Learning Classifier Systems From Principles to Modern Systems

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Instructors

Anthony Stein is a tenure track professor at the University of Hohenheim, where he heads the Artificial Intelligence in Agricultural Engineering lab. He received his bachelor's degree (B.Sc.) in Business Information Systems from the University of Applied Sciences Augsburg in 2012. He then moved on to the University of Augsburg for his master's degree (M.Sc.) in computer science with a minor in information economics which he received in 2014. Since November 2019, he also holds a doctorate (Dr. rer. nat.) in computer science from the University of Augsburg. His research is concerned with the application of AI methodology and evolutionary machine learning algorithms to complex self-adaptive and self-organizing (SASO) systems. Dr. Stein is involved in the organization of workshops on intelligent systems and evolutionary machine learning. He serves as reviewer for international conferences and journals, including ACM GECCO or IEEE T-EVC.

Masaya Nakata is an associate professor at Faculty of Engineering, Yokohama National University, Japan. He received his Ph.D. degree in informatics from the University of Electro-Communications, Japan, in 2016. He has been working on Evolutionary Rule-based Machine Learning, Reinforcement Learning, Data mining, more specifically, Learning Classifier System. His contributions have been published as more than 10 journal papers and more than 20 conference papers, e.g., CEC, GECCO, PPSN. He was an organizing committee member of International Workshop on Learning Classifier Systems 2015-2016, 2018-2020 in GECCO conference





What this tutorial is NOT!

- ❖ A comprehensive introduction to the huge field of LCS
- A review of all existent applications of LCS
- ❖ A in-depth comparison of Michigan vs. Pittsburgh LCS
- A complete introduction to the theory behind LCS
 - → But, we indeed will have a first look ©

What this tutorial actually is

- An attempt to get the audience in touch with LCS
- ❖ An illustrative introduction to make the LCS concept graspable
- A `simplification' to gain an intuition about the overarching learning framework which LCS provide
- A starting point to further dive into the broad field around LCS
- Therefore it is explicitly noted that...
 - · we restrict ourselves to Michigan-style LCS
 - · we see abstracted views of particular technical details
 - · at the end corresponding references for a 'deeper dive' are given

Course Agenda

- Introduction
 - · A Brief Definition
 - · Why LCS?
 - · Looking Back: LCS History
- Michigan-style Learning Classifier Systems
 - · Building Blocks of LCS
 - · Putting it together: A generic LCS
 - · Bridging the Gap: Approaching XCS
- XCS Theory in a Nutshell
 - · An Overview of Formal Theory Behind LCS
 - · Learning Optimality Theory
- Modern Systems
 - · XCSF: Piece-wise Online Function Approximation
 - · ExSTraCS: Large-scale Supervised Classification
- Summary & Conclusions
 - · A Different Perspective
 - · Why LCS?
 - · Resources & Current Research



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A Brief Definition of Learning Classifier Systems

Learning Classifier Systems (LCS) comprise a family of <u>flexible</u>, <u>evolutionary</u>, <u>rule-based machine learning</u> systems which involve a unique tandem of <u>local</u> <u>learning</u> and <u>global evolutionary optimization</u> of the collective models' localities.

Flexible

- · Applicability: Have proven successful in a vast variety of domains
- · Extensibility: Define more a framework rather than a specific algorithm

Evolutionary

- Steady-state Niche Genetic Algorithm (GA) at their heart
- Neo-Darwinian Survival-of-the-Fittest Principle: Selection, Recombination, Mutation Operators

Rule-based

- Knowledge is represented via IF(condition)-THEN(action) rules (aka `classifiers')
- Divide-and-Conquer: Rules partition the problem space and solve it collectively

Machine Learning

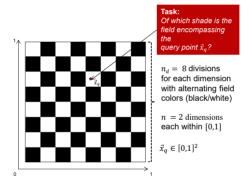
- Rules/Classifiers, i.e., their internal parameters are learnt via stochastic gradient-based algorithms (Widrow-Hoff delta rule, Recursive Least Squares (RLS), etc.)
- Capable of Reinforcement Learning (RL), Supervised Learning (SL) and Unsupervised Learning (UL) with only minor and straight-forward changes necessary
- Thus, applicable to Sequential Problems, Classification, Regression, Clustering

Why Learning Classifier Systems? (1/3)

- Interpretability by design
 - · Knowledge represented by IF-THEN rules
 - · Allows for explicit injection of expert knowledge
- Complexity reduction by design
- Online adaptivity to dynamic learning environments
- Inherent pressures toward generalization
- They are very cool ;-)
- Overarching framework
 - · Nearly any kind of ML algorithm can be integrated
- Comparative studies confirm competitive performance
- → Rich body of problem domain and application work in over 40 years of research!

Example Problem

Checkerboard Classification



Example Problem

Checkerboard Classification

Linearly separable?

→ e.g., Linear Model, Perceptron



Problem Space Partitioning → LCS!



Non-linearly separable?

→ e.g., Multi-layer Perceptron



Why Learning Classifier Systems? (2/3)

Investigated Problem Domains

- Adaptive Control (continuous and episodic)
- Uncertain Environments (Noise, Partial Observability)
- Dynamic Environments (Concept Drift/Shift)
- Data Imbalance
 - Class Imbalance
 - · Sparsity regarding payoff
- High Dimensionality / Scalability
 - · Exploration guidance via expert knowledge
 - · Transfer Learning approaches
 - · Dimensionality reduction via Autoencoders
- Complexity of underlying problem
 - · Heterogeneity, Epistasis
 - · Obliqueness, Curvature, Modality, etc.

Why Learning Classifier Systems? (3/3)

Fields of Real World Application

- Gas-Pipeline Control
- Autonomous Robotics
- Robotic Kinematics
- Motion Control
- Genetics
- Biomedical Knowledge Discovery
- Medical Diagnosis
- Cognitive Modeling
- Traffic Control
- Smart Camera Networks
- Games
- ... and many more!









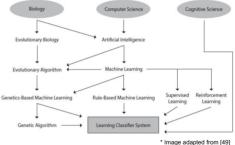






Looking Back: History of LCS*

- Learning Classifier System (LCS)
 - In retrospect, an odd name.
 - There are many machine learning systems that learn to classify but are not LCS algorithms.
 - E.g. Decision trees
- Also referred to as...
 - Rule-Based Machine Learning (RBML)
 - Genetics Based Machine Learning (GBML)
 - Adaptive Agents
 - Cognitive Systems
 - Production Systems
 - Classifier System (CS, CFS)



^{*} Adapted from Urbanowicz's previous tutorials

Looking Back: History of LCS*

1970's



- Genetic algorithms and CS-1 emerge
- Research flourishes, but application success is limited

1980's

- LCSs are one of the earliest artificial cognitive systems
 - developed by John Holland (1978) [14].
 - His work at the University of Michigan introduced and popularized the genetic algorithm.

1990's

- ❖ Holland's Vision: Cognitive System One (CS-1)
 - Fundamental concept of classifier rules and matching.
 - Combining a credit assignment scheme with rule discovery.
 - Function on environment with infrequent payoff/reward.

2000's

- The early work was ambitious and broad. This has led to many paths being taken to develop the concept over the following 40 years.
- CS-1 archetype would later become the basis for `Michigan-style' LCSs.

^{2010&#}x27;s

^{*} Adapted from Urbanowicz's previous tutorials

Looking Back: History of LCS*

1970's

 Pittsburgh-style algorithms introduced by Smith in Learning Systems One (LS-1) [35]

1980's



style

LCS subtypes appear: Michigan-style vs. Pittsburgh-

- Holland adds reinforcement learning to his system.
- Term `Learning Classifier System' adopted.
 Research follows Holland's vision with limited success.
- Interest in LCS begins to fade.

1990's

- Booker suggests niche-acting GA (in [M]) [5]
- Holland introduces bucket brigade credit assignment [15]

2000's

 Interest in LCS begins to fade due to inherent algorithm complexity and failure of systems to behave and perform reliably

2010's

^{*} Adapted from Urbanowicz's previous tutorials

Looking Back: History of LCS*

1970's

- Frey & Slate present an LCS with predictive accuracy fitness rather than payoff-based strength [11]
- Riolo introduces CFCS2, setting the scene for Q-learning like methods and anticipatory LCSs [34]
- Wilson introduces simplified LCS architecture with his Zeroth-level Classifier System (ZCS), a strength-based system [59]

1980's

REVOLUTION!

1990's →

Simplified LCS algorithm architecture with ZCS

- XCS is born: First reliable and more comprehensible LCS
- First classification and robotics applications (real-world)

2000's

- Wilson revolutionizes LCS algorithms with accuracy-based rule fitness in his XCS Classifier System (XCS) [60]
- * Holmes applies LCS to problems in epidemiology [16]

2010's

❖ Stolzmann introduces Anticipatory Classifier Systems (ACS) [44]

^{*} Adapted from Urbanowicz's previous tutorials

Looking Back: History of LCS*

1970's

- ❖ Wilson introduces XCS for function approximation (XCSF) [64]
- Kovacs explores a number of practical and theoretical LCS questions [21,22]

1980's

- Bernadó-Mansilla introduce sUpervised Classifier System (UCS) for supervised learning [4]
- * Bull explores LCS theory in simple systems [6]
- Bacardit introduces two Pitt-style LCS systems GAssist and BioHEL with emphasis on data mining and improved scalability to larger datasets [1,2]

1990's

- Holmes introduces EpiXCS for epidemiological learning. Paired with the first LCS graphical user interface to promote accessibility and ease of use [17]
- * Butz introduces first online learning visualization for function approximation
- Lanzi & Loiacono explore computed actions

2000's



- LCS algorithm specializing in supervised learning and data mining start appearing
- LCS scalability becomes a central research theme
- Increasing interest in epidemiological and bioinformatics
 - Facet-wise theory and applications

^{2010&#}x27;s

^{*} Adapted from Urbanowicz's previous tutorials

Looking Back: History of LCS*

1970's

Franco & Bacardit explored GPU parallelization of LCS for scalability.

Urbanowicz & Moore introduced statistical and visualization strategies for knowledge discovery in an LCS [53]. Also explored use of 'expert knowledge' to efficiently guide GA [55], introduced attribute tracking for explicitly characterizing heterogeneous patterns [54,57].

1980's

 Browne and Iqbal explore new concepts in reusing building blocks (i.e., code fragments). Solved the 135-bit multiplexer reusing building blocks from simpler multiplexer problems [19].

1990's

 Bacardit successfully applied BioHEL to large-scale bioinformatics problems also exploring visualization strategies for knowledge discovery [3].

 Urbanowicz introduced ExSTraCS for supervised learning [51,56]. Applied ExSTraCS to solve the 135-bit multiplexer directly.

2000's

- Increased interest in supervised learning applications persists.
- Emphasis on solution interpretability and knowledge discovery.
- Scalability improving 135-bit multiplexer solved!

2010's



GPU interest for computational parallelization.

Broadening research interest from American & European to include Australasian & Asian.

^{*} Adapted from Urbanowicz's previous tutorials

Looking Back: History of LCS*

1970's

1980's

1990's

2000's

2010's

~40 years of LCS research has...

- Clarified understanding.
- Produced algorithmic descriptions.
- ❖Determined 'sweet spots' for run parameters.
- Delivered understandable 'out of the box' code.
- ❖Demonstrated LCS algorithms to be...
 - Flexible
 - Widely applicable
 - Uniquely functional on particularly complex problems.

^{*} Adapted from Urbanowicz's previous tutorials

Course Agenda

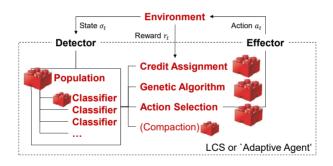
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Michigan-style Learning Classifier Systems

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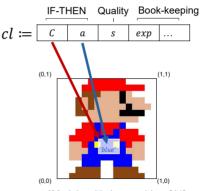
Building Blocks of a Learning Classifier System



BBs of LCS: Classifier

Classifier cl

- ❖ IF-THEN rule
 - Condition cl. C
 - Action cl. a
- ❖ Condition cl. C encodes input subspace $cl. C \subseteq X$
 - · Conditions of cl's are not disjoint!
- Rule strength cl. s, e.g.,
 - · Predicted Pavoff
 - · Prediction Accuracy
- . Book-keeping parameters
 - Experience
 - · Niche size
 - Numerosity
 - etc.



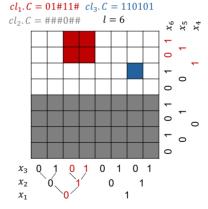
'Mario' multi-class problem [41]

 $^{^{\}ast}$ dot-notation denotes reference to parameters of specified classifier cl

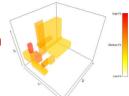
BBs of LCS: Classifier's Condition

Ternary Encoded Condition

- Encodes schema within problem's cl₂. C = ###0## input/state space
- ❖ For binary input spaces B^l
- One bit of input instance covered by one symbol in the condition
- Symbol from ternary alphabet Σ = {0.1, #}
 - "#" serves as don't care / wildcard
- Condition is concatenation of symbols
 - $C := (c_1, ..., c_l), c_i \in \{0, 1, \#\}$
- Condition also encodes chromosome for the GA
- Example Problems:
 - · k-Multiplexer, Majority-On, Parity, etc.

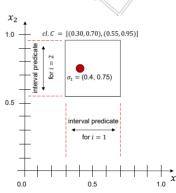


BBs of LCS: Classifier's Condition



Interval-based Condition

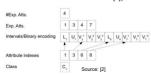
- Encodes subspace within problem's input/state space
- ❖ Real-valued input spaces R^d
- One dimension i = 1,..., d of an input instance is covered by one interval predicate in C
 - i-th interval predicate (l_i, u_i)
 - Lower bound l_i, upper bound u_i
 Ordered vs. unordered Bound
 - Orabiba to: anorabiba boan
- C is concatenation of intervals
 - $\bullet \qquad \mathcal{C} \coloneqq [(l_1,u_1),\ldots,(l_d,u_d)], l_i,u_i \in \mathbb{R}$
- Each bound is one gene in chromosome
- Example inputs:
 - Continuous values e.g., Traffic flows at intersections, Sensory data
- σ_t Nominal (gender, blood group) or ordinal features (age, salary, etc.)

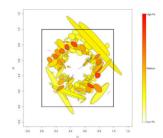


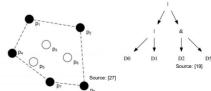
BBs of LCS: Classifier's Condition

Many more condition alphabets

- Hyperellipsoids (e.g., [9])
 - Covariance Matrix representationExplicit geometric representation
- ❖ S-expressions / Code Fragments [19]
- Convex Hulls 1271
- Mixed Discrete-Continuous Attribute List Knowledge Representation (ALKR) [2]
- Neural Networks [7], etc.







BBs of LCS: Classifier's Action

Discrete Actions

- Depends on the learning task
 - Reinforcement Learning: Action
 - Classification: Class/Endpoint Regression: No action needed!
- Examples:
 - Robot navigation: Turn left, right, up, down
 - Medical diagnosis: Tumor is benign or malignant

aprec

- Traffic light control: Signal plan A. B or C
- Large action spaces A
 - Each rule maintains a single action
 - Many rules needed for a complete mapping of the state-action-space
- Continuous Actions
 - Selection turns out difficult
 - But: Approaches do exist

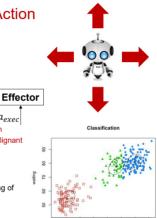


Fig. licensed according to CC BY-SA-NC

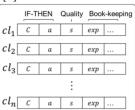
BBs of LCS: Population

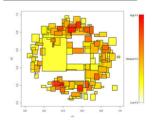
Population [P]

- * The set of all rules/classifiers
- Constitutes knowledge base
- ightharpoonup Entirety of $cl \in [P]$ collectively makes up the global model
- Contains many transient rules
- \diamond Contains n < N classifiers
 - N is a critical hyperparameter
 - Single classifier can subsume others
 → numerosity cl. num
 - Size of [P] is limited s.t.
 ∑_{cl∈[P]} cl. num ≤ N
- [P] usually starts 'tabula rasa'
- Can be initialized a priori
 - Randomly
 - · Expert Knowledge / Default rules



[P]





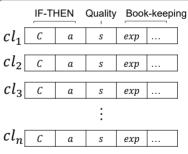


BBs of LCS: Population

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- Contains n < N classifiers</p>
 - N is a critical hyperparameter
 - Single classifier can subsume others
 → numerosity cl. num
 - Size of [P] is limited s.t. $\sum_{cl \in [P]} cl. num \le N$
- [P] usually starts `tabula rasa'
- Can be initialized a priori
 - Randomly
 - Expert Knowledge / Default rules

[*P*]



BBs of LCS: Compaction

Distillation of [P]

- Not necessary for learning success!
- Increases inference speed and comprehensibility of model
- Removes transient rules from [P]
 →Smaller collection of `predictive' rules
- Different approaches, e.g.,
 - · Condensation [60]
 - · Greedy compaction [9]
 - Quick Rule Filtering [47]
- Typically applied at the end of learning or after convergence
- ❖ Up to ~90 % smaller size of [P]
- But only marginal increase in prediction error











BBs of LCS: Action Selection

Action Selection

- The actual 'inference' step
- Chooses the action/prediction at each time step / for each situation
- Aka Policy π: S → A (from RL domain)
- More generally referred to as Performance Component
 - (1) Classifier Matching → determines niche!
 - (2) Classifier Mixing → collective solution!
 - (3) Action Selection
 - (4) Action Execution
- Handles Exploration vs. Exploitation trade-off, e.g.,
 - · Interleaving random/greedy selection
 - ε-greedy policy
 - Purely explore and exploit afterwards



* adapted from [39]

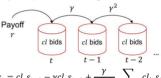


BBs of LCS: Credit Assignment

Credit Assignment

- Aka Reinforcement Component
- Learning comes into play
- Reward signal from environment
 - Immediate reward → may be 0
 - · Delayed payoff → goal reached, 1000
- Single-step vs. Multi-step
- Correct / Incorrect Action Selection
- Reward / Punish
- Problem: Long action sequences
- Which classifiers to reinforce / attenuate?
- Early `stage-setting' classifiers
- Adapts selected classifiers' learnable parameters, i.e., strength cl.s
- Updates book-keeping parameters

The early algorithm: (Implicit) Bucket Brigade [15,59]



$$cl.\,s_t = cl.\,s_{t-1} - \gamma cl.\,s_{t-1} + \frac{\gamma}{|[A]_t|} \sum_{cl_j \in [A]_t} cl_j.\,s_t$$

The modern approach: Temporal Difference Learning

$$\begin{array}{c} cl. \ s_t = cl. \ s_{t-1} + \beta (r_{t-1} + \gamma \max_{\underline{a}} \bar{s}_a - cl. \ s_{t-1}) \\ \\ \hline \text{Immediate reward} \ r_{t-1} + \\ \\ \text{current max. strength} \rightarrow \text{back-up} \end{array}$$

New estimate - old estimate → TD

^{*} Classifiers cl that were in [A] of the previous cycle are updated here!

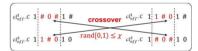


BBs of LCS: Genetic Algorithm

Genetic Algorithm

- Aka Discovery Component
- Steady-state Niche GA
- Periodic execution
- Optimizes coverage of the input space
- Usually, only conditions are altered
 - However, action mutation exists
- Fitness measure
 - · Strength cl.s in ZCS and older variants
 - Relative accuracy cl. κ' in XCS and descendants (XCSF, UCS, ExSTraCS)
- Hyperparameters
 - Mutation rate μ
 - Crossover probability γ
 - Selection mechanism (Roulette-wheel vs. Tournament)
 - GA activation threshold θ_{GA}

Ternary Case



^{*} adapted from [39]



BBs of LCS: Genetic Algorithm

Genetic Algorithm

- Still, steady-state niche GA
- Still, periodic execution
- Still, optimizes coverage of the input space
- Same fitness measure
- Additional hyperparameter
- Mutation spread m₀

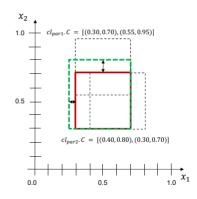
1st offspring after crossover:

$$cl_{off1}$$
. $C = [(0.30, 0.70), (0.30, 0.70)]$

1st offspring after mutation:

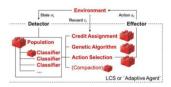
$$cl_{off1}$$
. $C = [(0.25, 0.70), (0.30, 0.80)]$

Real-valued case



Putting all together

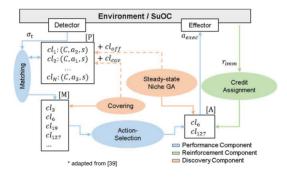
- De Co
- Building blocks are the most basic components of LCS
- Each block can have more than one `color'
- E.g., for credit assignment:
 - Bucket Brigade AlgorithmProfit Sharing Plan
 - Implicit Bucket Brigade
 - Q-Learning
 - Widrow-Hoff (single-step)
 - · Linear Least Square
 - · Recursive Least Square



- Select the most promising block for your problem and put it together
- ❖ → LCS provide a generic framework, not a single algorithm!

Putting all together: A Generic LCS



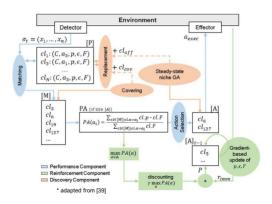


Bridging the Gap: Approaching XCS

- XCS Classifier System (XCS) [60]
- Due to Stewart W. Wilson
- * `Classifier fitness based on accuracy'
- Replaces strength cl.s with triplet
 - Predicted payoff cl. p
 - Prediction error cl. e
 - Fitness cl. F
- ❖ BBA credit assignment replaced with Q-learning-like update
- Applies niche instead of panmictic GA
 - first on [M] later on [A] instead of [P]
- Extension of the Zeroth-level Classifier System (ZCS) [59]

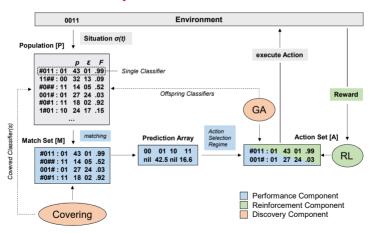
Michigan-style LCS

XCS Classifier System: Overview



Michigan-style LCS

XCS Classifier System: Overview

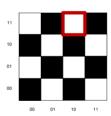


XCS Classifier System

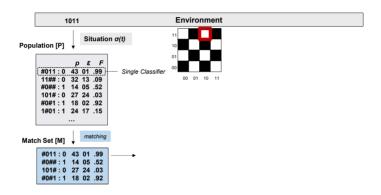
A quick main loop run-through

Discrete Checkerboard

- What is the situation $\sigma(t)$?
- The coordinates of the red boxed field (10,11)
- **Starting horizontally:** $\sigma(t)$ =1011
- ❖ What are the possible actions a∈A?
- `black' = 1
- ❖ `white' = 0
- What payoff can be retrieved?
- 1000 for correct action
- 0 for wrong action



Matching



Matching

- \diamond At each timestep t XCS retrieves a binary string on length n+m
- This string is denoted as $\sigma(t) \in \{0,1\}^{n+m}$
- ***** Example for discrete CBP (n=2, m=2 bits per dimension) and t=1: $\sigma(1)=1011$
- Each classifier maintains a condition C
- The conditions are encoded ternary, i.e. $C \in \{0,1,\#\}^{n+m}$
- The # symbol serves as wildcard or `don't care' operator
- Examples of conditions: (is matching $\sigma(1)$?)
 - 1#11
 - #011
 - 01#1

Matching is the process of scanning the entire population [P] for classifiers with a condition that is `fulfilled' by the situation $\sigma(t)$

Matching: A simple example

[P]	С	а	p	€	F
cl_1	01#	01	700	200	0.8
cl_2	111	00	990	110	0.9
cl_3	010	01	500	500	0.5
cl_4	##0	11	900	600	0.1
cl_5	1#1	10	300	500	0.4
cl_6	0#0	11	200	50	0.9
cl ₇	#10	01	500	400	0.7
	further i	non-ma	atching	classifi	ers

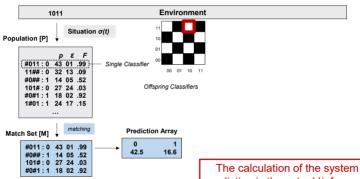
$\sigma_t = 010$	
Classifier Matching	

[M]	С	а	p	€	F
cl_1	01#	01	700	200	0.8
cl_3	010	01	500	500	0.5
cl ₄	##0	11	900	600	0.1
cl ₆	0#0	11	200	50	0.9
cl ₇	#10	01	500	400	0.7

 $t \rightarrow t+1$ Detector Environment

^{*} adapted from [39]

System Prediction



The calculation of the system prediction is the actual `inference' step! Here, the local models are combined (`mixed') into a collective target prediction!

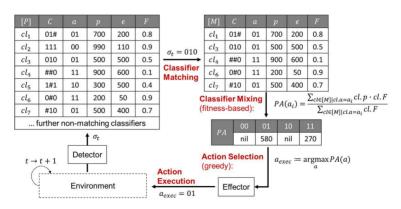
System Prediction

The system prediction P(a) is a fitness-weighted sum of predictions of all classifiers in [M] advocating action a

$$P(a) = \frac{\sum_{cl \in [M]|cl.a=a} cl. F * cl. p}{\sum_{cl \in [M]|cl.a=a} cl. F}$$

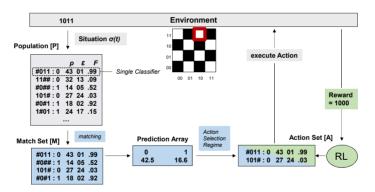
- Especially at this place, the separation of strength and accuracy becomes apparent!
- For each possible action $a \in A$ there exists one entry within the PA
- ❖ If a is not represented in [M], the PA entry is nil

System Prediction: A simple example



^{*} adapted from [39]

Credit Assignment



Credit Assignment

- $p_i \leftarrow p_i + \beta(P p_i)$

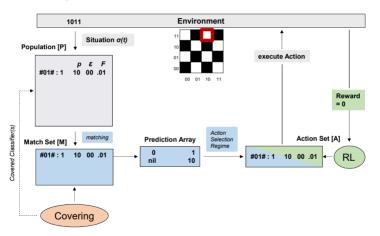
$$p_{j} \leftarrow p_{j} + \beta(P - p_{j})$$

$$\sum_{\ell, \ell_{0}} c. \text{(Butz et al.)}$$

$$F_{j} \leftarrow F_{j} + \beta(\kappa'_{j} - F_{j}), \ \kappa'_{j} = \frac{cl_{j} \kappa \cdot cl_{j} \cdot num}{\sum_{cl_{\ell} \in [A]} cl_{i} \kappa \cdot cl_{i} \cdot num}, \ \kappa_{j} = \alpha \left(\frac{\epsilon_{j}}{\epsilon_{0}}\right)^{-v}$$

- β is the learning rate (typically set to 0.2)
- α (often set to 0.1) and ν (usually set to 5) control how strong accuracy decreases when error is higher than ϵ_0
- ϵ_0 defines the targeted error level of the system
- In single-step problems, P is set to the immediate reward r_{imm}
- Classifier parameters are updated by means of the Widrow-Hoff (or delta) rule in combination with the moyenne adaptiv modifiée (MAM) technique

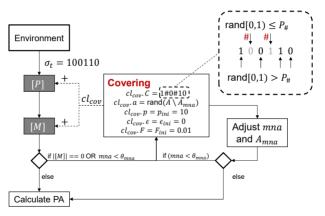
Covering



Covering

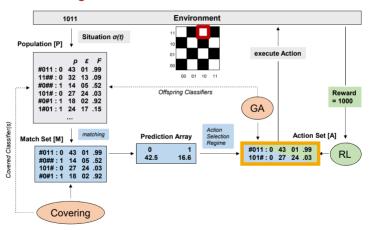
- Covering is the process of generating at least one novel classifier that matches the current input σ(t) whenever:
 - Match set [M] is empty (i.e. no matching cl in [P])
 - [M] is poor, i.e. average fitness below a certain threshold
 - [M] contains less then θ_{mna} distinct actions
- The condition of the covered classifier cl_{cov} is initially set to the current input
- Additionally, each bit is replaced by a # (for generalization purposes) with probability P_#
- The action is selected equiprobably between actions not present in [M]
- ❖ Values for p, ∈ and F are set to predefined initial values (typically 10.0, 0.0 and 0.01, respectively)

Covering



* adapted from [39]

Genetic Algorithm



Genetic Algorithm: Invocation and Selection

- One of the most essential parts of XCS is the incorporated steadystate niche GA (steady-state: only a small fraction of the population is replaced)
- It is triggered when the average time over all classifiers in [A] since the last GA invocation is greater than θ_{GA} (often set to 12)

•
$$t - \bar{ts} > \theta_{GA}$$
, where $\bar{ts} = \frac{\sum_{cl \in [A]} cl.ts}{|[A]|}$

- The GA selects two parents from [A] with a probability proportional to their fitness values (roulette-wheel selection)
 - · The higher a classifier's fitness, the higher the selection chance
- The selected parents are copied to generate two offspring classifiers cl¹_{off}, cl²_{off}

Genetic Algorithm: Crossover and Mutation

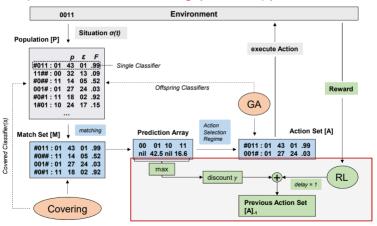
- * The conditions of both cl_{off} are crossed with probability $\chi=0.8$ (crossover operator)
 - One-point crossover: Each offspring classifier's condition is split at a certain point and switched with the other offspring classifier
 - · n-point crossover: more than one point is determined for switching
 - · Uniform crossover: Each value is switched with a certain probability (often 0.5)

$$cl_{off}^{c}, c \ 1 \ \# \ 0 \ \# \ 1 \ \# \quad \text{crossover} \quad cl_{off}^{c}, c \ 1 \ 1 \ \# \ 0 \ 1 \ \#$$

$$cl_{off}^{c}, c \ 1 \ 1 \ \# \ 0 \ 1 \ 0 \quad \text{rand} \ [0,1) \le \chi \quad cl_{off}^{c}, c \ 1 \ \# \ 0 \ \# \ 1 \ 0$$

- Afterward, each bit is flipped with probability μ = 0.04 to one of the other allowed alleles (mutation operator)
 - E.g. 2nd bit is set to `1', mutation can flip this bit to `0' or `#'

Sequential Problem Solving (Multi-step)



Sequential Problem Solving (Multi-step)

- * r may or may not be retrieved in each step
- One has to distinguish immediate reward (r^{imm}) and total reward or payoff r at the end of a task (e.g. finally food was found)
- ❖ Update of classifier attributes is performed on the action set of the previous timestep t − 1 ([A]₋₁)
- The maximum system prediction P(a) from the current PA is discounted by a factor γ (usually $\gamma = 0.95$)
- Additionally, the immediate reward gained for performing the action in the previous state (of time step t - 1) r_{t=1}^{imm} is added (may be 0)
- This delay allows to retrieve "information from the future"
- In single-step environments $P = r^{imm}$
- In multi-step problems $P = r_{t-1}^{imm} + \gamma * \max PA(a)$

Sequential Problem Solving (Multi-step)

Single-step update of p:

$$p_j \leftarrow p_j + \beta (P - p_j)$$

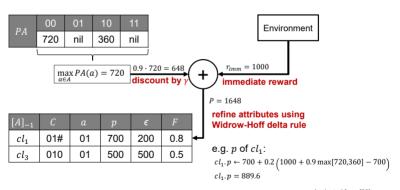
- Substituting P yields us the multi-step update formula
- Multi-step update of p:

$$p_j \leftarrow p_j + \beta (r_{t-1}^{imm} + \gamma \max_a PA(a) - p_j)$$

Do you know this update procedure from anywhere else?

$$Q(s,a) \leftarrow Q(s,a) + \alpha [r + \gamma \max_{a} Q(s',a) - Q(s,a)]$$

Multi-step Credit Assignment: A sample calculation

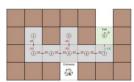


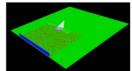
* adapted from [39]

Sequential Problem Solving (Multi-step)

Examples for multi-step environments:

- Animat scenarios:
 - · Agent is seeking food / gold / exit / etc.
 - · E.g., Woods or Maze scenarios
- Step-wise adjustment of a control variable:
 - · Pan, Tilt, Zoom in Smart Camera Networks
 - Mountain Car
 - Inverse Pendulum
- Movement decisions:
 - · `Move to beacon' minigame in StarCraft II LE







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 - √ Why LCS?
 - √ Looking Back: LCS History
- Michigan-style Learning Classifier Systems
 - ✓ Building Blocks of LCS
 - ✓ Putting it together: A generic LCS
 - ✓ Bridging the Gap: Approaching XCS
- * XCS Theory in a Nutshell (presented by Dr. Nakata)
 - · An Overview of Formal Theory Behind LCS
 - · Learning Optimality Theory
- Modern Systems
 - · XCSF: Piece-wise Online Function Approximation
 - · ExSTraCS: Large-scale Supervised Classification
- Summary & Conclusions
 - · A Different Perspective
 - · Why LCS?
 - Resources & Current Research



Much formal work already done!

One disadvantage of LCS often mentioned is...

"[...] less formal understanding and a relatively small body of theoretical work [...]"

- We should put emphasis on "relatively"
- Sometimes experienced misconception that...



This is not true!

An Overview of Formal Theory Behind LCS

Facetwise Theory

- Evolutionary Pressures (Butz et al.)
- Solution growth, sustenance
- · Effective search

Hyperparameter derivation

- Parameter bounds (Butz, Stalph)
- Optimal parameters (Nakata et al.)

Hypotheses

- Generalization Hypothesis (Wilson)
- · Optimality Hypothesis (Kovacs)
- * Theory on Strong Overgenerals (Kovacs)

GA analysis in XCS

- Markov-chain analysis (Bull, Butz)
- Selection pressure (Butz, Orriols-Puig)
- Selection probability (Kovacs et al.)

Convergence and time bounds ❖ PAC learnability of k-DNF (Butz)

- . Domino convergence model (Butz et al.)
- Convergence proofs under simplifications (Drugowitsch, Wada)

Learning problem analysis

- . Imbalanced domains (Orriols-Puig et al.)
- Complexity of classification problems (Bernadó-Mansilla et al.)

Formalizations (models)

XCS Theory

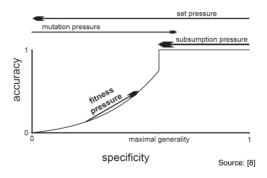
- Simple LCSs (Goldberg, Bull)
- Probabilistic model (Drugowitsch & Barry)

*see [33] for a brief survey

Facetwise Approach

- Facetwise Theory Approach (due to Goldberg [13])
 - · Proposed to analyze and understand GAs
 - Partitioning of a system into its most relevant components
 - · Analysis in separation
 - Afterward, combine and investigate interactions
 - Answer questions: What?, How? and When?
- Facetwise LCS Theory (due to Butz et al. [8,10])
 - I. Design evolutionary pressures most effectively
 - Fitness guidance, parameter estimation, generalization
 - II. Ensure solution growth and sustenance
 - Population initialization, schema supply, growth and sustenance
 - III. Enable effective solution search
 - Mutation, recombination, local vs. global structure
 - IV. Consider additional challenges in multi-step problems
 - Effective policy, problem sampling, reward propagation

Evolutionary Pressures (or `How it learns?')



Learning Bounds (or `When it learns?')

- Main challenges (schema and covering)
 - · Covering Challenge
 - Ensure coverage and GA application
 - Prevent being trapped in a covering-deletion-cycle
 - · Schema Challenge
 - Ensure that fitness pressure applies
 - From both directions: over-general and over-specific classifiers



Derived bounds:

- Covering bound
- Schema bound
- Reproductive opportunity bound
- Niche support bound
- Learning time bound

$$\frac{-\log(1 - P(cov.))}{-\log\left(1 - \left(\frac{2 - \sigma[P]}{2}\right)^{l}\right)} < N$$

Covering bound, cf. [10]

❖ PAC-learnability of k-DNF problem confirmed for XCS with those bounds!

Optimality Theory on XCS

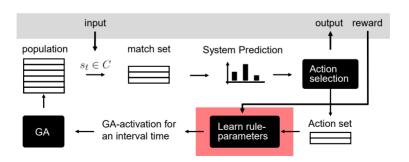
Motivation

- Latest theoretical studies (Very few)
 - · Shift to provide practical insights from hypothetical insights
 - Remove impractical assumptions
 - o E.g. infinite iteration, Wilson's generalization hypothesis
 - Capture the optimality of the XCS framework to maximize the performance
 - · Theoretical analysis for the "whole" behavior of XCS
 - How rule-learning affect rule-evolution?
 - Is there any "sweet spot" to achieve both the optimality of rule-learning and evolution?
 - A lot of things that we should reveal a complexity of evolutionary rule-based learning
- Which optimality we have known so far?
 - Optimality on Rule-learning (theoretically-validated) [31, 69]
 - · Optimality on Rule-evolution (hypothetical) [30]
 - · Dilemma between Rule-learning and Rule-evolution (theoretically-validated) [68]

Optimality Theory on XCS

Optimality on Rule-learning

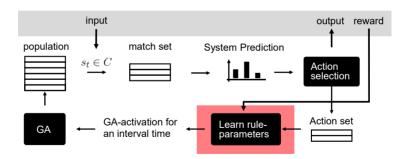
- Learning capacity: To estimate the true-worth of rules
 - · On classification tasks: confirmed [31, 69]
 - XCS Learning Theory enables XCS to identify accurate rules in as few training instances as possible



Optimality Theory on XCS

Optimality on Rule-evolution

- Search capacity: To generate accurate rules
 - · Non-deterministic, so hard to describe the optimality
 - Can we still say deterministic optimality to search capacity?



Overview

- Unconfirmed main capacities of XCS
 - To generate accurate rules
 - To estimate the true-worth of rules ← focus
- Learning optimality theory [31, 69]
 - Optimality: theoretically guarantee that XCS correctly distinguish accurate rules from inaccurate rules with the minimum training
 - . Benefit1: guideline to set the optimum parameter values of the XCS learning parameters
 - Benefit2: you can get optimality on your LCS if your LCS employs the same learning scheme as in XCS
 - Restriction: applicable only to classification problems with binary reward scheme (so far)

Optimality on Rule-learning Brief description 1/4

- Easy step to get optimality on the XCS learning scheme 1/3
- Definition
 - · A classification task with binary reward scheme
 - Correct class: a positive reward rmax
 - Incorrect class: a negative reward Tmin
 - · Accurate rules boundary:
 - Accurate rules: 100% classification accuracy $P_C^* = 1.0$
 - Inaccurate rules: < 100% classification accuracy $\ P_C{}' < P_C{}^*$
 - In fact, we can control the quality of inaccurate rule with $P_{C_{\max}}'$
 - Set^PC'_{max} to a user's defined value
 - Accurate rules (redefined): having PC'_{max} % 100% classification accuracy
 - Inaccurate rules: having <= P_C % classification accuracy

Brief description 2/4

- Easy step to get optimality on the XCS learning scheme 1/3
- Goal
 - · Guarantee to identify reliably accurate rules correctly
 - Is there any solutions of θ_{sub} , ϵ_0 to satisfy our conditions?

$$n > \theta_{sub}, \underline{\epsilon_n} < \epsilon_0 \implies n^*, \underline{n'} > \theta_{sub}, \epsilon_{n^*} < \underline{\epsilon_{n'}}$$

· We will answer the following questions

 $heta_{sub}$: How many times should a rule be updated to be considered for accurate?

 β : How much rate is adequate to update rules?

 ϵ_0 : How small a prediction error accurate rules must have?

Brief description 3/4

- Easy step to get optimality on the XCS learning scheme 1/2
- Step 1
 - Define the quality of accurate rules with ${P_C}'_{\max}$
- Step 2
 - · Calculate the minimum learning iteration given by

$$\theta_{sub} = \min\{n \in \mathbb{N} \mid 1/(1 - P_{C_{\max}}') \le n\} - 1.$$

- Step 3
 - Find solution β (leaning rate) of the boundary condition by Newton's method:

$$\max \hat{\epsilon}_{\theta_{sub}}(P_{C}^{*}) = \min \hat{\epsilon}_{\theta_{sub}}(P_{C}').$$

$$\max \hat{\epsilon}_{n^{*}}(P_{C}^{*}) = r_{\max}(1-\beta)^{n^{*}} + r_{\max}n^{*}\beta(1-\beta)^{n^{*}-1}.$$

$$\min \hat{\epsilon}_{n'}(P_{C}') = 2r_{\max}(P_{C_{\max}}' - P_{C_{\max}'}^{'2}) \left| 1 - (1-\beta)^{n'} \right| - r_{\max}n'\beta(1-\beta)^{n'-1}(1-2P_{C_{\infty}}')(P_{C_{\max}}' - P_{C_{\infty}'}')$$

Brief description 4/4

- Easy step to get optimality on the XCS learning scheme 2/2
- Step 4
 - Set error tolerance ϵ_0 with the solution β as:

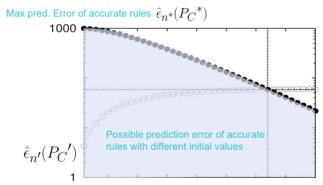
$$\epsilon_0 = \max \hat{\epsilon}_{\theta_{sub}}(P_C^*)$$

- That's all
 - Determined θ_{sub} β ϵ_0 are their optimum values to achieve the optimality on the XCS learning scheme

You can download an open source "theoretically-optimized XCS" at

http://www.nkt.ynu.ac.jp/en/download/

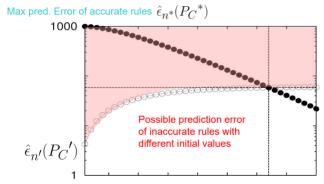
Graphical conclusion 1/3



Min Pred. Error of inaccurate rules

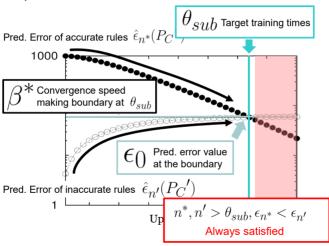
Update time

Graphical conclusion 2/3



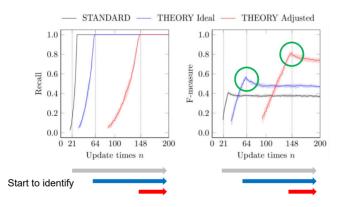
Min Pred. Error of inaccurate rules Update time

Graphical conclusion 3/3



Optimality on Rule-learning Impact 1/3

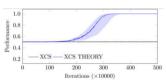
 The optimal parameter settings successfully captures the maximum Fmeasure score

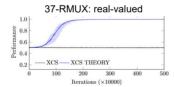


Impact 2/3

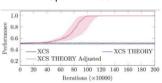
Benchmarks

135-MUX: 4.4 E+40 possible inputs 2.6 E+64 possible rules

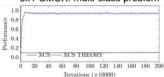




37-MUX: Noisy problem
Optimum = 90% cla. acc.

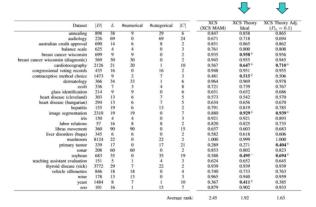






Impact 3/3

Real-world data classification

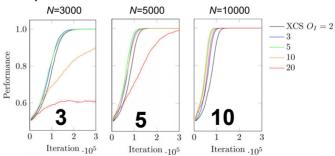


Motivation

- Unconfirmed main capacities of XCS
 - To generate accurate rules ← focus
 - · To identify accurate rules
- Optimality on Rule-evolution
 - · Hard to guarantee that XCS evolutionary generates accurate rules
 - · Instead, we here consider the maximize a probability to generate accurate rules
 - How?
- Optimality hypothesis [30]
 - . XCS employs a steady-state GA: generates ONLY two offspring rules for each generation
 - · Very inefficient

Difficulty

- Difficulty to determine the optimal number of generated offspring
 - The problematic cover-delete cycle occurs when increasing the number of generated offspring
- How can XCS safely increase offspring while preventing the coverdelete cycle?



Optimality hypothesis

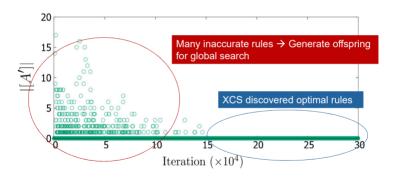
- Optimality hypothesis [30]
 - · XCS employs a steady-state GA: generates ONLY two offspring rules for each generation
 - · Hypothesis:
 - A probability to generate accurate rules can be maximized when maximizing the number of offspring rules. Then, the maximum number of offspring rules can be equal to the number of inaccurate rules exist in the current population."
- This suggests the optimal number of generated offspring can be dynamically changed and it is corresponding to the number of inaccurate rules existed in the population
- How to safely increase the number of generated solutions?
- ♦ How to safely delete unnecessary rules

Algorithm

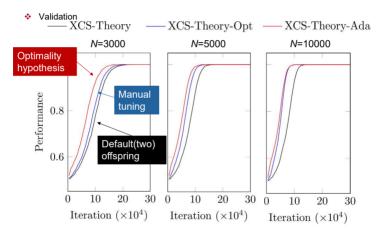
- Very easy to implement this optimality hypothesis
- Step 1
 - · Calculate and set the optimal parameter setting derived from the learning optimality theory
- Step 2
 - · Identify the inaccurate rules with the XCS learning scheme
- Step 3
 - · Replace inaccurate rules with newly-generated offspring rules
- That's all

Self-adaptation

Optimality hypothesis works as self-adaption of the number of offspring



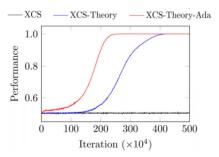
Impact 1/2



Optimality on Rule-evolution Impact 2/2

Impact of Optimality hypothesis

135-MUX: 4.4 E+40 possible inputs 2.6 E+64 possible rules



Optimality Theory on XCS

Summary

- Seeking of the optimality of the XCS framework
 - Optimality on Rule-learning:
 - Partially done in 2017 & 2020 (for classification problems)
 - Not yet for multiple reward scheme and for reinforcement learning task
 - Provides a reasonable guideline to set the XCS learning parameters
 - Easy to use (Get optimality in your XCS-based systems)
 - Theoretically-reliable extensions, e.g. self-adaptation of learning parameters [70]
 - Optimality on Rule-evolution:
 - Yet restricted in hypothetical insight
 - Hypothetical insight still work

Join us

- Theoretical works gradually get attention....
 - Potential to drastically improve the LCS performance
 - I.e. bottom-up of evolutionary symbolic approach like LCS
 - One of the "well theoretically-studied" evolutionary machine learning variants
- A lot of things that we should reveal
 - For multi-step problems
 - Wilson's generalization hypothesis...

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❖ Modern Systems

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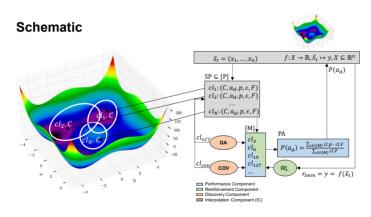
XCSF: Piece-wise Online Function Approximation

- XCS for function approximation introduced by Wilson in 2002 [64]
 - Supervised learning \rightarrow Actions become obsolete; only dummy action a_d
 - Online learning → Adapt model instance per instance
 - Local learning → Classifiers partition the input space; divide-and-conquer
 - Evolutionary Learning → Steady-state niche GA optimizes input space coverage

Alternative view: Evolutionary Ensemble Learner

- XCS' algorithmic structure as a general online ensemble learning framework
- · Classifiers as members of that ensemble
- · No Boosting, no Bagging, more like Stacking
- · Allows hybrid ensemble (cf. [26])

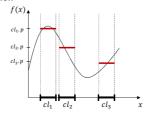
XCSF: Piece-wise Online Function Approximation

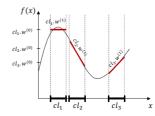


XCSF: Innovations to preceding XCS(R) (1/2)

- Development of Classifier Prediction
 - 90's: Wilson introduced ZCS and XCS as reinforcement learning algorithms
 - ❖ Classifiers cl advocate specific action cl. $a \in A$ for certain subset of states $\{\vec{x}_i\} \subseteq X$
 - ◆ Prediction attribute cl.p was defined to estimate the expected reward E[r|x,a].
 - 2000: XCS recognized to be well applicable to supervised learning tasks (classification).
 - since 2001: Not surprisingly, it was then also used to approximate functions (regression).
 - Prediction cl. p was used as XCS' output
 - ❖ Eventually, modeled as function $f(x) = \vec{w}^T \vec{x} + w_0$ of the current input $\vec{x} \in X$

Intuition





XCSF: Innovations to preceding XCSR (2/2)

❖ Competent update procedures (cf. Lanzi et al. [24])

- · Linear Least Square
- Kalman Filter
- · Gain Adaptation
- · Recursive Least Square

Various predictors

- · Polynomial approximation [25]
- Evolution Strategy [48]
- Neural Network [23]
- Support Vector Regression [29]
- RBF-Interpolation [42]

Guided Mutation (37)

- · Inspired by Covariance Matrix Adaptation
- · Store weights for matching samples
- Assign weight < 1 for instances with high error (and vice versa)
- Guide mutation towards positively weighted instances



Source: Gradient descent, Wikinedia



Source: [37]

XCSF: Applications

Robot Kinematics

- · Filtering of sensory information [20]
- · Locally linear forward kinematics [38]



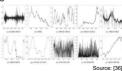
Continuous action spaces [63]

- · Hierarchical XCSF architectures
- · e.g., Continuous Actor-Critic approach



Stacking Approach for Ensemble Forecasting [36]

- · Use of hybrid forecasting techniques (ARIMA, Exp. Smooting, etc.)
- · Locally learning the weights for combination of those
- · Applied to different time series

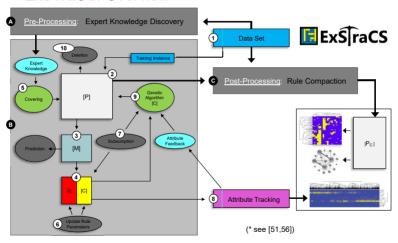




ExSTraCS: Large-scale Supervised Classification

- First introduced by Urbanowicz and Moore in 2014 [56]
- Conceived to tackle large-scale, complex classification problems
- Equipped with mechanisms for post-hoc Knowledge Discovery
- Proved very successful in large multiplexer problems (135-bit!)
- Focus on LCS scalability in terms of:
 - · Increasing number of training instances (big data)
 - Increase in problem dimensionality (relevant features)
 - · Increase in total number of features (curse of dimensionality)
- Open Source project (Python): https://github.com/ryanurbs/ExSTraCS 2.0
- Visit hands-on session at IWLCS@GECCO!

ExSTraCS: Overview



^{*} Adapted from Urbanowicz's previous tutorials



ExSTraCS: Adaptive Data Management (ADM)

- Automatically calculate training data statistics:
 - · Number of attributes
 - Number of instances
 - · Location of endpoint (class)
- ♣ Automatic shuffling to prevent bias
 Determines data characteristics:

 Location of categorical attributes
 Location of continuous attributes
 Determines min and max ranges

 Automatic shuffling to prevent bias

 #Exp. Alts.
 I 3 4 7
 I 3 4 7
 I 3 6 8
 I 3 6 8
 I 3 6 8
 - · Counts distinct values for each attribute within the training data
- Automatic selection of Rule-Specificity limit (RSL)

<u>Pre-Processing</u>: Expert Knowledge Discovery

ExSTraCS: Using Expert Knowledge (EK)

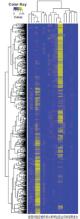


- Expert provides weights to the features/attributes
- Weights determine `predictive value'
- Weights guide covering mechanism and GA
- Weights can be provided manually by expert user, or...
- ... automatically by utilizing Relief-based attribute weighting
 - · RelieF, SURF, SURF*, MultiSURF
 - New to ExSTraCS 2.0 → Tuned-RelieF (TuRF)
- Introduces sort of automated feature selection
- But: without actual removal for knowledge discovery purposes!

Attribute Feedback 8 Attribute Tracking

ExSTraCS: Attribute Tracking und Feedback (AT&F)

- An extension to the LCS algorithm that allows for the explicit characterization of heterogeneity, and allows for the identification of heterogeneous subject groups.
- Akin to long-term memory. Experiential knowledge stored separately from the rule population that is never lost.
- Relies on learning that is both incremental and supervised.
- Stored knowledge may be fed back into LCS during learning.



^{*} see [54,57] for more details

^{*} Adapted from Urbanowicz's previous tutorials

Post-Processing: Rule Compaction

ExSTraCS: Knowledge Discovery from Output

- Outputs up to 5 distinct output files
 - a) Final population of learned rules
 - b) Population metrics (train/test accuracy, etc.)
 - c) Attribute co-occurrence in final rules
 - d) Attribute tracking scores per instance
 - e) Summary of predictions for testing data, including votes (for further use)



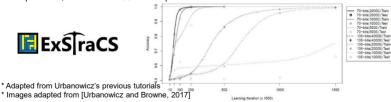
Facilitate algorithm transparency and interpretability!



ExSTraCS: Solving the 135-Multiplexer

æ	Address Bits	Order of Interaction	Heterogeneous Combinations	Unique Instances	Optimal Rules [O]
6-bit	2	3	4	64	8
11-bit	3	4	8	2048	16
20-bit	4	5	16	1.05×10^{6}	32
37-bit	5	6	32	1.37×10^{11}	64
70-bit	6	7	64	1.18×10^{21}	128
135-bit	7	8	128	4.36×10^{40}	256

- TO SOLVE: 135-bit Multiplexer
 - · All 135 features are predictive in at least some subset of the dataset.
 - Non-RBML approaches would need to include all 135 attributes together in a single model properly
 capturing underlying epistasis and heterogeneity.
- Few ML algorithms can make the claim that they can solve even the 6 or 11-bit multiplexer problems, let alone the 135-bit multiplexer.



Course Agenda

- Introduction
 - ✓ A Brief Definition
 - ✓ Why LCS?
 - √ Looking Back: LCS History
- Michigan-style Learning Classifier Systems
 - ✓ Building Blocks of LCS
 - ✓ Putting it together: A generic LCS
 - ✓ Bridging the Gap: Approaching XCS
- * XCS Theory in a Nutshell
 - ✓ An Overview of Formal Theory Behind LCS
 - ✓ Learning Optimality Theory
- Modern Systems
 - ✓ XCSF: Piece-wise Online Function Approximation
 - ✓ ExSTraCS: Large-scale Supervised Classification

Summary & Conclusions

- · A Different Perspective
- · Why LCS?
- Resources & Current Research



Summary & Conclusions

A Different (ML-centric) Perspective on LCS

- * Reconsider M-style LCS as an online ensemble learner
- Rules = ensemble members
- Each rule constitutes a local model / hypothesis
- ❖ Rules are experts of different problem niches → mixture of experts
- ❖ `Goodness' of each `expert' determined instance-by-instance without necessity to remember → one-pass (online) learning
- ❖ Modularity (recall building block intuition) allows for stacking
 - Different models for local prediction (ANN, RBF, polynomials) and fitness-weighted combination = stacked generalization
- Learning <u>Classifier</u> System not only about classification (alone)
 - XCSF: Function Approximation = Regression
 - XCS(R): Sequential Decision Making = Reinforcement Learning
 - XCSC: Clustering = Unsupervised Learning
- ❖ XCSF → similarities to Locally Weighted Projection Regression
- ❖ XCS(R) → generalizing Q-learner

Summary & Conclusions

So, again: Why LCS? (ex post)

- Flexibility (RL, SL) and modularity (building blocks)
- Interpretability by design (condition-action rules)
- Follow divide and conquer principle (mixture of experts)
- Capture complex associations (epistasis, heterogeneity)
- Evolution as central component allows adaptation to change (concept drift)
- Overarching framework for general ML techniques
 - · LCS and Deep Learning do not mutually exclude!
 - · E.g., put DNNs to locally model a policy
- And (again) finally...
 - · they are simply cool ;-)

Summary & Conclusions

Recent Research Directions (excerpt)

- Visual and statistical knowledge discovery from LCS rule sets (Urbanowicz et al. [57])
- Theoretical hyperparameter derivation (Nakata et al. [30,31])
- ❖ Hierarchical LCS and multi-domain learning (Liu, Browne, Xue [28])
- ❖ Absumption for Classifier Specialization (Liu, Browne, Xue [65])
- Lexicase Selection for Supervised LCS (Aenugu and Spector [67])
- LCS with active learning (Stein et al. [41])
- ❖ Experience Replay & Interpolation in XCS (Stein et al. [66,40,42,43])
- ❖ Algebraic formalization of LCS (Pätzel and Hähner [32])
- **...**
- ♦ nearly all of them regularly attend GECCO!

Thanks!

You feel triggered and want to learn for more?

Don't miss the annual
International Workshop on
Learning Classifier Systems (IWLCS)
at GECCO

Acknowledgements

Thanks to Ryan J. Urbanowicz for the permission to reuse parts of his previous tutorials on LCS.

Resources

- Additional Information:
 - Keep up to date with the latest LCS research
 - · Get in contact with an LCS researcher
 - Contribute to the LCS community research and discussions.
- GBML Central http://gbml.org/
- LCS Researcher Webpages:
 - Bacardit, Jaume http://homepages.cs.ncl.ac.uk/jaume.bacardit/
 - Browne, Will http://ecs.victoria.ac.nz/Main/WillBrowne
 - Bull, Larry http://www.cems.uwe.ac.uk/~lbull/
 - Holmes, John https://www.med.upenn.edu/apps/faculty/index.php/g5455356/p19936
 - Kovacs, Tim http://www.cs.bris.ac.uk/home/kovacs/
 - Lanzi, Pier Luca http://www.pierlucalanzi.net/
 - Nakata, Masaya http://www.nkt.ynu.ac.jp/en/people/
 - Stein, Anthony https://ki-agrartechnik.uni-hohenheim.de/anthony-stein
 - Urbanowicz, Ryan http://www.ryanurbanowicz.com/
 - Wilson, Stewart https://www.eskimo.com/~wilson/
- International Workshop Learning Classifier Systems (IWLCS)
 - held annually at GECCO
- Mailing List:: Yahoo Group: lcs-and-gbml[at]yahoogroups.com

^{*} Adapted from Urbanowicz's previous tutorials

Resources: Available Software

- Scitkit-compatible LCS (scikit-eLCS) in Python.
 - https://github.com/robertfrankzhang/Scikit-eLCS
 - A sklearn-compatible Python implementation of eLCS, a supervised learning variant of the Learning Classifier System, based off of UCS.
- Educational LCS (eLCS) in Python.
 - https://github.com/ryanurbs/eLCS
 - Simple Michigan-style LCS for learning how they work and how they are implemented.
 - Code intended to be paired with first LCS introductory textbook by Urbanowicz/Browne.
- ExSTraCS 2.0 Extended Supervised Learning LCS in Python
 - https://github.com/rvanurbs/ExSTraCS 2.0
 - For prediction, classification, data mining, knowledge discovery in complex, noisy, epistatic, or heterogeneous problems.
- BioHEL Bioinformatics-oriented Hierarchical Evolutionary Learning in C++
 - http://ico2s.org/software/biohel.html GAssist also available through this link.
- XCSLib (XCS and XCSF) (by Lanzi in C++)
 - http://xcslib.sourceforge.net/
- XCSF with function approximation visualization in Java
 - Martin Butz Chair website

^{*} Adapted from Urbanowicz's previous tutorials

Resources: LCS Review Papers & Books

Selected Review Papers:

- Pätzel, David, Stein, Anthony, and Hähner, Jörg. "A Survey on Formal Theoretical Advances Regarding XCS." Proc. of GECCO '19 Companion, July 2019, 1295-1302
- Bull, Larry. "A brief history of learning classifier systems: from CS-1 to XCS and its variants." Evolutionary Intelligence (2015): 1-16.
- Bacardit, Jaume, and Xavier Llorà. "Large-scale data mining using genetics-based machine learning." Wiley Interdisciplinary Reviews: Data Mining and Knowledge Discovery 3.1 (2013): 37-61.
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- Lanzi, Pier Luca, and Rick L. Riolo. "A roadmap to the last decade of learning classifier system research (from 1989 to 1999)." Learning Classifier Systems. Springer Berlin Heidelberg, 2000. 33-61.

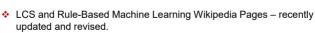
Books:

- Drugowitsch, J., (2008) <u>Design and Analysis of Learning Classifier Systems: A Probabilistic Approach</u>. Springer-Verlag.
- Bull, L., Bernado-Mansilla, E., Holmes, J. (Eds.) (2008) Learning Classifier Systems in Data Mining.
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^{*} Adapted from Urbanowicz's previous tutorials

Resources: Most recent

- Textbook: 'Introduction to Learning Classifier Systems' Springer, 2017 (Urbanowicz & Brown, 2017)
- LCS Introductory Chapter: 'Reaction Learning', Chapter 7.1 in book: 'Organic Computing – Technical Systems for Survival in the Real World', Birkhäuser, 2017 (Stein, 2017)
- YouTube video on LCS:
 - Learning Classifier Systems in a Nutshell
 - Animated, narrated explanation of basic LCS concepts.
 - https://www.voutube.com/watch?v=CRge_cZ2cJc



(https://en.wikipedia.org/wiki/Learning classifier system)

^{*} Adapted from Urbanowicz's previous tutorials

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Figures

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