CC-213L

Data Structures and Algorithms

Laboratory 11

Graphs and AVL

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Learning Objectives:

- Pointers and Dynamic Memory Allocation
- Non-Linear Data Structure
- Graph Data Structure

Resources Required:

- Desktop Computer or Laptop
- Microsoft ® Visual Studio 2022

General Instructions:

- In this Lab, you are **NOT** allowed to discuss your solution with your colleagues, not even allowed to ask how is s/he doing, this may result in negative marking. You can **ONLY** discuss with your Teaching Assistants (TAs) or Lab Instructor.
- Your TAs will be available in the Lab for your help. Alternatively, you can send your queries via email to one of the following.

Teachers:			
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Background and Overview

Non-Linear Data structures

Non-linear data structures are data structures in which elements are not arranged in a sequential, linear manner. Unlike linear data structures (e.g., arrays, linked lists) where elements are stored in a linear order, non-linear data structures allow for more complex relationships among elements

Graphs

A graph is a data structure that consists of a set of nodes (or vertices) and a set of edges connecting these nodes. Graphs are widely used to represent relationships and connections between different entities. The nodes in a graph can represent entities (such as people, cities, or web pages), and the edges represent relationships or connections between these entities.

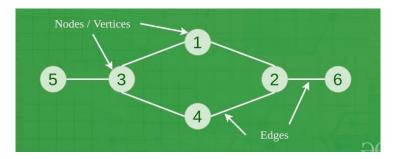


Figure 1(Graph)

There are two main types of graphs: directed and undirected.

1. Undirected Graph:

In an undirected graph, edges have no direction. If there is an edge between node A and node B, you can travel from A to B or from B to A along that edge. Mathematically, an undirected edge between nodes A and B can be represented as {A, B} or (A, B).

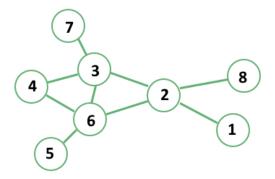


Figure 2(Undirected Graph)

2. Directed Graph (Digraph):

In a directed graph, edges have direction. If there is a directed edge from node A to node B, it means you can travel from A to B, but not necessarily from B to A. Mathematically, a directed edge from node A to node B can be represented as $(A \rightarrow B)$.

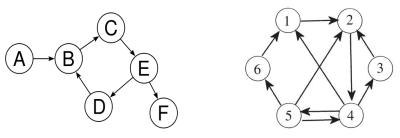


Figure 3(Directed Graphs)

Graphs can also have weighted edges, where each edge has an associated numerical value called a weight.

Common operations on graphs include adding or removing nodes and edges, traversing the graph to visit nodes in a specific order, and finding paths or cycles within the graph. Graphs can be classified into various types based on their properties and structures, such as:

3. Dense Graphs:

Definition: Dense graphs are graphs with many edges relative to the number of nodes.

Characteristics: In dense graphs, most pairs of nodes are connected by edges. The number of edges is close to the maximum possible for the given number of nodes.

Example: Complete graphs (where every pair of distinct nodes is connected by an edge) are an extreme example of dense graphs.

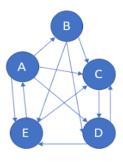


Figure 4(Dense Graph)

4. Sparse Graphs:

Definition: Sparse graphs are graphs with relatively few edges compared to the number of nodes.

Characteristics: In sparse graphs, only a small fraction of possible edges is present. The number of edges is much less than the maximum possible for the given number of nodes.

Example: Trees and forests are often sparse graphs.

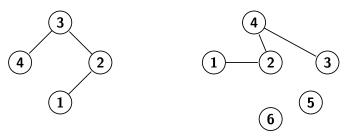


Figure 5(Sparse Graphs)

5. Cyclic Graphs:

Definition: Cyclic graphs are graphs that contain cycles, which are closed paths in the graph.

Characteristics: A cycle is a sequence of nodes where the first and last nodes are the same, and the edges form a closed loop.

Example: A simple example of a cyclic graph is a triangle (three nodes connected with edges in the shape of a triangle).

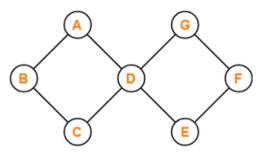


Figure 6(Cyclic Graph)

6. Acyclic Graphs:

Definition: Acyclic graphs are graphs that do not contain cycles.

Characteristics: There are no closed paths in acyclic graphs. These graphs have a natural hierarchy and are often used to represent relationships without circular dependencies.

Example: Trees are a common example of acyclic graphs. Directed acyclic graphs (DAGs) are often used in applications like task scheduling and dependency management.

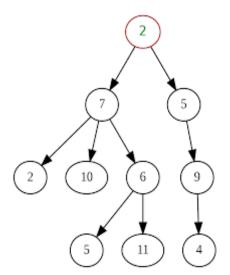


Figure 7(Acyclic Graph)

7. Connected Graphs:

Definition: Connected graphs are graphs where there is a path between every pair of nodes.

Characteristics: It is possible to travel from any node to any other node in the graph by following edges.

Example: A connected graph could be a fully connected graph where every node is directly or indirectly connected to every other node.

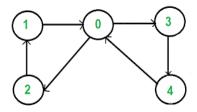


Figure 8(Connected Graphs)

8. Disconnected Graphs:

Definition: Disconnected graphs are graphs with components that are not connected to each other.

Characteristics: There are at least two nodes or sets of nodes in the graph that are not connected by any path.

Example: A graph consisting of two disconnected subgraphs (two separate groups of nodes) is an example of a.

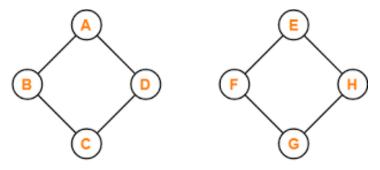


Figure 9(Disconnected Graphs)

Applications of Graphs:

Graphs have a wide range of applications across various domains due to their ability to model and represent relationships and connections between entities. Here are some common applications of graphs:

1. Social Network Analysis:

Graphs are used to model and analyze social networks, representing individuals as nodes and relationships as edges. This is crucial for understanding social structures, influence patterns, and information flow in networks like Facebook, Twitter, and LinkedIn.

2. Network Routing and Design:

Graphs play a key role in the design and optimization of computer networks. Nodes represent routers or computers, and edges represent communication links. Routing algorithms use graph theory concepts to find the most efficient paths for data transmission.

3. Recommendation Systems:

Graphs are employed in recommendation systems to model user-item interactions. Nodes represent users and items, and edges represent interactions or preferences. Algorithms analyze these graphs to suggest items that a user might be interested in based on their past behavior or preferences.

4. Web Page Ranking (PageRank):

Google's PageRank algorithm uses graph theory to rank web pages based on their importance. Web pages are represented as nodes, and hyperlinks between pages are represented as edges. Pages with more inbound links from important pages are considered more relevant and receive higher rankings in search results.

5. Transportation Networks:

Graphs model transportation systems such as road networks, subway systems, and airline routes. Nodes represent locations, and edges represent connections or routes. Algorithms can optimize travel routes, analyse traffic flow, and plan efficient transportation systems.

6. Epidemiology and Disease Spread Modelling:

Graphs are used to model the spread of diseases in populations. Nodes represent individuals, and edges represent possible paths of transmission. Analyzing the graph can help predict and control the spread of diseases.

7. Dependency Resolution and Task Scheduling:

Directed acyclic graphs (DAGs) are used to model dependencies between tasks in project management, software builds, and other scheduling applications. Nodes represent tasks, and edges represent dependencies. Efficient scheduling algorithms help optimize task execution.

8. Circuit Design:

Electrical circuits can be modeled as graphs, where components are nodes and connections between components are edges. Graph algorithms are used to analyze and optimize circuit design.

9. Recommendation Systems:

Graphs are utilized in recommendation systems to model user-item interactions. Nodes represent users and items, while edges represent interactions or preferences. Algorithms analyze these graphs to suggest items that a user might be interested in based on their past behavior or preferences.

10. Biological Networks:

Graphs are employed in bioinformatics to model biological interactions, such as protein-protein interactions, gene regulatory networks, and metabolic pathways. Nodes represent biological entities, and edges represent interactions or relationships.

11. Game Theory:

Graphs are used to model strategic interactions and dependencies in game theory. Nodes represent players, and edges represent relationships or interactions between players. This is applicable in areas like economics and political science.

Representation of Graphs

Adjacency Matrix:

In an adjacency matrix, a graph with n vertices is represented by an n x n matrix. The entry matrix[i][j] indicates whether there is an edge between vertices i and j. For an undirected graph, the matrix is symmetric.

Example:

Consider the following undirected graph:

The adjacency matrix for this graph would be:

	A	В	С
A	0	1	1
В	1	0	1
С	1	1	0

In this matrix:

- The entry matrix [0][1] (or matrix [1][0]) is 1, indicating there is an edge between vertex A and vertex B.
- The entry matrix [0][2] (or matrix [2][0]) is 1, indicating there is an edge between vertex A and vertex C.
- The entry matrix [1][2] (or matrix [2][1]) is 1, indicating there is an edge between vertex B and vertex C.

Adjacency List:

In an adjacency list representation, each vertex has a list of its neighboring vertices. This is an array of lists (or a HashMap), where each index represents a vertex, and the corresponding list contains the vertices adjacent to that vertex.

Example:

Using the same example graph:



The adjacency list for this graph would be:

A: [B, C]

B: [A, C]

C: [A, B]

In this list:

Vertex A is adjacent to vertices B and C.

Vertex B is adjacent to vertices A and C.

Vertex C is adjacent to vertices A and B.

Comparison:

1. Space Complexity:

Adjacency Matrix: Takes O(V^2) space for V vertices. It's more space-efficient for dense graphs.

Adjacency List: Takes O(V + E) space for V vertices and E edges. It's more space-efficient for sparse graphs.

2. Edge Existence Check:

Adjacency Matrix: Checking if an edge exists takes constant time (O (1)).

Adjacency List: Checking if an edge exists may take time proportional to the degree of the vertex (O(degree)).

3. Traversal:

Adjacency Matrix: Traversing all neighbors of a vertex takes O(V) time.

Adjacency List: Traversing all neighbors of a vertex takes O(degree) time, which is generally faster for sparse graphs.

Activities

Pre-Lab Activities:

Task 01: Adjacency Matrix representation of the Graph

Given declaration of the class Graph. Add necessary variables in the class and implement all the given methods of the class.

```
class Graph {
    private:
        int **adjMat;  // Adjacency matrix
        int vertex;  // Number of vertices
        int edge;  // Number of edges
    public:
        Graph();  // Constructor
        bool IsEmpty();
        void insertEdge(int u, int v);
        void deleteEdge(int u, int v);
};
You can also make extra helper functions, to visualize the graph!
```

In-Lab Activities:

Task 01: Adjacency List Representation of the Graph

Give implementation of the Adjacency List of the Graph.

```
#define max 10
class GraphNode {
public:
  int vertex;
  int weight;
  GraphNode * next;
  GraphNode() {
     vertex = 0;
    weight = 0;
    next = nullptr;
};
class Graph {
  GraphNode headnodes[max];
  int n;
  int visited[max];
public:
  Graph();
  // Destructor
  ~Graph();
  void create();
                                // To create graph
  void initialize visited();
  void addVertex(int vertex); // Add a new vertex to the graph
  void removeVertex(int vertex); // Remove a vertex and its associated edges from the graph
```

```
void addEdge(int vertex1, int vertex2); // Add an edge between two vertices
void removeEdge(int vertex1, int vertex2); // Remove an edge between two vertices
bool vertexExists(int vertex); // Check if a vertex exists in the graph
int examine_n() const; // Return value of n
int getWeight(int vertex1, int vertex2); // Get the weight of the edge between two vertices
void printGraph(); // Print the graph (adjacency list representation)
};
```

Task 02: Implement AVL Class

Given Following Structure implement AVL class.

```
// Node structure
struct Node {
               // Value of the node
  int value;
  int height; // Height of the node
  Node* left; // Pointer to the left child
  Node* right; // Pointer to the right child
  Node(int key) : value(key), height(1), left(nullptr), right(nullptr) {}
};
class AVLTree {
private:
  Node* root;
                    // Root of the AVL tree
public:
  // Constructor
  AVLTree(): root(nullptr) {}
  // Public methods
                                       // Inserts a value into the tree
  void insert(int kev):
  void remove(int key);
                                       // Removes a value from the tree
  bool search(int key);
                                       // Searches for a value in the tree
                                       // Displays the tree structure
  void display();
};
```

Post-Lab Activities

Task 01: Breadth First Search

Breadth-First Search (BFS) is a graph traversal algorithm that explores all the vertices of a graph in breadth ward motion, i.e., it visits all the vertices at the current level before moving on to the vertices at the next level. BFS is often used to find the shortest path in an unweighted graph and to explore the connected components of a graph.

1. Initialization:

- Start at a chosen source vertex.
- Mark the source vertex as visited.
- Enqueue the source vertex into a queue.

2. Exploration:

- While the queue is not empty:
- Dequeue a vertex from the front of the queue.
- Visit the dequeued vertex (perform any desired operation).
- Enqueue all unvisited neighbors of the dequeued vertex.
- Mark each visited neighbor as visited.

3. Termination:

• Continue this process until the queue is empty.

The BFS algorithm guarantees that it visits all the vertices in the connected component containing the source vertex and computes the shortest path from the source vertex to all other reachable vertices in an unweighted graph.

The data structure commonly used for the queue in BFS is First-In-First-Out (FIFO), which ensures that the vertices are processed in the order they are discovered.

BFS can be implemented using an adjacency list or adjacency matrix representation of the graph. The algorithm is particularly useful for applications like finding the shortest path in an unweighted graph, checking if there is a path between two vertices, and exploring the structure of graphs level by level.

BFS is a complete algorithm, meaning it explores the entire connected component of the graph. It also finds the shortest paths in unweighted graphs and is efficient in finding the shortest path when the graph is represented using an adjacency list.

Add this public member function to the Graph class.

void BFS (int v); // Breadth-First Search

Task 02 Depth First Search

Depth-First Search (DFS) is a graph traversal algorithm that explores as far as possible along each branch before backtracking. In other words, it goes as deep as possible along one branch of the graph before exploring other branches. DFS is often used to explore the structure of a graph, find paths, and perform various operations on the vertices.

1. Initialization:

- Start at a chosen source vertex.
- Mark the source vertex as visited.

2. Exploration:

- For each unvisited neighbour of the current vertex:
- Recursively apply DFS to that neighbour.
- Perform any desired operation while visiting the vertex (e.g., print it, store it, etc.).

3. Termination:

• Continue this process until all reachable vertices are visited.

DFS uses a stack to keep track of the vertices to visit. In practice, the recursive call stack itself is often used for this purpose.

DFS has various applications, including finding connected components, topological sorting, detecting cycles in a graph, and solving problems related to paths and connectivity.

DFS is not guaranteed to find the shortest path between two vertices, but it is often more memory-efficient than BFS. The order in which vertices are visited depends on the specific order in which neighbours are processed, and it may lead to different traversal orders for different starting vertices.

Add this public member function to the Graph class

void DFS(int v); // Depth-First Search

Submissions:

- For In-Lab Activity:
 - Save the files on your PC.
 - TA's will evaluate the tasks offline.
- For Pre-Lab & Post-Lab Activity:
 - Submit the .cpp file on Google Classroom and name it to your roll no.

Evaluations Metric:

• All the lab tasks will be evaluated offline by TA's

•	Division of Pre-Lab marks:	[25 marks]
	 Task 01: Adjacency Matrix Graph 	[25 marks]
•	Division of In-Lab marks:	[50 marks]
	 Task 01: Adjacency List Graph 	[25 marks]
	Task 02: AVL Class	[25 marks]
•	Division of Post-Lab marks:	[25 marks]
	Task 01: Breath First Search	[10 marks]
	 Task 02: Depth First Search 	[15 marks]

References and Additional Material:

Graphs

https://www.geeksforgeeks.org/graph-data-structure-and-algorithms/

Lab Time Activity Simulation Log:

•	Slot - 01 - 02:00 - 00:15:	Class Settlement
•	Slot - 02 - 02:15 - 02:30:	In-Lab Task 01
•	Slot $-03 - 02:30 - 02:45$:	In-Lab Task 01
•	Slot $-04 - 02:45 - 03:00$:	In-Lab Task 01
•	Slot - 05 - 03:00 - 03:15:	In-Lab Task 01
•	Slot $-06 - 03:15 - 03:30$:	In-Lab Task 01
•	Slot $-07 - 03:30 - 03:45$:	In-Lab Task 01
•	Slot - 08 - 03:45 - 04:00:	In-Lab Task 01
•	Slot - 09 - 04:00 - 04:15:	In-Lab Task 01
•	Slot - 10 - 04:15 - 04:30:	In-Lab Task 01
•	Slot - 11 - 4:300 - 04:45:	In-Lab Task 01
•	Slot - 12 - 04:45 - 05:00:	Discussion on Post-Lab