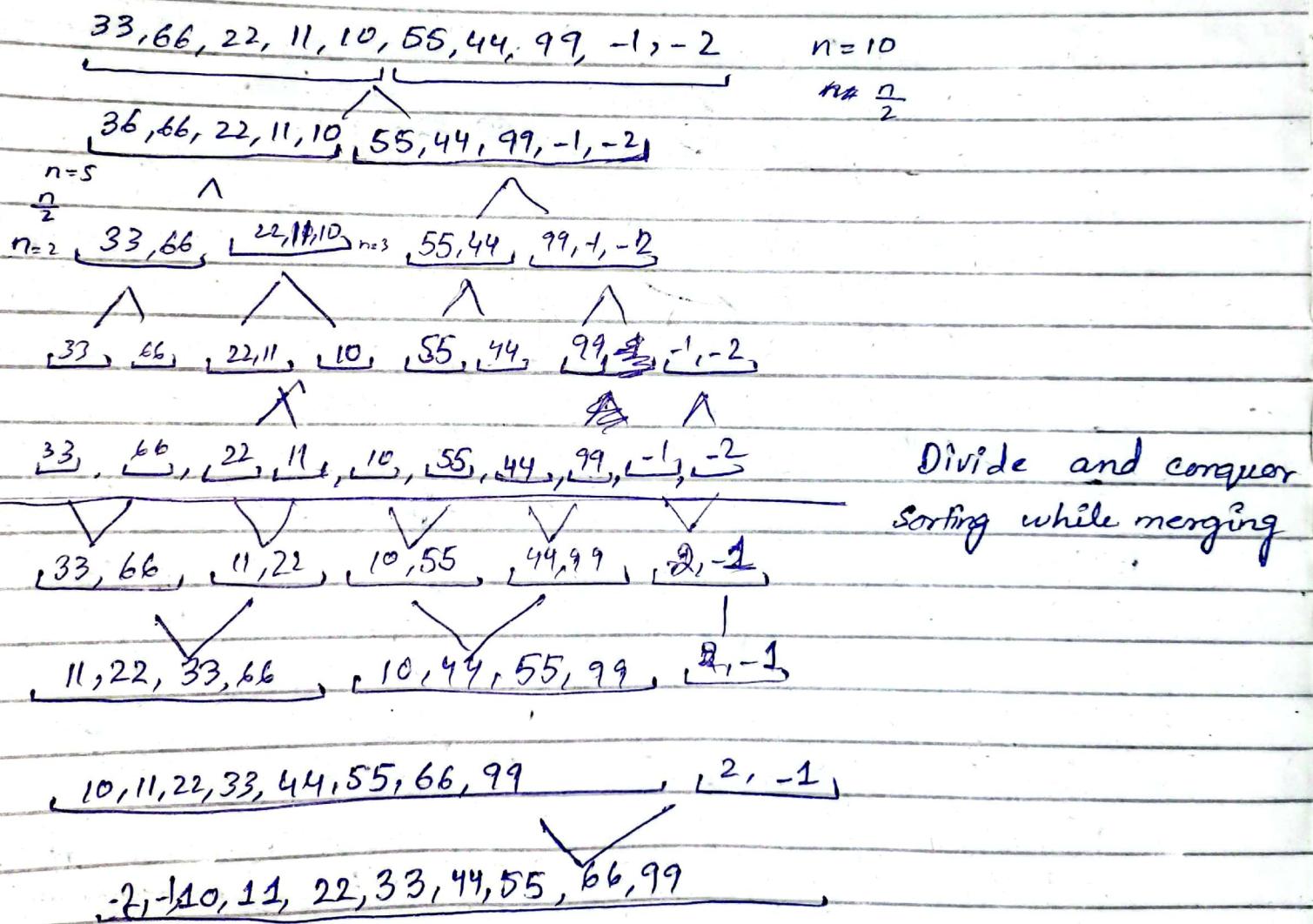
9 July June-2022

Data Structures (Theory)

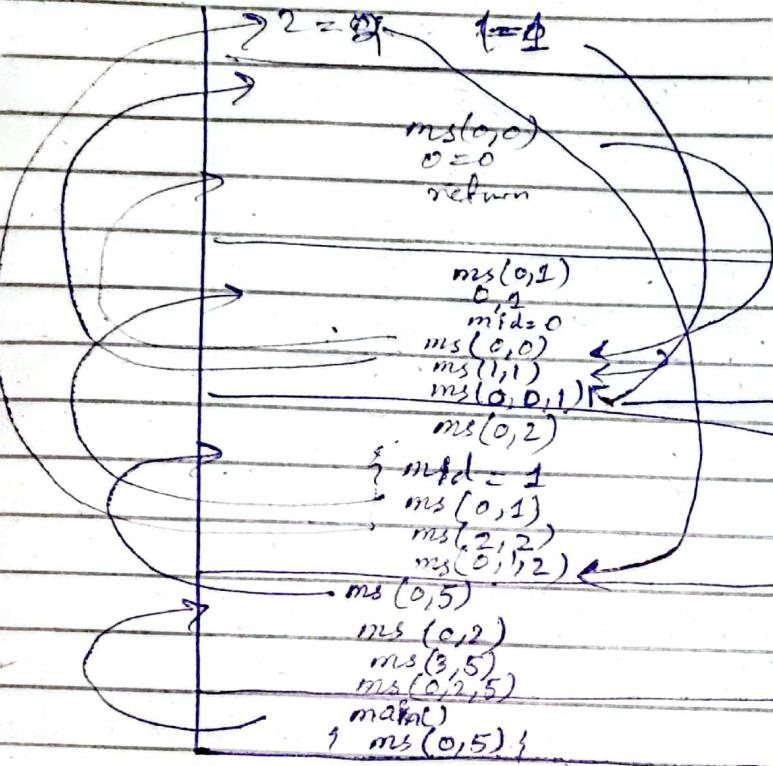
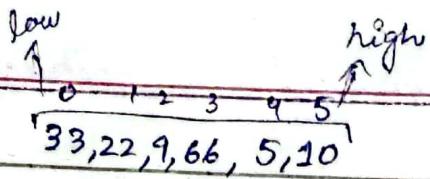
Thursday

* Non-linear Sorting Algorithms

- ① BST with inorder traversal.
 - ② Heap sort with Max heap/Min heap.
 - ③ Merge sort



$$\frac{5}{2} = 2$$



- uniform division
- uniform repeating
- uniform merging



merge-sort(int low, int high)

{ int mid;

 if (low != high)

 mid = (low+high)/2

 mergesort (low, mid);

 mergesort (mid+1, high);

 merge (low, mid, high)

 merge (int low, int mid,

 int high)

 { int temp[MAX];

 int i = low;

 int j = mid+1;

 int k = low;

 while ($i <= k <= mid$) { if

 ($j <= high$) ($i <= j$)

 if (array[i] <= array[j])

 temp[k++] = array[i++]

 else

 temp[k++] = array[j++]

Kisi doro array mn se
ek element rk jaye.

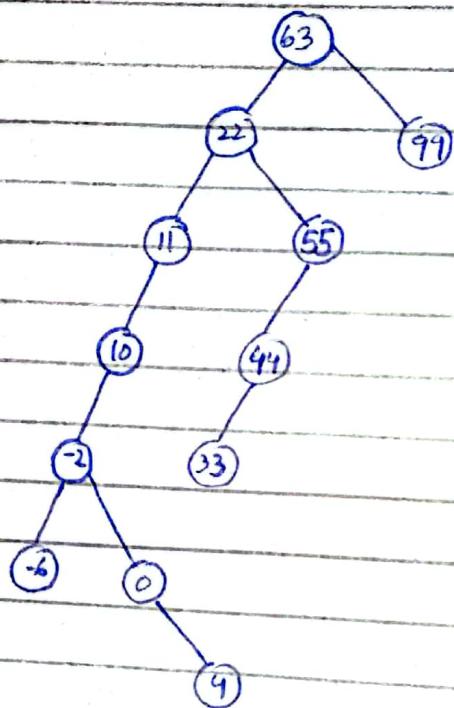
```
while (i <= mid)
    temp[k++] = array[i++];
while (j <= high)
    temp[k++] = array[j++];
for (i = low, i < high; i++)
    array[i] = temp[i];
```

DSA (Theory)

Non Linear Sorting Algorithms:

① BST

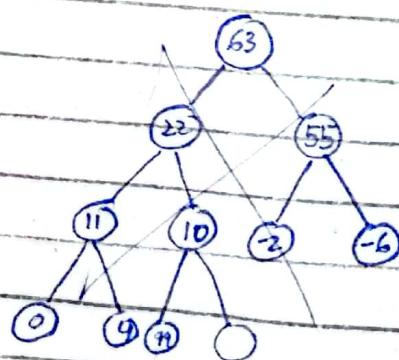
63, 22, 55, 11, 10, -2, -6, 0, 4, 99, 44, 33

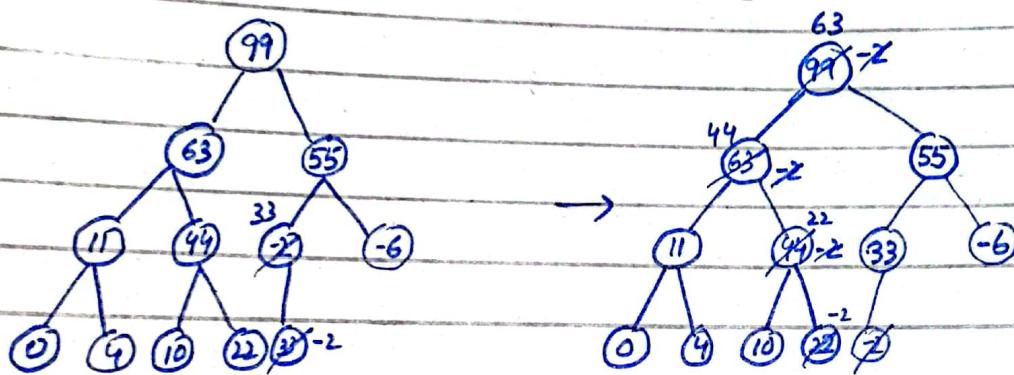
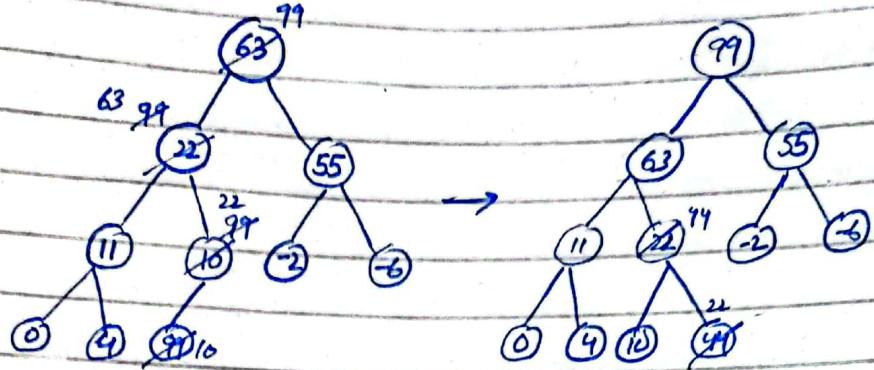


Inorder Traversal:

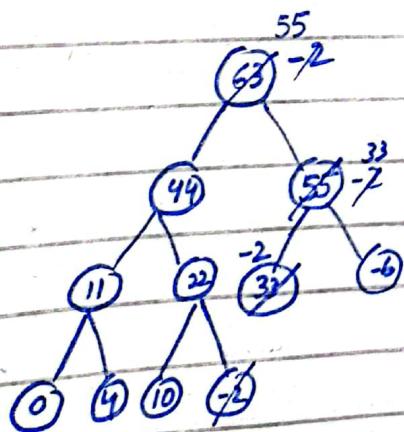
-6, -2, 0, 4, 10, 11, 22, 33, 44, 55, 63, 99

② Heap Sort:

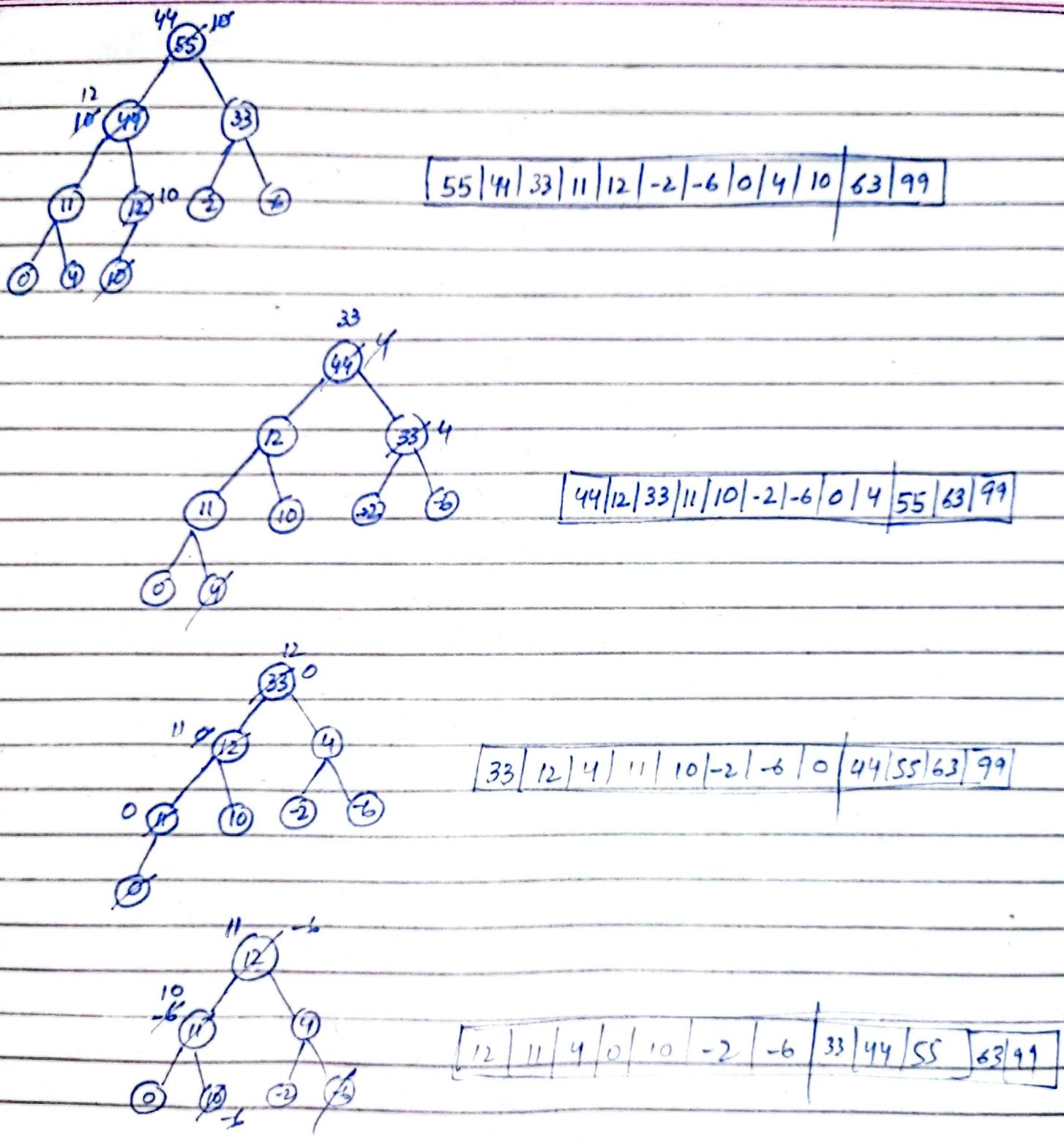


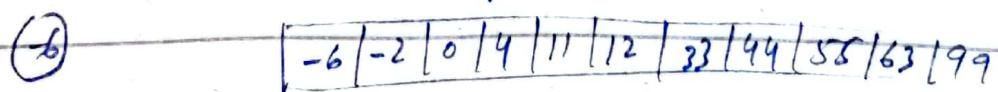
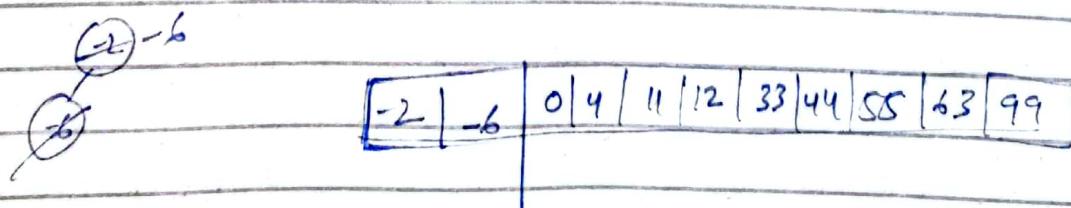
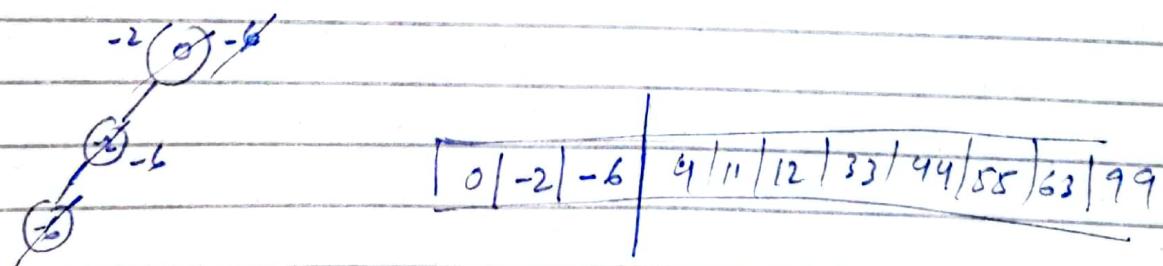
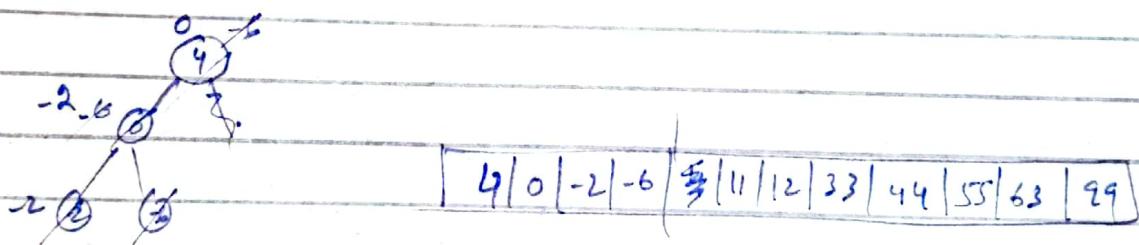
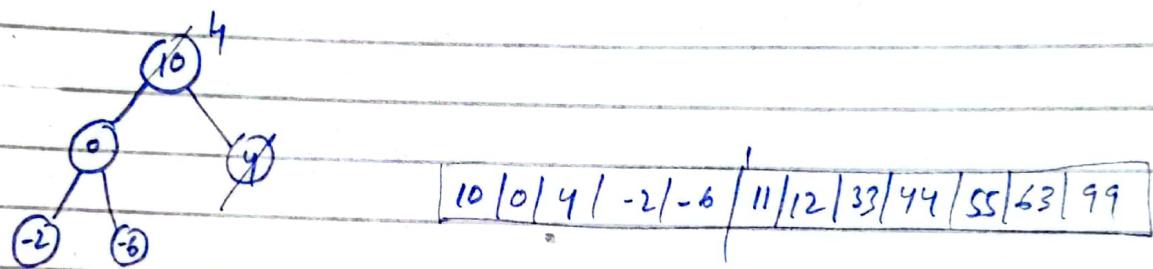
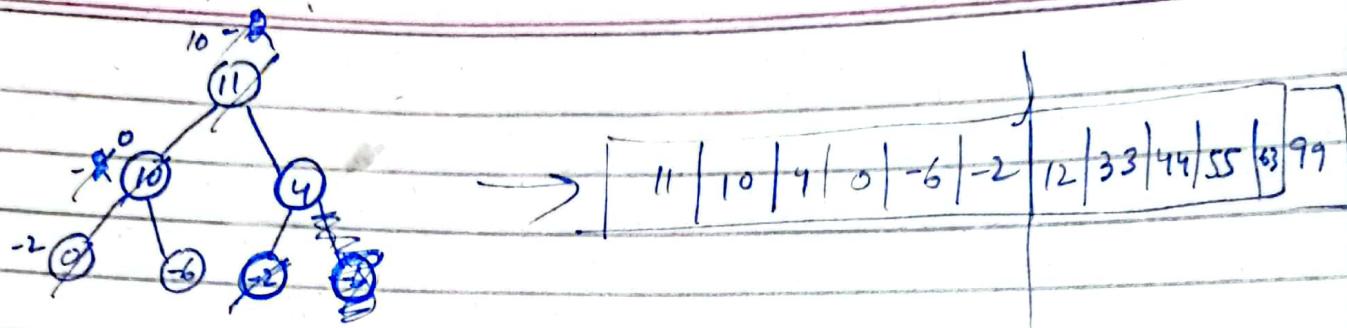


99	63	55	11	44	33	-6	0	4	10	22	-2
----	----	----	----	----	----	----	---	---	----	----	----



63	44	55	11	22	33	-6	0	4	10	-2	99
----	----	----	----	----	----	----	---	---	----	----	----





10 June 21

Time Complexity Analysis:

$$T(n) =$$

$O(1)$
$O(\log n)$
$O(n)$
$O(n \log n)$
$O(n^2)$
$O(n^3)$
$O(n!)$
$O(e^n)$

Merge Sort

Same Steps for all types of data.

$$T(n) = T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + n$$

↑ division ↑ Merging
for every step

$$\frac{n}{2} + \frac{n}{2} = \frac{2n}{2} = n$$

$$T(n) = 2T\left(\frac{n}{2}\right) + n \quad \text{--- ①}$$

Substitution: $n = \frac{n}{2}$ in eq ①
Method:

$$T\left(\frac{n}{2}\right) = 2T\left(\frac{n}{4}\right) + \frac{n}{2}$$

Put eq ② in eq ①

$$\begin{aligned} T(n) &= 2 \left[2T\left(\frac{n}{4}\right) + \frac{n}{2} \right] + n \\ &= 2^2 T\left(\frac{n}{2^2}\right) + \frac{n}{2} + n \\ &= 2^2 T\left(\frac{n}{2^2}\right) + 2n \end{aligned}$$

Substituting $n = \frac{n}{4}$ in eq ①

$$T\left(\frac{n}{4}\right) = 2T\left(\frac{n}{8}\right) + \frac{n}{4} \Rightarrow 2T\left(\frac{n}{4}\right)$$



① Best Case $B(n)$

② Worst Case $S(n)$ → ASC

③ Average Case $A(n)$

④ Every Case $T(n)$

↑
↓
Sara
ASC
DSC

↓
mixed
data

Put eq. ④ in eq. ③

$$T(n) = 2^2 \left[2T\left(\frac{n}{8}\right) + \frac{n}{4} \right] + n$$

$$= 2^3 T\left(\frac{n}{2^3}\right) + 3n$$

$$T(n) = 2^4 T\left(\frac{n}{2^4}\right) + 4n$$

$$T(n) = 2^i T\left(\frac{n}{2^i}\right) + in \quad \rightarrow \text{General Term.}$$

$$T(1) = 1 \quad \rightarrow \text{One cycle for one end.}$$

$$\frac{n}{2^i} = 1$$

$$n = 2^i$$

$$\log_2 n = \log_2 2^i$$

$$\log_2 n = 2 \log_2 i$$

$$\log_2 n = i$$

$$T(n) = n T(1) + n \log_2 n$$

$$= n + n \log_2 n$$

const ko
ignore kme
mai = $n(\log_2 n)$

$$T(n) = O(n \log n)$$

6 5 4 3 2 1

$$n=6$$

$$\frac{n}{2} + \frac{n}{2} + n$$

$$\frac{6}{2} + \frac{6}{2} + 6$$

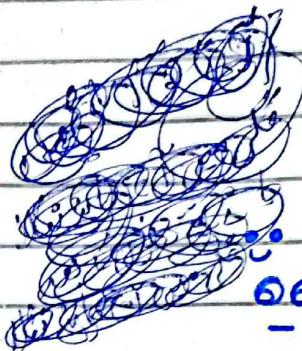
Merge sort is every case algorithm.

$$O(n \log n)$$

No of elements

\rightarrow A good time complexity

Non-linear data structure



①
②
③

④
⑤
⑥

Sorting \rightarrow Comparison + Interchange

Heap Sort

Reasons:

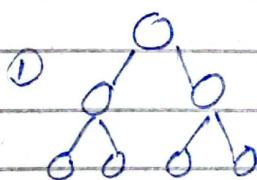
Bcz heap sort is tree BST

$$O(\log_2 n)$$

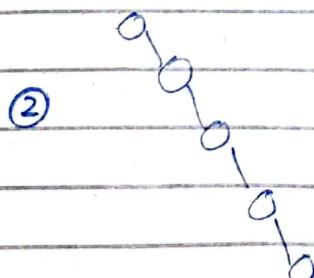
$$O(n \log_2 n)$$

\rightarrow bcz sorting.

BST



\rightarrow Not unbalanced \rightarrow hr level pr node present
 \hookrightarrow So its best case



\rightarrow unbalanced
↳ worst case

T

③ Adha idhe adha
udhan :D

Average case

$$w(n) = 1 + 2 + 3 + 4 + 5 + 6 + \dots + n$$

Comparison.

$$T(n) = 2i$$

$$= n \log_2 n$$

$$B(n) \in O(n \log_2 n)$$

$$w(n) = 1+2+3+4+5+6+\dots+n$$

$$= \frac{n}{2} [2n + (n-1)1] d.$$

$$= \frac{n}{2} [2 \times 1 + (n-1)1]$$

$$= \frac{n}{2} [2+n-1]$$

$$= \frac{n(n-1)}{2} = \frac{n^2-n}{2} \Rightarrow \frac{n^2}{2} - \frac{n}{2} \rightarrow \text{constant term ignored}$$

$$= \frac{n^2}{2}$$

$\rightarrow O(n^2)$ worst case

Highest term what's left

$\frac{n^2}{2}$ - $\frac{n}{2}$ → constant term ignored

14 June - 2022

DSA (Theory)

Tuesday

→ Non-linear Sorting Algorithms

- * Merge sort
 - * Binary Tree Sort
 - * Heap Sort

Linear Sorting Algorithms

① Bubble Sort

Loop for
Passes

for ($i=1$; $i \leq n-1$; $i++$)

{ for ($j=1$; $j \leq n-i$, $j++$)
 { if $a[j] < a[j+i]$

Less than for descending order

$\binom{n^2}{n-1}$ 65, 22, 33, 11, 20, -1, 0, 21, 14, 15
8 compositions

$$n=19$$

(n-1 → Passes) → Access

8 comparisons.

65, 22, 33, 11, 20, -1, 0, 21, 14, 15

7. Pass 1	8	22, 68, 33, 68, 11, nat
6. Pass 2	7	22, 68, 33, 68, 11,

Pass 1 8 22, 65 33, 65 11,
nat

(n-2) Pass 2 22, 38 11, 38 20, 38 -1, 38 0, 38 21, 38 14, 38 1, 33, 15
 (n-3) Pass 3 22 11, 22 20, 22 -1, 22 0, 22 21, 22 14, 22 32, 15

Comparison is greatest no of times operation.

(n-3) Pass 3 6 22.11, 22.20, 22.1, 22.0, 22.21, 22.14, 22.33, 65

6-4) Pass 4	5	11, 20.1, 260, 20, 2114 2A	21 22 33 65
-------------	---	----------------------------	-------------

(n-5) Pass 5 4 H=1, 14.0, 17, 20, 14, 21, 22, 23, 24, 25

(n-5) Pass 5	4	11, 22, 33, 20, 19, 20, 21, 22, 33, 65
(n-6) Pass 6	3	2, 7, 11, 14, 22, 23, 22, 23, 65

(n-6) Pass 6 3 -1, 0, 11, 14, 20, 21, 22, 33, 6
 (n-7) Pass 7 3 1, 11, 14

(n-7) Pass 7 2 -1, 0, 11, 14, 20, 21, 22, 33, 65
(n-8) P. 2 1

fn-8) Pass 8 1 -1 | 0, 11, 14, 20, 21, 22, 32, 65

↑

comparisons

cutting kx k
likhna hai or
phir neat kr
k likhna ha.

Pass 1	68 22, 68 33, 68 11, 68 20, 68 -1, 68 0, 68 21, 68 21, 68 14, 68 15, 65 22, 33, 11, 20, -1, 0, 21, 14, 15 65
Pass 2	22, 33 11, 33 20, 33 -1, 33 0, 33 21, 33 14, 33 15, 33, 65 22, 11, 20, -1, 0, 21, 14, 15 33, 65
Pass 3	22 11, 22 20, 22 -1, 22 0, 22 21, 22 14, 22 15, 22, 33, 65 11, 20, -1, 0, 21, 14, 15, 22, 33, 65
Pass 4	11, 20 -1, 20 0, 20, 21 14, 21 14, 21 15, 21, 22, 33, 65 11, -1, 0, 20, 14, 15 21, 22, 33, 65
Pass 5	
Pass 6	
Pass 7	
Pass 8	

There are 3 cases of time complexity of Bubble sort

Already sorted

- Best Case (Perhly Pass mn hi sorted data)
- Worst Case (Totally different (unsorted)) (last pass mn sort ho)
- Average Case (Data sorted in any middle Pass)
 - ↳ Rest of Passes nhe kamy chyaen)

Processor ko freq
nhi pata islie
jo zada no of
times operating pufi
hota hai to basic
operation usy length
to calculate $T(n)$
Bki operations km times ha

```

for (i=1; i <= n-1; i++)
{
    exchanges = 0;
    for (j=1, j <= n-2; j++)
    {
        if a[j] > a[j+1]
            interchang;
            exchanges++;
    }
    if exchanges == 0
        break;
}
    
```

For Passes. Passes
If in 1st Pass exchanges = 0

Best case

In Best Case

Passes + Comparison + Changes

1 time outer loop (Passes) and inner loop
for comparison executes. So greatest no of operations

Time complexity $1 + (n-1) = T(n) \in O(n)$

Worst Case

$$\begin{aligned}
T(n) &= (n-1) + (n-2) + (n-3) + \dots + 1 \\
&= 1 + 2 + 3 + \dots + (n-1) \\
\text{First term} &\leftarrow \frac{n}{2}[2a + (n-1)d] \quad \hookrightarrow \text{highest term} \\
&= \frac{n-1}{2}[2 \cdot 1 + (n-1-1)] \\
&\quad \hookrightarrow \text{differences}
\end{aligned}$$

$$= \frac{n}{2} [2 + n - 2]$$

$$= \frac{n}{2} [n - 1]$$

$$= \frac{n^2}{2} - \frac{n}{2} \text{ const term} = \frac{n^2}{2} \in O(n^2)$$

Average Case

↳ Also belongs to $O(n^2)$
 $n-1$ comparisons

Tayyaba



Aleena Khan

Selection Sort:

Every case

1st comparison with

R 33, 22, 5, 6, -1, 36, 42, 55, 44. : $n=9$ ($n-1$) Passes

$n-1$	Pass 1	[-1], 22, 5, 6, [33], 36, 42, 55, 44
$n-2$		-1, [5], 22, 6, 33, 36, 42, 55, 44
$n-3$		-1, 5, [6], [22], 33, 36, 42, 55, 44
$n-4$		-1, 5, 6, 22, 33, 36, 42, 55, 44
$n-5$		-1, 5, 6, 22, 33, [36], 42, 55, 44
$n-6$		-1, 5, 6, 22, 33, 36, [42], 55, 44
$n-7$		-1, 5, 6, 22, 33, 36, 42, [55], 44
$n-8$		-1, 5, 6, 22, 33, 36, 42, 44, [55]
1	Pass	

```
for(i=1; i<=n-1; i++)
```

{ smallest = a[i]

```
for(j=i+1; j<=n; j++)
```

{ if (a[j] < smallest)

smallest = a[j]

interchange a[j] and smallest;

Selection Sort,

Every case (of k) sort ho bijaye to say passes performed

Same as Worst case of bubble sort ki time complexity

Comparison is greatest no of times operations performed

③ [Insertion Sort]

33, 66, 22, 11, -5, 60, 77, 88, 44. ($n=9$)
($n-1$) passes

Pass 1 (i=1) | 33 | 66, 22, 11, -5, 60, 77, 88, 44.

Pass 2 (i=2) | 33 | 66 | 22, 11, -5, 60, 77, 88, 44. right side comparison

Pass 3 | 33, 66 | 22, 11, -5, 60, 77, 88, 44
| 33, 22, 66 | 11, -5, 60, 77, 88, 44

Sorting Modified

→ Sorting Modified pdf

Pass 4

22, ~~22~~, 33, 66 | 11, 66 |, 44, 60, 77, 88, 44
 22, 33 | 11, 66 |, -5, 60, 77, 88, 44
 22 | 11, 22, 33, 66 |, -5, 60, 77, 88, 44
11, 22, 33, 66 |, 60, 77, 88, 44 ~~Sete~~

Pass 5

11, 22, 33, 66 | 60, 66 |, 77, 88, 44
11, 22, 33, 60, 66 |, 77, 88, 44

Pass 6

11, 22, 33, 60, 66, 77 |, 88, 44.

Pass 7

11, 22, 33, 60, 66, 77, 88 |, 44



Pass 8

11, 22, 33, 60, 66, 77, 88 | 44, 88
11, 22, 33, 60, 66, 77 | 44, 77, 88
11, 22, 33, 60, 66 | 44, 66, 77, 88
11, 22, 33, 60 | 44, 66, 77, 88
11, 22, 33, 44, 60, 66, 77, 88.



for ($i=1$; $i < n-1$; $i++$)
 { smallest = a[i];

$j=i+1$

while ($a[j] > 0$ $\&$ $a[j] < \text{smallest}$) → ^{data already sorted in j loop}
 { interchange smallest with a[j];
 }

[↑]
 +
 the only
 go.

Worst Case $O(n^2)$ Average Case ^{also} $(O(n^2))$

$$\text{Comparisons} = 1 + 2 + 3 + 4 + \dots + n - 1$$

```
void Bubble-sort (node **start, int count)
```

5

```
struct node **h;  
int i,j, exchange;
```

```
for (i = 0; i <= count ; i++)
```

g #h = start;

$$x_{\text{change}} = 0$$

for (j=0; j < count - i - 1; j++)

$$P1 = \text{th}_3$$

$$p^2 = p^1 \rightarrow \text{link}_j$$

if ($p_1 \rightarrow \text{info} > p_2 \rightarrow \text{info}$)

$\{^* + h = \text{swap}(p1, p2);$

xchange = \$;

$$h = 8 (*h) \rightarrow \text{link},$$

if (xchange = 0)

break

3

```

struct node temp;
temp = ptr2->link;
ptr2->link = ptr1;
ptr1->link = ptr2 ptr1;
return ptr2;
}

```