

Module Interface Specification for CFS

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1 Revision History

Date	Version	Notes
Nov 10, 2018	1.0	First draft by Malavika
Nov 21, 2018	1.1	Corrections based on presentation by Malavika
Nov 24, 2018	1.2	MIS submission draft by Malavika

2 Symbols, Abbreviations and Acronyms

See CA Documentation at <https://github.com/Malavika-Srinivasan/CAS741/blob/master/docs/SRS/CA.pdf>

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3 Introduction

The following document details the Module Interface Specifications for CFS (Curve Fitting Software). The goal of CFS is to find the parameters of the curve which is the best possible fit through the given set of ‘ n ’ data points, where $n \geq 2$.

Complementary documents include the Commonality Analysis and Module Guide. The full documentation and implementation can be found at the repository <https://github.com/Malavika-Srinivasan/CAS741>.

4 Notation

The structure of the MIS for modules comes from Hoffman and Strooper (1995), with the addition that template modules have been adapted from Ghezzi et al. (2003). The mathematical notation comes from Chapter 3 of Hoffman and Strooper (1995). For instance, the symbol $:=$ is used for a multiple assignment statement and conditional rules follow the form $(c_1 \implies r_1 | c_2 \implies r_2 | \dots | c_n \implies r_n)$.

The following table summarizes the primitive data types used by CFS.

Data Type	Notation	Description
character	char	a single symbol or digit
integer	\mathbb{Z}	a number without a fractional component in $(-\infty, \infty)$
natural number	\mathbb{N}	a number without a fractional component in $[1, \infty)$
real	\mathbb{R}	any number in $(-\infty, \infty)$
boolean	\mathbb{B}	a value from the set $\{True, False\}$

The specification of CFS uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, CFS uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

5 Module Decomposition

[Needs to be changed in MG based on Dr. Smith’s suggestion —Malavika] The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding Module	
Behaviour-Hiding Module	Input Output
Software Decision Module	Sequence Services Interpolation Regression Plot

Table 1: Module Hierarchy

6 MIS of Input module

This module corresponds to R??, R?? and R?? in the CA document. The secrets of this module are how the data points are input and how they are verified. The load and verify secrets are isolated to their own access programs.

6.1 Module

input

6.2 Uses

Sequence services(10)

6.3 Syntax

Name	In	Out	Exceptions
loadInput	inFile : string	-	FileError
verifyInput	-	-	ValueError, TypeError
verifyDegree	degree:ℕ	<i>degVerify</i> :℔	ValueError

6.3.1 Exported Constants

NA

6.3.2 Exported Access Programs

Name	In	Out	Exceptions
verifyDegree	degree:ℕ	<i>degVerify</i> :℔	ValueError

[I need the verifyDegree as an exported access program because I will be verifying the degree input from regression module if necessary. —Malavika]

[You don't have a Syntax section and an Exported Access Programs. The syntax section is already listing all access programs that are exported. —SS]

6.4 Semantics

6.4.1 State Variables

From R?? in CA

$t: \mathbb{R}^n$

$y: \mathbb{R}^n$

6.4.2 Environment Variables

inFile: sequence of string [I am leaving it as sequence of strings because sometimes, you may want to append a file name to a path name. —Malavika] [Also, I am thinking if I really need a file input. I think this should be the user program's responsibility. My access programs do not have an interface to accept filename. They will accept only x and y arrays. This needs to be discussed. —Malavika]

[The environment variable for a file is not the name of the file, but the contents of the file. You need to decide what your design is. I see the input module as providing services that you can use. Since your module has state information, you need a way to get this state information into the module. A file is a logical choice. —SS] [You cannot use the same name for your environment variable as you use for the first field of your loadInput method. It is confusing. I think this might be part of why you are confusing the file name and the file contents. —SS]

6.4.3 Assumptions

- The loadInput will be called before calling the verifyInput method.
- Regression module will be called before calling verifyDegree method.
- The loadInput will be called before the values of any state variables will be accessed.

6.4.4 Access Routine Semantics

input.t: [You don't actually list an access program with this name? —SS]

- transition: NA
- output: $out := t$
- exception: NA

input.y: [You don't actually list an access program with this name? —SS]

- transition: NA
- output: $out := y$
- exception: NA

loadInput(s):

- transition: inFile is used to modify the state variables using the following procedural specification:
 1. Read data sequentially from inputFile to populate the state variables t and y .

2. verifyInput()

- output: NA
- exception: $exc :=$ a file name s cannot be found \vee the format of inFile is incorrect \implies FileError. [I am yet to decide if the library will take a .txt and .csv or both. This specification will become formal once we decide the type of the input file. —Malavika]

verifyInput():

- transition: NA
- output: NA
- exception: $exc :=$

Name	Exception
$(t \leq 1 \vee y \leq 1)$	\implies LengthError
$(t \neq y)$	\implies LengthMismatchError
$(\exists x \in t \wedge x \notin \mathbb{R})$	\implies TypeError
$(\exists x \in y \wedge x \notin \mathbb{R})$	\implies TypeError

verifyDegree():

- transition:
 - $(deg \in \mathbb{N}) \implies \text{degVerify} = \text{True}$
- output:
- exception: $exc :=$

Name	Exception
$(deg \notin \mathbb{N})$	\implies ValueError

6.4.5 Local Functions

NA

7 MIS of Interpolation module

This module corresponds to R??, R??, R??, R?? and R?? in section ?? of CA document.

7.1 Module

interp

7.2 Uses

Input(6), Output(9), Sequence services(10)

7.3 Syntax

7.3.1 Exported Constants

NA

7.3.2 Exported Access Programs

Name	In	Out	Exceptions
interpMonomial	$t:\mathbb{R}^n, y:\mathbb{R}^n$	-	-
interpLagrange	$t:\mathbb{R}^n, y:\mathbb{R}^n$	-	-
interpNewton	$t:\mathbb{R}^n, y:\mathbb{R}^n$	-	-
interpHermiteCubic	$t:\mathbb{R}^n, y:\mathbb{R}^n$	-	-
interpBSpline	$t:\mathbb{R}^n, y:\mathbb{R}^n$	-	-
evalMonomial	$t:\mathbb{R}^n, y:\mathbb{R}^n$	$yNew:\mathbb{R}^n$	-
evalLagrange	$t:\mathbb{R}^n, y:\mathbb{R}^n$	$yNew:\mathbb{R}^n$	-
evalNewton	$t:\mathbb{R}^n, y:\mathbb{R}^n$	$yNew:\mathbb{R}^n$	-
evalHermiteCubic	$t:\mathbb{R}^n, y:\mathbb{R}^n$	$yNew:\mathbb{R}^n$	-
evalBSpline	$t:\mathbb{R}^n, y:\mathbb{R}^n$	$yNew:\mathbb{R}^n$	-

[Your input module has state information, yet you are explicitly providing inputs of this same information. You need to decide what your design is and stick to it. —SS]

7.4 Semantics

7.4.1 State Variables

- $x:\mathbb{R}^{m \times n}$, where n is the number of data points and m is the number of sections.

- interval: \mathbb{R}^m , m is the number of sections

[Why do you have a state variable? The connection between your inputs and your outputs is unclear. Is the state variable keeping the information that you need for evaluation? That would make sense. I think your design would make more sense if you followed the design we used for SFS. You can have one interpolating polynomial object and the specific method it uses to build its state variables comes as an input parameter. This would be similar to the 2AA4/2ME3 assignment I showed in class, where the order of interpolation was a parameter. This would mean that you only needed one eval. The object itself would know how to interpret eval —SS]

7.4.2 Environment Variables

NA

7.4.3 Assumptions

- evalMonomial() will be called after interpMonomial().
- evalLagrange() will be called after interpLagrange().
- evalNewton() will be called after interpNewton().
- evalHermiteCubic() will be called after interpHermiteCubic.
- evalBSpline() will be called after interpBSpline().

7.4.4 Access Routine Semantics

interp.x:

- transition: NA
- output: $out := x$
- exception: NA

interpMonomial(t, y):

- transition:
 - 1. $x: \mathbb{R}^{m \times n} = 0.0$, this is initialization. This is necessary as all the methods will be using the same state variable.

2. $x: \mathbb{R}^{m \times n}$ obtained by solving for x using the equation below.

$$\begin{bmatrix} 1 & t_1 & t_1^2 & \dots & t_1^{n-1} \\ 1 & t_2 & t_2^2 & \dots & t_2^{n-1} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & t_n & t_n^2 & \dots & t_n^{n-1} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

– $interval[0] := t[0]$, this is initialized to starting point for non piecewise functions.

- output: NA
- exception: NA

evalMonomial(t, y):

- transition: NA
- output: $out := yNew$

$\forall t_i \in t, yNew \text{---} y_1$ where y_1 is obtained as shown below.

$$y_1 = x_1 + x_2 t_i + x_3 t_i^2 + x_4 t_i^3 + \dots x_n t_i^{n-1}$$

- exception: NA

interpLagrange(t, y):

- transition:

- 1. $x: \mathbb{R}^{m \times n} = 0.0$, this is initialization. This is necessary as all the methods will be using the same state variable.
- 2. $x: \mathbb{R}^{m \times n}$ obtained by solving for x using the equation below.

$$\begin{bmatrix} 1 & 0 & 0 & \dots & 0 \\ 0 & 1 & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

– $interval[0] := t[0]$, this is initialized to starting point for non piecewise functions.

- output: NA

- exception: NA

evalLagrange(t, y):

- transition: NA
- output: $out := yNew$

$\forall t_i \in t, yNew \longrightarrow y_0$ where y_0 is obtained as shown below.

$$y_0 = y_1 l_1(t) + y_2 l_2(t) + \dots y_n l_n(t).$$

where $l_j(t)$ is given by,

$$l_j(t) = \frac{\prod_{k=1, k \neq j}^n (t - t_k)}{\prod_{k=1, k \neq j}^n (t_j - t_k)}$$

- exception: NA

interpNewton(t, y):

- transition:
 - 1. $x: \mathbb{R}^{m \times n} = 0.0$, this is initialization. This is necessary as all the methods will be using the same state variable.
 2. $x: \mathbb{R}^{m \times n}$ obtained by solving for x using the equation below.

$$\begin{bmatrix} \pi_0(t_0) & 0 & 0 & \dots & 0 \\ \pi_0(t_1) & \pi_1(t_1) & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & 0 \\ \pi_0(t_n) & \pi_1(t_n) & \pi_2(t_n) & \dots & \pi_n(t_n) \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

where,

$$i < j \implies \pi_j(t) = 0, i \geq j \implies \pi(t) = \prod_{k=1}^{j-1} (t - t_k)$$

- $interval[0] := t[0]$, this is initialized to starting point for non piecewise functions.

- output: NA
- exception: NA

evalNewton(t, y):

- transition: NA
- output: $out := yNew$
 $\forall t_i \in t, yNew \longrightarrow y_0$ where y_0 is obtained as shown below.

$$y_0 = x_1 + x_2(t - t_1) + x_3(t - t_1)(t - t_2) + \dots x_n(t - t_1)(t - t_2) \dots (t - t_{n-1})$$

- exception: NA

interpHermiteCubic(t, y):

- transition:
 - 1. $x: \mathbb{R}^{m \times n} = 0.0$, this is initialization. This is necessary as all the methods will be using the same state variable.
 - 2. $x: \mathbb{R}^{m \times n}$ obtained by solving for x using the equation below.

$$\begin{bmatrix} 1 & t_0 & t_0^2 & t_0^3 \\ \vdots & \vdots & \vdots & \vdots \\ 1 & t_n & t_n^2 & t_n^3 \\ 0 & 1 & 2t_0 & 3t_0^2 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 1 & 2t_n & 3t_n^2 \\ 0 & 0 & 2 & 6t_0 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 2 & 6t_n \\ 0 & 0 & 0 & 6 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & 6 \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ x_{n(m+1)} \end{bmatrix} = \begin{bmatrix} y_0 \\ \vdots \\ y_n \\ y_0^{(1)} \\ \vdots \\ y_n^{(1)} \\ y_0^{(2)} \\ \vdots \\ y_n^{(2)} \\ y_0^{(3)} \\ \vdots \\ y_n^{(3)} \end{bmatrix}$$

Where $y_0^{(3)}$ represents the third derivative of y_0 .

- interval: $\mathbb{R}^k = t[0]$ to $t[n - 2]$, by default we make each point a breakpoint and hence there is a piecewise polynomial between $[t_{i-1}, t_i)$.

- output: NA.
- exception: NA

evalHermiteCubic(t, y):

- transition:

- output: $out := yNew$

$\forall t_i \in t, yNew \text{---} y_0$ where y_0 is obtained as shown below.

$$y_0 = x_{k0} + x_{k1}t + x_{k2}t^2 + x_{k3}t^3 \text{ for } k = 0 \text{ to } n - 2$$

- exception: NA

interpBSpline(t, y):

- transition:

- 1. $x: \mathbb{R}^{m \times n} = 0.0$, this is initialization. This is necessary as all the methods will be using the same state variable.
- 2. $x: \mathbb{R}^{m \times n}$ obtained by using the formula below.
For $k > 0$ to n , where n is the number of data points

$$x = v_i^k = \frac{t - t_i}{t_{i+k} - t_i}$$

[BSpline gives the v values which will be used recursively in formula defined in IM?? of the CA document —Malavika]

- interval: $\mathbb{R}^k = t[0]$ to $t[n - 2]$, by default we make each point a breakpoint and hence there is a piecewise polynomial between $[t_{i-1}, t_i)$.

- output: NA

- exception: NA

evalBSpline(t, y):

- transition:

- output: $out := yNew$

$\forall t_i \in t, yNew \text{---} y_0$ where y_0 is obtained as shown below.

$$y_0 = B_i^k(t) = v_i^k(t)B_i^{k-1}(t) + (1 - v_{i+1}^k(t))B_{i+1}^{k-1}(t)$$

for $k > 0$.

[I want the notation of ‘B’ so that it is easy to understand the coefficients, thats why I have $y_0 = B...$ —Malavika]

- exception: NA

7.4.5 Local Functions

NA

8 MIS of Regression module

This module corresponds to R??, R?? and R?? in section ?? of CA document.

8.1 Module

reg

8.2 Uses

Input(6), Output(9), Sequence services(10)

8.3 Syntax

8.3.1 Exported Constants

NA

8.3.2 Exported Access Programs

Name	In	Out	Exceptions
regNormalEq	$t:\mathbb{R}^n, y:\mathbb{R}^n, \text{deg}:\mathbb{N}$	-	-
regAugSys	$t:\mathbb{R}^n, y:\mathbb{R}^n, \text{deg}:\mathbb{N}$	-	-
regOrthogonalTn	$t:\mathbb{R}^n, y:\mathbb{R}^n, \text{deg}:\mathbb{N}$	-	-
evalReg	$t:\mathbb{R}^n$	$y_{\text{New}}:\mathbb{R}^n$	-

[Again, it is unclear why you have an input parameters module with state information if you aren't going to use that state information. —SS]

8.4 Semantics

8.4.1 State Variables

- $x: \mathbb{R}^m$

[You should give a clue on how to interpret this state variable. Is it the coefficients for the polynomial? —SS]

8.4.2 Environment Variables

NA

8.4.3 Assumptions

- `input.verifyDegree()` will be called before any of the access programs will be used.
- `evalReg()` will be called after calling `(regNormalEq() ∨ regAugSys() ∨ regOrthogonalTn())`.

8.4.4 Access Routine Semantics

`reg.x:`

- transition: NA
- output: `out := x`
- exception: NA

`regNormalEq(t,y,deg):`

- transition:
 - `degVerify = verifyDegree(deg)`
 - `(degVerify == True) ⇒ x : ℝn is initialized to 0.0.` [This is initialization with maximum length possible. For a data of length n, you can maximum get n coefficients in the polynomial. —Malavika]
 - `x : ℝm`, obtained by solving for `x` in the equation below. [m is the degree of the coefficients of the polynomial. —Malavika]

$$A^T A x = A^T y$$

- output: NA
- exception: NA

`regAugSys(t,y,deg):`

- transition:
 - `degVerify = verifyDegree(deg)`
 - `(degVerify == True) ⇒ x : ℝn is initialized to 0.0.` [This is initialization with maximum length possible. For a data of length n, you can maximum get n coefficients in the polynomial. —Malavika]

- $x : \mathbb{R}^m$, obtained by solving for x in the equation below. [m is the degree of the coefficients of the polynomial. —Malavika]

$$r + Ax = y$$

$$A^T r = 0$$

Where r is the residual vector.

- output: NA
- exception: NA

regOrthogonalTn(t, y, deg):

- transition:
 - $degVerify = \text{verifyDegree}(deg)$
 - $(degVerify == True) \ x : \mathbb{R}^n$ is initialized to 0.0. [This is initialization with maximum length possible. For a data of length n, you can maximum get n coefficients in the polynomial. —Malavika]
 - $x : \mathbb{R}^m$, obtained by solving for x in the equation below. [m is the degree of the coefficients of the polynomial. —Malavika]

$$Ax = Py$$

Where P is the orthogonality matrix.

- output: NA
- exception: NA

evalReg(t):

- transition: NA
- output: $out := yNew$, where $\forall t_i \in t$,

$$yNew || (np.poly1d(x)(t_i))$$

- exception: NA

[Is this connected to the state variable? I think so? —SS] [You should use calls to Python in your specification. Say things mathematically. —SS]

8.4.5 Local Functions

NA

9 MIS of Output module

This module corresponds to R?? in the CA document. The secrets of this module are how the output is given to the user program.

9.1 Module

output

9.2 Uses

Plot([11](#)), Sequence services([10](#))

9.3 Syntax

Name	In	Out	Exceptions
plotDataFit	$t:\mathbb{R}^n, y:\mathbb{R}^n$		-
coeffPlotScreen	$t:\mathbb{R}^n, y:\mathbb{R}^n, x:\mathbb{R}^m$	$x:\mathbb{R}^m$, plot	-
coeffFile	$x:\mathbb{R}^m, t:\mathbb{R}^n, y:\mathbb{R}^n$	$x:\mathbb{R}^m$	-

9.3.1 Exported Constants

NA

9.3.2 Exported Access Programs

Name	In	Out	Exceptions
plotDataFit	$t:\mathbb{R}^n, y:\mathbb{R}^n$		-
coeffPlotScreen	$t:\mathbb{R}^n, y:\mathbb{R}^n, x:\mathbb{R}^m$	$x:\mathbb{R}^m$, plot	-
coeffFile	$x:\mathbb{R}^m, t:\mathbb{R}^n, y:\mathbb{R}^n$	$x:\mathbb{R}^m$	-

9.4 Semantics

9.4.1 State Variables

NA

9.4.2 Environment Variables

OutputFile: String

The OutputFile represents a file in the hardware's file system.

The name of the file will be results.txt.

9.4.3 Assumptions

- The interpolation or the regression module will be called before the output module.

9.4.4 Access Routine Semantics

plotDataFit(t,y):

- transition:
 - Call the appropriate evaluate method from the interpolation or regression module as shown below..
 1. $y_{New} = \text{interp.evalMonomial}(t,y)$ or $\text{interp.evalLagrange}(t,y)$ or $\text{interp.evalNewton}(t,y)$ or $\text{interp.evalHermiteCubic}(t,y)$ or $\text{interp.evalBSpline}(t,y)$ or $\text{reg.evalReg}(t)$
 2. $\text{plot}(t,y)$ and $\text{plot}(t,y_{New})$
- output: $\text{out} := \text{plot}$
- exception: NA

coeffPlotScreen(t,y):

- transition :
 - $\text{plotDataFit}(t,y)$
- output: $\text{Out} := \text{interp}.x$ or $\text{reg}.x$, plot
- exception: NA

coeffFile():

- transition:
 - Create OutputFile.
 - write $\text{interp}.x$ or $\text{reg}.x$
- output: NA
- exception: NA

9.4.5 Local Functions

NA

10 MIS of Sequence Services

10.1 Module

seqSer [\[Provided by numpy Python —Malavika\]](#)

10.2 Uses

NA

10.3 Syntax

10.3.1 Exported Constants

NA

10.3.2 Exported Access Programs

Name	In	Out	Exceptions
isAscending	$arr : \mathbb{R}^n$	\mathbb{B}	-
unique	$arr : \mathbb{R}^n$	$uniArr : \mathbb{R}^m$	-
array_equal	$arr1 : \mathbb{R}^n, arr2 : \mathbb{R}^n$	\mathbb{B}	-

10.4 Semantics

10.4.1 State Variables

NA

10.4.2 Environment Variables

NA

10.4.3 Assumptions

NA

10.4.4 Access Routine Semantics

unique(*arr*):

- transition: NA
- output: $out := uniArr : \mathbb{R}^m$ where *uniArr* is given by,
 1. $arr[i] \neq arr[j], \forall i, j \in [(0 \text{ to } (|arr| - 1)) \wedge j \neq i] \implies \forall i \in [0 \text{ to } |arr| - 1], uniArr[i] := arr[i]$
- exception: NA

isAscending(*arr*)

- transition: NA
- output: $out := \neg \exists (i | i \in [0..|arr| - 2] : arr_{i+1} < arr_i)$
- exception: NA

array_equal(*arr1*,*arr2*):

- transition: NA
- output: $out := (|arr1| == |arr2|) \wedge (\forall i \in [0 \text{ to } |arr1| - 1], arr1[i] == arr2[i]) \implies True$
- exception: NA

10.4.5 Local Functions

NA

10.4.6 Considerations

This module is provided by numpy in Python.

11 MIS of Plot Module

11.1 Module

plot

11.2 Uses

NA

11.3 Syntax

11.3.1 Exported Access Programs

Name	In	Out	Exceptions
Plot	$X : \mathbb{R}^n, Y : \mathbb{R}^n$		SeqSizeMismatch

11.4 Semantics

11.4.1 State Variables

NA

11.4.2 Environment Variables

win: 2D sequence of pixels displayed on the screen
[\[good —SS\]](#)

11.4.3 Assumptions

NA

11.4.4 Access Routine Semantics

Plot(X, Y)

- transition: modify win so that it displays an x-y graph of the data points showing X and the corresponding Y values. X is the independent variable and Y as the dependent variable.
- exception: ($|X| \neq |Y| \implies \text{SeqSizeMismatch}$)

References

- Carlo Ghezzi, Mehdi Jazayeri, and Dino Mandrioli. *Fundamentals of Software Engineering*. Prentice Hall, Upper Saddle River, NJ, USA, 2nd edition, 2003.
- Daniel M. Hoffman and Paul A. Strooper. *Software Design, Automated Testing, and Maintenance: A Practical Approach*. International Thomson Computer Press, New York, NY, USA, 1995. URL <http://citeseer.ist.psu.edu/428727.html>.