# Module Interface Specification for CFS

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November 24, 2018

# 1 Revision History

Date	Version	Notes
Nov 10, 2018	1.0	First draft by Malavika
Nov 21, 2018	1.1	Corrections based on presentation by Malavika
Nov 24, 2018	1.2	MIS submission draft by Malavika

# 2 Symbols, Abbreviations and Acronyms

See CA Documentation at  $\label{lower} {\tt Malavika-Srinivasan/CAS741/blob/master/docs/SRS/CA.pdf}$ 

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### 3 Introduction

The following document details the Module Interface Specifications for CFS(Curve Fitting Software). The goal of CFS is to find the parameters of the curve which is the best possible fit through the given set of 'n' data points, where  $n \ge 2$ .

Complementary documents include the Commonality Analysis and Module Guide. The full documentation and implementation can be found at the repository https://github.com/Malavika-Srinivasan/CAS741.

### 4 Notation

The structure of the MIS for modules comes from Hoffman and Strooper (1995), with the addition that template modules have been adapted from Ghezzi et al. (2003). The mathematical notation comes from Chapter 3 of Hoffman and Strooper (1995). For instance, the symbol := is used for a multiple assignment statement and conditional rules follow the form  $(c_1 \Rightarrow r_1|c_2 \Rightarrow r_2|...|c_n \Rightarrow r_n)$ .

The following table summarizes the primitive data types used by CFS.

Data Type	Notation	Description
character	char	a single symbol or digit
integer	$\mathbb{Z}$	a number without a fractional component in $(-\infty, \infty)$
natural number	N	a number without a fractional component in $[1, \infty)$
real	$\mathbb{R}$	any number in $(-\infty, \infty)$

The specification of CFS uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, CFS uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

## 5 Module Decomposition

[Needs to be changed in MG based on Dr.Smith's suggestion —Malavika] The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding Module	
Behaviour-Hiding Module	Input Output
Software Decision Module	Sequence Services Interpolation Regression Plot

Table 1: Module Hierarchy

## 6 MIS of Input module

This module corresponds to R1, R2 and R3 in the CA document. The secrets of this module are how the data points are input and how they are verified. The load and verify secrets are isolated to their own access programs.

### 6.1 Module

input

### 6.2 Uses

### 6.3 Syntax

Name	In	Out	Exceptions
loadInput	string	-	FileError
verifyInput	-	-	ValueError, TypeError
verifyDegree	-	-	ValueError

#### 6.3.1 Exported Constants

NA

### 6.3.2 Exported Access Programs

Name	In	Out	Exceptions
verifyDegi	ree	$\mathbb{N}$	ValueError

[I need the verifyInput as an exported access program because I will be verifying the degree input from regression module. —Malavika]

#### 6.4 Semantics

#### 6.4.1 State Variables

```
# From R1 in CA
```

 $t: \mathbb{R}^n$ 

 $y: \mathbb{R}^n$ 

degVerify: boolean

[This will say if the degree input to regression module has been verified or not —Malavika]

#### 6.4.2 Environment Variables

inputFile: sequence of string

### 6.4.3 Assumptions

- The loadInput will be called before the calling the verifyInput method.
- Regression module will be called before calling verifyDegree method.
- The loadInput will be called before the values of any state variables will be accessed.

#### 6.4.4 Access Routine Semantics

### input.t:

- transition: NA
- output: out := t
- exception: None

### input.y:

- transition: NA
- output: out := y
- exception: None

### input.degVerify:

- transition: NA
- output: out := degVerify
- exception: None

### loadInput(s):

- transition: inputFile is used to modify the state variables using the following procedural specification:
  - 1. Read data sequentially from inputFile to populate the state variables t and y.
  - 2. verifyInput()
- output: NA
- exception: exc := a file name s cannot be found OR the format of inputFile is incorrect  $\Rightarrow$  FileError.

## verifyInput():

• transition:NA

• output: NA

• exception: exc :=

Name	Exception
$( t  \le 1 \lor  y  \le 1)$	$\Rightarrow$ LengthError
( t   eq  y )	$\Rightarrow {\sf LengthMismatchError}$
$(\forall x \in t \land x \notin \mathbb{R})$	$\Rightarrow$ TypeError
$(\forall x \in y \land x \notin \mathbb{R})$	$\Rightarrow$ TypeError

### verifyDegree():

• transition:

$$- (deg > 0 \land deg \in \mathbb{N}) \Longrightarrow degVerify = True$$

• output:

 $\bullet$  exception: exc :=

Name	Exception
$(deg \le 0 \lor deg \notin \mathbb{N})$	$\Rightarrow$ ValueError

### 6.4.5 Local Functions

NA

# 7 MIS of Interpolation module

This module corresponds to R4, R5, R6, R7 and R9 in section 7.1 of CA document.

### 7.1 Module

interp

### 7.2 Uses

6, 9

### 7.3 Syntax

### 7.3.1 Exported Constants

NA

### 7.3.2 Exported Access Programs

Name	In	Out	Exceptions
interpMonomial	$t:\mathbb{R}^n,y:\mathbb{R}^n$	-	-
interp Lagrange	$t:\mathbb{R}^n,y:\mathbb{R}^n$	-	-
interpNewton	$t:\mathbb{R}^n,y:\mathbb{R}^n$	-	-
interpHermiteCubic	$t:\mathbb{R}^n,y:\mathbb{R}^n$	-	-
interpBSpline	$t:\mathbb{R}^n,y:\mathbb{R}^n$	-	-
evalMonomial	$t:\mathbb{R}^n,y:\mathbb{R}^n$	$y$ New: $\mathbb{R}^n$	-
evalLagrange	$t:\mathbb{R}^n,y:\mathbb{R}^n$	$y$ New: $\mathbb{R}^n$	-
evalNewton	$t:\mathbb{R}^n,y:\mathbb{R}^n$	$y$ New: $\mathbb{R}^n$	-
eval Hermite Cubic	$\mathbf{t}:\mathbb{R}^n,\mathbf{y}:\mathbb{R}^n$	$y$ New: $\mathbb{R}^n$	-
evalBSpline	$\mathbf{t}:\mathbb{R}^n,\mathbf{y}:\mathbb{R}^n$	$y$ New: $\mathbb{R}^n$	-

### 7.4 Semantics

#### 7.4.1 State Variables

- $x:\mathbb{R}^{n-1Xm}$ , Where m = degree of polynomial + 1 and n is the number of data points.
- interval: $\mathbb{R}^k$ , Where k is the number of sections

#### 7.4.2 Environment Variables

NA

### 7.4.3 Assumptions

- evalMonomial() will be called after interpMonomial().
- evalLagrange() will be called after interpLagrange().
- evalNewton() will be called after interpNewton().
- evalHermiteCubic() will be called after interpHermiteCubic.
- evalBSpline() will be called after interpBSpline().

#### 7.4.4 Access Routine Semantics

### interp.x:

- transition: NA
- output: out := x
- exception: None

### interpMonomial(t,y):

- transition:
  - 1. x:  $\mathbb{R}^{n-1Xm} = 0.0$ , this is initialization. This is necessary as all the methods will be using the same state variable.
    - 2. x:  $\mathbb{R}^{n-1Xm}$  obtained by solving for x using the equation below.

$$\begin{bmatrix} 1 & t_1 & t_1^2 & \dots & t_1^{n-1} \\ 1 & t_2 & t_2^2 & \dots & t_2^{n-1} \\ \vdots & \vdots & \vdots & \vdots \\ 1 & t_n & t_n^2 & \dots & t_n^{n-1} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

- interval:  $\mathbb{R}^k = t[0]$ , this is initialized to starting point for non piecewise functions.
- output: NA
- exception: NA

### evalMonomial(t,y):

• transition: NA

 $\bullet$  output: out := yNew

 $\forall t_i \in t$ , yNew.append(y1) where y1 is obtained as shown below.

$$y1 = x_1 + x_2t_i + x_3t_i^2 + x_4t_i^3 + \dots + x_nt_i^{n-1}$$

• exception: NA

### interpLagrange(t,y):

- transition:
  - 1. x:  $\mathbb{R}^{n-1Xm} = 0.0$ , this is initialization. This is necessary as all the methods will be using the same state variable.
    - 2. x:  $\mathbb{R}^{n-1Xm}$  obtained by solving for x using the equation below.

$$\begin{bmatrix} 1 & 0 & 0 & \dots & 0 \\ 0 & 1 & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

- interval:  $\mathbb{R}^k = t[0]$ , this is initialized to starting point for non piecewise functions.
- output: NA
- exception: NA

### evalLagrange(t,y):

- transition: NA
- output: out := yNew

 $\forall t_i \in t$ , yNew.append $(y_0)$  where  $y_0$  is obtained as shown below.

$$y_0 = y_1 l_1(t) + y_2 l_2(t) + \dots + y_n l_n(t).$$

where  $l_j(t)$  is given by,

$$l_{j}(t) = \frac{\prod_{k=1, k \neq j}^{n} (t - t_{k})}{\prod_{k=1, k \neq j}^{n} (t_{j} - t_{k})}$$

• exception: NA

### interpNewton(t,y):

- transition:
  - 1. x:  $\mathbb{R}^{n-1Xm} = 0.0$ , this is initialization. This is necessary as all the methods will be using the same state variable.
    - 2. x:  $\mathbb{R}^{n-1Xm}$  obtained by solving for x using the equation below.

$$\begin{bmatrix} \pi_0(t_0) & 0 & 0 & \dots & 0 \\ \pi_0(t_1) & \pi_1(t_1) & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & 0 \\ \pi_0(t_n) & \pi_1(t_n) & \pi_2(t_n) & \dots & \pi_n(t_n) \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

where,  $i < j \implies \pi_j(t) = 0, i \ge j \implies \pi(t) = \prod_{k=1}^{j-1} (t - t_k)$  When the limits make it vacuous, the product is taken to be 1. [work on vacuous —Malavika]

- interval:  $\mathbb{R}^k = t[0]$ , this is initialized to starting point for non piecewise functions.
- output: NA
- $\bullet$  exception: NA

### evalNewton(t,y):

- transition: NA
- output: out := yNew $\forall t_i \in t$ , yNew.append $(y_0)$  where  $y_0$  is obtained as shown below.

$$y_0 = x_1 + x_2(t - t_1) + x_3(t - t_1)(t - t_2) + ...x_n(t - t_1)(t - t_2)...(t - t_{n-1})$$

• exception: NA

### interpHermiteCubic(t,y):

• transition:

- 1. x:  $\mathbb{R}^{n-1Xm} = 0.0$ , this is initialization. This is necessary as all the methods will be using the same state variable.
  - 2. x:  $\mathbb{R}^{n-1Xm}$  obtained by solving for x using the equation below.

$$\begin{bmatrix} 1 & t_0 & t_0^2 & t_0^3 \\ \vdots & \vdots & \vdots & \vdots \\ 1 & t_n & t_n^2 & t_n^3 \\ 0 & 1 & 2t_0 & 3t_0^2 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 1 & 2t_n & 3t_n^2 \\ 0 & 0 & 2 & 6t_0 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 2 & 6t_n \\ 0 & 0 & 0 & 6 \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & 6 \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_1 \\ \vdots \\ \vdots \\ \vdots \\ x_n(m+1) \end{bmatrix} = \begin{bmatrix} y_0 \\ \vdots \\ y_0^{(1)} \\ y_1^{(1)} \\ \vdots \\ y_n^{(1)} \\ y_1^{(1)} \\ \vdots \\ \vdots \\ y_n^{(2)} \\ y_n^{(3)} \\ \vdots \\ y_n^{(3)} \end{bmatrix}$$

- interval:  $\mathbb{R}^k = t[0]$  to t[n-2], by default we make each point a breakpoint and hence there is a piecewise polynomial between  $[t_{i-1}, t_i)$ .
- output: NA.
- exception: NA

### evalHermiteCubic(t,y):

- transition:
- output: out := yNew $\forall t_i \in t$ , yNew.append $(y_0)$  where  $y_0$  is obtained as shown below.

$$y_0 = x_{k0} + x_{k1}t + x_{k2}t^2 + x_{k3}t^3$$
 for  $k = 0$  to  $n - 2$ 

• exception: NA

### interpBSpline(t,y):

- transition:
  - 1. x:  $\mathbb{R}^{n-1Xm} = 0.0$ , this is initialization. This is necessary as all the methods will be using the same state variable.

2. x: obtained by using the formula below. for k > 0.

$$x = v_i^k = \frac{t - t_i}{t_{i+k} - t_i}$$

[BSpline gives the v values which will be used recursively in formula defined in IM7 of the CA document —Malavika]

- interval:  $\mathbb{R}^k = t[0]$  to t[n-2], by default we make each point a breakpoint and hence there is a piecewise polynomial between  $[t_{i-1}, t_i)$ .
- output: NA
- exception: NA

### evalBSpline(t,y):

- transition:
- output: out := yNew $\forall t_i \in t$ , yNew.append $(y_0)$  where  $y_0$  is obtained as shown below.

$$y_0 = B_i^k(t) = v_i^k(t)B_i^{k-1}(t) + (1 - v_{i+1}^k(t))B_{i+1}^{k-1}(t)$$

for k > 0.

[I want the notation of 'B' so that it is easy to understand the coefficients, thats why I have  $y_0 = B...$ —Malavika]

• exception: NA

#### 7.4.5 Local Functions

NA

## 8 MIS of Regression module

This module corresponds to R4, R8 and R9 in section 7.1 of CA document.

### 8.1 Module

reg

### 8.2 Uses

6, 9

### 8.3 Syntax

### 8.3.1 Exported Constants

NA

### 8.3.2 Exported Access Programs

Name	In	Out	Exceptions
regNormalEq	$t:\mathbb{R}^n,y:\mathbb{R}^n, \text{ deg:}\mathbb{N}$	-	-
regAugSys	$t:\mathbb{R}^n,y:\mathbb{R}^n, \text{ deg:}\mathbb{N}$	-	-
${\rm regOrthogonalTn}$	$t:\mathbb{R}^n,y:\mathbb{R}^n, \text{ deg:}\mathbb{N}$	-	-
evalReg	$\mathrm{t}{:}\mathbb{R}^n$	yNew: $\mathbb{R}^n$	-

### 8.4 Semantics

#### 8.4.1 State Variables

• x:  $\mathbb{R}^m$ 

#### 8.4.2 Environment Variables

NA

### 8.4.3 Assumptions

- input.verifyDegree() will be called before any of the access programs will be used.
- evalReg() will be called after calling (regNormalEq()  $\vee$  regAugSys()  $\vee$  regOrthogonalTn()).

#### 8.4.4 Access Routine Semantics

reg.x:

• transition: NA

• output: out := x

• exception: None

### regNormalEq(t,y,deg):

• transition:

- degVerify = verifyDegree(deg)
- $(degVerify == True) \Longrightarrow x^n = 0.0$  [This is initialization with maximum length possible. For a data of length n, you can maximum get n coefficients in the polynomial. —Malavika]
- $-x^m = \mathbb{R}^m$ , obtained by solving for x in the equation below.[m is the degree of the coefficients of the polynomial. —Malavika]

$$A^T A x = A^T y$$

• output: NA

• exception: NA

### regAugSys(t,y,deg):

- transition:
  - degVerify = verifyDegree(deg)
  - $-(degVerify == True) \Longrightarrow x^n = 0.0$  [This is initialization with maximum length possible. For a data of length n, you can maximum get n coefficients in the polynomial. —Malavika]
  - $-x^m = \mathbb{R}^m$ , obtained by solving for x in the equation below.[m is the degree of the coefficients of the polynomial. —Malavika]

$$r + Ax = y$$

$$A^T r = 0$$

Where r is the residual vector.

• output: NA

• exception: NA

### $\mathbf{regOrthogonalTn}(t, y, deg)$ :

- transition:
  - degVerify = verifyDegree(deg)

- $-(degVerify == True) \Longrightarrow x^n = 0.0$  [This is initialization with maximum length possible. For a data of length n, you can maximum get n coefficients in the polynomial. —Malavika]
- $-x^m = \mathbb{R}^m$ , obtained by solving for x in the equation below.[m is the degree of the coefficients of the polynomial. —Malavika]

$$Ax = Py$$

Where P is the orthogonality matrix.

• output: NA

• exception: NA

### evalReg(t):

• transition: NA

• output: out := yNew, where  $\forall t_i \in t$ ,

 $ynew.append(np.poly1d(x)(t_i))$ 

• exception: NA

#### 8.4.5 Local Functions

NA

## 9 MIS of Output module

This module corresponds to R10 in the CA document. The secrets of this module are how the output is given to user program.

### 9.1 Module

output

#### 9.2 Uses

matplotlib(Python)

### 9.3 Syntax

Name	In	Out	Exceptions
plotDataFit	$t:\mathbb{R}^n,y:\mathbb{R}^n$		-
${\it coeffPlotScreen}$	$\mathbf{t}{:}\mathbb{R}^{n},\!\mathbf{y}{:}\mathbb{R}^{n},\!\mathbf{x}{:}\mathbb{R}^{m}$	$x:\mathbb{R}^m$ , plot	-
coeffFile	$\mathbf{x}$ : $\mathbb{R}^m$ , $\mathbf{t}$ : $\mathbb{R}^n$ , $\mathbf{y}$ : $\mathbb{R}^n$	$\mathbf{x}$ : $\mathbb{R}^m$	-

#### 9.3.1 Exported Constants

NA

### 9.3.2 Exported Access Programs

Name	In	Out	Exceptions
plotDataFit	$t:\mathbb{R}^n,y:\mathbb{R}^n$		-
${\it coeffPlotScreen}$	$\mathbf{t}{:}\mathbb{R}^{n},\!\mathbf{y}{:}\mathbb{R}^{n},\!\mathbf{x}{:}\mathbb{R}^{m}$	$x:\mathbb{R}^m$ , plot	-
coeffFile	$\mathbf{x}{:}\mathbb{R}^m,\!\mathbf{t}{:}\mathbb{R}^n,\!\mathbf{y}{:}\mathbb{R}^n$	$\mathbf{x}$ : $\mathbb{R}^m$	-

### 9.4 Semantics

#### 9.4.1 State Variables

NA

#### 9.4.2 Environment Variables

OutputFile: Results.csv

#### 9.4.3 Assumptions

• The interpolation or the regression module will be called before the output module.

#### 9.4.4 Access Routine Semantics

### plotDataFit(t,y):

- transition:
  - Call the appropriate evaluate method from the interpolation or regression module as shown below..
    - 1.  $yNew = \text{interp.evalMonomial}(t,y) \lor \text{interp.evalLagrange}(t,y) \lor \text{interp.evalNewton}(t,y) \lor \text{interp.evalHermiteCubic}(t,y) \lor \text{interp.evalBSpline}(t,y) \lor \text{reg.evalReg}(t)$

- 2. plot(t,y) and plot(t,yNew)
- $\bullet$  output: Out:= plot
- exception: NA

### coeffPlotScreen(t,y):

- transition :
  - plotDataFit(t,y)
- output: Out:=  $interp.x \lor reg.x$ , plot
- exception: NA

### coeffFile():

- transition:
  - Create a csv file named 'Result'
  - write interp.x  $\vee$  reg.x
- output: NA
- $\bullet$  exception: NA

### 9.4.5 Local Functions

NA

# References

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Daniel M. Hoffman and Paul A. Strooper. Software Design, Automated Testing, and Maintenance: A Practical Approach. International Thomson Computer Press, New York, NY, USA, 1995. URL http://citeseer.ist.psu.edu/428727.html.

# 10 Appendix

 $[{\bf Extra~information~if~required~-\!SS}]$