

Recursion and Backtracking

Data Structures CS 218

Week 2 and Week 3

Introduction

- Basics of Recursion
- Different types of Recursion
 - Direct
 - Indirect
 - Tail
 - Non Tail

Recursion: The main ingredients

- To formulate a recursive solution:

- Identify the “simplest” instance

The **base case(s)** that can be solved *without recursion*

- Identify “simpler” instances of the same problem

The **recursive case(s)** that requires *recursive* calls to solve them

- Identify how the solution from the simpler problem can help to construct the final result
- Be sure we are able to reach the “simplest” instance
 - So that we will not get an infinite recursion

Examples of Recursion discussed in class

- Finding factorial
- Traversing linked list
- Reversing linked list
- Fibonacci series
- Sum of digits
- Digital Root
- Tower of hanoi
- Backtracking
 - N-Queen problem
 - Maze problem

Recursion Behind the Scenes/ Activation Records using Stacks

Finding Factorial

```
...  
f = factorial(4);  
...
```

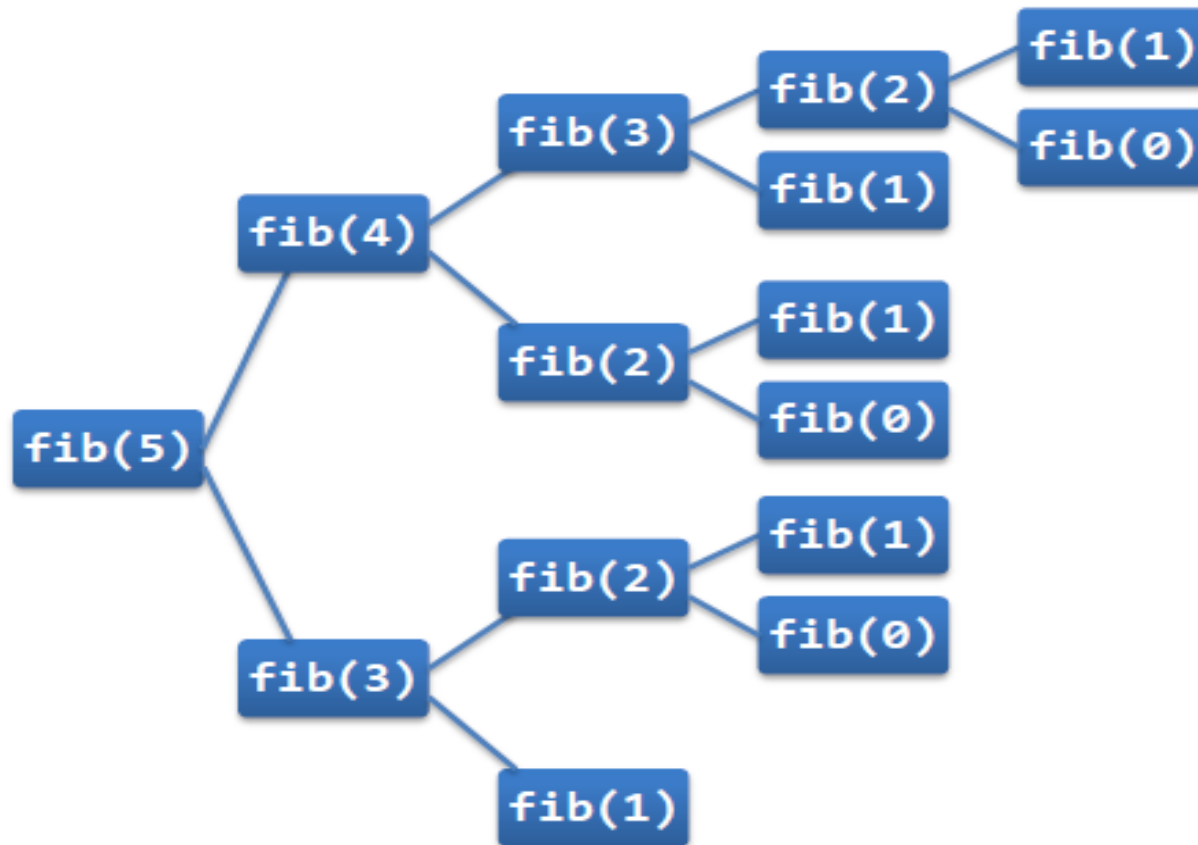
```
int factorial(int 4)  
  if (4 <= 1) return 1;  
  else return 4 * factorial(3);  
  
int factorial(int 3)  
  if (3 <= 1) return 1;  
  else return 3 * factorial(2);  
  
int factorial(int 2)  
  if (2 <= 1) return 1;  
  else return 2 * factorial(1);  
  
int factorial(int 1)  
  if (1 <= 1) return 1;  
  else return 1 * factorial(n-1);
```

```
...  
f = 24;  
...
```

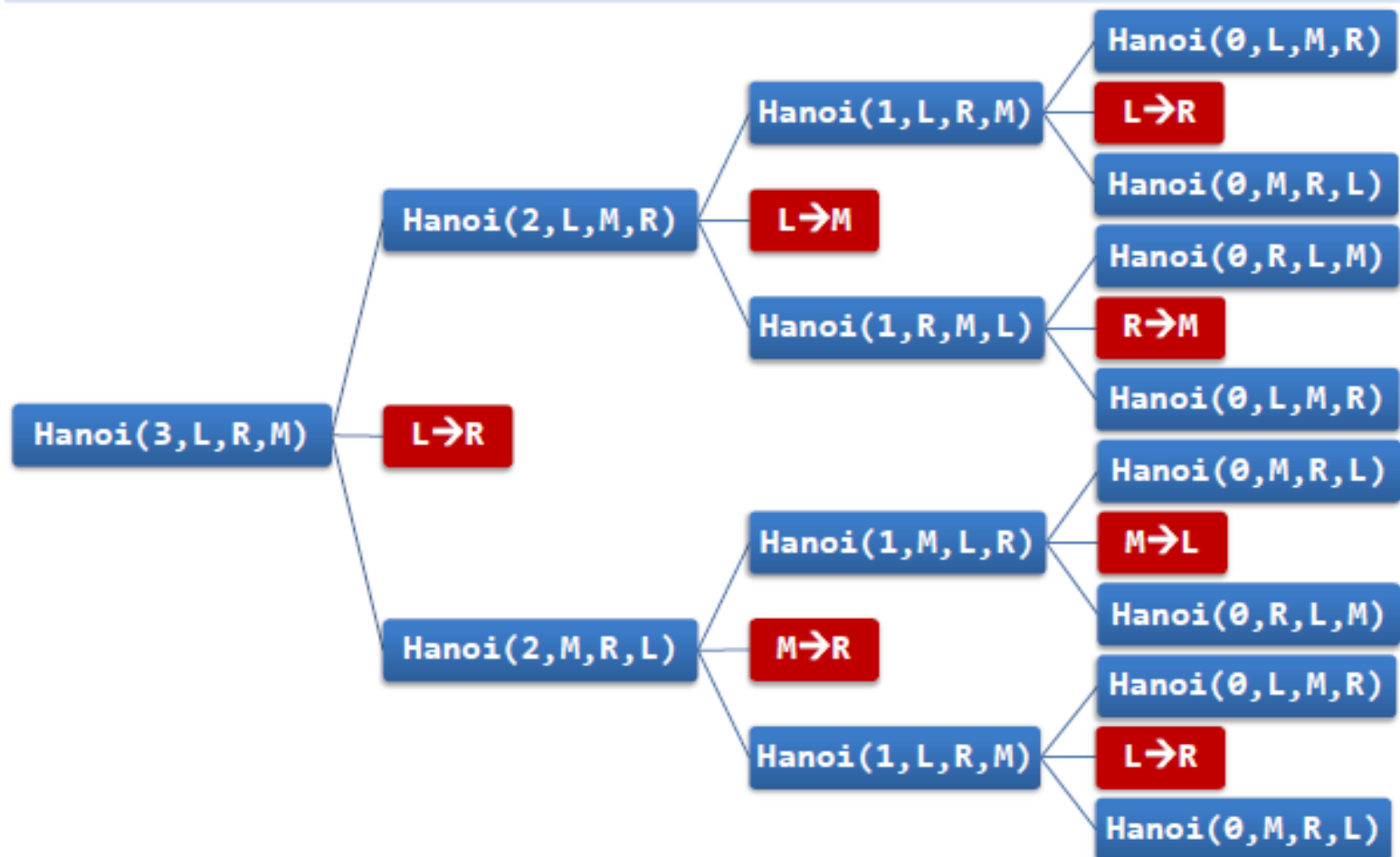
```
24 factorial(int 4)  
  if (4 <= 1) return 1;  
  else return 24;  
  
6 factorial(int 3)  
  if (3 <= 1) return 1;  
  else return 6;  
  
2 factorial(int 2)  
  if (2 <= 1) return 1;  
  else return 2;  
  
1 factorial(int 1)  
  if (1 <= 1) return 1;  
  else return 1 * factorial(n-1);
```

Fibonacci Series

The tree of calls for `fib(5)` would be:



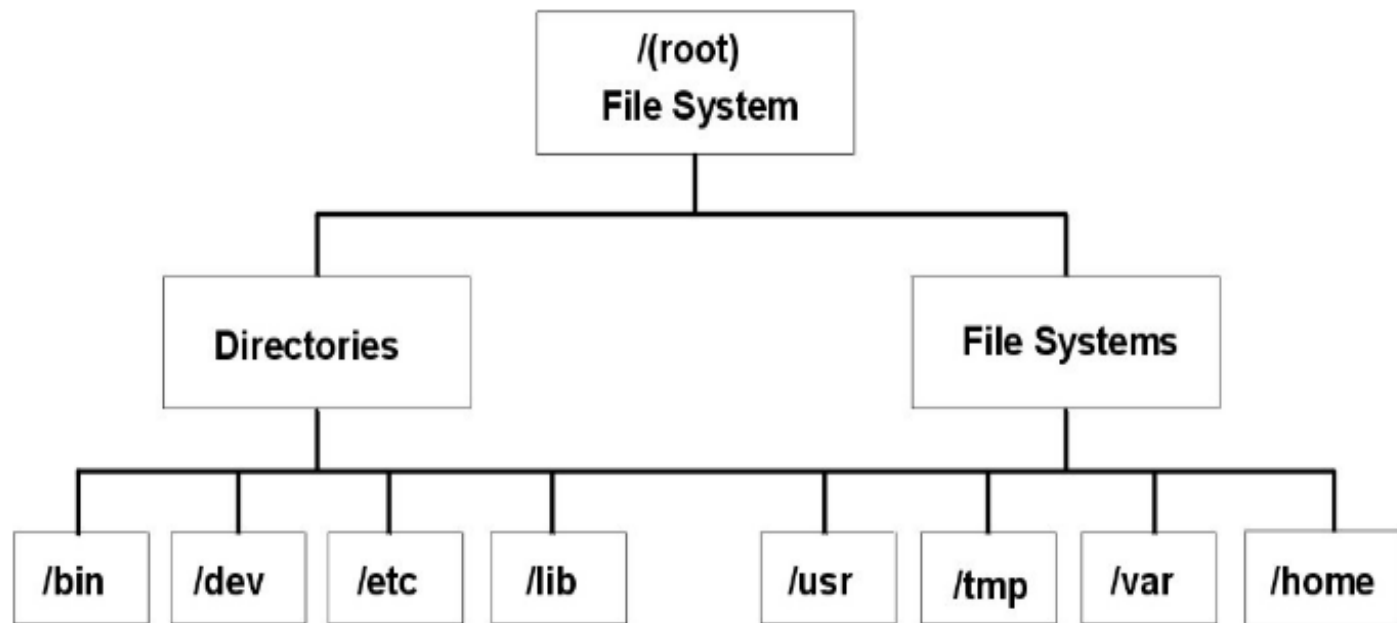
Tower of Hanoi



Iterative methods Vs Recursive methods

- Iterative methods vs recursion
- When to use iterative methods?
- When to use recursion?
- When not to use recursion?

An other good example



Backtracking

- Introduction to backtracking
- Is recursion and backtracking are same?
- N-Queen Problem discussion